

## C++ Logical & Bitwise Operators – Concise Notes

### 1. Two Categories of Operators

**Bitwise Operators:** Work on individual bits of integers.

- &, |, ^, ~

**Logical Operators:** Work on truth values (true/false).

- &&, ||, !

### 2. Bitwise Operators

& → AND (bit-by-bit)

| → OR (bit-by-bit)

^ → XOR (1 if bits differ)

~ → NOT (flips every bit, including sign bit)

### 3. Logical Operators

&& → Logical AND (short-circuit)

|| → Logical OR (short-circuit)

! → Logical NOT

Note: Logical operators return only 0 or 1.

### 4. Key Difference

a & b → Bitwise operation on bits

a && b → Logical operation on truth values

Logical operators may skip evaluation (short-circuit).

### 5. Logic Gates Using Operators

AND → a & b / a && b

OR → a | b / a || b

XOR → a ^ b

NOT → ~a / !a

NAND → ~(a & b) / !(a && b)

NOR → ~(a | b) / !(a || b)

XNOR → ~(a ^ b)

### 6. Sign Bit

The leftmost bit in a signed integer.

0 → positive number

1 → negative number

### 7. Two's Complement Representation

Used by almost all modern systems.

Rule:  $\sim x = -x - 1$

Negative numbers are represented by flipping bits and adding 1.

### 8. Why ~ Changes Sign

~ flips all bits including the sign bit.

Result depends on integer size (8-bit, 32-bit, etc.).

### 9. Important Takeaways

- Use bitwise operators for low-level bit manipulation.
- Use logical operators for conditions and control flow.
- Never confuse & with && or | with ||.
- Sign bit flip is a side effect, not intent.