

# Homework 1

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**Due date: 3rd of March, 2022**, before the start of the lecture

Submission via email: [b.negyesi@tudelft.nl](mailto:b.negyesi@tudelft.nl).

Submissions should consist of an offline, compilable copy of the jupyter notebook and potentially a *short* .pdf report of your findings.

In this homework we are concerned with the classification task of handwritten digits. We aim to fit a statistical model which, given an input image of a handwritten digit, recognizes the digit and assigns the image to the proper class. For data we use the well-known [MNIST](#) database. The data can be downloaded by executing the following code snippet in a Google Colab notebook.

```
from torchvision.datasets import MNIST
dataset = MNIST('', train=False, download=True)

X = dataset.data.detach().numpy()
y = dataset.targets.detach().numpy()
```

This data is already preprocessed into the regression matrix  $X$  and the dependent variable  $y$ . In this example the regression matrix is an  $\mathbb{R}^{M \times 28 \times 28}$  *tensor* consisting of  $M = 10000$  samples of  $28 \times 28$  pixel images. Each sample corresponds to a different measurement. In every sample's image, each pixel's *value* corresponds to a *regressor* – these are the explanatory variables of the classification model. The true labels are found in the vector  $y \in \mathbb{R}^{10000}$ . In order to display a single image of the dataset you can deploy the `matplotlib` library. For instance, the following code snippet displays the first image in the dataset.

```
import matplotlib.pyplot as plt

idx = 0
img = X[idx, :, :]

plt.imshow(img)
plt.title('true_label: ' + str(y[idx]))
plt.show()
```

Using this dataset, and supplementary material provided on the Iris classification problem, solve the following exercises:

- Ex. 1 Formulate a binary Single Layer Perceptron model which classifies images based on whether it is an 8 or not. Report on the classification accuracy. In order to avoid infinite loops, replace your convergence condition with a `max_iteration`  $\leq 10^4$  criterion in your iteration scheme.

Extend your model in such a way that it distinguishes between *all* digits, i.e. given input image it assigns it a label in  $\{0, 1, \dots, 9\}$ . *Hint: recall how we extended binary logistic regression to the multinomial case during the lecture.*

- Ex. 2 Formulate a multinomial logistic regression model which distinguishes between digits. Fit it accordingly on the data using Newton's method. (You can use the corresponding module of [scikit](#) but be careful not to apply regularization.)
- Ex. 3 Use the pre-specified example's neural network class, and train both a shallow and deep neural network of given widths and depths. (Consider the provided `.train()` method as a *black-box* optimizer, and leave its specification as is.) Try different *activation* functions and justify your choices.
- Ex. 4 Compare the classification accuracy across the latter 3 methods. Gather confusion matrices. Highlight a few wrongly classified images and see if you can find a pattern.