

# Vehicle Dynamics and Simulation

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# Torque Generation

# Intake manifold

- Can be represented as open system of constant volume.
- System stores mass and energy, represented by state variables  $P$  and  $T$ .

- Mass balance;

$$\frac{dm}{dt} = \dot{m}_{in} - \dot{m}_{out} \quad (1)$$

- Energy balance;

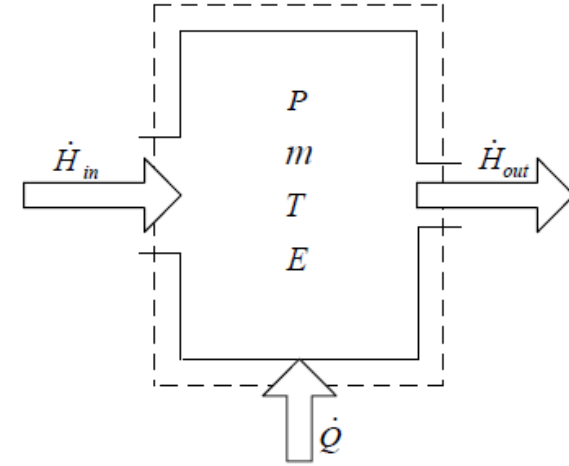
$$\frac{dE}{dt} = \dot{m}_{in}h_{0_{in}} - \dot{m}_{out}h_{0_{out}} + \dot{Q} \quad (2)$$

- Where;

$$h_0 = C_p T + \frac{u^2}{2}$$

And the energy within the volume is;

$$E = mc_v T + \frac{mu^2}{2} + mgz$$



# Intake manifold

- Making some assumptions
  - GPE change is 0
  - KE change is 0
- So that;

$$\begin{aligned} E &= mc_v T \\ h_0 &= c_p T \end{aligned} \quad (3)$$

- Taking the derivative wrt to  $t$ ;

$$\frac{dE}{dt} = c_v T \frac{dm}{dt} + c_v m \frac{dT}{dt} \quad (4)$$

- And by substitution (1, 3, 4 into 2);

$$c_v T (\dot{m}_{in} - \dot{m}_{out}) + c_v m \frac{dT}{dt} = \dot{m}_{in} C_p T_{in} - \dot{m}_{out} C_p T_{out} + \dot{Q} \quad (5)$$

# Intake manifold

- Coupling the energy and mass balances using the ideal gas law;

$$m = \frac{PV}{RT} \quad (6)$$

- Taking the derivative;

$$\frac{dm}{dt} = \frac{V}{RT} \frac{dP}{dt} - \frac{PV}{RT^2} \frac{dT}{dt} \quad (7)$$

- Substituting (1, 6 and 7 into 5) and assuming  $T_{out} = T$ ;

$$\frac{dT}{dt} = \left[ c_p \dot{m}_{in} T_{in} - c_p \dot{m}_{out} T - c_v T \dot{m}_{in} + \frac{dQ}{dt} \right] \frac{RT}{c_v PV} \quad (8)$$

$$\frac{dP}{dt} = \left[ c_p \dot{m}_{in} T_{in} - c_p \dot{m}_{out} T + \frac{dQ}{dt} \right] \frac{R}{c_v V} \quad (9)$$

And;

$$\frac{dQ}{dt} = hA_{wall}(T_{wall} - T) \quad (7)$$

# Torque model

- Torque produced is a function of;
  - Spark advance
  - Inducted air mass flow
  - AFR
- Data is usually obtained experimentally and incorporated within a regression model.
- Friction torque is deducted (imep – bmep) to establish output torque.
- Fmep is calculated;

$$fmep = 0.97 + 0.15 \left( \frac{N}{1000} \right) + 0.05 \left( \frac{N}{1000} \right)^2$$

- And;

$$T_f = \frac{fmep V_{sw}}{4\pi} = \frac{0.97 + 0.15 \left( \frac{N}{1000} \right) + 0.05 \left( \frac{N}{1000} \right)^2}{4\pi} V_{sw}$$

