Bamboo Team Notes

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1 Number theory

1.1 Count primes up to N

```
// To initialize, call init_count_primes() first.
// Function count_primes(N) will compute the number of prime numbers lower than
// or equal to N.
//
// Time complexity: Around O(N ^ 0.75)
//
// Constants to configure:
// - MAX is the maximum value of sqrt(N) + 2
bool prime[MAX];
int prec[MAX];
int prec[MAX];
vector<int> P;
lint rec(llint N, int K) {
   if (N <= 1 | | K < 0) return 0;
   if (N <= P[K]) return N-1;

   if (N < MAX && llint(P[K]) *P[K] > N) return N-1 - prec[N] + prec[P[K]];
   const int LIM = 250;
   static int memo[LIM*LIM][LIM];
   bool ok = N < LIM*LIM;
   if (ok && memo[N][K]) return memo[N][K];
   llint ret = N/P[K] - rec(N/P[K], K-1) + rec(N, K-1);
   if (ok) memo[N][K] = ret;
   return ret;
}
llint count_primes(llint N) {
   if (N < MAX) return prec[N];
   int K = prec((int) sqrt(N) + 1];
   return N-1 - rec(N, K) + prec[P[K]];
}
void init_count_primes() {
   prime[2] = true;
   for (int i = 3; i < MAX; i += 2) prime[i] = true;
   for (int i = 3; i < MAX; i += 2) if (prime[i])</pre>
```

```
for (int j = i*i; j < MAX; j += i+i)
    prime[j] = false;
REP(i, MAX) if (prime[i]) P.push_back(i);
FOR(i, 1, MAX) prec[i] = prec[i-1] + prime[i];</pre>
```

1.2 Extended Euclide

```
int bezout(int a, int b) {
    // return x such that ax + by == gcd(a, b)
    int xa = 1, xb = 0;
    while (b) {
        int q = a / b;
        int r = a - q + b, xr = xa - q + xb;
        a = b; xa = xb;
        b = r; xb = xr;
    }
    return xa;
}

pair<int, int> solve(int a, int b, int c) {
    // solve ax + by == c
    int d = __gcd(a, b);
    int x = bezout(a, b);
    int y = (d - a + x) / b;
    c /= d;
    return make_pair(x + c, y + c);
}

int main() {
    int a = 100, b = 128;
    int c = __gcd(a, b);
    int x = bezout(a, b);
    int x = bezout(a, b);
    int y = (c - a + x) / b;
    cout << x < ' ' << y << endl;
    pair<int, int> xy = solve(100, 128, 40);
    cout << xy, first << ' ' << xy.second << endl;
    return 0;
}</pre>
```

1.3 System of linear equations

```
// extended version, uses diophantine equation solver to solve system of
    congruent equations
pair<int, int> solve(int a, int b, int c) {
    int cc = c;
    // solve ax + by == c
    int d = __gcd(a, b);
    int x = bezout(a / d, b / d);
    int y = (d - a * x) / b;
    c /= d;
    return make_pair(x * c, y * c);
}

int lcm(int a, int b) {
    return a / __gcd(a, b) * b;
}

// use this if input is large, make sure (#define int long long)
int mul(int a, int b, int p) {
        a % = p, b % = p;
        int q = (int) ((long double) a * b / p);
        int r = a * b - q * p;
        while (r < 0) r += p;
        while (r > 0) r += p;
        while (r > p) r -= p;
    return r;
}

int solveSystem(vector<int> a, vector<int> b) {
        // xi mod bi = ai
        int A = a[0], B = b[0];
        // x mod B = A
        for (int i = 1; i < a.size(); ++i) {
            int curB = b[i], curA = a[i];
            // x = Bi + A = curB * j + curA
            pair<int, int> ij = solve(B, -curB, curA - A);
            if (B * ij.first + A! = curB * ij.second + curA) return -1;
            int newB = lcm(B, curB);
            int newB = lcm(B, curB);
            int newB = newB;
            A = newA; B = newB;
            A = newA; B = newB;
            if (i + 1 == a.size()) return A;
        }

return -1;
}

int main() {
        vector<int> b = {3, 6, 9};
        cout << solveSystem(a, b) << endl;
        return 0;
}</pre>
```

1.4 Pollard Rho

```
#include <bits/stdc++.h>
using namespace std;

struct PollardRho {
   long long n;
   map<long long, int> ans;
   PollardRho (long long n) : n(n) {}
   long long random(long long u) {
      return abs(rand()) % u;
}
```

```
long long mul(long long a, long long b, long long p) {
                  g long mul(long long a, long long b, long long p) {
a %= p; b %= p;
long long q = (long long)((long double) a * b / p);
long long r = a * b - q * p;
while (r < 0) r += p;
while (r >= p) r -= p;
return r;
         long long pow(long long u, long long v, long long n) {
   long long res = 1;
   while (v) {
      if (v & 1) res = mul(res, u , n);
      u = mul(u, u, n);
      v >>= 1;
}
                    return res;
        bool rabin(long long n) {
   if (n < 2) return 0;
   if (n = 2) return 1;
   long long s = 0, m = n - 1;
   while (m % 2 == 0) {
      s++;
      m >>= 1;
   }
}
                  }
}// 1 - 0.9 ^ 40
for (int it = 1; it <= 40; it++) {
long long u = random(n - 2) + 2;
long long f = pow(u, m, n);
if (f == 1 || f == n - 1) continu
for (int i = 1; i < s; i++) {
    f = mul(f, f, n);
    if (f == 1) return 0;
    if (f == n - 1) break;
}</pre>
                                                                                          continue:
                            if (f != n - 1) return 0;
         long long f (long long x, long long n) {
    return (mul(x, x, n) + 1) % n;
         long long p - x,
while (p == 1) {
    x = f(x, n);
    y = f(f(y, n), n);
    p = __gcd(abs(x - y), n);
}
                   return p;
         if (n > 1) ans[n]++;
                            return;
                   if (rabin(n)) {
    ans[n]++;
                            return;
                   long long p = 0;
while (p == 0 || p == n) {
    p = findfactor(n);
}
                  pollard_rho(n / p);
pollard_rho(p);
};
int main() {
         main() {
long long n;
cin >> n;
PollardRho f(n);
f.pollard_rho(f.n);
for (auto x : f.ans) {
    cout << x.first << " " << x.second << endl;
}</pre>
```

