Bamboo Team Notes

Contents

Nun	nber theory	1
1.1	Count primes up to N	1
1.2	Extended Euclide	1
1.3	System of linear equations	1
1.4	Pollard Rho	1
Stri	ng	2
2.1	Suffix Array	2
2.2	Aho Corasick	2
2.3	Z algorithm	2
2.4	Manacher	3
2.5	Suffix Automaton	3
Con	nbinatorial optimization	3
Geo	metry	3
4.1	Geometry	3
Nun	nerical algorithms	5
5.1		5
5.2	Simplex Algorithm	5
5.3	NTT	5
5.4	FFT	6
5.5	Bitwise FFT	6
5.6	FFT chemthan	6
5.7	Partition Formula	7
5.8	Generating function	7
Gra	ph algorithms	7
6.1	Bridges and Articulations	7
6.2	Bipartite Maximum Matching	7
6.3	General Matching	8
6.4	Dinic Flow	8
6.5	Min Cost-Max Flow	8
6.6	Bounded Feasible Flow	9
6.7	Hungarian Algorithm	9
6.8	Undirected mincut	9
6.9	Eulerian Path/Circuit	0
6.10	2-SAT	0
Data	a structures 1	0
7.1	Treap	0
7.2	Big Integer	. 1
7.3	Convex Hull IT	.1
Mise	cellaneous 1	2
8.1		2
	1.1 1.2 1.3 1.4 Strit 2.1 2.2 2.3 2.4 2.5 Con Strit 5.2 5.3 5.4 5.5 5.6 6.7 6.8 6.9 6.10 Dat: 7.1 7.2 7.3 Miss	1.1 Count primes up to N 1.2 Extended Euclide 1.3 System of linear equations 1.4 Pollard Rho String 2.1 Suffix Array 2.2 Aho Corasick 2.3 Z algorithm 2.4 Manacher 2.5 Suffix Automaton Combinatorial optimization Geometry 4.1 Geometry 4.1 Geometry 4.1 Geometry 5.1 Gauus Elimination 5.2 Simplex Algorithms 5.1 Gauus Elimination 5.3 NTT 5.4 FFT 5.5 Bitwise FFT 5.6 FFT chemthan 5.7 Partition Formula 5.8 Generating function Graph algorithms 6.1 Bridges and Articulations 6.2 Bipartite Maximum Matching 6.3 General Matching 6.4 Dinic Flow 6.5 Min Cost-Max Flow 6.6 Bounded Feasible Flow 6.7 Hungarian Algorithm 6.8 Undirected mincut 6.9 Eulerian Path/Circuit 6.9 Eulerian Path/Circuit 6.1 Treap 7.1 Treap 7.2 Big Integer 7.3 Convex Hull IT Miscellaneous

1 Number theory

1.1 Count primes up to N

```
prime[j] = false;
REP(i, MAX) if (prime[i]) P.push_back(i);
FOR(i, 1, MAX) prec[i] = prec[i-1] + prime[i];
```

1.2 Extended Euclide

```
int bezout(int a, int b) {
    // return x such that ax + by == gcd(a, b)
    int xa = 1, xb = 0;
    while (b) {
        int q = a / b;
        int r = a - q * b, xr = xa - q * xb;
        a = b; xa = xb;
        b = r; xb = xr;
    }
    return xa;
}

pair<int, int> solve(int a, int b, int c) {
        // solve ax + by == c
        int d = __gcd(a, b);
        int x = bezout(a, b);
        int y = (d - a * x) / b;
        c /= d;
        return make_pair(x * c, y * c);
}

int main() {
        int a = 100, b = 128;
        int c = __gcd(a, b);
        int y = (c - a * x) / b;
        cout << x < ' ' < y << endl;
        pair<int, int> xy = solve(100, 128, 40);
        cout << x < ' ' << y <, second << endl;
        return 0;
}</pre>
```

1.3 System of linear equations

1.4 Pollard Rho

```
#include <bits/stdc++.h>
using namespace std;

struct PollardRho {
   long long n;
   map<long long, int> ans;
   PollardRho(long long n) : n(n) {}
   long long random(long long u) {
      return abs(rand()) % u;
   }
}
```

```
long long mul(long long a, long long b, long long p) {
                  g long mul(long long a, long long b, long long p) {
   a \( \pm \) p b \( \pm \) p;
   long long q = (long long)((long double) a * b / p);
   long long r = a * b - q * p;
   while (r < 0) r += p;
   while (r >= p) r -= p;
}
         u = mul(u, u, n);
v >>= 1;
                   return res:
         bool rabin(long long n) {
   if (n < 2) return 0;
   if (n == 2) return 1;
   long long s = 0, m = n - 1;
   while (m % 2 == 0) {</pre>
                           s++;
m >>= 1;
               m >> - .
}
// 1 - 0.9 ^ 40
for (int it = 1; it <= 40; it++) {
   long long u = random(n - 2) + 2;
   long long f = pow(u, m, n);
   if (f == 1 | | f == n - 1) continue;
   for (int i = 1; i < s; i++) {
      f = mul(f, f, n);
      if (f == 1) return 0;
      if (f == n - 1) break;
   }
}
'' return 0;</pre>
                   return 1;
         long long f (long long x, long long n) {
    return (mul(x, x, n) + 1) % n;
         long long findfactor(long long n) {
  long long x = random(n - 1) + 2;
  long long y = x;
  long long p = 1;
  while (p == 1) {
                   while (p == 1) {
    x = f(x, n);
    y = f(f(y, n), n);
    p = __gcd(abs(x - y), n);
                   return p;
         if (n > 1) ans[n]++;
                   if (rabin(n)) {
                           return;
                   long long p = 0;
while (p == 0 || p == n) {
    p = findfactor(n);
                  pollard_rho(n / p);
pollard_rho(p);
int main() {
    long long n;
         long long n;
cin >> n;
PollardRho f(n);
f.pollard_rho(f.n);
for (auto x : f.ans) {
    cout << x.first << " " << x.second << end];</pre>
```

2 String

};

