## **PROBABILITY**

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## $13.3.4^{-1}$

In answering a question on a multiple choice test, a student either knows the answer or guesses. Let  $\frac{3}{4}$  be the probability that he knows the answer and  $\frac{1}{4}$  be the probability that he guesses. Assuming that a student who guesses at the answer will be correct with probability  $\frac{1}{4}$  what is the probability that the student knows the answer given that he answered it correctly?

**Solution:** Let  $X \in \{0,1\}$  where 0 denotes a guess and 1 denotes that he knows the answer. Let  $Y \in \{0,1\}$  where 0 being the case when the answer is incorrect and 1 being the case that the answer is correct. From the given information, The probability that the student knows the answer and he

Random variable	Description
X=0	Student guesses the answer
X=1	Student knows the answer
Y=0	Answer is incorrect
Y=1	Answer is correct

Table 2: Random variables X and Y

Pr(Event)	Value
Pr(Y=1   X=0)	0.25
Pr(Y=1 X=1)	1
Pr(X=0)	0.75
Pr(X=1)	0.25

Table 4: Probability of events X and Y

answered it correctly is

$$\Pr(X = 1 | Y = 1) = \frac{\Pr(Y = 1 | X = 1) \Pr(X = 1)}{\Pr(Y = 1 | X = 1) \Pr(X = 1) + \Pr(Y = 1 | X = 0) \Pr(X = 0)}$$
Hence,
$$\Pr(X = 1 | Y = 1) = \frac{0.25}{0.25 + 0.25 \times 0.75}$$

$$\Pr(X = 1 | Y = 1) = 0.571$$

<sup>&</sup>lt;sup>1</sup>Read question numbers as (CHAPTER NUMBER).(EXERCISE NUMBER).(QUESTION NUMBER)