2 String

2.1 Suffix Array

```
#include <bits/stdc++.h>
using namespace std;

struct SuffixArray {
    static const int N = 100010;
    int n;
    char *s;
    int sa[N], tmp[N], pos[N];
    int len, cnt[N], lcp[N];

SuffixArray(char *t) {
        s = t;
}
```

```
n = strlen(s + 1);
buildSA();
                 bool cmp(int u, int v) {
   if (pos[u] != pos[v]) {
      return pos[u] < pos[v];
}</pre>
                                      return (u + len <= n && v + len <= n) ? pos[u + len] < pos[v + len] :
                   void radix(int delta) {
                                       fraction in the content of the 
                                      for (int i = 1; i < N; i++) {
    cnt[i] += cnt[i - 1];</pre>
                                      for (int i = n; i > 0; i--) {
   int id = sa[i];
   tmp[cnt[id + delta <= n ? pos[id + delta] : 0]--] = id;</pre>
                                      for (int i = 1; i <= n; i++) {
    sa[i] = tmp[i];</pre>
                   void buildSA() {
   for (int i = 1; i <= n; i++) {
     sa[i] = i;</pre>
                                      while (1) {
                                                        for (int i = 1; i <= n; i++) {
   pos[sa[i]] = tmp[i];
}</pre>
                                                           if (tmp[n] == n) {
                                                                            break:
                                                           len <<= 1;
                                      len = 0;
for (int i = 1; i <= n; i++) {
    if (pos[i] == n) {</pre>
                                                                            continue;
                                                         int j = sa[pos[i] + 1];
while (s[i + len] == s[j + len]) {
                                                         lcp[pos[i]] = len;
if (len) {
                                                       len--;
                                  }
};
```

2.2 Aho Corasick

2.3 Z algorithm

```
vector<int> calcZ(const string &s) {
  int L = 0, R = 0;
  int n = s.size();
  vector<int> Z(n);
  Z[0] = n;
  for (int i = 1; i < n; i++) {
    if (i > R)
    {
        L = R = i;
        while (R < n && s[R] == s[R - L]) R++;
        Z[i] = R - L; R--;
    }
  else
    {
        int k = i - L;
        if (Z[k] < R - i + 1) Z[i] = Z[k];
        else
        {
        L = i;
        while (R < n && s[R] == s[R - L]) R++;
        Z[i] = R - L; R--;
        }
    }
  }
  return Z;
}</pre>
```

2.4 Manacher

2.5 Suffix Automaton

```
//set last = 0 everytime we add new string
struct SuffixAutomaton {
    static const int N = 100000;
    static const int CHARACTER = 26;
    int suf[N * 2], nxt[N * 2][CHARACTER], cnt, last, len[N * 2];

SuffixAutomaton() {
    memset (suf, -1, sizeof suf);
    memset (nxt, -1, sizeof nxt);
    memset (nxt, -1, sizeof nxt);
    memset (len, 0, sizeof len);
    last = cnt = 0;
}

int getNode(int last, int u) {
    int q = nxt[last][u];
    if (len[last] + 1 == len[q]) {
        return q;
    }
    int clone = ++cnt;
    len[clone] = len[last] + 1;
    for (int i = 0; i < CHARACTER; i++) {
        nxt[clone][i] = nxt[q][i];
    }
    while (last != -1 && nxt[last][u] == q) {
        nxt[last][u] = clone;
        last = suf[last];
    }
    suf[clone] = suf[q];
    return suf[q] = clone;
}

void add(int u) {
    if (nxt[last][u] == -1) {
        int newNode = ++cnt;
        len[newNode] = len[last] + 1;
        while (last != -1 && nxt[last][u] == -1) {
            nxt[last][u] = newNode;
            last = suf[last];
    }
    if (last == -1) {
            suf[newNode] = 0;
            last = newNode;
            return;
    }
    suf[newNode] = qetNode (last, u);
}</pre>
```

```
last = newNode;
} else {
    last = getNode(last, u);
}
};
```