# Parameterisation effort

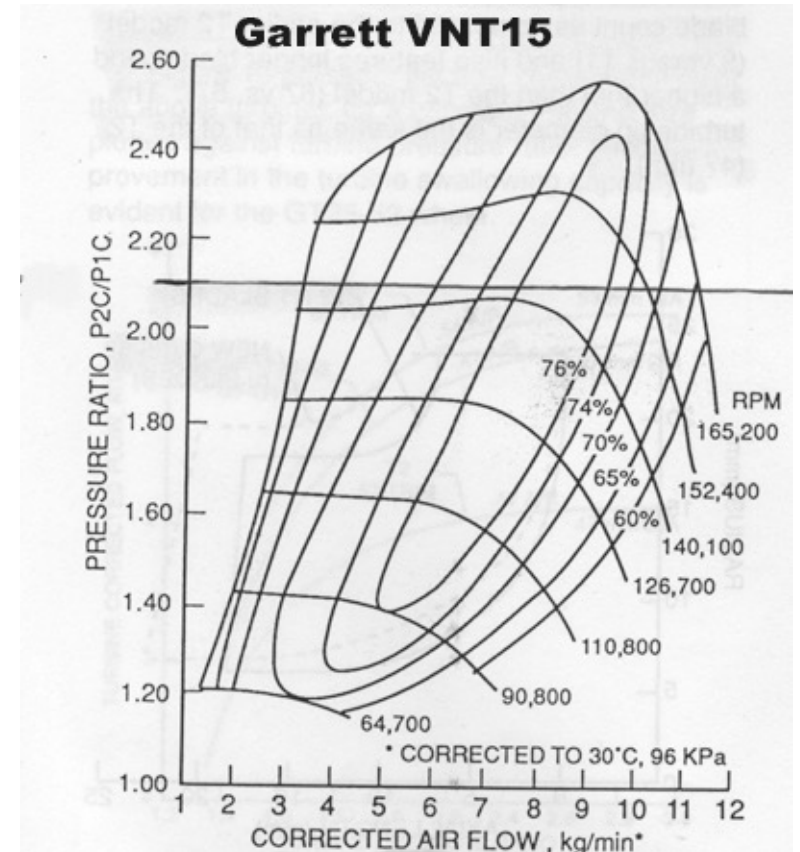
- Model has 5 unknown parameters,  $C_d$ ,  $\eta_{vol}$ ,  $h$ ,  $V$  and  $V_{disp}$ .
- With  $\eta_{vol} = f(P, T, N, IVO, EVC)$
- $\eta_{vol}$  is obtained by experiment at some  $P, T, N, IVO, EVC$ . Recall;

$$\eta = \frac{120\dot{m}_{actual}}{\rho V_{disp} N_{eng}}$$

- $C_d$  is also experimentally obtained (usually on flow rigs)
- Obtaining  $h$  in reality is very difficult and this is normally one of the tuned parameters.
- $V$  and  $V_{disp}$  are obtained relatively easily but can also be used to tune the model response to match reality.

# Other considerations

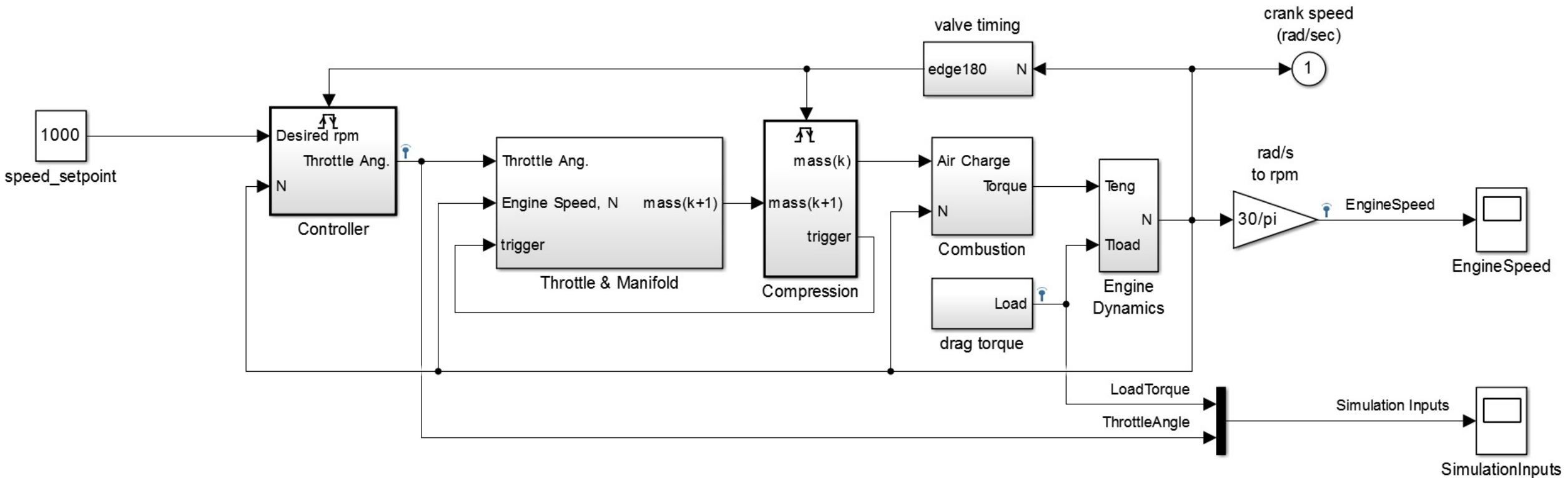
- Adding a turbocharger complicates matters significantly and introduces a causality loop.
  - The loop is normally broken by a delay.
- Heat transfer from the exhaust manifold has a significant effect on the turbo performance.
- Errors in the 'turbo loop' are accumulated within the loop.
- Each additional volume adds two model states (T and P) increasing significantly the computational burden.
- Volumes of very different sizes result in stiff models i.e. slow and fast dynamics.





