

This assignment will introduce you to basic Java constructs and give you a glimpse into how Discrete Math will come into play in coding and understanding code. You will implement a few Java programs, test them thoroughly, and hand them in. Additionally, you will do some math, type it up, and hand in a PDF. It's imperative that you use Java 17. You'll hand in this assignment on Canvas.

For each task, write helper functions as you see fit. Strive to write code that promotes clarity.

Typesetting Requirements. For written questions, you must *properly typeset* your answer, produce a PDF file called `hw1.pdf`, and add it to the zip file that you will upload to Canvas. No other format will be accepted. To typeset your homework, apart from Microsoft Word, there are LibreOffice and LaTeX, which we recommend. Note that a scan of your handwritten solution will not be accepted. You can find helpful resources about how to typeset your work on the course website.

Our policy on (gen)AI Usage for this assignment:

For this assignment, you must write every element of the code yourself. If you wish, use generative AI (genAI) to help you with Java syntax questions and steer you towards the solution. Using AI to fully solve the tasks for you will defeat the purpose of this assignment.

Hand-in Files: The zip file that you hand in must contain only the files listed below, all in the top-level directory. No extraneous files should be included. For us, filenames are case sensitive—that is to say, `Hello.java` is different from `hello.java`.

`workspace.jpg` `hw1.pdf` `SumEven.java` `Diamond.java` `Roman.java`
`Fib.java` `Subsel.java` `Happy.java` `Hidden.java`

Collaboration

We interpret collaboration very liberally. You may work with other students. However, each student **must** write up and hand in his or her assignment separately. Let us repeat: You need to write your own code. You must not look at or copy someone else's code. You need to write up answers to written problems individually. The fact that you can recreate the solution from memory will be taken as proof that you actually understood it, and you may actually be interviewed about your answers.

Be sure to indicate who you have worked with (refer to the hand-in instructions).

Logistics

We're using a script to grade your submission before any human being looks at it. Sadly, the script is not very forgiving. *So, make sure you follow the instructions strictly.* It's a bad omen when the course staff has to manually recover your file because the script doesn't like it. Hence:

- Save your work in a file as described in the task description. This will be different for each task.
Do not save your file(s) with names other than specified.
- You'll zip these files into a single file called `a1.zip` and you will upload this one zip file to Canvas before the due date.
- Attempt to solve each task on your own first. After a day, if you still can't solve a task, come to office hours.
- Before handing anything in, you should thoroughly test everything you write.
- The course staff is here to help. We'll steer you toward solutions. Catch us in real-life or online.

Task 1: Install Java 17 and an IDE on your computer (0 points)

In the first few weeks of this class, we'll be using a text/code editor to write Java programs. We recommend IntelliJ as the IDE of choice and VSCode if you somehow can't use IntelliJ or it is too resource hungry.

What to Hand In? You are handing in one JPEG file called `workspace.jpg`, featuring on the same screen your code editor and a “terminal” that shows you successfully compiling a program.

Task 2: Oh My Magical Math (OHMM...) (4 points)

For this task, save your work in `hw1.pdf`, `SumEven.java`

The first n even numbers are $0, 2, 4, \dots, 2(n - 1)$. This task involves computing the sum of the first n even numbers and understanding their performance implications.

Subtask I We begin by writing a function `public static long sumEven(int n)` that computes the sum of the first n even numbers by looping over the even numbers in that range and adding them up.

At the top of your function, answer the following question as a comment block: *Approximately how many steps does this function need as a function of n ?*

Subtask II Directly using the method discussed in Lecture 1 (Gauss's pairing trick), find a simple formula for the sum of the first n even numbers. Please show your work in detail. Derive it directly without referencing other formulas.

Subtask III If we are to use this formula instead of what we have in the `sumEven` function, how many steps would this implementation need when the input is n ? Please answer this question in the PDF file.

Task 3: Diamond (2 points)

For this task, save your work in `Diamond.java`

Write a public class `Diamond`. Inside it, implement a function

```
public static void printDiamond(int k)
```

that takes a nonnegative integer k denoting the size of the diamond and prints to the screen (using `System.out`) a diamond of size k .

A diamond of size k contains a total of $2k - 1$ lines, where every line contains a total of $2k + 1$ characters (each character is either a `#` or a `*`). A few examples are given in Figure 1 for you to discover the pattern. Be warned that this task is **not** identical to a similar task you saw in Intro to Programming.

Specific Implementation Details: Your code can only use `for`-loops. You will print using either `print`, `println`, or `printf`. You may wish to learn about the `repeat` method, available for the `String` data type.