3 Combinatorial optimization

4 Geometry

4.1 Geometry

```
#define EPS 1e-6 inline int cmp(double a, double b) { return (a < b - EPS) ? -1 : ((a > b + EPS) ? -1 : (ta > b + EPS) ) ? 1 : 0); } struct Point {
       double x, y;
Point() { x = y = 0.0; }
Point(double x, double y) : x(x), y(y) {}
      Point operator + (const Point& a) const { return Point(x+a.x, y+a.y); } Point operator - (const Point& a) const { return Point(x-a.x, y-a.y); } Point operator + (double k) const { return Point(x+k, y+k); } Point operator / (double k) const { return Point(x/k, y/k); }
       double operator * (const Point& a) const { return x*a.x + y*a.y; } // dot
       double operator % (const Point& a) const { return x*a.y - y*a.x; } //
       double angle(Point a, Point o, Point b) { // min of directed angle AOB & BOA
    a = a - o; b = b - o;
    return acos((a * b) / sqrt(a.norm()) / sqrt(b.norm()));
double directed_angle(Point a, Point o, Point b) { // angle AOB, in range [0,
       return t;
}
// Distance from p to Line ab (closest Point --> c)
double distToLine(Point p, Point a, Point b, Point &c) {
   Point ap = p - a, ab = b - a;
   double u = (ap * ab) / ab.norm();
   c = a + (ab * u);
   return (p-c).len();
}
}
// Distance from p to segment ab (closest Point --> c)
double distToLineSegment(Point p, Point a, Point b, Point &c) {
   Point ap = p - a, ab = b - a;
   double u = (ap * ab) / ab.norm();
   if (u < 0.0) {
      c = Point(a.x, a.y);
      return (p - a).len();
}</pre>
       if (u > 1.0) {
    c = Point(b.x, b.y);
}
              return (p - b).len();
       return distToLine(p, a, b, c);
 ^{
m } // NOTE: WILL NOT WORK WHEN a = b = 0.
Line(double a, double b, double c) : a(a), b(b), c(c) {}
       Line(Point A, Point B) : A(A), B(B) {
    a = B.y - A.y;
    b = A.x - B.x;
              c = - (a * A.x + b * A.y);
       Line (Point P, double m) {
              a = -m; b = 1;

c = -((a * P.x) + (b * P.y));
       double f(Point A) {
   return a*A.x + b*A.y + c;
bool areParallel(Line 11, Line 12) {
   return cmp(11.a*12.b, 11.b*12.a) == 0;
}
bool areIntersect(Line 11, Line 12, Point &p) {
    if (areParallel(11, 12)) return false;
    double dx = 11.b*12.c - 12.b*11.c;
    double dy = 11.c*12.a - 12.c*11.a;
    double d = 11.a*12.b - 12.a*11.b;
    p = Point(dx/d, dy/d);
    return true;
}
 void closestPoint(Line 1, Point p, Point &ans) {
   if (fabs(1.b) < EPs) {
        ans.x = -(1.c) / 1.a; ans.y = p.y;
}</pre>
```

```
return;
           if (fabs(1.a) < EPS) {
    ans.x = p.x; ans.y = -(1.c) / 1.b;</pre>
                    return;
           Line perp(1.b, -1.a, - (1.b*p.x - 1.a*p.y));
areIntersect(1, perp, ans);
 void reflectionPoint(Line 1, Point p, Point &ans) {
           Point b;
closestPoint(l, p, b);
ans = p + (b - p) * 2;
 struct Circle : Point {
           double r;
           double r;
Circle(double x = 0, double y = 0, double r = 0) : Point(x, y), r(r) {}
Circle(Point p, double r) : Point(p), r(r) {}
bool contains(Point p) { return (*this - p).len() <= r + EPS; }</pre>
  // Find common tangents to 2 circles
            http://codeforces.com/gym/100803/ - H
 break:
                    if (ok) ret.push_back(ans[i]);
           return ret:
 // Circle & line intersection
vector<Point> intersection(Line l, Circle cir) {
   double r = cir.r, a = l.a, b = l.b, c = l.c + l.a*cir.x + l.b*cir.y;
   vector<Point> res;
   double x0 = -a*c*/(a*a+b*b), y0 = -b*c*/(a*a+b*b);
   if (c*c > r*r**(a*a+b*b)+EPS) return res;
   else if (fabs(c*c - r*r**(a*a+b*b)) < EPS) {
      res.push_back(Point(x0, y0) + Point(cir.x, cir.y));
      return res;
   }</pre>
  // Circle & line intersection
           else {
                   e {
    double d = r*r - c*c/(a*a+b*b);
    double mult = sqrt (d / (a*a+b*b));
    double ax, ay, bx, by;
    ax = x0 + b * mult;
    bx = x0 - b * mult;
    ay = y0 - a * mult;
    by = y0 + a * mult;
    by = y0 + a * mult;
    res. push_back(Point(ax, ay) + Point(cir.x, cir.y));
    res. push_back(Point(bx, by) + Point(cir.x, cir.y));
    return res:
                    return res;
 // helper functions for commonCircleArea
double cir_area_solve(double a, double b, double c) {
   return acos((a*a + b*b - c*c) / 2 / a / b);
}
double cir_area_cut(double a, double r) {
  double s1 = a * r * r / 2;
  double s2 = sin(a) * r * r / 2;
  return s1 - s2;
 double commonCircleArea(Circle c1, Circle c2) { //return the common area of
          ble commonCircleArea(Circle c1, Circle c2) { //return the con
two circle
if (cl.r < c2.r) swap(c1, c2);
double d = (cl - c2).len();
if (d + c2.r <= c1.r + EPS) return c2.r*c2.r*M_PI;
if (d >= c1.r + c2.r - EPS) return 0.0;
double al = cir_area_solve(d, c1.r, c2.r);
double a2 = cir_area_solve(d, c2.r, c1.r);
return cir_area_cut(a1*2, c1.r) + cir_area_cut(a2*2, c2.r);
        Check if 2 circle intersects. Return true if 2 circles touch
bool areIntersect(Circle u, Circle v) {
   if (cmp((u - v).len(), u.r + v.r) > 0) return false;
   if (cmp((u - v).len() + v.r, u.r) < 0) return false;
   if (cmp((u - v).len() + u.r, v.r) < 0) return false;</pre>
           return true;
 }
// If 2 circle touches, will return 2 (same) points
// If 2 circle are same --> be careful
vector<Point> circleIntersect(Circle u, Circle v) {
    vector<Point> res;
    if (!areIntersect(u, v)) return res;
    double d = (u - v).len();
    double alpha = acos((u.r * u.r + d*d - v.r * v.r) / 2.0 / u.r / d);
           Point p1 = (v - u).rotate(alpha);

Point p2 = (v - u).rotate(-alpha);

res.push_back(p1 / p1.len() + u.r + u);

res.push_back(p2 / p2.len() + u.r + u);
           return res:
```

```
Point centroid(Polygon p) {
    Point c(0,0);
    double scale = 6.0 * signed_area(p);
    for (int i = 0; i < p.size(); i++) {
        int j = (i+1) % p.size();
        c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
}</pre>
          return c / scale;
 /// Cut a polygon with a line. Returns one half.
// To return the other half, reverse the direction of Line 1 (by negating 1.a,
                1.b)
 // The line must be formed using 2 points
Polygon polygon_cut (const Polygon& P, Line 1) {
         polygon Q;
Polygon Q;
for(int i = 0; i < P.size(); ++i) {
    Point A = P[i], B = (i == P.size()-1) ? P[0] : P[i+1];
    if (ccw(l.A, l.B, A) != -1) Q.push_back(A);
    if (ccw(l.A, l.B, A) +ccw(l.A, l.B, B) < 0) {
        Point p; areIntersect(Line(A, B), l, p);
        Q.push_back(p);
}</pre>
          return 0:
  // Find intersection of 2 convex polygons
// Find intersection of 2 convex polygons
// Helper method
bool intersect_lpt(Point a, Point b,
    Point c, Point d, Point &r) {
    double D = (b - a) % (d - c);
    if (cmp(D, 0) == 0) return false;
    double t = ((c - a) % (d - c)) / D;
    double s = -((a - c) % (b - a)) / D;
    r = a + (b - a) * t;
    return cmp(t, 0) >= 0 && cmp(t, 1) <= 0 && cmp(s, 0) >= 0 && cmp(s, 1) <=
}</pre>
Polygon convex_intersect(Polygon P, Polygon Q) {
   const int n = P.size(), m = Q.size();
   int a = 0, b = 0, aa = 0, ba = 0;
   enum { Pin, Qin, Unknown } in = Unknown;
          Polygon R;
          do {
                  [
int al = (a+n-1) % n, bl = (b+m-1) % m;
double C = (P[a] - P[a1]) % (Q[b] - Q[b1]);
double A = (P[a1] - Q[b]) % (P[a] - Q[b]);
double B = (Q[b1] - P[a]) % (Q[b] - P[a]);
                  double B = (Q[b1] - P[a]) % (Q[b] - P[a]);
Point r;
if (intersect_lpt(P[a1], P[a], Q[b1], Q[b], r)) {
   if (in == Unknown) aa = ba = 0;
   R.push_back(r);
   in = B > 0 ? Pin : A > 0 ? Qin : in;
                  { if (in == Qin) R.push_back(Q[b]); b = (b+1)%m; ++ba;
                                         }
                  } else {
                            if (B > 0) { if (in == Qin) R.push_back(Q[b]); b = (b+1)%m; ++ba;
                                                    { if (in == Pin) R.push back(P[a]); a = (a+1)%n; ++aa;
                            else
         } while ( (aa < n || ba < m) && aa < 2*n && ba < 2*m );
if (in == Unknown) {
   if (in_convex(Q, P[0])) return P;
   if (in_convex(P, Q[0])) return Q;</pre>
          return R;
 }
// Find the diameter of polygon.
// Rotating callipers
double convex_diameter(Polygon pt) {
   const int n = pt. size();
   int is = 0, js = 0;
   for (int i = 1; i < n; ++i) {
      if (pt[i].y > pt[is].y) is = i;
      if (pt[i].y < pt[js].y) js = i;
   }
}</pre>
          double maxd = (pt[is]-pt[js]).norm();
          int i, maxi = (pt[1s]
int i, maxi, j, maxj;
i = maxi = is;
j = maxj = js;
                  {
int jj = j+1; if (jj == n) jj = 0;
if ((pt[i] - pt[j]).norm() > (pt[i] - pt[j]).norm()) j = (j+1) % n;
else i = (i+1) % n;
if ((pt[i]-pt[j]).norm() > maxd) {
    maxd = (pt[i]-pt[j]).norm();
    maxi = i; maxj = j;
}
          } while (i != is || j != js);
return maxd; /* farthest pair is (maxi, maxj). */
   ^{\prime\prime} Check if we can form triangle with edges x, y, z.
 bool isSquare(long long x) { /* */ }
bool isIntegerCoordinates(int x, int y, int z) {
  long long se(long long) (x+y+z) * (x+y-z) * (x+z-y) * (y+z-x);
  return (s%4==0 && isSquare(s/4));
 // Given non-intersecting polygon.
// S = area
 Circle getCircle(vector<Point> points) {
   assert(!points.empty());
   random_shuffle(points.begin(), points.end());
```

