Goldman Sachs - Hackerrank - Car Popularity

Bala Kesavan

February 10, 2018

Context

To predict the popularity of a car given potential explanatory variables.

Exploratory data analysis

There are certain inferences we can draw about lack of popularity. Cars that are high on 'buying_price' or 'maintenance_cost' don't make the cut. Similarly, cars low on 'number_of_seats' or 'safety_rating' are not popular. 'number_of_doors' don't seem to make a difference while 'luggage_boot_size' has a weak effect on popularity.

The response variable, 'popularity', is ordinal. This has been taken care of in the preprocessing and in algorithm selection.

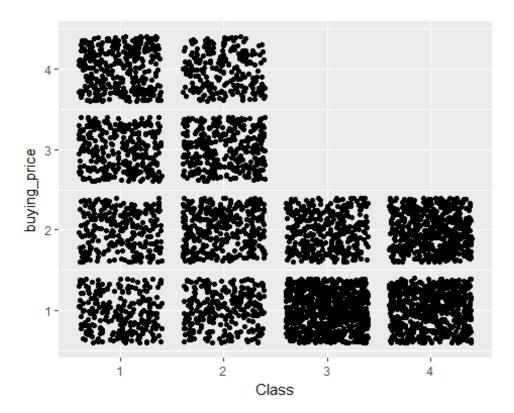
Next, several explanatory variables, like 'buying_price', are also ordinal. The choice was made to treat these as continuous variables after studying the well laid out arguments in this paper: Paper 248-2009, "Learning When to Be Discrete: Continuous vs. Categorical Predictors," David J. Pasta, ICON Clinical Research, San Francisco, CA.

Popularity levels 3 and 4 are under represented in the dataset. Since there are only 44 and 40 records each, a variety of subsampling techniques were tried, including SMOTE. Finally, 'upsample' was chosen since it performed best. This is understandable since SMOTE reduced the total count of data and that made it harder for the algorithm to learn.

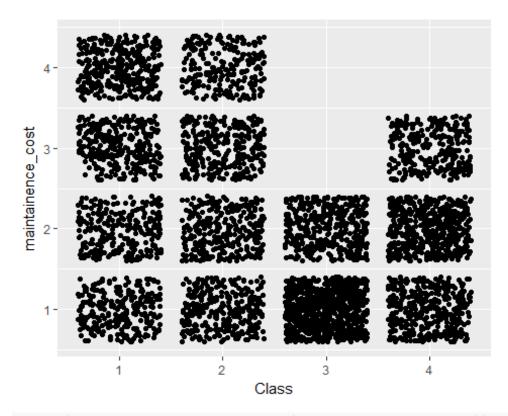
```
library(caret)
library(ggplot2)
train GS <- read.csv('train.csv')</pre>
summary(train_GS)
     buying_price
                    maintainence_cost number_of_doors number_of_seats
##
                           :1.000
## Min.
          :1.000
                    Min.
                                      Min.
                                             :2.000
                                                       Min.
                                                              :2.000
   1st Ou.:2.000
                    1st Ou.:2.000
                                      1st Ou.:2.000
                                                       1st Ou.:2.000
##
                                                       Median :4.000
## Median :3.000
                    Median :3.000
                                      Median :3.000
##
   Mean
           :2.533
                           :2.528
                                              :3.494
                                                              :3.633
                    Mean
                                      Mean
                                                       Mean
                    3rd Qu.:4.000
##
   3rd Qu.:4.000
                                      3rd Qu.:4.250
                                                       3rd Qu.:5.000
## Max.
          :4.000
                    Max.
                           :4.000
                                      Max.
                                             :5.000
                                                       Max.
                                                              :5.000
##
   luggage_boot_size safety_rating
                                        popularity
## Min.
          :1.000
                      Min.
                             :1.000
                                      Min.
                                              :1.000
   1st Ou.:1.000
##
                      1st Qu.:1.000
                                      1st Qu.:1.000
## Median :2.000
                      Median :2.000
                                      Median :1.000
```

```
## Mean :1.987
                            :1.978
                     Mean
                                    Mean :1.348
## 3rd Qu.:3.000
                     3rd Qu.:3.000
                                    3rd Qu.:2.000
## Max.
          :3.000
                     Max.
                           :3.000
                                    Max.
                                           :4.000
str(train GS)
## 'data.frame':
                   1628 obs. of 7 variables:
                     : int 3 3 1 4 3 2 1 3 1 2 ...
## $ buying_price
## $ maintainence_cost: int 2 2 4 4 3 1 3 1 1 1 ...
## $ number_of_doors : int 4 2 2 2 3 2 5 2 3 4 ...
## $ number of seats : int 2 5 5 2 4 2 2 4 5 2 ...
## $ luggage_boot_size: int 2 2 1 1 3 1 2 3 2 2 ...
                     : int 2 1 3 2 3 1 2 2 1 2 ...
## $ safety_rating
## $ popularity
                      : int 1111211211...
train GS proc <- train GS
train GS proc$popularity <- as.ordered(train GS$popularity)</pre>
str(train_GS_proc)
## 'data.frame':
                   1628 obs. of 7 variables:
## $ buying_price
                     : int 3 3 1 4 3 2 1 3 1 2 ...
## $ maintainence cost: int 2 2 4 4 3 1 3 1 1 1 ...
## $ number of doors : int 4 2 2 2 3 2 5 2 3 4 ...
## $ number_of_seats : int 2 5 5 2 4 2 2 4 5 2 ...
## $ luggage boot size: int 2 2 1 1 3 1 2 3 2 2 ...
## $ safety_rating : int 2 1 3 2 3 1 2 2 1 2 ...
                      : Ord.factor w/ 4 levels "1"<"2"<"3"<"4": 1 1 1 1 2 1
## $ popularity
1 2 1 1 ...
lapply(train GS[, names(train GS)], table)
## $buying_price
##
        2
            3
##
    1
## 384 408 421 415
##
## $maintainence cost
##
##
    1
        2
            3
## 392 404 412 420
##
## $number of doors
##
##
    2
        3
## 411 409 401 407
##
## $number_of_seats
##
    2
##
        4
## 565 530 533
##
```