# Crossley and Cook Model

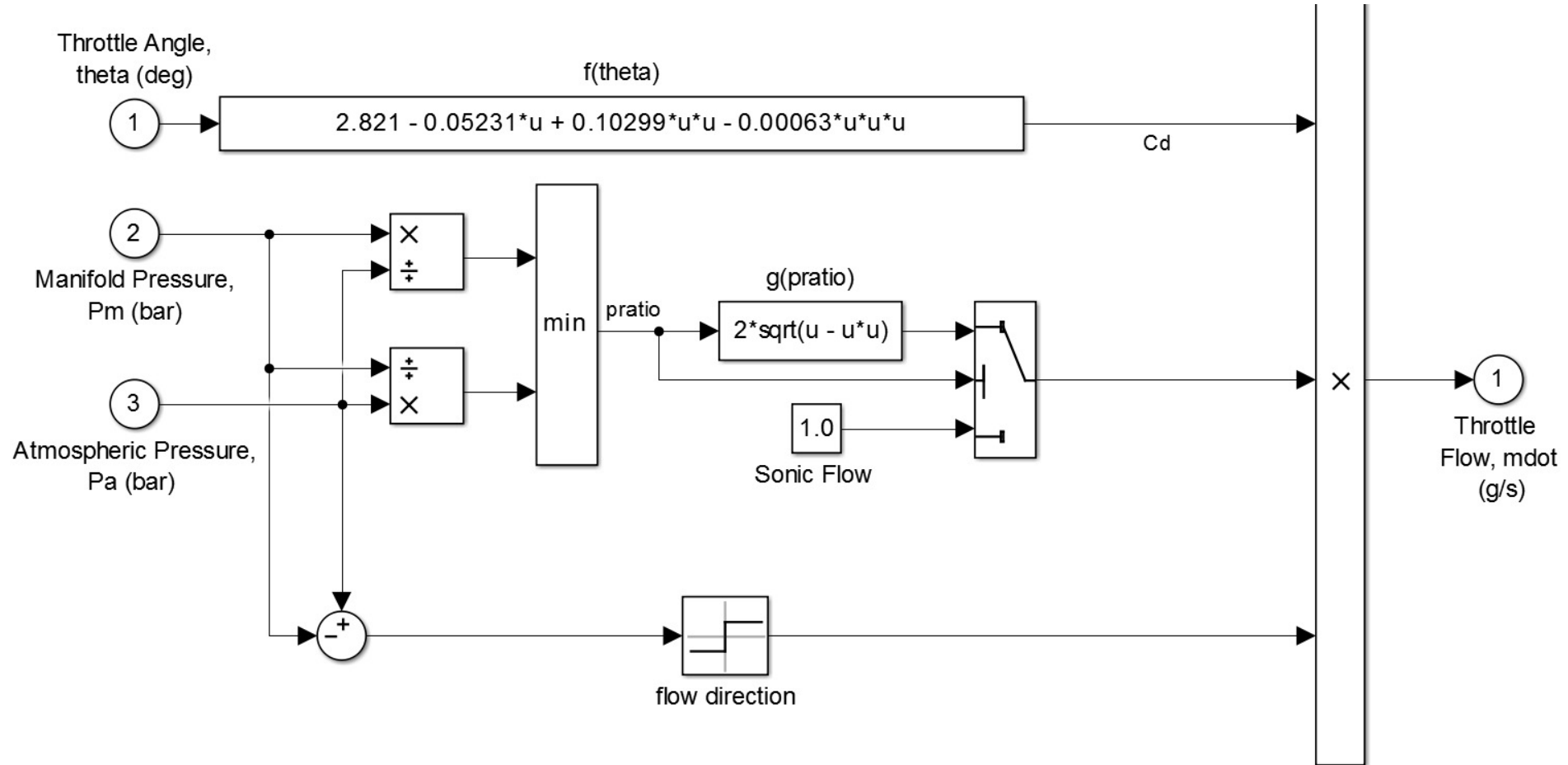
## Engine Timing Model with Closed-Loop Control