Suffix Array

```
#include <bits/stdc++.h>
using namespace std;
struct SuffixArray /
     static const int N = 100010;
    int n:
    int sa[N], tmp[N], pos[N];
int len, cnt[N], lcp[N];
    SuffixArray(char *t) {
         s = t;
n = strlen(s + 1);
```

```
buildSA();
      bool cmp(int u, int v) {
   if (pos[u] != pos[v]) {
      return pos[u] < pos[v];
}</pre>
              return (u + len <= n && v + len <= n) ? pos[u + len] < pos[v + len] :
              i radix(int delta) {
    memset(cnt, 0, sizeof cnt);
    for (int i = 1; i <= n; i++) {
        cnt[i + delta <= n ? pos[i + delta] : 0]++;
    }
}</pre>
              for (int i = 1; i < N; i++) {
    cnt[i] += cnt[i - 1];</pre>
              for (int i = n; i > 0; i--) {
   int id = sa[i];
                      tmp[cnt[id + delta <= n ? pos[id + delta] : 0]--] = id;</pre>
              for (int i = 1; i <= n; i++) {
                      sa[i] = tmp[i];
      void buildSA() {
   for (int i = 1; i <= n; i++) {
     sa[i] = i;
     pos[i] = s[i];</pre>
              }
len = 1;
while (1) {
                      radix(len);
radix(len);
radix(0);
tmp[1] = 1;
for (int i = 2; i <= n; i++) {
   tmp[i] = tmp[i - 1] + cmp(sa[i - 1], sa[i]);
                      for (int i = 1; i <= n; i++) {
   pos[sa[i]] = tmp[i];
}</pre>
                      if (tmp[n] == n) {
    break;
                      len <<= 1:
              for (int i = 1; i <= n; i++) {
   if (pos[i] == n) {</pre>
                             continue;
                      int j = sa[pos[i] + 1];
while (s[i + len] == s[j + len]) {
    len++;
                      lcp[pos[i]] = len;
if (len) {
    len--;
};
```

2.2Aho Corasick

```
struct AhoCorasick
       const int N = 30030:
      int to[N][2];
int ending[N];
      void add(const string &s) {
   int node = 1;
   for (int i = 0; i < s.size(); ++i) {
      if (!to[node][s[i] - 'a']) {
         to[node][s[i] - 'a'] = ++sz;
}</pre>
                  node = to[node][s[i] - 'a'];
            ending[node] = true;
       void push() {
            int av = co.;
if (!v) {
    v = u == 1 ? 1 : to[fail[u]][i];
                       } else {
    fail[v] = u == 1 ? 1 : to[fail[u]][i];
                            Q.push(v);
};
```

2.3 Z algorithm

```
vector<int> calcZ(const string &s) {
  int L = 0, R = 0;
  int n = s.size();
  vector<int> Z(n);
  Z[0] = n;
  for (int i = 1; i < n; i++) {
    if (i > R)
    {
        L = R = i;
        while (R < n && s[R] == s[R - L]) R++;
        Z[i] = R - L; R--;
    }
  else
    {
        int k = i - L;
        if (Z[k] < R - i + 1) Z[i] = Z[k];
        else
        {
        L = i;
        while (R < n && s[R] == s[R - L]) R++;
        Z[i] = R - L; R--;
        }
    }
  }
  return Z;
}</pre>
```

2.4 Manacher

2.5 Suffix Automaton

```
//set last = 0 everytime we add new string
struct SuffixAutomaton {
    static const int N = 100000;
    static const int CHARACTER = 26;
    int suf[N * 2], nxt[N * 2][CHARACTER], cnt, last, len[N * 2];

SuffixAutomaton() {
    memset (suf, -1, sizeof suf);
    memset (nxt, -1, sizeof nxt);
    memset (nxt, -1, sizeof nxt);
    memset (len, 0, sizeof len);
    last = cnt = 0;
}

int getNode(int last, int u) {
    int q = nxt[last][u];
    if (len[last] + 1 == len[q]) {
        return q;
    }
    int clone = ++cnt;
    len[clone] = len[last] + 1;
    for (int i = 0; i < CHARACTER; i++) {
        nxt[clone][i] = nxt[q][i];
    }
    while (last != -1 && nxt[last][u] == q) {
        nxt[last][u] = clone;
        last = suf[last];
    }
    suf[clone] = suf[q];
    return suf[q] = clone;
}

void add(int u) {
    if (nxt[last][u] == -1) {
        int newNode = ++cnt;
        len[newNode] = len[last] + 1;
        while (last != -1 && nxt[last][u] == -1) {
            nxt[last][u] = newNode;
            last = suf[last];
    }
    if (last == -1) {
            suf[newNode] = 0;
            last = newNode;
            return;
    }
    suf[newNode] = qetNode (last, u);
}</pre>
```

```
last = newNode;
} else {
    last = getNode(last, u);
}
};
```