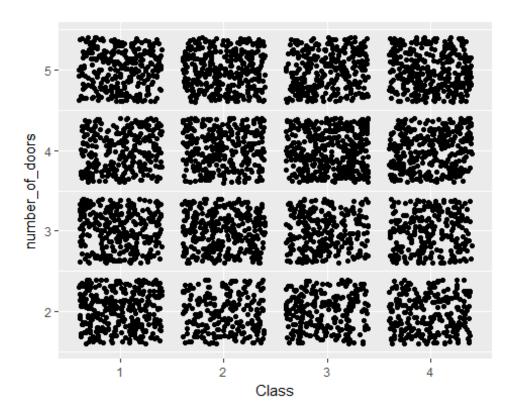
```
## $luggage_boot_size
##
    1 2 3
##
## 553 543 532
##
## $safety_rating
##
        2 3
##
    1
## 565 534 529
##
## $popularity
##
##
      1
           2
               3
                     4
## 1185 359
              44
                    40
#(ftable(xtabs(popularity~buying_price+maintainence_cost , data = train_GS)))
#fixing the severe under representation of popularity levels 3 & 4
train_GS_proc_upsample <- upSample(x=train_GS_proc[,-7], y=</pre>
train_GS_proc$popularity)
table(train_GS_proc_upsample$Class)
##
##
      1 2
               3
                     4
## 1185 1185 1185 1185
#visual checks of informativeness/ ability to discriminate the response
variable
ggplot(train_GS_proc_upsample, aes(Class, buying_price)) + geom_jitter()
```



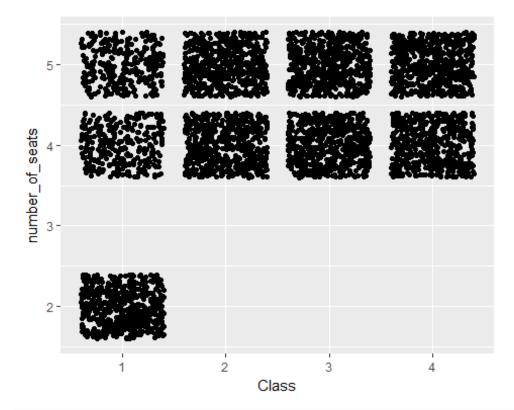
ggplot(train_GS_proc_upsample, aes(Class, maintainence_cost)) + geom_jitter()