5 Numerical algorithms

5.1 Gauus Elimination

5.2 Simplex Algorithm

```
* minimize c^T * x

* subject to Ax <= b
```

```
* The input matrix a will have the following form * O c c c c c c * b A A A A A
  * Result vector will be: val x x x x x **/
for (int i = 0; i <= n; i++) {
   if (fabs(a[i][y]) < EPS || i == x) continue;
   k = a[i][y];
   a[i][y] = 0;</pre>
                  for (int j : pos) a[i][j] -= k * a[x][j];
         };
while (1) {
   int x = -1;
   for (int i = 1; i <= n; i++) {
    if (a[i][0] < -EPS && (x == -1 || a[i][0] < a[x][0])) {</pre>
              if (x == -1) break;
             int y = -1;
for (int j = 1; j <= m; j++) {
    if (a[x][j] < -EPS && (y == -1 || a[x][j] < a[x][y])) {</pre>
              if (y == -1) return vector<ld>(); // infeasible
          while (1) {
             -1;
             if (x == -1) return vector<ld>(); // unbounded
             pivot(x, v);
         for (int i = 1; i <= n; i++) {
   if (left[i] <= m) ans[left[i]] = a[i][0];</pre>
         ans[0] = -a[0][0];
return ans;
};
```

5.3 NTT

```
void fft (vector<int> &a) {
                         a fit(vector<int> &a) {
   int n = a.size();
   int curBase = 0;
   while (1 << curBase) < n) curBase++;
   int shift = base - curBase;
   for (int i = 0; i < n; i++) {
      if (i < (rev[i] >> shift)) swap(a[i], a[rev[i] >> shift]);
    }
}
                                      (int k = 1; k < n; k <<= 1) {
for (int i = 0; i < k; i++) {
   for (int j = i; j < n; j += k * 2) {
      int foo = a[j];
      int bar = mul(a[j + k], w[i + k]);
      a[j] = add(foo, bar);
      a[j + k] = sub(foo, bar);
   }
}</pre>
                          for (int k = 1; k < n; k <<= 1) {
                                     }
              vector<int> mult(vector<int> a, vector<int> b) {
  int nResult = a.size() + b.size() - 1;
  int curBase = 0;
  while (1 << curBase) < nResult) curBase++;</pre>
                         while ((1 << curBase) < nResult) curBase
ensure(curBase);
int n = 1 << curBase;
a.resize(n), b.resize(n);
fft(a);
fft(b);
int invN = inv(n);
for (int i = 0; i < n; i++) {
    a[i] = mul(mul(a[i], b[i]), invN);
}</pre>
                          reverse(a.begin() + 1, a.end());
fft(a);
a.resize(nResult);
                          return a;
              vector<int> polyInv(vector<int> r, vector<int> f) {
                         corsint> polylinv(vectorsint> r, vectorsi
vectorsint> foo = mult(r, f);
foo.resize(f.size());
foo[0] = sub(2, foo[0]);
for (int i = 1; i < foo.size(); i++) {
    foo[i] = sub(0, foo[i]);
}</pre>
                          }
vector<int> res = mult(r, foo);
res.resize(f.size());
                          return res:
             }
vector<int> polySqrt(vector<int> s, vector<int> invS, vector<int> f) {
    vector<int> res = mult(f, invS);
    res.resize(f.size());
    for (int i = 0; i < s.size(); i++) {
        res[i] = add(res[i], s[i]);
}</pre>
                          for (int i = 0; i < res.size(); i++) {
    res[i] = mul(res[i], INV_2);</pre>
                          return res:
            }
vector<int> getSqrt(vector<int> c, int sz) {
    vector<int> sqrtC = {1}, invSqrtC = {1}; //change this if c[0] != 1
    for (int k = 1; k < (1 << sz); k <<= 1) {
        vector<int> foo(c.begin(), c.begin() + (k + 2));
        vector<int> bar = sqrtC;
        bar.resize(bar.size() + 2, 0);
        vector<int> tempInv = polyInv(invSqrtC, bar);
        sqrtC = polySqrt(sqrtC, tempInv, foo);
        invSqrtC = polyInv(invSqrtC, sqrtC);
}
                          return sqrtC;
            }
vector<int> getInv(vector<int> c, int sz) {
    vector<int> res = {INV_2}; // change this if c[0] != 2
    for (int k = 1; k < (1 << sz); k <<= 1) {
        vector<int> foo (c.begin(), c.begin() + (k * 2));
        res = polyInv(res, foo);
    }
}
                          return res;
1 ntt:
```