3 Combinatorial optimization

4 Geometry

4.1 Geometry

```
#define EPS 1e-6 inline int cmp(double a, double b) { return (a < b - EPS) ? -1 : ((a > b + EPS) ? -1 : (ta > b + EPS) ) ? 1 : 0); } struct Point {
       double x, y;
Point() { x = y = 0.0; }
Point(double x, double y) : x(x), y(y) {}
      Point operator + (const Point& a) const { return Point(x+a.x, y+a.y); } Point operator - (const Point& a) const { return Point(x-a.x, y-a.y); } Point operator + (double k) const { return Point(x+k, y+k); } Point operator / (double k) const { return Point(x/k, y/k); }
       double operator * (const Point& a) const { return x*a.x + y*a.y; } // dot
       double operator % (const Point& a) const { return x*a.y - y*a.x; } //
       double angle(Point a, Point o, Point b) { // min of directed angle AOB & BOA
    a = a - o; b = b - o;
    return acos((a * b) / sqrt(a.norm()) / sqrt(b.norm()));
double directed_angle(Point a, Point o, Point b) { // angle AOB, in range [0,
       return t;
}
// Distance from p to Line ab (closest Point --> c)
double distToLine(Point p, Point a, Point b, Point &c) {
   Point ap = p - a, ab = b - a;
   double u = (ap * ab) / ab.norm();
   c = a + (ab * u);
   return (p-c).len();
}
}
// Distance from p to segment ab (closest Point --> c)
double distToLineSegment(Point p, Point a, Point b, Point &c) {
   Point ap = p - a, ab = b - a;
   double u = (ap * ab) / ab.norm();
   if (u < 0.0) {
      c = Point(a.x, a.y);
      return (p - a).len();
}</pre>
       if (u > 1.0) {
    c = Point(b.x, b.y);
}
              return (p - b).len();
       return distToLine(p, a, b, c);
 ^{
m } // NOTE: WILL NOT WORK WHEN a = b = 0.
Line(double a, double b, double c) : a(a), b(b), c(c) {}
       Line(Point A, Point B) : A(A), B(B) {
    a = B.y - A.y;
    b = A.x - B.x;
              c = - (a * A.x + b * A.y);
       Line (Point P, double m) {
              a = -m; b = 1;

c = -((a * P.x) + (b * P.y));
       double f(Point A) {
   return a*A.x + b*A.y + c;
bool areParallel(Line 11, Line 12) {
   return cmp(11.a*12.b, 11.b*12.a) == 0;
}
bool areIntersect(Line 11, Line 12, Point &p) {
    if (areParallel(11, 12)) return false;
    double dx = 11.b*12.c - 12.b*11.c;
    double dy = 11.c*12.a - 12.c*11.a;
    double d = 11.a*12.b - 12.a*11.b;
    p = Point(dx/d, dy/d);
    return true;
}
 void closestPoint(Line 1, Point p, Point &ans) {
   if (fabs(1.b) < EPs) {
        ans.x = -(1.c) / 1.a; ans.y = p.y;
}</pre>
```

```
return;
           if (fabs(1.a) < EPS) {
    ans.x = p.x; ans.y = -(1.c) / 1.b;</pre>
                    return;
           Line perp(1.b, -1.a, - (1.b*p.x - 1.a*p.y));
areIntersect(1, perp, ans);
 void reflectionPoint(Line 1, Point p, Point &ans) {
           Point b;
closestPoint(l, p, b);
ans = p + (b - p) * 2;
 struct Circle : Point {
           double r;
           double r;
Circle(double x = 0, double y = 0, double r = 0) : Point(x, y), r(r) {}
Circle(Point p, double r) : Point(p), r(r) {}
bool contains(Point p) { return (*this - p).len() <= r + EPS; }</pre>
  // Find common tangents to 2 circles
            http://codeforces.com/gym/100803/ - H
 break:
                    if (ok) ret.push_back(ans[i]);
           return ret:
 // Circle & line intersection
vector<Point> intersection(Line l, Circle cir) {
   double r = cir.r, a = l.a, b = l.b, c = l.c + l.a*cir.x + l.b*cir.y;
   vector<Point> res;
   double x0 = -a*c*/(a*a+b*b), y0 = -b*c*/(a*a+b*b);
   if (c*c > r*r**(a*a+b*b)+EPS) return res;
   else if (fabs(c*c - r*r**(a*a+b*b)) < EPS) {
      res.push_back(Point(x0, y0) + Point(cir.x, cir.y));
      return res;
   }</pre>
  // Circle & line intersection
           else {
                   e {
    double d = r*r - c*c/(a*a+b*b);
    double mult = sqrt (d / (a*a+b*b));
    double ax, ay, bx, by;
    ax = x0 + b * mult;
    bx = x0 - b * mult;
    ay = y0 - a * mult;
    by = y0 + a * mult;
    by = y0 + a * mult;
    res. push_back(Point(ax, ay) + Point(cir.x, cir.y));
    res. push_back(Point(bx, by) + Point(cir.x, cir.y));
    return res:
                    return res;
 // helper functions for commonCircleArea
double cir_area_solve(double a, double b, double c) {
   return acos((a*a + b*b - c*c) / 2 / a / b);
}
double cir_area_cut(double a, double r) {
   double s1 = a * r * r / 2;
   double s2 = sin(a) * r * r / 2;
   return s1 - s2;
 double commonCircleArea(Circle c1, Circle c2) { //return the common area of
          ble commonCircleArea(Circle c1, Circle c2) { //return the con
two circle
if (cl.r < c2.r) swap(c1, c2);
double d = (cl - c2).len();
if (d + c2.r <= c1.r + EPS) return c2.r*c2.r*M_PI;