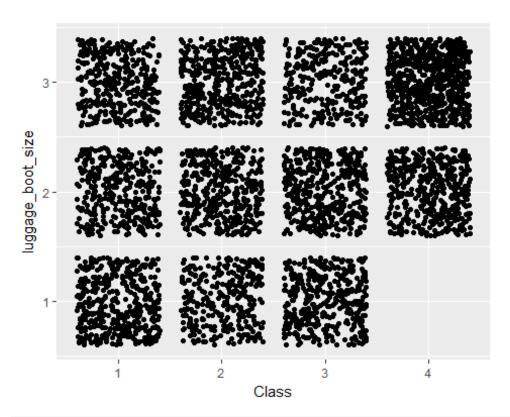
ggplot(train_GS_proc_upsample, aes(Class, number_of_doors)) + geom_jitter()



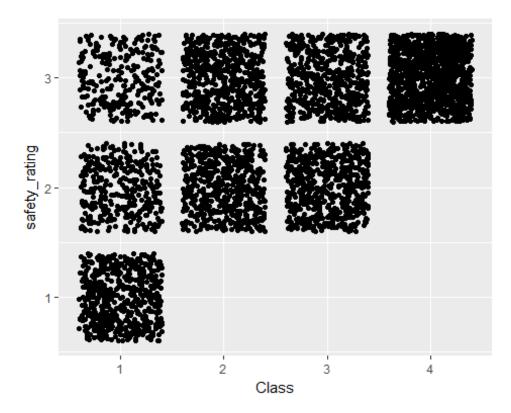
ggplot(train_GS_proc_upsample, aes(Class, number_of_seats)) + geom_jitter()

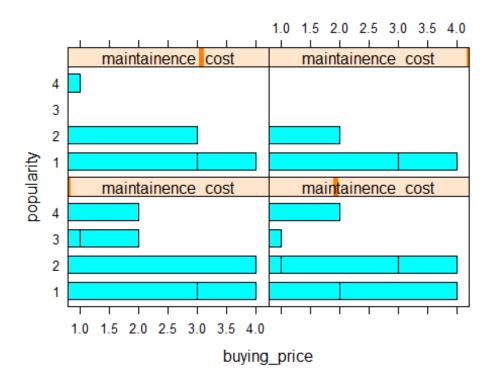


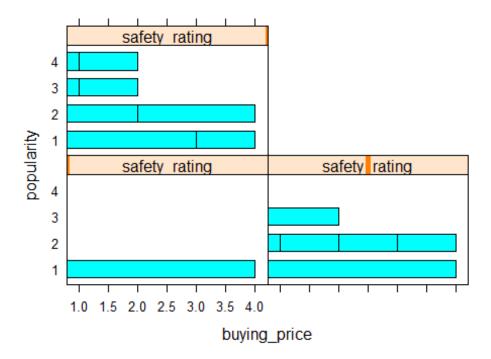
ggplot(train_GS_proc_upsample, aes(Class, luggage_boot_size)) + geom_jitter()

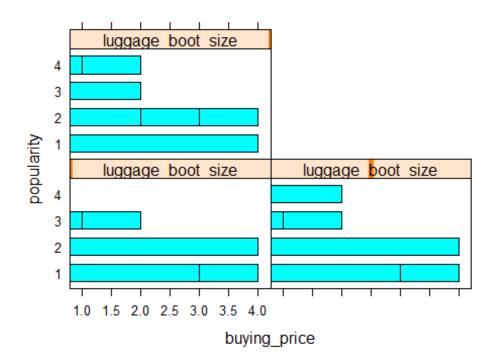


ggplot(train_GS_proc_upsample, aes(Class, safety_rating)) + geom_jitter()









```
#satistical tests of independence
chisq.test(table(as.factor(train_GS$number_of_doors), train_GS$popularity))
##
## Pearson's Chi-squared test
##
## data: table(as.factor(train_GS$number_of_doors), train_GS$popularity)
## X-squared = 8.0269, df = 9, p-value = 0.5314

chisq.test(table(as.factor(train_GS$number_of_seats), train_GS$popularity))
##
## Pearson's Chi-squared test
##
## data: table(as.factor(train_GS$number_of_seats), train_GS$popularity)
## X-squared = 323.68, df = 6, p-value < 2.2e-16</pre>
```

