

COT 4420: Homework 2

Finite Automata

Unless stated otherwise, the base alphabet in this problem set is $\Sigma = \{0,1\}$.

1. Tricky: The language $L = \{w \mid w \text{ contains as many occurrences of the substring "01" as occurrences of the substring "10"}\}$ is regular. Prove it by giving an FA (deterministic or non-deterministic) for L . Explain why this FA accepts this language. **[1]**

Examples:

- accepted: 010, 1000101
 - not accepted: 011, 010101
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2. Give a DFA for all strings that have an odd number of 1s and an even number of 0s. **[1/2]**

3. Give a DFA for the language D :

- ϵ is in D
- if s is in D , then both $s00$ and $s11$ are also in D **[1/2]**

4. Give an FA (NFA is probably easiest) that accepts $\{w \mid w \text{ ends with an even number of 0s}\}$. **[1]**

5. Specify (in English) an algorithm that takes a DFA (as a graph or a table, your choice) and checks whether the language of the DFA is finite **[1]**