Task 4: Roman to Number (2 points)

For this task, save your work in `Roman.java`

You surely have encountered Roman numerals: I, II, III, XXII, MCMXLVI, etc. Roman numerals are represented by repeating and combining the following seven characters: I = 1, V = 5, X = 10, L = 50,

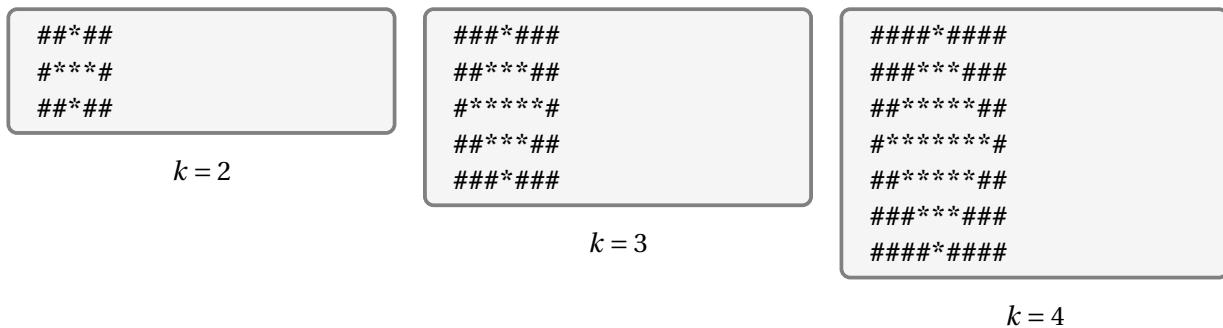


Figure 1: Examples of diamonds of different sizes.

$C = 100$, $D = 500$, $M = 1000$. To understand how they must be composed, we borrow the following excerpt from *Dive Into Python*:

- Characters are additive. I is 1, II is 2, and III is 3. VI is 6 (“5 and 1”), VII is 7, and VIII is 8.
- The tens characters (I, X, C, and M) can be repeated up to three times. At 4, you need to subtract from the next highest fives character. You can't represent 4 as IIII; instead, it is represented as IV (“1 less than 5”). The number 40 is written as XL (10 less than 50), 41 as XLI, 42 as XLII, 43 as XLIII, and then 44 as XLIV (10 less than 50, then 1 less than 5).
- Similarly, at 9, you need to subtract from the next highest tens character: 8 is VIII, but 9 is IX (1 less than 10), not VVII (since the I character cannot be repeated four times). The number 90 is XC, 900 is CM.
- The fives characters cannot be repeated. The number 10 is always represented as X, never as VV. The number 100 is always C, never LL.
- Roman numerals are always written highest to lowest, and read left to right, so the order the of characters matters very much. DC is 600; CD is a completely different number (400, 100 less than 500). CI is 101; IC is *not* a valid Roman numeral (because you can't subtract 1 directly from 100; you would need to write it as XCIX, for 10 less than 100, then 1 less than 10).

Your Task: You will write a public class Roman. Inside it, implement a function

```
public static int romanToInt(String romanNum)
```

that takes a string that is a number represented using Roman numerals and returns the number, as an integer, equals in value to the input. For example:

- | | |
|--|--|
| <ul style="list-style-type: none"> • romanToInt("I") == 1 • romanToInt("V") == 5 • romanToInt("VII") == 7 | <ul style="list-style-type: none"> • romanToInt("MCMIV") == 1954 • romanToInt("MCMXC") == 1990 |
|--|--|

Implementation Tips: Instead of a series of **if-else** constructs, you might wish to learn about the **switch**-case construct. This may simplify your life quite a bit.

For this problem, you don't need a Map, HashMap, or anything like that. It's best to stay away from them.

Task 5: N-Digit Fibonacci Number (2 points)

For this task, save your work in Fib.java

In this task, we'll play with the beloved Fibonacci sequence. The first two numbers in the sequence are 1 and 1. Each subsequent term is the sum of the previous two. Mathematically, we have that $F_1 = 1$, $F_2 = 1$, and for $n \geq 3$,

$$F_n = F_{n-1} + F_{n-2}.$$

Therefore, the initial 12 numbers of the sequence are: 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144

As can be seen, the 12-th Fibonacci number, F_{12} , is 144, which has 3 digits.

Your Task: You will write a public class Fib, inside which you will implement a function

```
public static int firstNDigit(int n)
```

that takes an integer n as input and returns the smallest index k such that F_k has at least n digits. We'll only test your function with $k \leq 40,000$. For example:

- `firstNDigit(1)==1`
- `firstNDigit(2)==7`
- `firstNDigit(3)==12`

HINT: Consider using BigInteger (or BigDecimal) as F_{47} already exceeds the capacity of an **int** and F_{100} is easily beyond the capacity of a **long**.