Modeling

Simple models are usually best and the 'ordinal' model with the logistic link has been used. The model coefficients are along expected lines. e.g. 'popularity' and 'buying_price' have an inverse relationship while there is a positive reeationship to 'safety_rating'. Several options were tested, like polynomial and interaction terms. The best performing option, with one interaction term, was determined using the ANOVA test as shown below.

```
library(ordinal)
model clm GS upsample <-
clm(Class~buying price+maintainence cost+luggage boot size+safety rating,
data = train_GS_proc_upsample)
summary(model clm GS upsample)
## formula:
## Class ~ buying price + maintainence_cost + luggage_boot_size +
safety_rating
## data:
           train_GS_proc_upsample
##
## link threshold nobs logLik
                                AIC
                                        niter max.grad cond.H
## logit flexible 4740 -3611.70 7237.40 6(0) 1.37e-08 2.7e+03
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
## buying price
                    -1.77383
                               0.04510 -39.33 <2e-16 ***
## maintainence cost -1.32913
                               0.04047 -32.84
                                                <2e-16 ***
                                                 <2e-16 ***
## luggage_boot_size 1.64197
                               0.04816 34.10
                                                <2e-16 ***
                               0.07700 44.52
## safety_rating
                     3.42819
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Threshold coefficients:
```

```
Estimate Std. Error z value
## 1 2
       2.9580
                    0.2034
                             14.54
## 2|3
         6.0688
                    0.2154
                             28.17
## 3 4
        8.6892
                    0.2370
                             36.66
model clm GS upsample1 <- update(model clm GS upsample, ~. +</pre>
buying_price*safety_rating)
anova(model_clm_GS_upsample, model_clm_GS_upsample1)
## Likelihood ratio tests of cumulative link models:
##
##
                          formula:
## model_clm_GS_upsample Class ~ buying_price + maintainence_cost +
luggage boot size + safety rating
## model_clm_GS_upsample1 Class ~ buying_price + maintainence_cost +
luggage_boot_size + safety_rating + buying_price:safety_rating
                          link: threshold:
## model clm GS upsample logit flexible
## model clm GS upsample1 logit flexible
##
##
                          no.par
                                    AIC logLik LR.stat df Pr(>Chisq)
## model_clm_GS_upsample
                               7 7237.4 -3611.7
## model clm GS upsample1
                               8 7088.2 -3536.1 151.16 1 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
test GS <- read.csv('test.csv')
names(test GS) <-</pre>
c("buying_price", "maintainence_cost", "number_of_doors", "number_of_seats", "lug
gage_boot_size", "safety_rating")
prediction <- predict(model clm GS upsample1, newdata = test GS, type =</pre>
'class')
write.csv(prediction, file = 'prediction.csv', row.names = FALSE)
```

Conclusion

The best score obtained during submissions by Hackerrank's checker was: F1 score = [1: 0.181818, 2: 0.260870, 3: 0.444444, 4: 0.333333]. In a way, the better performance for levels 3 and 4 is to be expected. It is easier to model the fact that cars cannot reach levels 3 or 4 of popularity without performing very well on 'buying_price', 'maintainence_cost' and 'safety_rating'.

But the reverse isn't true. Just because a car performs very well on 'buying_price', 'maintainence_cost' and 'safety_rating' doesn't lead to higher popularity. Finding this out could be the next step.

Appendix showing confusion matrices and demonstrating the use of other algorithms