if (d >= c1.r + c2.r - EPS) return 0.0;
double al = cir_area_solve(d, c1.r, c2.r);
double a2 = cir_area_solve(d, c2.r, c1.r);
return cir_area_cut(a1*2, c1.r) + cir_area_cut(a2*2, c2.r);
        Check if 2 circle intersects. Return true if 2 circles touch
bool areIntersect(Circle u, Circle v) {
   if (cmp((u - v).len(), u.r + v.r) > 0) return false;
   if (cmp((u - v).len() + v.r, u.r) < 0) return false;
   if (cmp((u - v).len() + u.r, v.r) < 0) return false;</pre>
           return true;
 }
// If 2 circle touches, will return 2 (same) points
// If 2 circle are same --> be careful
vector<Point> circleIntersect(Circle u, Circle v) {
    vector<Point> res;
    if (!areIntersect(u, v)) return res;
    double d = (u - v).len();
    double alpha = acos((u.r * u.r + d*d - v.r * v.r) / 2.0 / u.r / d);
           Point p1 = (v - u).rotate(alpha);

Point p2 = (v - u).rotate(-alpha);

res.push_back(p1 / p1.len() + u.r + u);

res.push_back(p2 / p2.len() + u.r + u);
           return res:
```

```
Point centroid(Polygon p) {
    Point c(0,0);
    double scale = 6.0 * signed_area(p);
    for (int i = 0; i < p.size(); i++) {
        int j = (i+1) % p.size();
        c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
}</pre>
          return c / scale;
 /// Cut a polygon with a line. Returns one half.
// To return the other half, reverse the direction of Line 1 (by negating 1.a,
                1.b)
 // The line must be formed using 2 points
Polygon polygon_cut (const Polygon& P, Line 1) {
         polygon Q;
Polygon Q;
for(int i = 0; i < P.size(); ++i) {
    Point A = P[i], B = (i == P.size()-1) ? P[0] : P[i+1];
    if (ccw(l.A, l.B, A) != -1) Q.push_back(A);
    if (ccw(l.A, l.B, A) +ccw(l.A, l.B, B) < 0) {
        Point p; areIntersect(Line(A, B), l, p);
        Q.push_back(p);
    }
}</pre>
          return 0:
  // Find intersection of 2 convex polygons
// Find intersection of 2 convex polygons
// Helper method
bool intersect_lpt(Point a, Point b,
    Point c, Point d, Point &r) {
    double D = (b - a) % (d - c);
    if (cmp(D, 0) == 0) return false;
    double t = ((c - a) % (d - c)) / D;
    double s = -((a - c) % (b - a)) / D;
    r = a + (b - a) * t;
    return cmp(t, 0) >= 0 && cmp(t, 1) <= 0 && cmp(s, 0) >= 0 && cmp(s, 1) <=
}</pre>
Polygon convex_intersect(Polygon P, Polygon Q) {
   const int n = P.size(), m = Q.size();
   int a = 0, b = 0, aa = 0, ba = 0;
   enum { Pin, Qin, Unknown } in = Unknown;
          Polygon R;
          do {
                  [
int al = (a+n-1) % n, bl = (b+m-1) % m;
double C = (P[a] - P[a1]) % (Q[b] - Q[b1]);
double A = (P[a1] - Q[b]) % (P[a] - Q[b]);
double B = (Q[b1] - P[a]) % (Q[b] - P[a]);
                  double B = (Q[b1] - P[a]) % (Q[b] - P[a]);
Point r;
if (intersect_lpt(P[a1], P[a], Q[b1], Q[b], r)) {
   if (in == Unknown) aa = ba = 0;
   R.push_back(r);
   in = B > 0 ? Pin : A > 0 ? Qin : in;
                  { if (in == Qin) R.push_back(Q[b]); b = (b+1)%m; ++ba;
                                         }
                  } else {
                            if (B > 0) { if (in == Qin) R.push_back(Q[b]); b = (b+1)%m; ++ba;
                                                    { if (in == Pin) R.push back(P[a]); a = (a+1)%n; ++aa;
                            else
         } while ( (aa < n || ba < m) && aa < 2*n && ba < 2*m );
if (in == Unknown) {
   if (in_convex(Q, P[0])) return P;
   if (in_convex(P, Q[0])) return Q;</pre>
          return R;
 }
// Find the diameter of polygon.
// Rotating callipers
double convex_diameter(Polygon pt) {
   const int n = pt. size();
   int is = 0, js = 0;
   for (int i = 1; i < n; ++i) {
      if (pt[i].y > pt[is].y) is = i;
      if (pt[i].y < pt[js].y) js = i;
   }
}</pre>
          double maxd = (pt[is]-pt[js]).norm();
          int i, maxi = (pt[1s]
int i, maxi, j, maxj;
i = maxi = is;
j = maxj = js;
                  {
int jj = j+1; if (jj == n) jj = 0;
if ((pt[i] - pt[j]).norm() > (pt[i] - pt[j]).norm()) j = (j+1) % n;
else i = (i+1) % n;
if ((pt[i]-pt[j]).norm() > maxd) {
    maxd = (pt[i]-pt[j]).norm();
    maxi = i; maxj = j;
}
          } while (i != is || j != js);
return maxd; /* farthest pair is (maxi, maxj). */
   ^{\prime\prime} Check if we can form triangle with edges x, y, z.
 bool isSquare(long long x) { /* */ }
bool isIntegerCoordinates(int x, int y, int z) {
  long long se(long long) (x+y+z) * (x+y-z) * (x+z-y) * (y+z-x);
  return (s%4==0 && isSquare(s/4));
 // Given non-intersecting polygon.
// S = area
 Circle getCircle(vector<Point> points) {
   assert(!points.empty());
   random_shuffle(points.begin(), points.end());
```

