

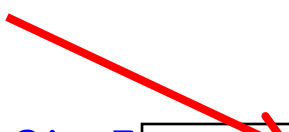
CMSC 330

Organization of Programming Languages

OCaml
Higher Order Functions

Anonymous Functions

- ▶ Use `fun` to make a function with no name

Parameter  Body
(in which parameter `x` is bound)

```
(fun x -> x + 3) 5
```

`fun x -> x + 3`

`= 8`

Anonymous Functions

► Syntax

- **fun** *x1* ... *xn* \rightarrow *e*

or $\text{let twice } f\ x = f(f\ x);$
 $(\text{* } ('a \rightarrow 'a) \rightarrow 'a \rightarrow 'a) \text{*})$

► Evaluation

- An anonymous function is an expression
- In fact, *it is a value*.

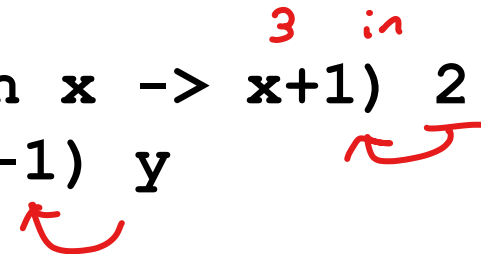
$\text{twice } (\text{fun } x \rightarrow x+1) 10;$
 /* returns 12 */

► Type checking

- $(\text{fun } x1 \dots xn \rightarrow e) : (t1 \rightarrow \dots \rightarrow tn \rightarrow u)$
when $e : u$ under assumptions $x1 : t1, \dots, xn : tn$.
 - (Same rule as $\text{let } f\ x1 \dots xn = e$)

Quiz 1: What does this evaluate to?

`let y = (fun x -> x+1) 2 in
(fun z -> z-1) y`



A. *Error*

B. 2

C. 1

D. 0

let y = 3 in (fun z -> z-1) y

fun z -> 3 - 1

2

Quiz 1: What does this evaluate to?

```
let y = (fun x -> x+1) 2 in  
(fun z -> z-1) y
```

A. *Error*

B. 2

C. 1

D. 0

Quiz 2: What is this expression's type ?

`(fun x y -> x) 2 3`

A. *Type error*

B. `int`

C. `int -> int -> int`

~~D. `'a -> 'b -> 'a`~~

Quiz 2: What is this expression's type ?

`(fun x y -> x) 2 3`

A. *Type error*

B. **int**

C. `int -> int -> int`

D. `'a -> 'b -> 'a`

Functions and Binding

- ▶ Functions are **first-class**, so you can bind them to other names as you like

```
let f x = x + 3;;
```

```
let g = f; ≠ 8
```

```
g 5
```


Example Shorthands

- ▶ `let` for functions is a syntactic shorthand
`let f x = body` is semantically equivalent to
`let f = fun x -> body`
- ▶ `let next x = x + 1`
 - Short for `let next = fun x -> x + 1`
- ▶ `let plus x y = x + y`
 - Short for `let plus = fun x y -> x + y`

Quiz 3: What does this evaluate to?

```
let f = fun x -> 0 in
let g = f in
let h = fun y -> g (y+1) in
h 1
```

- A. 0
- B. 1
- C. 2
- D. *Error*

Quiz 3: What does this evaluate to?

```
let f = fun x -> 0 in  
let g = f in  
let h = fun y -> g (y+1)  
h 1
```

A. 0

B. 1

C. 2

D. *Error*

Nested Functions

```
(* Filter the odd numbers from a list *)  
let filter lst =  
    let rec aux l =  
        match l with  
        | [] -> []  
        | h::t-> if h mod 2 <> 0 then h::aux t  
                  else aux t  
    in  
    aux lst  
  
filter [1;2;3;4;5;6] (* int list = [1; 3; 5] *)
```

Passing Functions as Arguments

You can pass functions as arguments

```
let plus3 x = x + 3 (* int -> int *)
```

```
let twice f z = f (f z)  
(* ('a->'a) -> 'a -> 'a *)
```

```
twice plus3 5 = 11
```