

## Derivative Securities Fall 2019: Assignment 2

1. You believe that interest rates will rise. Accordingly, you

- A. Buy a December Eurodollar futures (true/false)
- B. Sell a December Eurodollar futures (true/false)
- C. Pay fixed on a 5-year swap (true/false)
- D. Receive fixed on a 5-year swap (true/false)

Explain carefully your answers.

2. Consider a FRA in which you will borrow money for 6 months on December 20, 2019 (T) based on the 3-month LIBOR rate:

Borrow \$1 on date T, return  $\$[1 + (0.5) \times (3M \text{ LIBOR}(T))]$  on date T+6 months.

Assume that you know the zero-coupon bond values (a) from today to the loan's inception (T), (b) from today to T+3M, and (c) from today to T+6M. What is the no-arbitrage value of the FRA?

[Hint: replicate the cash-flow of the loan by lending X dollars forward for 3 months, and reinvesting the proceeds and borrowing Y dollars forward for 6 months. Also note that if forward 3M-LIBOR < forward 6M-LIBOR, the FRA value should be positive, and it should be negative if the opposite inequality holds.]

Give a possible application of this result in the real world of swap pricing.

3. Build a smooth discount curve (Z-curve) with monthly granularity for LIBOR rates on October 8, 2019, using the following information:

LIBOR	
30 days	1.94%
90 days	2.01%
LIBOR SWAPS	
1-Year	1.67%
2-Year	1.47%
3-Year	1.39%
5-Year	1.35%
7-Year	1.38%
10-Year	1.45%
30-year	1.63%

4. Build the curve using the Hagan-West iteration method explained in p. 92 of that paper.