

Global cooling: the Snowball Earth transition in a climate model with drifting parameters

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Motivation

The current configuration of our planet allows two stable climates

- A warm state, resembling today's climate
- An ice-covered Snowball Earth.

Drastic changes in solar irradiance (e. g. volcanic ash in the atmosphere) may trigger a transition to the Snowball state.

Conversely, the sudden melting can be induced by greenhouse gases.

The driving mechanism behind both the freezing and melting processes is the **ice-albedo feedback**.

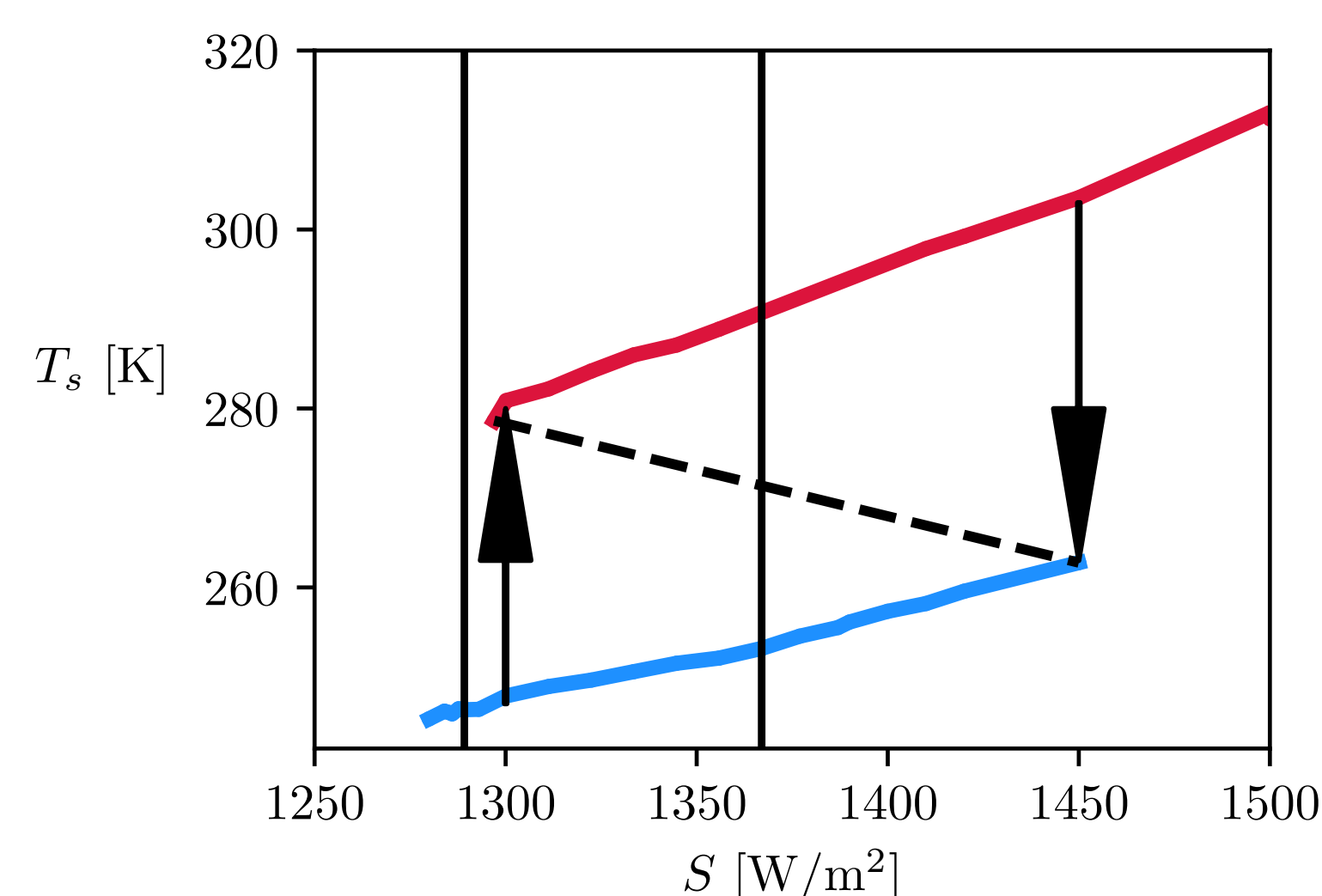
Plasim

The Snowball Earth transition is investigated in an intermediate-complexity climate model, **PlaSim** [1].