Task 6: Subselection (2 points)

For this task, save your work in Subsel.java

This task involves writing a utility function for fixed arrays. You will make a public class called Subsel, inside which you will implement two functions

```
public static int[] takeEvery(int[] a, int stride, int beginWith) and  
public static int[] takeEvery(int[] a, int stride)
```

with the following specifications:

- The call `takeEvery(a, s, b)` returns an **int** array containing the elements $a[b], a[b+s], a[b+2*s], a[b + 3*s], \dots$ until the index in this progression falls out of a.
 - The call `takeEvery(a, s)` has the same effect as calling `takeEvery(a, s, 0)`.
 - The output may be empty; the **stride** parameter could be positive or negative—but never 0.
- Abusing notation, this means:
- `takeEvery([1, 2, 3, 4], 2) == [1, 3]`
 - `takeEvery([2, 7, 1, 8, 4, 5], 3, 2) == [1, 5]`
 - `takeEvery([3, 1, 4, 5, 9, 2, 6, 5], -1, 5) == [2, 9, 5, 4, 1, 3]`

Your functions must **NOT** use any built-in collections such as the `ArrayList`, `LinkedList`, or similar constructs. Work directly with primitive arrays.

(Hint #1: We can have two functions with the same name; read about method overloading online.)

(Hint #2: One of them can be implemented by simply calling the other one.)

Task 7: Happy Time, Once Again (8 points)

For this task, save your work in Happy.java

You might remember happy numbers from a previous course. It is time for happy numbers once again. All your implementations for this task will live inside a public class called Happy.

Recap: Happy numbers are a nice mathematical concept. Just as only certain numbers are prime, only certain numbers are happy—under the mathematical definition of happiness. We'll tell you exactly what happiness means under this definition.

To test whether a number is happy, we can follow a simple step-by-step procedure:

- (1) Write that number down
- (2) Stop if that number is either 1 or 4.
- (3) Cross out the number you have now. Write down instead the sum of the squares of its digits.
- (4) Repeat Step (2)

When you stop, if the number you have is 1, the initial number is *happy*. If the number you have is 4, the initial number is *sad*. There are only two possible outcomes, happy or sad.

By this definition, 19 is a happy number because $1^2 + 9^2 = 82$, then $8^2 + 2^2 = 68$, then $6^2 + 8^2 = 100$, and then $1^2 + 0^2 + 0^2 = 1$. However, 145 is sad because $1^2 + 4^2 + 5^2 = 42$, $4^2 + 2^2 = 20$, and $2^2 + 0^2 = 4$.

Subtask I: First, you'll implement a function `public static long sumOfDigitsSquared(long n)` that takes a positive number `n` and returns the sum of each of its digits squared. For example,

- `sumOfDigitsSquared(7)` should return 49
- `sumOfDigitsSquared(145)` should return 42 (i.e., $1^2 + 4^2 + 5^2 = 1 + 16 + 25$)
- `sumOfDigitsSquared(199)` should return 163 (i.e., $1^2 + 9^2 + 9^2 = 1 + 81 + 81$)

Subtask II: Write a function `public static boolean isHappy(long n)` that takes as input a positive number `n` and tests if `n` is happy. You may wish to use what you wrote in the previous subtask.

- `isHappy(100)` should return `true`
- `isHappy(111)` should return `false`
- `isHappy(1234)` should return `false`
- `isHappy(989)` should return `true`

We will test your `isHappy` function with `n` up to 1,000,000. Recursion (i.e., writing `isHappy` in a way that calls itself) may not fare well with large `n`.

Subtask III: Write a function `public static long[] firstK(int k)` that takes in a number `k ≥ 0` and returns an array of `long` of length exactly `k` that contains the first `k` happy numbers. For example: `firstK(11)` should return the array {1, 7, 10, 13, 19, 23, 28, 31, 32, 44, 49}.

We will only test this function with `k ≤ 20,000,000`.

Task 8: Hidden String (2 points)

For this task, save your work in `Hidden.java`

Meow is playing a game with her friend. She gives her friend a string s and asks her whether another string t “hides” inside s . Let’s be a bit more precise about hiding. Say you have two strings s and t . The string t hides inside s if all the letters of t appear in s in the order that they originally appear in t . There may be additional letters between the letters of s , interleaving with them.

Under this definition, every string hides inside itself: `"cat"` hides inside `"cat"`. For a more interesting example, the string `"cat"` hides inside the string `"afciurfdasctxz"` as the diagram below highlight the letters of `"cat"`:

`afciurfdasctxz.`

Importantly, these letters must appear in the order they originally appear. Hence, this means that `"cat"` does not hide inside the string `"xaytpc"`. In this case, although the letters c, a, and t individually appear, they don’t appear in the correct order.

As another example, the string `"moo"` does not hide inside `"mow"`. This is because although we can find an m and an o, the second o doesn’t appear in `"mow"`.

In this problem, you’ll help Meow’s friend by implementing a function

```
public static boolean isHidden(String s, String t)
```

that determines whether t hides inside s . The function returns a Boolean value: `true` if t hides inside s and `false` otherwise.

Here are some more examples:

```
isHidden("welcometothehotelcalifornia", "melon") == true;
isHidden("welcometothehotelcalifornia", "space") == false;
isHidden("TQ89MnQU3IC7t6", "MUIC") == true;
isHidden("VhHTdipc07", "htc") == false;
isHidden("VhHTdipc07", "hTc") == true;
```