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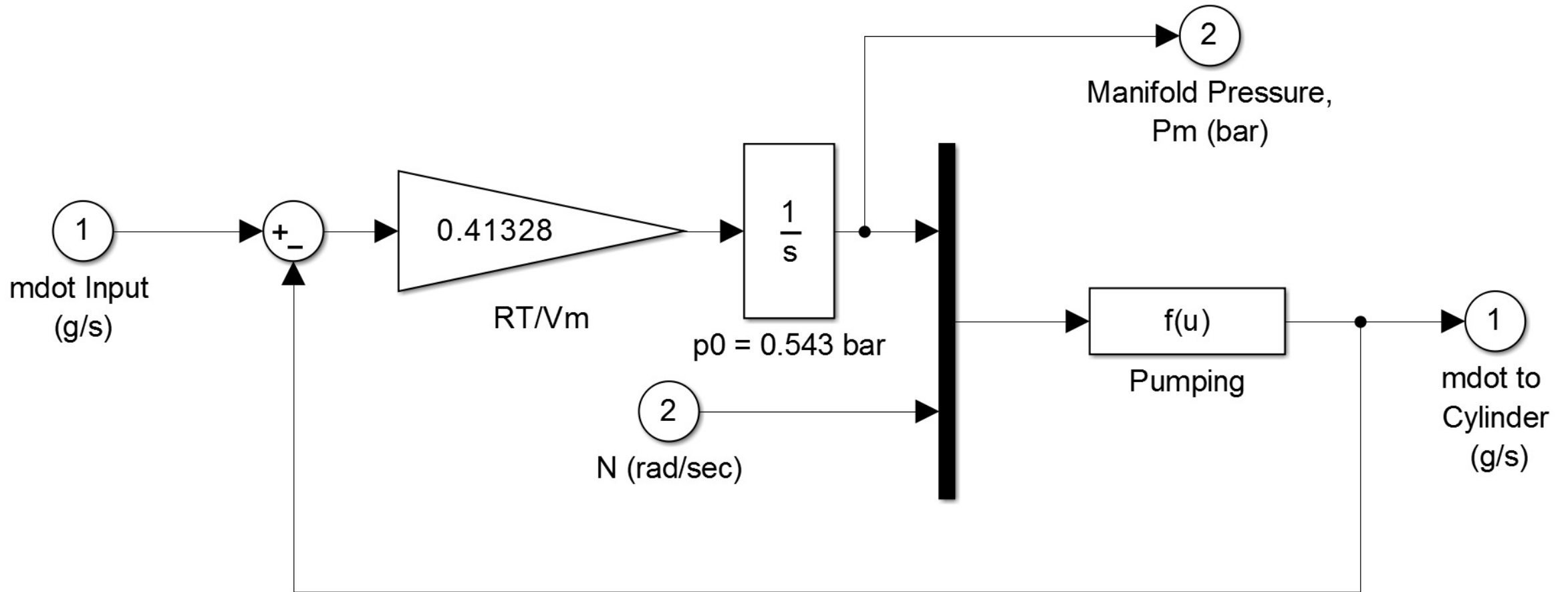
# Crossley and Cook Model

## Throttle



# Crossley and Cook Model

## Intake Manifold



# Crossley and Cook Model

## Torque Generation

