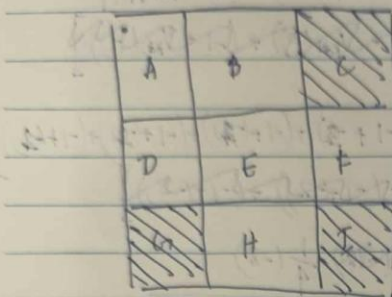


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Exercise 4: 3x3 Gridworld



States $S = \{A, B, C, D, E, F, G, H, I\}$

Actions $A = \{UP, DOWN, LEFT, RIGHT\}$

Policy P = From every state, choose each action with probability 0.25

Reward $R = -1$ per step

Discount factor $\gamma = 1$

Step 1: Compute value functions at $k=1$

$$v_{k+1}(s) = \frac{1}{4} \sum_{a \in A} [r(s, a) + v_k(s')]$$

• Reward $r(s, a) = -1$ for each step

• $v_0(s) = 0$ for all non-terminal states

• terminals $\{C, G, I\}$ remain 0

$$v_1(s) = \frac{1}{4} [(-1 + v_1(s_1)) + (-1 + v_1(s_2)) + (-1 + v_1(s_3)) + (-1 + v_1(s_4))]$$

$$v_1(A) = v_1(B) = v_1(D) = v_1(E) = v_1(F) = v_1(H) = -1$$

$$v_1(C) = v_1(G) = v_1(I) = 0$$

Since all $v_0 = 0$,
each term $= -1$
Thus, $v_1(s) = -1$

-1	-1	0
-1	-1	-1
0	-1	0

Step 2: Compute the action-value function and update the policy of states at $k=1$

• State A

$$q_{k+1}(A, \text{Left}) = -1 + (-1) = -2 \quad (A)$$

$$q_{k+1}(A, \text{Right}) = -1 + (-1) = -2 \quad (B)$$

$$q_{k+1}(A, \text{Up}) = -1 + (-1) = -2 \quad (A)$$

$$q_{k+1}(A, \text{Down}) = -1 + (-1) = -2 \quad (D)$$

$$\pi_{k+1}(A) = \{\text{Left, Right, Up, Down}\} \rightarrow$$

• State B

$$q_{k+1}(B, \text{Left}) = -1 + (-1) = -2 \quad (A)$$

$$q_{k+1}(B, \text{Right}) = -1 + 0 = -1 \quad (C)$$

$$q_{k+1}(B, \text{Up}) = -1 + (-1) = -2 \quad (B)$$

$$q_{k+1}(B, \text{Down}) = -1 + (-1) = -2 \quad (E)$$

$$\pi_{k+1}(B) = \{\text{Right}\} \rightarrow$$

• State D

$$q_{k+1}(D, \text{Left}) = -2 \quad (D)$$

$$(D, \text{Right}) = -2 \quad (E)$$

$$(D, \text{Up}) = -2 \quad (A)$$

$$(D, \text{Down}) = -1 \quad (G)$$

$$\pi_{k+1}(D) = \{\text{Down}\} \rightarrow$$

• State E

$$q_{k+1}(E, \text{Left}) = -2 \quad (D)$$

$$(E, \text{Right}) = -2 \quad (F)$$

$$(E, \text{Up}) = -2 \quad (B)$$

$$(E, \text{Down}) = -2 \quad (H)$$

$$\pi_{k+1}(E) = \{\text{Left, Right, Up, Down}\} \rightarrow$$

State F :- action set $S_F = \{ \text{left, right, up, down} \}$

$$g_{k+1}(F, \text{left}) = -2 \quad (E)$$

$$(F, \text{Right}) = -2 \quad (F)$$

$$(F, \text{Up}) = -1 \quad (C)$$

$$(F, \text{Down}) = -1 \quad (I)$$

$$A(F) = \{ \text{Up, Down} \}$$

State H :- $(-1) + (-1) = (-2)$

$$g_{k+1}(H, \text{left}) = -1 \quad (A)(G)$$

$$(H, \text{Right}) = -1 \quad (I)$$

$$(H, \text{Up}) = -2 \quad (E)$$

$$(H, \text{Down}) = -2 \quad (H)$$

$$A(H) = \{ \text{left, right} \}$$