- T21 resolution, grid of $5^\circ \times 5^\circ$
- Atmosphere is coupled to a mixed layer ocean
- A dynamical system with 10^5 degrees of freedom

Introduction

Our goal is to investigate the transition between the two stable states (**attractors, from a dynamical point of view**), that coexist for a wide range of the solar constant S .



- Two dynamically different stable states exist. These are displayed on the **bifurcation diagram** [2, 3].
- Between the attractors, an unstable **edge state** is embedded in the basin boundary (dashed lines)
- At $S = S_{bif}$, the warm state loses stability
- **Assume a parameter drift scenario** $S(t)$ [see middle panel] for the solar constant

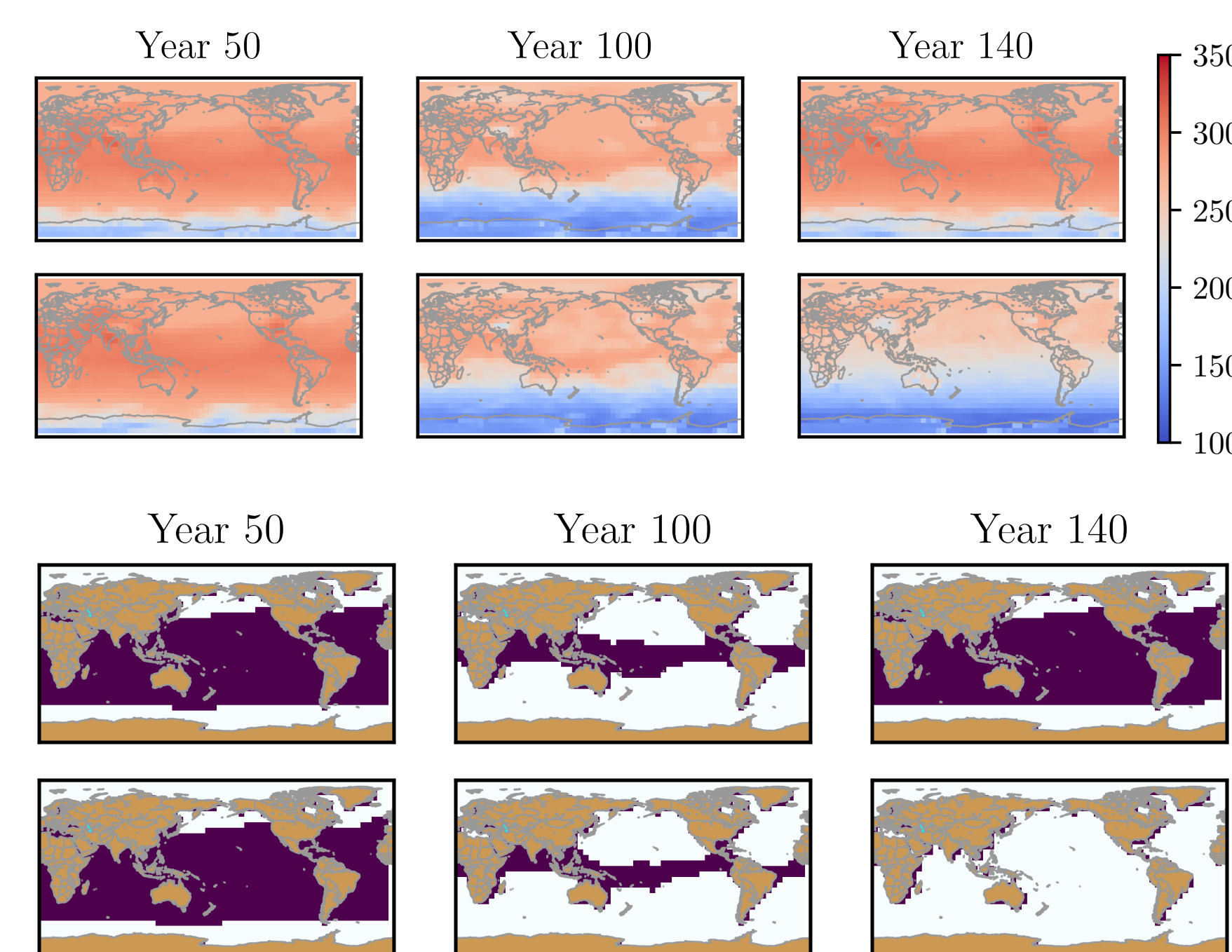
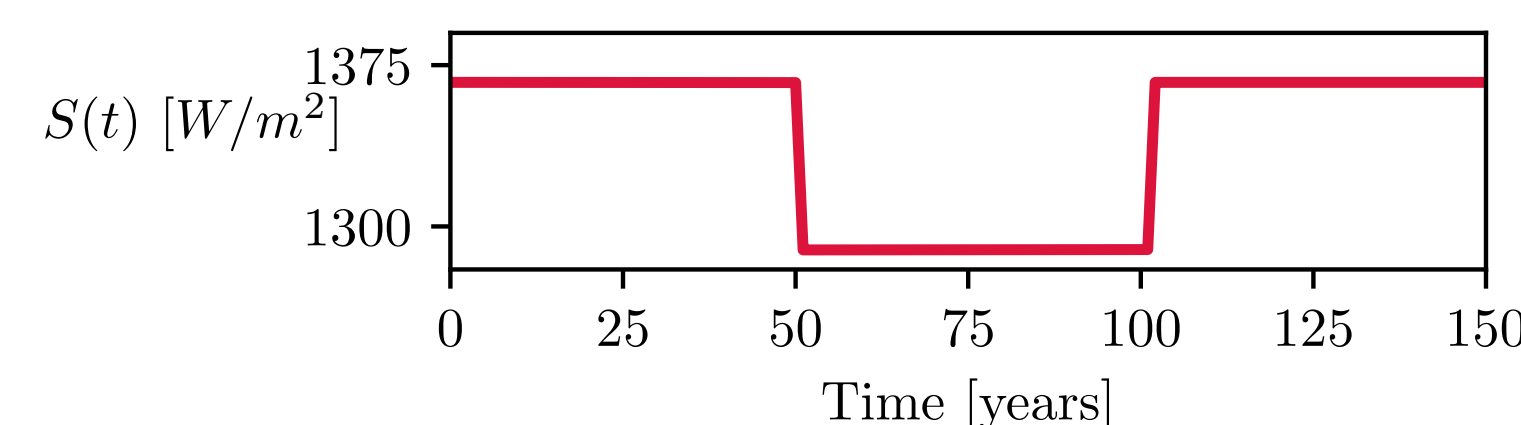
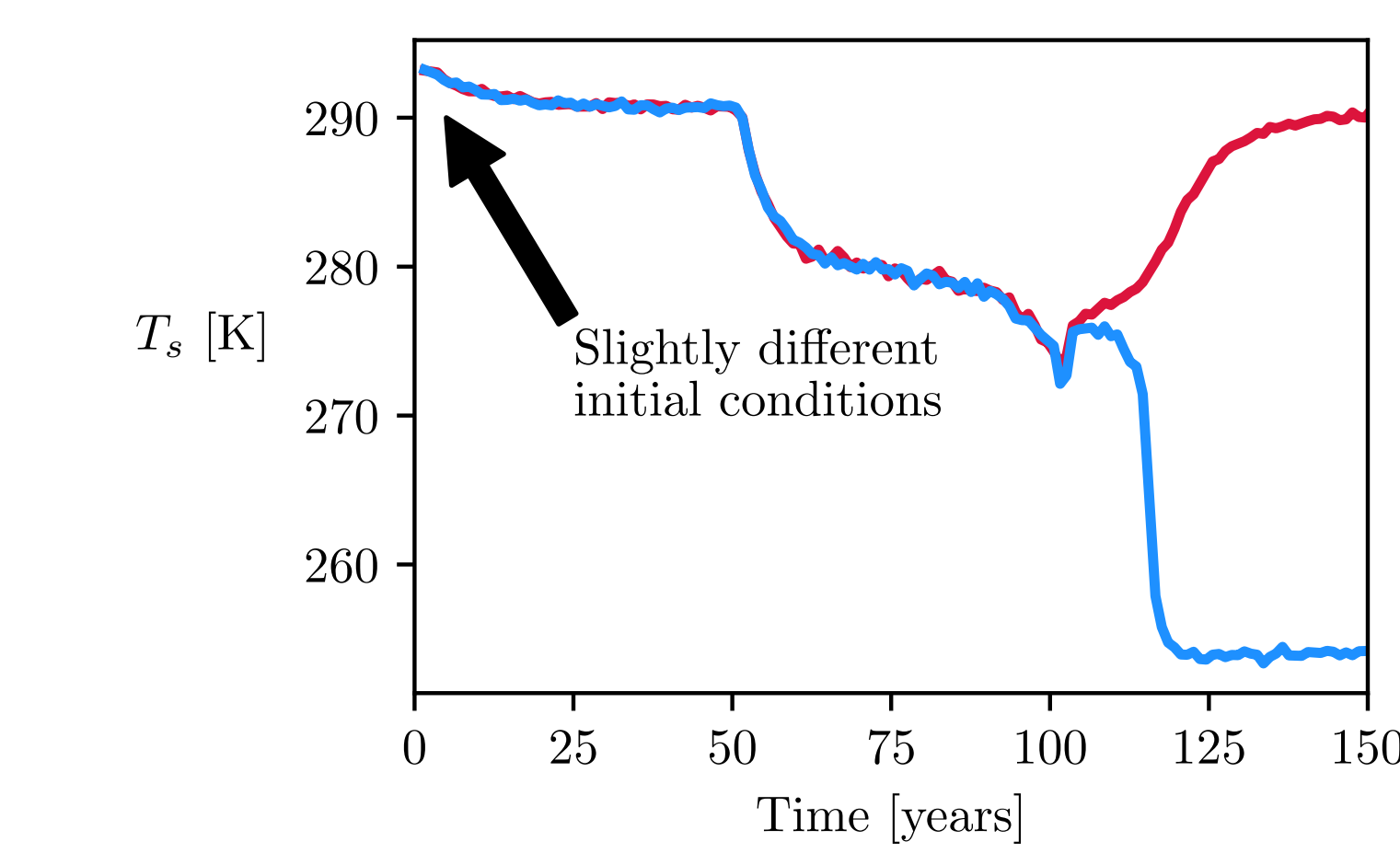
References, Acknowledgements