5.4 FFT

```
while (fftSz < newSz) {
    fftSz <<= 1;
}
VC aa(fftSz, 0.), bb(fftSz, 0.);
for (int i = 0; i < a.size(); i++) {
    aa[i] = a[i];
}
for (int i = 0; i < b.size(); i++) {
    bb[i] = b[i];
}
fft(aa, 1);
fft(bb, 1);
for (int i = 0; i < fftSz; i++) {
    aa[i] *= bb[i];
}
fft(aa, -1);
vector</pre>
vector
for (int i = 0; i < fftSz; i++) {
    res[i] = (int) (aa[i].real() / fftSz + 0.5);
}
return res;
}
</pre>
```

5.5 Bitwise FFT

```
/*
* matrix:
* +1 +1
* +1 -1
*/
void XORFFT(int a[], int n, int p, int invert) {
   for (int i = 1; i < n; i <<= 1) {
      for (int j = 0; j < n; j += i << 1) {
        for (int k = 0; k < i; k++) {
            int u = a[j + k], v = a[i + j + k];
            a[j + k] = u + v;
            if (a[j + k] >= p) a[j + k] -= p;
            a[i + j + k] = u - v;
            if (a[i + j + k] < 0) a[i + j + k] += p;
      }
}</pre>
                              }
                     }
           if (invert) {
                      long long inv = fpow(n, p - 2, p);
for (int i = 0; i < n; i++) a[i] = a[i] * inv % p;</pre>
 * Matrix:
* +1 +1
* +1 +0
else (
                                                      a {
   a[j + k] = v;
   a[i + j + k] = u - v;
   if (a[i + j + k] < 0) a[i + j + k] += p;</pre>
                   }
         }
 * matrix:
 * +0 +1
* +1 +1
 void ANDFFT(int a[], int n, int p, int invert) {
          d ANDFFT(int a[], int n, int p, int invert) {
  for (int i = 1; i < n; i <<= 1) {
    for (int j = 0; j < n; j += i << 1) {
      for (int k = 0; k < i; k++) {
        int u = a[j + k], v = a[i + j + k];
        if (!invert) {
            a[j + k] = v;
            a[i + j + k] = u + v;
            if (a[i + j + k] >= p) a[i + j + k] -= p;
      }
}
                                            lse {
    a[j + k] = v - u;
    if (a[j + k] < 0) a[j + k] += p;
    a[i + j + k] = u;</pre>
                                          }
      }
```

5.6 FFT chemthan

```
#define double long double
namespace FFT {
    const int maxf = 1 << 17;
    struct cp {
        double x, y;
        cp (double x = 0, double y = 0) : x(x), y(y) {}
        cp operator + (const cp& rhs) const {
            return cp(x + rhs.x, y + rhs.y);
        }
        cp operator - (const cp& rhs) const {
            return cp(x - rhs.x, y - rhs.y);
        }
}</pre>
```

```
return cp(x * rhs.x - y * rhs.y, x * rhs.y + y * rhs.x);
          cp operator !() const {
                   return cp(x, -y);
 } rts[maxf + 1];
cp fa[maxf], fb[maxf];
cp fc[maxf], fd[maxf];
rts[0] = rts[maxf] = cp(1, 0);

for (int i = 1; i + i <= maxf; i++) {

   rts[i] = cp(cos(i * 2 * PI / maxf), sin(i * 2 * PI / maxf));
          for (int i = maxf / 2 + 1; i < maxf; i++) {</pre>
                   rts[i] = !rts[maxf - i];
 }
void dft(cp a[], int n, int sign) {
    static int isinit;
    if (!isinit) {
        isinit = 1;
    }
}
                  fftinit();
          }
int d = 0; while ((1 << d) * n != maxf) d++;
for (int i = 0; i < n; i++) {
   if (i < (bitrev[i] >> d)) {
       swap(a[i], a[bitrev[i] >> d]);
}
         }
for (int len = 2; len <= n; len <<= 1) {
    int delta = maxf / len * sign;
    for (int i = 0; i < n; i += len) {
        cp *x = a + i, *y = a + i + (len >> 1), *w = sign > 0 ? rts :
            rts + maxf;
        for (int k = 0; k + k < len; k++) {
            cp z = *y * *w;
            *y = *x - z, *x = *x + z;
            x++, y++, w += delta;
    }
}</pre>
                  }
         if (sign < 0) {
   for (int i = 0; i < n; i++) {
      a[i] x /= n;
      a[i] y /= n;
}</pre>
}
void multiply(int a[], int b[], int na, int nb, long long c[]) {
    int n = na + nb - 1; while (n != (n & -n)) n += n & -n;
    for (int i = 0; i < n; i++) fa[i] = fb[i] = cp();
    for (int i = 0; i < na; i++) fa[i] = cp(a[i]);
    for (int i = 0; i < nb; i++) fb[i] = cp(a[i]);
    dft(fa, n, 1), dft(fb, n, 1);
    for (int i = 0; i < n; i++) fa[i] = fa[i] * fb[i];
    dft(fa, n, -1);
    for (int i = 0; i < n; i++) c[i] = (long long) floor(fa[i].x + 0.5);
}</pre>
        void multiply(int a[], int b[], int na, int nb, int c[], int mod = (int) 1
          }
dft(fc, n, -1), dft(fd, n, -1);
for (int i = 0; i < n; i++) {
   long long u = ((long long) floor(fc[i].x + 0.5)) % mod;
   long long v = ((long long) floor(fd[i].x + 0.5)) % mod;
   long long w = ((long long) floor(fd[i].y + 0.5)) % mod;
   c[i] = ((u << 15) + v + (w << 30)) % mod;</pre>
  vector<int> multiply(vector<int> a, vector<int> b, int mod = (int) 1e9 +
          static int fa[maxf], fb[maxf], fc[maxf];
         int na = a.size(), nb = b.size();
for (int i = 0; i < na; i++) fa[i] = a[i];
for (int i = 0; i < nb; i++) fb[i] = b[i];
multiply(fa, fb, na, nb, fc, mod);
int k = na + nb - 1;</pre>
          rector(int) res(k);
for (int i = 0; i < k; i++) res[i] = fc[i];
return res;</pre>
```