5 Numerical algorithms

5.1 Gauus Elimination

5.2 Simplex Algorithm

```
* minimize c^T * x

* subject to Ax <= b
```

```
* The input matrix a will have the following form * O c c c c c c * b A A A A A
  * Result vector will be: val x x x x x **/
for (int i = 0; i <= n; i++) {
   if (fabs(a[i][y]) < EPS || i == x) continue;
   k = a[i][y];
   a[i][y] = 0;</pre>
                  for (int j : pos) a[i][j] -= k * a[x][j];
         };
while (1) {
   int x = -1;
   for (int i = 1; i <= n; i++) {
    if (a[i][0] < -EPS && (x == -1 || a[i][0] < a[x][0])) {</pre>
              if (x == -1) break;
             int y = -1;
for (int j = 1; j <= m; j++) {
    if (a[x][j] < -EPS && (y == -1 || a[x][j] < a[x][y])) {</pre>
              if (y == -1) return vector<ld>(); // infeasible
          while (1) {
             -1;
             if (x == -1) return vector<ld>(); // unbounded
             pivot(x, v);
         for (int i = 1; i <= n; i++) {
   if (left[i] <= m) ans[left[i]] = a[i][0];</pre>
         ans[0] = -a[0][0];
return ans;
};
```

5.3 NTT

```
void fft (vector<int> &a) {
                         a fit(vector<int> &a) {
   int n = a.size();
   int curBase = 0;
   while (1 << curBase) < n) curBase++;
   int shift = base - curBase;
   for (int i = 0; i < n; i++) {
      if (i < (rev[i] >> shift)) swap(a[i], a[rev[i] >> shift]);
    }
}
                                      (int k = 1; k < n; k <<= 1) {
for (int i = 0; i < k; i++) {
   for (int j = i; j < n; j += k * 2) {
      int foo = a[j];
      int bar = mul(a[j + k], w[i + k]);
      a[j] = add(foo, bar);
      a[j + k] = sub(foo, bar);
   }
}</pre>
                          for (int k = 1; k < n; k <<= 1) {
                                     }
              vector<int> mult(vector<int> a, vector<int> b) {
  int nResult = a.size() + b.size() - 1;
  int curBase = 0;
  while (1 << curBase) < nResult) curBase++;</pre>
                         while ((1 << curBase) < nResult) curBase
ensure(curBase);
int n = 1 << curBase;
a.resize(n), b.resize(n);
fft(a);
fft(b);
int invN = inv(n);
for (int i = 0; i < n; i++) {
    a[i] = mul(mul(a[i], b[i]), invN);
}</pre>
                          reverse(a.begin() + 1, a.end());
fft(a);
a.resize(nResult);
                          return a;
              vector<int> polyInv(vector<int> r, vector<int> f) {
                         corsint> polylinv(vectorsint> r, vectorsi
vectorsint> foo = mult(r, f);
foo.resize(f.size());
foo[0] = sub(2, foo[0]);
for (int i = 1; i < foo.size(); i++) {
    foo[i] = sub(0, foo[i]);
}</pre>
                          }
vector<int> res = mult(r, foo);
res.resize(f.size());
                          return res:
             }
vector<int> polySqrt(vector<int> s, vector<int> invS, vector<int> f) {
    vector<int> res = mult(f, invS);
    res.resize(f.size());
    for (int i = 0; i < s.size(); i++) {
        res[i] = add(res[i], s[i]);
}</pre>
                          for (int i = 0; i < res.size(); i++) {
    res[i] = mul(res[i], INV_2);</pre>
                          return res:
            }
vector<int> getSqrt(vector<int> c, int sz) {
    vector<int> sqrtC = {1}, invSqrtC = {1}; //change this if c[0] != 1
    for (int k = 1; k < (1 << sz); k <<= 1) {
        vector<int> foo(c.begin(), c.begin() + (k + 2));
        vector<int> bar = sqrtC;
        bar.resize(bar.size() + 2, 0);
        vector<int> tempInv = polyInv(invSqrtC, bar);
        sqrtC = polySqrt(sqrtC, tempInv, foo);
        invSqrtC = polyInv(invSqrtC, sqrtC);
}
                          return sqrtC;
            }
vector<int> getInv(vector<int> c, int sz) {
    vector<int> res = {INV_2}; // change this if c[0] != 2
    for (int k = 1; k < (1 << sz); k <<= 1) {
        vector<int> foo (c.begin(), c.begin() + (k * 2));
        res = polyInv(res, foo);
    }
}
                          return res;
1 ntt:
```

5.4 FFT

```
while (fftSz < newSz) {
    fftSz <<= 1;
}
VC aa(fftSz, 0.), bb(fftSz, 0.);
for (int i = 0; i < a.size(); i++) {
    aa[i] = a[i];
}
for (int i = 0; i < b.size(); i++) {
    bb[i] = b[i];
}
fft(aa, 1);
fft(bb, 1);
for (int i = 0; i < fftSz; i++) {
    aa[i] *= bb[i];
}
fft(aa, -1);
vector</pre>
vector
for (int i = 0; i < fftSz; i++) {
    res[i] = (int) (aa[i].real() / fftSz + 0.5);
}
return res;
}
</pre>
```

5.5 Bitwise FFT

```
/*
* matrix:
* +1 +1
* +1 -1
*/
void XORFFT(int a[], int n, int p, int invert) {
   for (int i = 1; i < n; i <<= 1) {
      for (int j = 0; j < n; j += i << 1) {
        for (int k = 0; k < i; k++) {
            int u = a[j + k], v = a[i + j + k];
            a[j + k] = u + v;
            if (a[j + k] >= p) a[j + k] -= p;
            a[i + j + k] = u - v;
            if (a[i + j + k] < 0) a[i + j + k] += p;
      }
}</pre>
                              }
                     }
           if (invert) {
                      long long inv = fpow(n, p - 2, p);
for (int i = 0; i < n; i++) a[i] = a[i] * inv % p;</pre>
 * Matrix:
* +1 +1
* +1 +0
else (
                                                      a {
   a[j + k] = v;
   a[i + j + k] = u - v;
   if (a[i + j + k] < 0) a[i + j + k] += p;</pre>
                   }
         }
 * matrix:
 * +0 +1
* +1 +1
 void ANDFFT(int a[], int n, int p, int invert) {
          d ANDFFT(int a[], int n, int p, int invert) {
  for (int i = 1; i < n; i <<= 1) {
    for (int j = 0; j < n; j += i << 1) {
      for (int k = 0; k < i; k++) {
        int u = a[j + k], v = a[i + j + k];
        if (!invert) {
            a[j + k] = v;
            a[i + j + k] = u + v;
            if (a[i + j + k] >= p) a[i + j + k] -= p;
      }
}
                                            lse {
    a[j + k] = v - u;
    if (a[j + k] < 0) a[j + k] += p;
    a[i + j + k] = u;</pre>
                                          }
      }
```

5.6 FFT chemthan

```
#define double long double
namespace FFT {
    const int maxf = 1 << 17;
    struct cp {
        double x, y;
        cp (double x = 0, double y = 0) : x(x), y(y) {}
        cp operator + (const cp& rhs) const {
            return cp(x + rhs.x, y + rhs.y);
        }
        cp operator - (const cp& rhs) const {
            return cp(x - rhs.x, y - rhs.y);
        }
}</pre>
```

```
return cp(x * rhs.x - y * rhs.y, x * rhs.y + y * rhs.x);
          cp operator !() const {
                   return cp(x, -y);
 } rts[maxf + 1];
cp fa[maxf], fb[maxf];
cp fc[maxf], fd[maxf];
rts[0] = rts[maxf] = cp(1, 0);

for (int i = 1; i + i <= maxf; i++) {

   rts[i] = cp(cos(i * 2 * PI / maxf), sin(i * 2 * PI / maxf));
          for (int i = maxf / 2 + 1; i < maxf; i++) {</pre>
                   rts[i] = !rts[maxf - i];
 }
void dft(cp a[], int n, int sign) {
    static int isinit;
    if (!isinit) {
        isinit = 1;
    }
}
                fftinit();
          }
int d = 0; while ((1 << d) * n != maxf) d++;
for (int i = 0; i < n; i++) {
   if (i < (bitrev[i] >> d)) {
      swap(a[i], a[bitrev[i] >> d]);
}
         }
for (int len = 2; len <= n; len <<= 1) {
    int delta = maxf / len * sign;
    for (int i = 0; i < n; i += len) {
        cp *x = a + i, *y = a + i + (len >> 1), *w = sign > 0 ? rts :
            rts + maxf;
        for (int k = 0; k + k < len; k++) {
            cp z = *y * *w;
            *y = *x - z, *x = *x + z;
            x++, y++, w += delta;
    }
}</pre>
                  }
         if (sign < 0) {
   for (int i = 0; i < n; i++) {
      a[i] x /= n;
      a[i] y /= n;
}</pre>
}
void multiply(int a[], int b[], int na, int nb, long long c[]) {
    int n = na + nb - 1; while (n != (n & -n)) n += n & -n;
    for (int i = 0; i < n; i++) fa[i] = fb[i] = cp();
    for (int i = 0; i < na; i++) fa[i] = cp(a[i]);
    for (int i = 0; i < nb; i++) fb[i] = cp(a[i]);
    dft(fa, n, 1), dft(fb, n, 1);
    for (int i = 0; i < n; i++) fa[i] = fa[i] * fb[i];
    dft(fa, n, -1);
    for (int i = 0; i < n; i++) c[i] = (long long) floor(fa[i].x + 0.5);
}</pre>
        void multiply(int a[], int b[], int na, int nb, int c[], int mod = (int) 1
          }
dft(fc, n, -1), dft(fd, n, -1);
for (int i = 0; i < n; i++) {
   long long u = ((long long) floor(fc[i].x + 0.5)) % mod;
   long long v = ((long long) floor(fd[i].x + 0.5)) % mod;
   long long w = ((long long) floor(fd[i].y + 0.5)) % mod;
   c[i] = ((u << 15) + v + (w << 30)) % mod;</pre>
  vector<int> multiply(vector<int> a, vector<int> b, int mod = (int) 1e9 +
          static int fa[maxf], fb[maxf], fc[maxf];
         int na = a.size(), nb = b.size();
for (int i = 0; i < na; i++) fa[i] = a[i];
for (int i = 0; i < nb; i++) fb[i] = b[i];
multiply(fa, fb, na, nb, fc, mod);
int k = na + nb - 1;</pre>
          rector(int) res(k);
for (int i = 0; i < k; i++) res[i] = fc[i];
return res;</pre>
```

