

## Cryptopangrams (10pts, 15pts)

### Problem

On the Code Jam team, we enjoy sending each other *pangrams*, which are phrases that use each letter of the English alphabet at least once. One common example of a pangram is "the quick brown fox jumps over the lazy dog". Sometimes our pangrams contain confidential information — for example, CJ QUIZ: KNOW BEVY OF DP FLUX ALGORITHMS — so we need to keep them secure.

We looked through a cryptography textbook for a few minutes, and we learned that it is very hard to factor products of two large prime numbers, so we devised an encryption scheme based on that fact. First, we made some preparations:

- We chose 26 different prime numbers, none of which is larger than some integer **N**.
- We sorted those primes in increasing order. Then, we assigned the smallest prime to the letter **A**, the second smallest prime to the letter **B**, and so on.
- Everyone on the team memorized this list.

Now, whenever we want to send a pangram as a message, we first remove all spacing to form a plaintext message. Then we write down the product of the prime for the first letter of the plaintext and the prime for the second letter of the plaintext. Then we write down the product of the primes for the second and third plaintext letters, and so on, ending with the product of the primes for the next-to-last and last plaintext letters. This new list of values is our ciphertext. The number of values is one smaller than the number of characters in the plaintext message.

For example, suppose that **N** = 103 and we chose to use the first 26 odd prime numbers, because we worry that it is too easy to factor even numbers. Then **A** = 3, **B** = 5, **C** = 7, **D** = 11, and so on, up to **Z** = 103. Also suppose that we want to encrypt the CJ QUIZ... pangram above, so our plaintext is CJQUIZKNOWBEVYOFDPFLUXALGORITHMS. Then the first value in our ciphertext is 7 (the prime for **C**) times 31 (the prime for **J**) = 217; the next value is 1891, and so on, ending with 3053.