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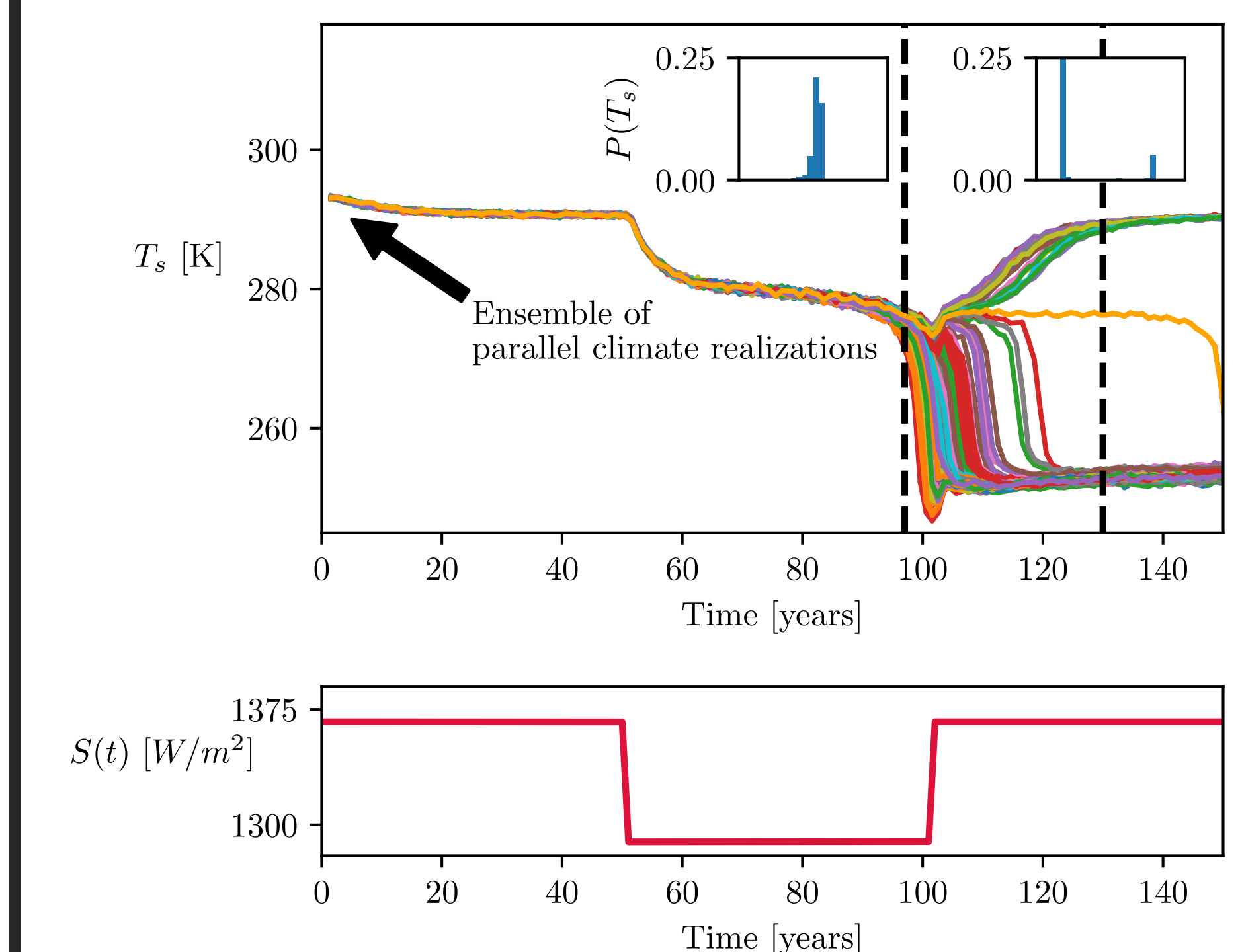
Individual simulations