More algorithms are available in caret.

```
#data partitioning
set.seed(123)
inTraining <- createDataPartition(train GS proc upsample$Class, p = 0.8, list</pre>
= FALSE)
training <- train_GS_proc_upsample[inTraining, ]</pre>
testing <- train_GS_proc_upsample[-inTraining, ]</pre>
#modeling wth CLM
library(ordinal)
#model clm GS upsample <-
clm(Class~buying_price+maintainence_cost+luggage_boot_size+safety_rating,
data = training)
model clm GS upsample <- readRDS('model clm GS upsample.rds')</pre>
summary(model clm GS upsample)
## formula:
## Class ~ buying price + maintainence_cost + luggage_boot_size +
safety_rating
## data:
           training
##
## link threshold nobs logLik AIC
                                         niter max.grad cond.H
## logit flexible 3792 -2918.81 5851.62 6(0) 5.87e-09 2.7e+03
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
                     -1.71273
## buying_price
                                0.04997 -34.27 <2e-16 ***
                                                   <2e-16 ***
## maintainence_cost -1.32530
                                 0.04477 -29.60
                                0.05443 30.39
## luggage boot size 1.65398
                                                   <2e-16 ***
                                0.08454 39.48 <2e-16 ***
## safety rating
                    3.33787
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Threshold coefficients:
      Estimate Std. Error z value
## 1 2
        2.9690
                    0.2302
                            12.90
## 2|3 6.0286
                            24.87
                    0.2424
## 3 4 8.6054
                   0.2658
                            32.38
#saveRDS(model_clm_GS_upsample, file='model_clm_GS_upsample.rds')
#model_clm_GS_upsample1 <- update(model_clm_GS_upsample, ~. +</pre>
buying price*safety rating)
model_clm_GS_upsample1 <- readRDS('model_clm_GS_upsample1.rds')</pre>
summary(model_clm_GS_upsample1)
```

```
## formula:
## Class ~ buying price + maintainence cost + luggage boot size +
safety_rating + buying_price:safety_rating
## data:
           training
##
## link threshold nobs logLik AIC
                                         niter max.grad cond.H
## logit flexible 3792 -2863.11 5742.23 6(0) 5.20e-09 2.0e+04
##
## Coefficients:
##
                             Estimate Std. Error z value Pr(>|z|)
## buying_price
                              0.05637
                                         0.16453
                                                 0.343
                                                           0.732
                                                          <2e-16 ***
                             -1.35113
                                         0.04520 -29.891
## maintainence cost
## luggage boot size
                              1.69395
                                         0.05525 30.659 <2e-16 ***
                                                          <2e-16 ***
## safety_rating
                              4.71824
                                         0.16072 29.357
## buying_price:safety_rating -0.70803
                                         0.06505 -10.884
                                                          <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Threshold coefficients:
##
      Estimate Std. Error z value
## 1 2
        6.3666
                   0.4012
                          15.87
## 2 3
                   0.4126
                            22.90
        9.4468
## 3 4 12.1727
                   0.4425 27.51
anova(model clm GS_upsample, model clm GS_upsample1)
## Likelihood ratio tests of cumulative link models:
##
                         formula:
##
## model_clm_GS_upsample Class ~ buying_price + maintainence_cost +
luggage boot size + safety rating
## model_clm_GS_upsample1 Class ~ buying_price + maintainence_cost +
luggage boot size + safety rating + buying price:safety rating
                         link: threshold:
## model clm GS upsample logit flexible
## model clm GS upsample1 logit flexible
##
                                   AIC logLik LR.stat df Pr(>Chisq)
##
                         no.par
## model clm GS upsample
                            7 5851.6 -2918.8
## model_clm_GS_upsample1
                             8 5742.2 -2863.1 111.39 1 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
#saveRDS(model clm GS upsample1, file='model clm GS upsample1.rds')
prediction <- predict(model_clm_GS_upsample1, newdata = testing, type =</pre>
'class')
confusionMatrix(as.numeric(prediction$fit), as.numeric(testing$Class))
## Confusion Matrix and Statistics
##
```

```
##
             Reference
                             4
## Prediction
                1
                     2
                         3
                             0
##
            1 172
                   55
                         0
               40 136
                       38
                             0
##
            2
##
            3
               16
                  46 146
                            34
                        53 203
##
                9
                     0
##
## Overall Statistics
##
##
                  Accuracy: 0.693
##
                     95% CI: (0.6626, 0.7223)
##
       No Information Rate: 0.25
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                      Kappa: 0.5907
##
   Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                         Class: 1 Class: 2 Class: 3 Class: 4
## Sensitivity
                           0.7257
                                    0.5738
                                              0.6160
                                                       0.8565
                                    0.8903
## Specificity
                           0.9226
                                              0.8650
                                                       0.9128
## Pos Pred Value
                           0.7577
                                    0.6355
                                              0.6033
                                                       0.7660