5.7 Partition Formula

```
* generating function : PI: (1 / (1 - x^k))
```

```
* p(n) = p(n-1) + p(n-2) - p(n-5) - p(n-7) + p(n-12) + p(n-15) - p(n-22) - \dots

* p\_k = k * (3k - 1) / 2 with k = 1, -1, 2, -2, 3, -3, \dots

*/
```

5.8 Generating function

```
// 1 / ( (1-ax) ^ (k+1) ) = sum_(0->INF)_{ a^n * C(n+k, k) * x^n }
```

6 Graph algorithms

6.1 Bridges and Articulations

6.2 Bipartite Maximum Matching

```
struct BipartiteGraph {
   vector< vector<int> a;
   vector<int> match;
       vector<bool> was:
      BipartiteGraph(int m, int n) {
           // zero-indexed
this->m = m; this->n = n;
a.resize(m);
            match.assign(n.
            was.assign(n, false);
      void addEdge(int u, int v) {
     bool dfs(int u) {
  for (int v : a[u]) if (!was[v]) {
    was[v] = true;
    if (match[v] == -1 || dfs(match[v])) {
        match[v] == u;
    }
}
            return false;
     int maximumMatching() {
            weetor<int> buffer;
for (int i = 0; i < m; ++i) buffer.push_back(i);
bool stop = false;
int ans = 0;</pre>
                 ++ans;
stop = false;
buffer[i] = buffer.back();
buffer.pop_back();
                        }
            } while (!stop);
            return ans;
      vector<int> konig() {
   // returns minimum vertex cover, run this after maximumMatching()
   vector<bool> matched(m);
```

```
for (int i = 0; i < n; ++i) {
    if (match[i] != -1) matched[match[i]] = true;
}
queue<int> Q;
was.assign(m + n, false);
for (int i = 0; i < m; ++i) {
    if (!matched[i]) {
        was[i] = true;
        Q.push(i);
}

while (!Q.empty()) {
    int u = Q.front(); Q.pop();
    for (int v : a[u]) if (!was[m + v]) {
        was[m + v] = true;
        if (match[v]! -1 && !was[match[v]]) {
            was[match[v]] = true;
        Q.push(match[v]];
        }
}

vector<int> res;
for (int i = 0; i < m; ++i) {
        if (!was[i]) res.push_back(i);
}
for (int i = m; i < m + n; ++i) {
        if (was[i]) res.push_back(i);
}
return res;
}
</pre>
```

6.3 General Matching

```
* Complexity: O(E*sqrt(V))
* Indexing from 1
struct Blossom {
        act Blossom {
static const int MAXV = 1e3 + 5;
static const int MAXE = 1e6 + 5;
int n, E, lst[MAXV], next[MAXE], adj[MAXE];
int nxt[MAXV], mat[MAXV], dad[MAXV], col[MAXV];
int que[MAXV], qh, qt;
int vis[MAXV], act[MAXV];
int tat teal.
        int tag, total;
       void init(int n) {
   this->n = n;
   for (int i = 0; i <= n; i++) {
      lst[i] = nxt[i] = mat[i] = vis[i] = 0;
      ,</pre>
                 E = 1, tag = total = 0;
         rwoid add(int u,int v) {
    if (!mat[u] && !mat[v]) mat[u] = v, mat[v] = u, total++;
    E++, adj[E] = v, next[E] = lst[u], lst[u] = E;
    E++, adj[E] = u, next[E] = lst[v], lst[v] = E;
         int lca(int u, int v) {
               vis[u] = tag;
u = nxt[mat[u]];
        }
woid blossom(int u, int v, int g) {
    while (dad[u] != g) {
        nxt[u] = v;
        if (col[mat[u]] == 2) {
            col[mat[u]] = 1;
            que[++qt] = mat[u];
        }
}
                          if (u == dad[u]) dad[u] = g;
if (mat[u] == dad[mat[u]]) dad[mat[u]] = g;
                          v = mat[u];
        int augument(int s) {
    for (int i = 1; i <= n; i++) {
        col[i] = 0;
        dad[i] = i;
}</pre>
                for (; v; v = u) {
    u = mat[nxt[v]];
    mat[v] = nxt[v];
    mat[nxt[v]] = v;
                                                     return 1:
                                           col[mat[v]] = 1;
que[++qt] = mat[v];
                                   else if (dad[u] != dad[v] && col[v] == 1) {
   int g = lca(u, v);
   blossom(u, v, g);
```