5.7 Partition Formula

```
* generating function : PI: (1 / (1 - x ^k))
```

```
* p(n) = p(n-1) + p(n-2) - p(n-5) - p(n-7) + p(n-12) + p(n-15) - p(n-22) - \dots

* p\_k = k * (3k - 1) / 2 with k = 1, -1, 2, -2, 3, -3, \dots

*/
```

5.8 Generating function

```
// 1 / ( (1-ax) ^ (k+1) ) = sum_{(0->INF)_{(n+k,k)}} * C(n+k,k) * x^n }
```

5.9 Chinese Remainder Theorem

```
Let m, n, a, b be any interger. Let g = gcd(m, n).

x \% m = a

x \% n = b

if (a \% g == b \% g): it has unique solution modulo lcm(n, m)

else: no solution

g = u * m + v * n

x = (a * v * n + b * u * m) / g
```

6 Graph algorithms

6.1 Bridges and Articulations

6.2 Bipartite Maximum Matching

```
struct BipartiteGraph {
  vector< vector<int> a;
  vector<int> match;
  vectorSool> was;
  int m, n;

BipartiteGraph(int m, int n) {
    // zero-indexed
    this->m = m; this->n = n;
    a.resize(m);
    match.assign(n, -l);
    was.assign(n, false);
}

void addEdge(int u, int v) {
    a[u].push_back(v);
}

bool dfs(int u) {
    for (int v : a[u]) if (!was[v]) {
        was[v] = true;
        if (match[v] == -1 || dfs(match[v])) {
            match[v] = u;
            return true;
        }
    return false;
}

int maximumMatching() {
    vector<int> buffer;
    for (int i = 0; i < m; ++i) buffer.push_back(i);
    bool stop = false;
    int ans = 0;
    do {
        stop = true;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
        for (int i = 0; i < n; ++i) was[i] = false;
```

6.3 General Matching

6.4 Dinic Flow

```
const int V = 1e5;
const int INF = 1e9;
const Int Inf = ley;
struct Flow {
   vector<int> adj[V];
   int to[V], c[V], f[V];
   int n, s, t, cnt;
   int d[V];
         int d[V];
int cur[V];
Flow(int n, int s, int t) {
    this->n = n;
    this->s = s;
    this->t = t;
    cnt = 0;
         }
int addEdge(int u, int v, int _c) {
    to[ent] = v, c[ent] = _c, f[ent] = 0;
    adj[u].push_back(ent++);
    to[ent] = u, c[ent] = 0, f[ent] = 0;
    adj[v].push_back(ent++);
                  lbis() {
for (int i = 0; i < n; i++) d[i] = -1;
d[s] = 0;
queue<iint> q;
                  queuexinty
q,
q.push(s);
while (!q.empty()) {
   int u = q.front();
   q.pop();
   for (int id : adj[u]) {
                                    int v = to[id];

if (d[v] == -1 && f[id] < c[id]) {

    d[v] = d[u] + 1;
                                            q.push(v);
                          }
                  return d[t] != -1;
        return foo;
                            }
                  return 0:
         int maxFlow() {
                  maxfilow() {
  int res = 0;
  while (bfs()) {
    for (int i = 0; i < n; i++) cur[i] = 0;
    while (1) {
        int foo = dfs(s, INF);
    }
}</pre>
                                int foo = als(s,
if (!foo) break;
res += foo;
                  return res;
};
```

6.5 Min Cost-Max Flow

```
struct Flow {
    static const int V = 100000;
    int head[V], to[V], c[V], cost[V], f[V], nxt[V], h[V], par[V], inQueue[V];
    int s, t, n, cnt;
    queue <int> q;
    Flow (int n, int s, int t) {
```

```
this->n = n;
                 this->s = s;
this->t = t;
                 cnt = 0;
for (int i= 0; i < n; i++) {
   head[i] = -1;
   inQueue[i] = 0;</pre>
        pair<int, int> maxFlow () {
  int res = 0, minCost = 0;
  while (1) {
                          le (1) {
  for (int i = 0; i < n; i++) {
    par[i] = -1;
    h[i] = 2e9;</pre>
                          h[s] = 0;
                          h(s) = 0;
q.push(s);
inQueue[s] = 1;
while (!q.empty()) {
    int u = q.front();
                                  inqueue[u] = 0;
inqueue[u] = 0;
for (int id = head[u]; id != -1; id = nxt[id]) {
   int v = to[id];
   if (h[v] > h[u] + cost[id] && f[id] < c[id]) {
      h[v] = h[u] + cost[id];
      par[v] = id;
   if (!inqueue[v]) {
      inqueue[v] = 1;
      q.push(v);
   }
}</pre>
                                    q.pop();
inQueue[
                           if (par[t] == -1) {
                                   break;
                          }
int x = t;
int now = 2e9;
while (x != s) {
   int id = par[x];
   now = min(now, c[id] - f[id]);
   x = to[id ^ 1];
                           while (x != s) {
                                   int id = par[x];
minCost += cost[id] * now;
f[id] += now;
f[id ^ 1] -= now;
x = to[id ^ 1];
                 return make_pair(res, minCost);
};
```