## Neg Pred Value
                           0.9098
                                    0.8624
                                              0.8711
                                                       0.9502
## Prevalence
                           0.2500
                                    0.2500
                                              0.2500
                                                       0.2500
## Detection Rate
                           0.1814
                                    0.1435
                                              0.1540
                                                       0.2141
## Detection Prevalence
                           0.2395
                                    0.2257
                                              0.2553
                                                       0.2795
## Balanced Accuracy
                           0.8242
                                    0.7321
                                              0.7405
                                                       0.8847
#modeling with 'CART or Ordinal Responses'
Control <- trainControl(method = 'cv', 10)</pre>
set.seed(21)
#model_GS_rpartScore <- train(Class~., data = train_GS_proc_upsample,</pre>
method="rpartScore", trControl=Control)
(model GS rpartScore <- readRDS('model GS rpartScore.rds'))</pre>
## CART or Ordinal Responses
##
## 4740 samples
##
      6 predictor
      4 classes: '1', '2', '3', '4'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 4267, 4266, 4267, 4266, 4267, 4267, ...
## Resampling results across tuning parameters:
##
##
                split
                        prune Accuracy
     ср
                                           Kappa
##
     0.1136428
                abs
                        mr
                               0.5647882
                                          0.4196945
##
     0.1136428
                abs
                        mc
                               0.3905061 0.1873336
```

```
##
                               0.5261631 0.3682044
     0.1136428
                quad
                       mr
##
     0.1136428
                quad
                       mc
                               0.3905061 0.1873336
##
     0.1477731
                abs
                               0.5261631 0.3682044
                       mr
##
     0.1477731
                abs
                       mc
                              0.3905061 0.1873336
##
     0.1477731 quad
                       mr
                              0.5261631 0.3682044
##
     0.1477731
                quad
                              0.3905061 0.1873336
                       mc
                abs
##
     0.1589311
                              0.5261631 0.3682044
                       mr
##
     0.1589311
                abs
                       mc
                              0.3905061 0.1873336
##
     0.1589311
                quad
                       mr
                              0.5261631 0.3682044
##
     0.1589311
                quad
                              0.3905061 0.1873336
                       mc
##
## Accuracy was used to select the optimal model using the largest value.
## The final values used for the model were cp = 0.1136428, split = abs
## and prune = mr.
#saveRDS(model_GS_rpartScore, file = 'model_GS_rpartScore.rds')
prediction <- predict(model GS rpartScore, newdata = testing)</pre>
confusionMatrix((prediction), (testing$Class))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                1
                    2
                        3
                            4
            1 139 119
                            0
##
##
            2
                0
                    0
                            0
            3
##
               79
                   68 128
               19
##
            4
                   50 109 237
##
## Overall Statistics
##
##
                  Accuracy : 0.5316
##
                    95% CI: (0.4993, 0.5638)
##
       No Information Rate : 0.25
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa : 0.3755
   Mcnemar's Test P-Value : < 2.2e-16
##
##
## Statistics by Class:
##
##
                        Class: 1 Class: 2 Class: 3 Class: 4
## Sensitivity
                          0.5865
                                      0.00
                                             0.5401
                                                      1.0000
                                      1.00
## Specificity
                          0.8326
                                             0.7932
                                                      0.7496
## Pos Pred Value
                                       NaN
                          0.5388
                                             0.4655
                                                      0.5711
## Neg Pred Value
                          0.8580
                                      0.75
                                             0.8380
                                                      1.0000
## Prevalence
                          0.2500
                                      0.25
                                             0.2500
                                                      0.2500
## Detection Rate
                                      0.00
                                             0.1350
                          0.1466
                                                      0.2500
## Detection Prevalence
                          0.2722
                                      0.00
                                             0.2901
                                                      0.4378
## Balanced Accuracy
                          0.7096
                                      0.50
                                             0.6667
                                                      0.8748
```

```
#modeling with 'Ordered Logistic or Probit Regression'
Control <- trainControl(method = 'cv', 10)</pre>
set.seed(21)
#model GS polr <- train(Class~., data = train GS proc upsample,
method="polr", trControl=Control)
(model_GS_polr <- readRDS('model_GS_polr.rds'))</pre>