6.4 Dinic Flow

```
const int V = 1e5:
const int INF = 1e9;
struct Flow {
              vector<int> adi[V];
            vector<int> adj[V];
int to[V], c[V], f[V];
int n, s, t, cnt;
int d[V];
int cur[V];
Flow(int n, int s, int t) {
   this=>n = n;
   this=>t = t;
   cnt = 0.
                            cnt = 0;
             }
int addEdge(int u, int v, int _c) {
    to[cnt] = v, c[cnt] = _c, f[cnt] = 0;
    adj[u].push_back(cnt++);
    to[cnt] = u, c[cnt] = 0, f[cnt] = 0;
    adj[v].push_back(cnt++);
                          l bfs() {
for (int i = 0; i < n; i++) d[i] = -1;
d[s] = 0;
queue<int> q;
q.push(s);
while (!q.empty()) {
    int u = q.front();
    q.pop();
    for (int id : adj[u]) {
        int v = to[id];
        if (d[v] = -1 && f[id] < c[id]) {
            d[v] = d[u] + 1;
            q.push(v);
        }
    }</pre>
                            return d[t] != -1;
           }
int dfs(int u, int res) {
    if (u == t) return res;
    for (int &it = cur[u]; it < adj[u].size(); it++) {
        int id = adj[u][it];
        int v = to[id];
        if (d[v] == d[u] + 1 && f[id] < c[id]) {
            int foo = dfs(v, min(c[id] - f[id], res));
            if (foo) {</pre>
                                                       if (foo) {
    f[id] += foo;
    f[id ^ 1] -= foo;
    return foo;
                            return 0;
              int maxFlow() {
                           int res = 0;
while (bfs()) {
   for (int i = 0; i < n; i++) cur[i] = 0;
   while (1) {
      int foo = dfs(s, INF);
      if (!foo) break;
   }
}</pre>
                            return res:
```

6.5 Min Cost-Max Flow

6.6 Bounded Feasible Flow

```
} n += 2;
return maxFlow() == sum;
}
};
```

6.7 Hungarian Algorithm

```
struct BipartiteGraph {
   const int INF = 1e9;
       vector<vector<int> > c; // cost matrix
vector<int> fx, fy; // potentials
vector<int> matchX, matchY; // corresponding vertex
vector<int> trace; // last vertex from the left side
vector<int> d, arg; // distance from the tree && the corresponding node
queue<int> Q; // queue used for BFS
        int n; // assume that |L| = |R| = n int start; // current root of the tree int finish; // leaf node of the augmenting path
        BipartiteGraph(int n) {
               this=>n = n;
c = vector<vector<int> >(n + 1, vector<int>(n + 1, INF));
fx = fy = matchX = matchY = trace = d = arg = vector<int>(n + 1);
        void initBFS(int root) {
    start = root;
    Q = queue<int>();    Q.push(start);
    for (int i = 1; i <= n; ++1) {
        trace[i] = 0;
        d[i] = cost(start, i);
        arg[i] = start;
    }</pre>
        int findPath() {
               Q.push(matchY[v]);
                               if (d[v] > w) d[v] = w, arg[v] = u;
                       }
       void enlarge() {
   for (int y = finish, next; y; y = next) {
      int x = trace[y];
      next = matchX[x];
      matchX[x] = y;
      matchY[y] = x;
}
              }
       fx(matchY[i]] += delta;
fy(i] -= delta;
} else {
    d[i] -= delta;
    if (d[i] == 0) {
        trace[i] = arg[i];
        if (matchY[i] == 0)
            finish = i;
        else
                                      else
                                               O.push(matchY[i]);
                              }
             }
        void hungarian() {
   for (int i = 1; i <= n; ++i) {
     initBFS(i);</pre>
                      inttrs(1),
do {
    finish = findPath();
    if (finish == 0) update();
} while (finish == 0);
                       enlarge();
              }
        }
       void show() {
   int ans = 0;
   for (int i = 1; i <= n; ++i) if (matchX[i]) ans += c[i][matchX[i]];
   cout << ans << endl;
   for (int i = 1; i <= n; ++i) cout << i << ' ' << matchX[i] << endl;</pre>
1:
```

6.8 Undirected mincut

```
* Find minimum cut in undirected weighted graph * Complexity: O(V^3)
#define SW StoerWagner
#define cap_t int
namespace StoerWagner {
          int n;
vector<vector<cap_t> > graph;
          vector<int> cut;
                   n = _n;

graph = vector < vector < cap_t >> (n, vector < cap_t > (n, 0));
          void addEdge(int a, int b, cap_t w) {
                   if (a == b) return;
graph[a][b] += w;
graph[b][a] += w;
         }
pair<cap_t, pair<int, int> > stMinCut(vector<int> &active) {
    vector<cap_t> key(n);
    vector<int> v(n);
    int s = -1, t = -1;
    for (int i = 0; i < active.size(); i++) {
        cap_t maxv = -1;
        int cur = -1;
        for (auto j : active) {
            if (v[j] == 0 && maxv < key[j]) {
                 maxv = key[j];
                  cur = j;
        }
}</pre>
                             t = s;
s = cur;
v[cur] = 1;
                             for (auto j : active) key[j] += graph[cur][j];
                    return make pair (key[s], make pair(s, t));
         cap_t solve() {
  cap_t res = numeric_limits <cap_t>::max();
  vector<vector<int>> grps;
                    vector<int> active;
                   vector<int> active;
cut.resize(n);
for (int i = 0; i < n; i++) grps.emplace_back(1, i);
for (int i = 0; i < n; i++) active.push_back(i);
while (active.size() >= 2) {
   auto stcut = stMinCut(active);
   if (stcut.first < res) {
      res = stcut.first;
      fill(cut.begin(), cut.end(), 0);
      for (auto v : grps[stcut.second.first]) cut[v] = 1;
   }</pre>
                               int s = stcut.second.first, t = stcut.second.second;
                             int s = stcut.second.first, t = stcut.second.second;
if (grps[s].size() < grps[t].size()) swap(s, t);
active.erase(find(active.begin(), active.end(), t));
grps[s].insert(grps[s].end(), grps[t].begin(), grps[t].end());
for (int i = 0; i < n; i++) {
    graph[i][s] += graph[i][t];
    graph[i][t] = 0;
}</pre>
                              for (int i = 0; i < n; i++) {
    graph[s][i] += graph[t][i];
    graph[t][i] = 0;</pre>
                              graph[s][s] = 0;
                    return res;
```