6.6 Bounded Feasible Flow

```
while (findPath()) incFlow();
    return flow;
}
bool feasible() {
    c[t][s] = INF;
    s = n + 1; t = n + 2;
    int sum = 0;
    for (int u = 1; u <= n; ++u) for (int v = 1; v <= n; ++v) {
        c[s][v] + = low[u][v];
        c[u][t] + = low[u][v];
        c[u][v] + = high[u][v] - low[u][v];
        sum += low[u][v];
    }
    n += 2;
    return maxFlow() == sum;
};</pre>
```

6.7 Hungarian Algorithm

```
struct BipartiteGraph {
   const int INF = 1e9;
       vector<vector<int> > c; // cost matrix
vector<int> fx, fy; // potentials
vector<int> matchX, matchY; // corresponding vertex
vector<int> trace; // last vertex from the left side
vector<int> d, arg; // distance from the tree && the corresponding node
queue<int> Q; // queue used for BFS
       int n; // assume that |L| = |R| = n int start; // current root of the tree int finish; // leaf node of the augmenting path
       BipartiteGraph(int n) {
    this>n = n;
    c = vector<vector<int> >(n + 1, vector<int>(n + 1, INF));
    fx = fy = matchX = matchY = trace = d = arg = vector<int>(n + 1);
       void initBFS(int root) {
               start = root;
Q = queue(int)(); Q.push(start);
for (int i = 1; i <= n; ++i) {
    trace[i] = 0;
    d[i] = cost(start, i);
    arg[i] = start;
}</pre>
       int findPath() {
               findPath() {
while (!Q.empty()) {
   int u = Q.front(); Q.pop();
   for (int v = 1; v <= n; ++v) if (trace[v] == 0) {
      int w = cost(u, v);
      if (w == 0) {
            trace[v] = u;
            if (matchY[v] == 0) return v;
            Q.push(matchY[v]);
      }
}</pre>
                                if (d[v] > w) d[v] = w, arg[v] = u;
                       }
       void enlarge() {
   for (int y = finish, next; y; y = next) {
      int x = trace[y];
      next = matchX[x];
      matchX[x] = y;
      matchY[y] = x;
}
              }
       O.push(matchY[i]);
                              }
              }
       }
       void hungarian() {
   for (int i = 1; i <= n; ++i) {
     initBFS(i);</pre>
                       initBFS(1);
do {
    finish = findPath();
    if (finish == 0) update();
} while (finish == 0);
enlarge();
              }
       void show() {
    int ans = 0;
               for (int i = 1; i <= n; ++i) if (matchX[i]) ans += c[i][matchX[i]];</pre>
```

```
cout << ans << endl;
    for (int i = 1; i <= n; ++i) cout << i << ' ' << matchX[i] << endl;
};</pre>
```

6.8 Undirected mincut

```
* Find minimum cut in undirected weighted graph * Complexity: O(V^3)
#define SW StoerWagner
#define cap_t int
namespace StoerWagner {
        int n;
vector<vector<cap_t> > graph;
          vector<int> cut;
         void init(int _n) {
                 n = _n;
graph = vector<vector<cap_t>>(n, vector<cap_t>(n, 0));
         void addEdge(int a, int b, cap_t w) {
                  if (a == b) return;
graph[a][b] += w;
graph[b][a] += w;
        int cur = -1
for (auto j : active) {
   if (v[j] == 0 && maxv < key[j]) {
      maxv = key[j];
      cur = j;
      cur = j;
}</pre>
                         t = s;
s = cur;
v[cur] = 1;
                           for (auto j : active) key[j] += graph[cur][j];
                  return make_pair(key[s], make_pair(s, t));
        }
cap_t solve() {
   cap_t res = numeric_limits <cap_t>::max();
   vector<vector<int>> grps;
   vector<int>> active;
   resize(n).
                 vector<int> active;
cut.resize(n);
for (int i = 0; i < n; i++) grps.emplace_back(1, i);
for (int i = 0; i < n; i++) active.push_back(i);
while (active.size() >= 2) {
    auto stcut = stMinCut(active);
    if (stcut.first < res) {
        res = stcut.first;
        fill(cut.begin(), cut.end(), 0);
        for (auto v : grps[stcut.second.first]) cut[v] = 1;
    }
}</pre>
                           }
int s = stcut.second.first, t = stcut.second.second;
if (grps[s].size() < grps[t].size()) swap(s, t);
active.erase(find(active.begin(), active.end(), t));
grps[s].insert(grps[s].end(), grps[t].begin(), grps[t].end());
for (int i = 0; i < n; i++) {
    graph[i][s] += graph[i][t];
    graph[i][t] = 0;</pre>
                           for (int i = 0; i < n; i++) {
    graph[s][i] += graph[t][i];
    graph[t][i] = 0;</pre>
                           graph[s][s] = 0;
                  return res:
```

6.9 Eulerian Path/Circuit

```
struct EulerianGraph {
  vector< vector< pair<int, int> >> a;
  int num_edges;

EulerianGraph(int n) {
    a.resize(n + 1);
    num_edges = 0;
}

void add_edge(int u, int v, bool undirected = true) {
    a[u].push_back(make_pair(v, num_edges));
    if (undirected) a[v].push_back(make_pair(u, num_edges));
    num_edges++;
}

vector<int> get_eulerian_path() {
    vector<int> path, s;
    vector<bool> was(num_edges);
    s.push_back(1); // start of eulerian path
    while (!s.empty()) {
        int u = s.back();
        bool found = false;
        while (!a[u].empty()) {
            int v = a[u].back().first;
            int e = a[u].back().second;
            a[u].pop_back();
            if (was[e]) continue;
            was[e] = true;
```

```
s.push_back(v);
    found = true;
    break;
}
if (!found) {
    path.push_back(u);
    s.pop_back();
}
reverse(path.begin(), path.end());
return path;
};
```