## Ordered Logistic or Probit Regression
##
## 4740 samples
      6 predictor
##
      4 classes: '1', '2', '3', '4'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 4265, 4266, 4267, 4266, 4266, 4264, ...
## Resampling results across tuning parameters:
##
##
     method
               Accuracy
                          Kappa
##
     cauchit
               0.7293173
                          0.6390929
##
     cloglog
                     NaN
##
     logistic 0.7248882 0.6331878
##
     loglog
               0.6862684 0.5816932
##
     probit
               0.7139114 0.6185500
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was method = cauchit.
#saveRDS(model_GS_polr, file = 'model_GS_polr.rds')
prediction <- predict(model GS polr, newdata = testing)</pre>
confusionMatrix((prediction), (testing$Class))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                1
                    2
                        3
                            4
##
            1 182 23
                        0
            2 47 164 27
##
            3
                6
                  42 170 47
##
            4
##
                2
                    8
                      40 190
##
## Overall Statistics
##
##
                  Accuracy : 0.7447
                    95% CI: (0.7157, 0.7722)
##
##
       No Information Rate: 0.25
       P-Value [Acc > NIR] : < 2.2e-16
##
##
```

```
##
                     Kappa : 0.6596
##
  Mcnemar's Test P-Value : 9.184e-05
##
## Statistics by Class:
##
##
                        Class: 1 Class: 2 Class: 3 Class: 4
## Sensitivity
                                   0.6920
                                             0.7173
                                                      0.8017
                          0.7679
## Specificity
                          0.9677
                                   0.8959
                                             0.8664
                                                      0.9297
## Pos Pred Value
                          0.8878
                                   0.6891
                                             0.6415
                                                      0.7917
## Neg Pred Value
                          0.9260
                                   0.8972
                                             0.9019
                                                      0.9336
## Prevalence
                          0.2500
                                   0.2500
                                            0.2500
                                                      0.2500
## Detection Rate
                                   0.1730
                          0.1920
                                            0.1793
                                                      0.2004
                          0.2162
                                                      0.2532
## Detection Prevalence
                                   0.2511
                                             0.2795
## Balanced Accuracy
                          0.8678
                                   0.7940
                                            0.7918
                                                      0.8657
#modeling with 'Adjacent Categories Probability Model for Ordinal Data'
Control <- trainControl(method = 'cv', 10)</pre>
set.seed(21)
#model GS_vglmAdjCat <- train(Class~., data = train GS_proc_upsample,
method="vglmAdjCat", trControl=Control)
(model GS vglmAdjCat <- readRDS('model GS vglmAdjCat.rds'))</pre>
## Adjacent Categories Probability Model for Ordinal Data
##
## 4740 samples
      6 predictor
##
      4 classes: '1', '2', '3', '4'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 4265, 4266, 4267, 4266, 4266, 4264, ...
## Resampling results across tuning parameters:
##
##
     parallel Accuracy
                          Kappa
##
     FALSE
               0.8750812 0.8334416
##
      TRUE
               0.7250956 0.6334630
##
## Tuning parameter 'link' was held constant at a value of loge
## Accuracy was used to select the optimal model using the largest value.
## The final values used for the model were parallel = FALSE and link = loge.
#saveRDS(model_GS_vglmAdjCat, file = 'model_GS_vglmAdjCat.rds')
prediction <- predict(model GS vglmAdjCat, newdata = testing)</pre>
confusionMatrix((prediction), (testing$Class))
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                1
                    2
                        3
                            4
            1 200 218 157 176
##
```

```
##
              25 8 80
                          25
##
                       0 36
            3
              12
                  11
##
            4
               0
                   0
                          0
                       0
##
## Overall Statistics
##
                 Accuracy: 0.2194
##
##
                   95% CI: (0.1934, 0.2471)
##
      No Information Rate: 0.25
##
      P-Value [Acc > NIR] : 0.9874
##
##
                    Kappa: -0.0408
## Mcnemar's Test P-Value : <2e-16
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4
## Sensitivity
                         0.8439 0.033755 0.00000
                                                      0.00
## Specificity
                         0.2250 0.817159
                                                      1.00
                                          0.91702
## Pos Pred Value
                         0.2663 0.057971 0.00000
                                                       NaN
## Neg Pred Value
                         0.8122 0.717284 0.73341
                                                      0.75
## Prevalence
                         0.2500 0.250000 0.25000
                                                      0.25
## Detection Rate
                         0.2110 0.008439 0.00000
                                                      0.00
## Detection Prevalence
                         0.7922 0.145570 0.06224
                                                      0.00
## Balanced Accuracy 0.5345 0.425457 0.45851
                                                      0.50
```