6.9 Eulerian Path/Circuit

};

6.10 2-SAT

7 Data structures

7.1 Treap

```
splitByKey(v->1, x, 1, v->1), r = v;
        update(v):
void splitByIndex(Node *v, int x, Node* &1, Node* &r) {
   if (!v) return void(1 = r = nullptr);
        push(v);
int index = size(v->1) + 1;
if (index < x)</pre>
                 splitByIndex(v\rightarrow r, x - index, v\rightarrow r, r), l = v;
        splitByIndex(v->1, x, 1, v->1), r = v;
update(v);
void show(Node *x) {
        if (!x) return;
push(x);
show(x->1);
cerr << x->key << ' ';</pre>
        show(x->r);
Node *root;
Node *1, *m, *r;
public:
Treap() { root = NULL; }
  Treap() { delete root; }
int size() { return size(root); }
int insert(int x) {
        insert(int x) {
splitByKey(mot, x, 1, m);
splitByKey(m, x + 1, m, r);
int ans = 0;
if (!m) m = new Node(x), ans = size(1) + 1;
join(1, 1, m);
join(root, 1, r);
return ans.
        return ans;
int erase(int x) {
    splitByKey(root, x, l, m);
    splitByKey(m, x + 1, m, r);
    int ans = 0;
    if (m) {
        ans = size(l) + 1;
    }
}
               delete m;
         join(root, l, r);
        return ans:
void insertAt(int pos, int x) {
        splitByIndex(root, pos, i
join(l, l, new Node(x));
join(root, l, r);
void eraseAt(int x) {
    splitByIndex(root, x, 1, m);
    splitByIndex(m, 2, m, r);
        delete m;
         join(root, 1, r);
void updateAt(int pos, int newValue) {
        eraseAt(pos);
insertAt(pos, newValue);
 int valueAt(int pos) {
        valueA(int pos) (
splitByIndex(root, pos, 1, m);
splitByIndex(m, 2, m, r);
int res = m->key;
join(l, 1, m);
join(root, 1, r);
        return res:
void reverse(int from, int to) {
   splitByIndex(root, from, l, m);
   splitByIndex(m, to - from + 2, m, r);
   m->rev_lazy ^= 1;
   join(l, l, m);
   join(root, l, r);
}
void show() {
   cerr << "Size = " << size() << " ";
   cerr << "[";</pre>
        show(root);
cerr << "]\n";</pre>
```

7.2 Big Integer

```
typedef vector<int> bigInt;
const int BASE = 1000;
const int LENGTH = 3;

// * Refine function
bigInt& fix(bigInt &a) {
    a.push_back(0);
    for (int i = 0; i + 1 < a.size(); ++i) {
        a[i + 1] += a[i] / BASE; a[i] %= BASE;
        if (a[i] < 0) a[i] += BASE, --a[i + 1];
    }
    while (a.size() > 1 && a.back() == 0) a.pop_back();
    return a;
}
// * Constructors
```

```
bigInt big(int x) {
         bigInt result;
while (x > 0) {
    result.push_back(x % BASE);
    x /= BASE;
         return result;
bigInt big(string s) {
   bigInt result(s.size() / LENGTH + 1);
   for (int i = 0; i < s.size(); ++i) {
      int pos = (s.size() - i - 1) / LENGTH;
      result[pos] = result[pos] * 10 + s[i] - '0';
}</pre>
         return fix(result), result;
 // * Compare operators
int compare(bigInt &a, bigInt &b) {
   if (a.size() != b.size()) return (int)a.size() - (int)b.size();
   for (int i = (int) a.size() - 1; i >= 0; --i)
      if (a[i] != b[i]) return a[i] - b[i];
 #define DEFINE OPERATOR(x) bool operator x (bigInt &a, bigInt &b) { return
 compare (a, b) x 0; }
DEFINE_OPERATOR(==)
DEFINE_OPERATOR(!=)
 DEFINE OPERATOR (>)
 DEFINE_OPERATOR(<)
DEFINE_OPERATOR(>=)
DEFINE_OPERATOR(<=)
 #undef DEFINE OPERATOR
 // * Arithmetic operators
fix(a);
void operator -= (bigInt &a, bigInt b) {
    for (int i = 0; i < b.size(); ++i)
        a[i] -= b[i];
    fix(a);</pre>
 void operator *= (bigInt &a, int b) {
  for (int i = 0; i < a.size(); ++i)
      a[i] *= b;</pre>
void divide(bigInt a, int b, bigInt &q, int &r) {
    for (int i = int(a.size()) - 1; i >= 0; --i) {
        r = r + BASE + a[i];
        q.push_back(r / b); r %= b;
         reverse(q.begin(), q.end());
fix(q);
bigInt operator + (bigInt a, bigInt b) { a += b; return a; }
bigInt operator - (bigInt a, bigInt b) { a -= b; return a; }
bigInt operator * (bigInt a, int b) { a *= b; return a; }
bigInt operator / (bigInt a, int b) {
   bigInt q; int r = 0;
   divide(a, b, q, r);
   return q;
}
 int operator % (bigInt a, int b) {
         bigInt q; int r = 0;
divide(a, b, q, r);
return r;
bigInt operator * (bigInt a, bigInt b) {
  bigInt result (a.size() + b.size());
  for (int i = 0; i < a.size(); ++i)
    for (int j = 0; j < b.size(); ++j)
      result[i + j] += a[i] * b[j];
  return fix(result);</pre>
 // * I/O routines
 istream& operator >> (istream& cin, bigInt &a) {
         string s; cin >> s;
a = big(s);
         return cin;
ostream& operator << (ostream& cout, const bigInt &a) {</pre>
         cout << a.back();
for (int i = (int)a.size() - 2; i >= 0; --i)
    cout << setw(LENGTH) << setfill('0') << a[i];</pre>
         cout << s
return cout;</pre>
```

7.3 Convex Hull IT

```
struct Line {
  long long a, b; // y = ax + b
  Line(long long a = 0, long long b = -INF): a(a), b(b) {}
  long long eval(long long x) {
    return a * x + b;
  }
};
```

8 Miscellaneous

8.1 RNG

```
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
//use mt19937_64 if we want 64-bit number
```