

Laboratory work 2  
(Variant 3)  
Geometrical Transformations, Convolution, and Maxpooling

**Objective:** the purpose of this laboratory work is to study basic geometric transformations and core CNN operations.

**The submission includes:** ipynb and the report file. The report should include step-by-step description, results, and screenshots. Format the report according to the template.

**Task 1. Geometrical transformations affine**

Resize the image to  $256 \times 256$ . Use source points  $(x, y)$ :  $(30, 30), (200, 40), (40, 210)$  and destination points  $(x, y)$ :  $(40, 50), (210, 60), (60, 220)$ . Compute the affine matrix using `cv2.getAffineTransform` and apply it using `cv2.warpAffine`. Use the same order for source and destination points: point1 to point1, point2 to point2, point3 to point3. Display side by side the original image and the affine transformed image.

**Task 2. Affine matrix printing and point verification**

Print the affine matrix  $M (2 \times 3)$  from Task 1. Use three points  $(x, y)$  on the original image:  $(30, 30), (128, 128), (220, 180)$ . Transform these points using `cv2.transform()` with matrix  $M$  and print the coordinates before and after. Draw the original points on the original image and the transformed points on the affine image.

**Task 3. Nonlinear geometric transformation using remap**

Create a nonlinear warp using `cv2.remap`. Build `map_x` and `map_y` as `float32` arrays of size  $256 \times 256$ . Apply a sinusoidal horizontal shift using amplitude  $A = 12$  pixels and frequency  $f = 2$  periods across the image width. Use interpolation `cv2.INTER_LINEAR` and borderMode `cv2.BORDER_REFLECT`. Apply `cv2.remap` and display side by side the original image and the nonlinear transformed image.

**Task 4. Pixel value check for nonlinear transform**

Use pixel coordinate  $(x, y) = (70, 160)$  where  $x$  is the column index and  $y$  is the row index. Print the RGB value at  $(70, 160)$  in the original image and print the RGB value at  $(70, 160)$  in the nonlinear transformed image from Task 3. Add 1–2 sentences explaining why pixel values at the same coordinate may differ after nonlinear transformation.

**Task 5. Convolution with OpenCV blur**

Create a  $3 \times 3$  blur kernel and apply convolution using `cv2.filter2D`. Convert the original image and the blurred image to grayscale. Display the grayscale original image and the grayscale blurred image side by side. Print the  $5 \times 5$  grayscale patch from rows 90 to 94 and columns 90 to 94 for the original grayscale image and for the blurred grayscale image.

**Task 6. Convolution with OpenCV sharpening**

Create a  $3 \times 3$  sharpening kernel and apply convolution using `cv2.filter2D`. Convert the sharpened result to grayscale. Display the grayscale original image and the grayscale sharpened image side by side. Print the same  $5 \times 5$  grayscale patch from rows 90 to 94 and columns 90 to 94 for the sharpened grayscale image. Write 2–3 sentences comparing blur and sharpen.

### Task 7. Convolution from scratch NumPy

Implement 2D convolution manually using NumPy for the blur kernel from Task 5. Use zero padding so that the output size matches  $256 \times 256$ . Display your manual convolution result and the cv2.filter2D blur result side by side. Print the same  $5 \times 5$  grayscale patch from rows 90 to 94 and columns 90 to 94 from both results.

### Task 8. Maxpooling NumPy

Using the blurred grayscale image from Task 5, implement maxpooling with window size  $2 \times 2$  and stride 2. Print the input shape and output shape. Print the  $4 \times 4$  grayscale block from rows 90 to 93 and columns 90 to 93 from the input and print the corresponding  $2 \times 2$  pooled block from rows 45 to 46 and columns 45 to 46 from the output because stride = 2. Display the input grayscale image and the pooled image side by side.

### Task 9. Manual calculation of convolution

Compute the convolution output value manually for the given input patch and kernel. Show all 9 multiplications and the final sum. Do not use OpenCV or NumPy convolution functions.

Input patch

2 1 3

0 4 2

1 2 0

Kernel

1 1 1

1 1 1

1 1 1

### Task 10. Manual calculation of maxpooling

Compute maxpooling manually for the given  $4 \times 4$  matrix using window size  $2 \times 2$  and stride 2. Show the four  $2 \times 2$  windows and the chosen maximum for each window. Write the final  $2 \times 2$  output matrix. Do not use OpenCV or NumPy pooling functions.

Input matrix

3 1 4 2

0 5 2 1

6 2 1 7

4 3 0 5