- Small difference in initial conditions \Rightarrow **completely different outcomes**
- Individual simulations are **not representative** of the transition
- There is no way to determine which attractor the system will end up on

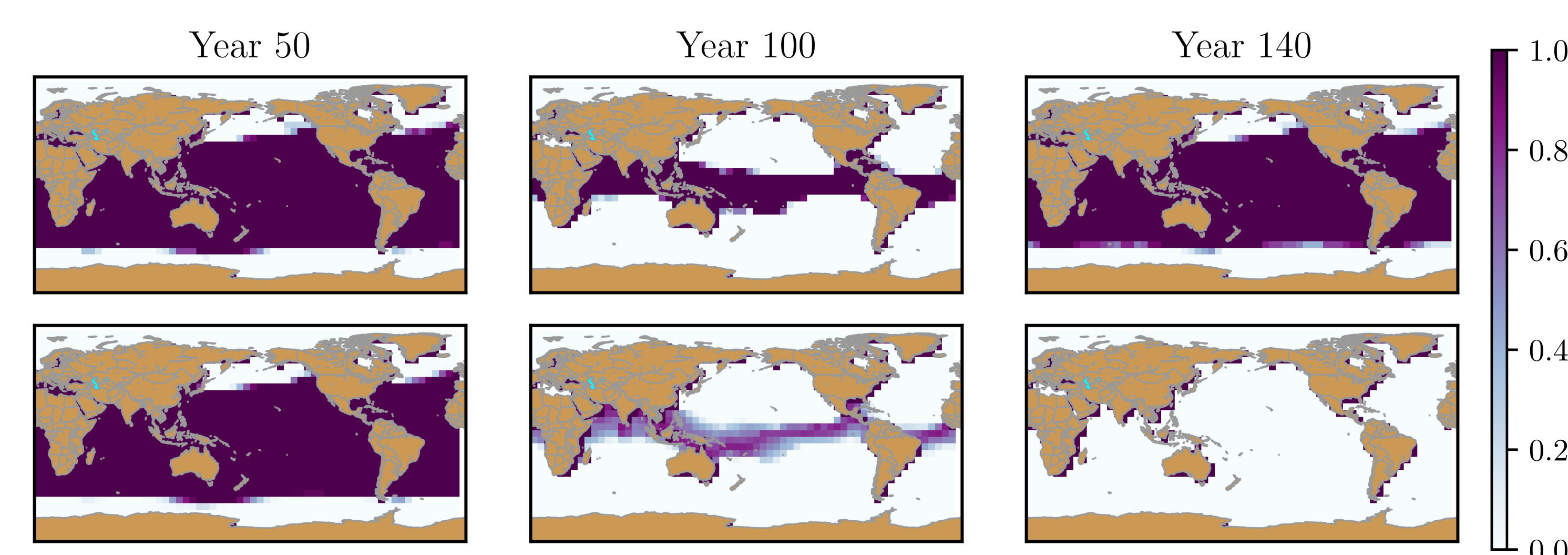
Ensemble of climate realizations

- Instead, follow an **ensemble** of parallel climate realizations [4]
- The 125 ensemble members converge to the **snapshot attractor** (or pullback attractor [5])
- Statistical quantities can be computed: **average, standard deviation**, with respect to its natural measure



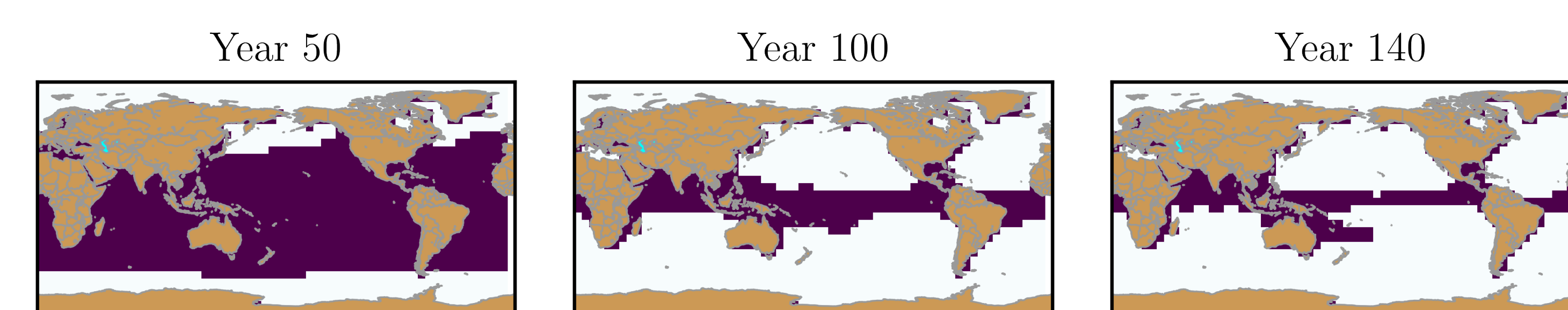
- The transition to Snowball Earth is **probabilistic**, no prediction is possible based on a single simulation
- The **snapshot attractor** splits into two, resulting in two types of typical behavior
- Before the splitting, the **standard deviation** of the ensemble grows: **precursor**
- The **orange curve** runs near the **time dependent edge state**

Typical sea ice cover ending in the two snapshot attractors



- The expected behavior (average) is computed over the two snapshot attractors
- **Local probability of sea ice formation**

Sea ice cover in the edge state



- Narrow band of **unfrozen sea** remaining at the Equator

Summary

- Individual trajectories are not meaningful
- Constructing the snapshot attractor with ensemble methods
- The snapshot attractor splits, which is preceded by increased standard deviation
- All three equilibria (two attractors and the edge state) are found

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Additional material on

