

```

theory Hnr_Rules_Bind
  imports Hnr_Base Keep_Drop Norm Merge
begin

lemma hnr_bind [hnr_rule]:
  assumes
    "hnr  $\Gamma$   $vi$   $\Gamma_1$   $v$ "
    " $\wedge x\ xi.$  hnr ( $\Gamma_1\ x\ xi$ ) ( $fi\ xi$ ) ( $\Gamma'\ x\ xi$ ) ( $f\ x$ )"
    " $\wedge x\ xi\ r\ ri.$  Keep_Drop ( $\Gamma'\ x\ xi\ r\ ri$ ) ( $\Gamma''\ r\ ri$ ) ( $\Gamma_1'\ x\ xi\ r\ ri$ )"
    " $\wedge r\ ri.$  Norm ( $\Gamma''\ r\ ri$ ) ( $\Gamma'''\ r\ ri$ )"
  shows
    "hnr  $\Gamma$  (do {  $x \leftarrow vi$ ;  $fi\ x$  })  $\Gamma'''$  (do {  $x \leftarrow v$ ;  $f\ x$  })"
  supply[sep_heap_rules] = assms(1, 2)[THEN hnrD]
  apply(rule hnrI)
  apply(sep_auto split: option.splits Option.bind_splits(2))
  apply(sep_drule  $r$ : assms(3)[unfolded Keep_Drop_def])
  apply(sep_drule  $r$ : assms(4)[unfolded Norm_def])
  by sep_auto

end

```