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	AA
1	3	5	7	11	13	17	19	23	29	31	37	41	43	47	53	59	61	67	71	73	79	83	89	97	101	103	
2	9	15	21	33	39	51	57	69	87	93	111	123	129	141	159	177	183	201	213	219	237	249	267	291	303	309	3
3	15	25	35	55	65	85	95	115	145	155	185	205	215	235	265	295	305	335	355	365	395	415	445	485	505	515	5
4	21	35	49	77	91	119	133	161	203	217	259	287	301	329	371	413	427	469	497	511	553	581	623	679	707	721	7
5	33	55	77	121	143	187	209	253	319	341	407	451	473	517	583	649	671	737	781	803	869	913	979	1067	1111	1133	11
6	39	65	91	143	169	221	247	299	377	403	481	533	559	611	689	767	793	871	923	949	1027	1079	1157	1261	1313	1339	13
7	51	85	119	187	221	289	323	391	493	527	629	697	731	799	901	1003	1037	1139	1207	1241	1343	1411	1513	1649	1717	1751	17
8	57	95	133	209	247	323	361	437	551	589	703	779	817	893	1007	1121	1159	1273	1349	1387	1501	1577	1691	1843	1919	1957	19
9	69	115	161	253	299	391	437	529	667	713	851	943	989	1081	1219	1357	1403	1541	1633	1679	1817	1909	2047	2231	2323	2369	23
10	87	145	203	319	377	493	551	667	841	899	1073	1189	1247	1363	1537	1711	1769	1943	2059	2117	2291	2407	2581	2813	2929	2987	29
11	93	155	217	341	403	527	589	713	899	961	1147	1271	1333	1457	1643	1829	1891	2077	2201	2263	2449	2573	2759	3007	3131	3193	31
12	111	185	259	407	481	629	703	851	1073	1147	1369	1517	1591	1739	1961	2183	2257	2479	2627	2701	2923	3071	3293	3589	3737	3811	37
13	123	205	287	451	533	697	779	943	1189	1271	1517	1681	1763	1927	2173	2419	2501	2747	2911	2993	3239	3403	3649	3977	4141	4223	41
14	129	215	301	473	559	731	817	989	1247	1333	1591	1763	1849	2021	2279	2537	2623	2881	3053	3139	3397	3569	3827	4171	4343	4429	43
15	141	235	329	517	611	799	893	1081	1363	1457	1739	1927	2021	2209	2491	2773	2867	3149	3337	3431	3713	3901	4183	4559	4747	4841	47
16	159	265	371	583	689	901	1007	1219	1537	1643	1961	2173	2279	2491	2809	3127	3233	3551	3763	3869	4187	4399	4717	5141	5353	5459	53
17	177	295	413	649	767	1003	1121	1357	1711	1829	2183	2419	2537	2773	3127	3481	3599	3953	4189	4307	4661	4897	5251	5723	5959	6077	59
18	183	305	427	671	793	1037	1159	1403	1769	1891	2257	2501	2623	2867	3233	3599	3721	4087	4331	4453	4819	5063	5429	5917	6161	6283	61
19	201	335	469	737	871	1139	1273	1541	1943	2077	2479	2747	2881	3149	3551	3953	4087	4489	4757	4891	5293	5561	5963	6499	6767	6901	67
20	213	355	497	781	923	1207	1349	1633	2059	2201	2627	2911	3053	3337	3763	4189	4331	4757	5041	5183	5609	5893	6319	6887	7171	7313	71
21	219	365	511	803	949	1241	1387	1679	2117	2263	2701	2993	3139	3431	3869	4307	4453	4891	5183	5329	5767	6059	6497	7081	7373	7519	73
22	237	395	553	869	1027	1343	1501	1817	2291	2449	2923	3239	3397	3713	4187	4661	4819	5293	5609	5767	6241	6557	7031	7663	7979	8137	79
23	249	415	581	913	1079	1411	1577	1909	2407	2573	3071	3403	3569	3901	4399	4897	5063	5561	5893	6059	6557	6889	7387	8051	8383	8549	83
24	267	445	623	979	1157	1513	1691	2047	2581	2759	3293	3649	3827	4183	4717	5251	5429	5963	6319	6497	7031	7387	7921	8633	8989	9167	89
25	291	485	679	1067	1261	1649	1843	2231	2813	3007	3589	3977	4171	4559	5141	5723	5917	6499	6887	7081	7663	8051	8633	9409	9797	9991	97
26	303	505	707	1111	1313	1717	1919	2323	2929	3131	3737	4141	4343	4747	5353	5959	6161	6767	7171	7373	7979	8383	8989	9797	10201	10403	101
27	309	515	721	1133	1339	1751	1957	2369	2987	3193	3811	4223	4429	4841	5459	6077	6283	6901	7313	7519	8137	8549	9167	9991	10403	10609	103

We will give you a ciphertext message and the value of **N** that we used. We will not tell you which primes we used, or how to decrypt the ciphertext. Do you think you can recover the plaintext anyway?

## Input

The first line of the input gives the number of test cases, **T**. **T** test cases follow; each test case consists of two lines. The first line contains two integers: **N**, as described above, and **L**, the length of the list of values in the ciphertext. The second line contains **L** integers: the list of values in the ciphertext.

## Output

For each test case, output one line containing `Case #x: y`, where *x* is the test case number (starting from 1) and *y* is a string of **L** + 1 uppercase English alphabet letters: the plaintext.

## Limits

$1 \leq T \leq 100$ .

Time limit: 20 seconds per test set.

Memory limit: 1 GB.

$25 \leq L \leq 100$ .

The plaintext contains each English alphabet letter at least once.

### Test set 1 (Visible)

$101 \leq N \leq 10000$ .

### Test set 2 (Hidden)

$101 \leq N \leq 10^{100}$ .

## Sample

### Input

```
2
103 31
217 1891 4819 2291 2987 3811 1739 2491 4717 445 65 1079 8383 5353 901 187 649 1003
697 3239 7663 291 123 779 1007 3551 1943 2117 1679 989 3053
10000 25
3292937 175597 18779 50429 375469 1651121 2102 3722 2376497 611683 489059 2328901
3150061 829981 421301 76409 38477 291931 730241 959821 1664197 3057407 4267589
4729181 5335543
```

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### Output

```
Case #1: CJQUIZKNOWBEVYOFDPFLUXALGORITHMS
Case #2: SUBDERMATOGLYPHICFJKNQVWXZ
```