6.10 2-SAT

7 Data structures

7.1 Treap

```
join(1->r, 1->r, r), t = 1;
        else
                join(r->1, 1, r->1), t = r;
        update(t);
void splitByKey(Node *v, int x, Node* &1, Node* &r) {
   if (!v) return void(l = r = nullptr);
   push(v);
       -- (ν->κεγ < x)
splitByKeγ(ν->r, x, ν->r, r), l = v;
else
                splitByKey(v\rightarrow 1, x, 1, v\rightarrow 1), r = v;
        update(v);
void splitByIndex(Node *v, int x, Node* &l, Node* &r) {
   if (!v) return void(l = r = nullptr);
        push(v);
int index = size(v->l) + 1;
if (index < x)</pre>
       splitByIndex(v->r, x - index, v->r, r), 1 = v;
else
                splitByIndex(v->1, x, 1, v->1), r = v;
        update(v);
void show(Node *x) {
        if (!x) return;
        push(x);
show(x->1);
cerr << x->key << ' ';</pre>
        show(x->r);
Node *root;
Node *1, *m, *r;
public:
Treap() { root = NULL; }
   Treap() { delete root; }
int size() { return size(root); }
int insert(int x) {
       inser(int x {
    splitByKey(root, x, 1, m);
    splitByKey(m, x + 1, m, r);
    int ans = 0;
    if (!m) m = new Node(x), ans = size(1) + 1;
    join(1, 1, m);
    join(root, 1, r);
        return ans:
int erase(int x) {
       erase(int x) {
splitByKey(root, x, 1, m);
splitByKey(m, x + 1, m, r);
int ans = 0;
if (m) {
    ans = size(1) + 1;
               delete m;
         join(root, l, r);
        return ans;
void insertAt(int pos, int x) {
   splitByIndex(root, pos, 1, :
   join(1, 1, new Node(x));
   join(root, 1, r);
void eraseAt(int x) {
       splitByIndex(root, x, 1, m);
splitByIndex(m, 2, m, r);
        delete m;
join(root, 1, r);
void updateAt(int pos, int newValue) {
    eraseAt(pos);
        insertAt(pos, newValue);
int valueAt(int pos) {
       valueat(int pos) {
    splitByIndex(root, pos, 1, m);
    splitByIndex(m, 2, m, r);
    int res = m->key;
    join(l, 1, m);
    join(root, 1, r);
    return res;
void reverse(int from, int to) {
    splitByIndex(root, from, 1, m);
    splitByIndex(m, to - from + 2, m, r);
    m>rev_lazy ^= 1;
    join(1, 1, m);
    join(root, 1, r);
}
void show() {
    cerr << "Size = " << size() << " ";
    cerr << "[";</pre>
        show(root);
cerr << "]\n";</pre>
```

7.2 Big Integer

};

```
typedef vector<int> bigInt;
const int BASE = 1000;
const int LENGTH = 3;
```

```
// * Refine function
bigInt& fix(bigInt &a) {
   a.push_back(0);
   for (int i = 0; i + 1 < a.size(); ++i) {
        a[i + 1] += a[i] / BASE; a[i] %= BASE;
        if (a[i] < 0) a[i] += BASE, --a[i + 1];
}</pre>
           while (a.size() > 1 && a.back() == 0) a.pop_back();
          return a;
// * Constructors
bigInt big(int x) {
   bigInt result;
   while (x > 0) {
                result.push_back(x % BASE);
x /= BASE;
bigInt big(string s) {
   bigInt result(s.size() / LENGTH + 1);
   for (int i = 0; i < s.size(); ++i) {
      int pos = (s.size() - i - 1) / LENGTH;
      result[pos] = result[pos] * 10 + s[i];
}</pre>
          return fix(result), result;
 // * Compare operators
int compare(bigInt &a, bigInt &b) {
   if (a.size() != b.size()) return (int)a.size() - (int)b.size();
   for (int i = (int) a.size() - 1; i >= 0; --i)
        if (a[i] != b[i]) return a[i] - b[i];
 \texttt{\#define} \ \texttt{DEFINE\_OPERATOR}(x) \ \textbf{bool operator} \ x \ (\texttt{bigInt \&a, bigInt \&b}) \ \{ \ \textbf{return} \\
 compare(a, b) x 0; }
DEFINE_OPERATOR(==)
DEFINE_OPERATOR(!=)
 DEFINE OPERATOR (>)
 DEFINE_OPERATOR(>)
DEFINE_OPERATOR(>=)
DEFINE_OPERATOR(<=)
 #undef DEFINE OPERATOR
 // * Arithmetic operators
void operator += (bigInt &a, bigInt b) {
   a.resize(max(a.size(), b.size()));
   for (int i = 0; i < b.size(); ++i)
      a[i] += b[i];
   fix(a);</pre>
void operator -= (bigInt &a, bigInt b) {
   for (int i = 0; i < b.size(); ++i)
       a[i] -= b[i];
   fix(a);</pre>
 void operator *= (bigInt &a, int b) {
   for (int i = 0; i < a.size(); ++i)
        a[i] *= b;
   fix(a);</pre>
void divide(bigInt a, int b, bigInt &q, int &r) {
   for (int i = int(a.size()) - 1; i >= 0; --i) {
      r = r * BASE + a[i];
      q.push_back(r / b); r %= b;
}
             reverse(q.begin(), q.end());
          fix(q);
 bigInt operator + (bigInt a, bigInt b) { a += b; return a; }
bigInt operator - (bigInt a, bigInt b) { a -= b; return a; }
bigInt operator * (bigInt a, int b) { a *= b; return a; }
bigInt operator / (bigInt a, int b) {
  bigInt q; int r = 0;
  divide(a, b, q, r);
  return q;
}
 int operator % (bigInt a, int b) {
  bigInt q; int r = 0;
  divide(a, b, q, r);
  return r;
bigInt operator * (bigInt a, bigInt b) {
  bigInt result (a.size() + b.size());
  for (int i = 0; i < a.size(); ++i);
    for (int j = 0; j < b.size(); ++j);
    result[i + j] += a[i] * b[j];
  return fix(result);</pre>
 // * I/O routines
 istream& operator >> (istream& cin, bigInt &a) {
   string s; cin >> s;
   a = big(s);
          return cin;
 ostream& operator << (ostream& cout, const bigInt &a) {
```

7.3 Convex Hull IT

```
left->update(i, j, newLine);
    right->update(i, j, newLine);
}

long long getMax(int i) {
    if (1 == r) return line.eval(valueX[i]);
    if (i <= (1 + r >> 1)) return max(line.eval(valueX[i]), left->getMax(i));
    return max(line.eval(valueX[i]), right->getMax(i));
};

Node * build(int l, int r) {
    Node *x = new Node(l, r);
    if (1 == r) return x;
    x->left = build(l, l + r >> 1);
    x->right = build((l + r >> 1) + 1, r);
    return x;
}
```

8 Miscellaneous

8.1 RNG