Bamboo Team Notes

Contents

1	Nun	iber theory
	1.1	Count primes up to N
	1.2	Extended Euclide
	1.3	System of linear equations
	1.4	Pollard Rho
	1.5	Formula
	1.6	Cubic
	1.7	PythagoreTriple
2	Strir	ng
	2.1	Suffix Array
	2.2	Aho Corasick
	2.3	Z algorithm
	2.4	Manacher
	2.5	Suffix Automaton
	2.6	ACLS
	2.7	Palindromic Tree
3	Com	binatorial optimization
4	G	
4	4.1	metry Geometry
5		nerical algorithms
	5.1	Gauus Elimination
	5.2	Simplex Algorithm
	5.3	NTT
	5.4	FFT
	5.5	Bitwise FFT
	5.6	FFT chemthan
	5.7 5.8	Interpolation Binary vector space
	_	
6	-	oh algorithms
	6.1	Bridges and Articulations
	6.2	Bipartite Maximum Matching
	6.3	General Matching
	6.4	Dinic Flow
	6.5	Min Cost-Max Flow
6	6.6	Bounded Feasible Flow
	6.7	Hungarian Algorithm
	6.8	Undirected mincut
	6.9	Eulerian Path/Circuit
	6.10	2-SAT
7	Data	a structures 1
	7.1	Treap
	7.2	Big Integer
	7.3	Convex Hull IT
	7.4	Link Cut Tree
8	Misc	cellaneous 1
-	8.1	RNG

1 Number theory

1.1 Count primes up to N

1.2 Extended Euclide

```
int bezout(int a, int b) {
    // return x such that ax + by == gcd(a, b)
    int xa = 1, xb = 0;
    while (b) {
        int q = a / b;
        int r = a - q * b, xr = xa - q * xb;
        a = b; xa = xb;
        b = r; xb = xr;
    }
    return xa;
}

pair<int, int> solve(int a, int b, int c) {
    // solve ax + by == c
    int d = __gcd(a, b);
    int y = (d - a * x) / b;
    c /= d;
    return make_pair(x * c, y * c);
}

int main() {
    int a = 100, b = 128;
    int c = __gcd(a, b);
    int y = (c - a * x) / b;
    cout << x < ' ' < y < endl;
    pair<int, int> xy = solve(100, 128, 40);
    cout << xy, first << ' ' << xy.second << endl;
    return 0;
}</pre>
```

1.3 System of linear equations

```
// extended version, uses diophantine equation solver to solve system of
    congruent equations
pair<int, int> solve(int a, int b, int c) {
    int cc = c;
    // solve ax + by == c
    int d = __gcd(a, b);
    int x = bezout(a / d, b / d);
    int y = (d - a * x) / b;
    c /= d;
    return make_pair(x * c, y * c);
}

int lcm(int a, int b) {
    return a / __gcd(a, b) * b;
}

// use this if input is large, make sure (#define int long long)
int mul(int a, int b, int p) {
    a %= p, b %= p;
    int q = (int) ((long double) a * b / p);
    int r = a * b - q * p;
    while (r < 0) r *= p;
    while (r < 0) r *= p;
    return r;
}

int solveSystem(vector<int> a, vector<int> b) {
    // xi mod bi = ai
    int A = a[0], B = b[0];
    // x mod B = A
    for (int i = 1; i < a.size(); ++i) {
        int curB = b[i], curA = a[i];
        // x = Bi + A = curB * j + curA
        pair<int, int> ij = solve(B, -curB, curA - A);
        if (B * ij.first + A != curB * ij.second + curA) return -1;
        int newB = lcm(B, curB);
        int newA = (mul(B, ij.first, newB) + A) % newB;
        if (newA < 0) newA += newB;
        A = newA; B = newB;
        if (i + 1 == a.size()) return A;
}

int main() {
    vector<int> a = {0, 3, 3};
    vector<int> b = {3, 6, 9};
    cout << solveSystem(a, b) << endl;
}
</pre>
```

return 0;

1.4 Pollard Rho

```
#include <bits/stdc++.h>
using namespace std;
struct PollardRho {
       long long n;
map<long long, int> ans;
PollardRho(long long n) : n(n) {}
long long random(long long u) {
               return abs(rand()) % u;
        long long mul(long long a, long long b, long long p) {
               g long mul(long long a, long long b, long long p) { a \neq p; b \neq p; long long q = (long long) ((long double) a \star b / p); long long r = a \star b - q \star p; while (r < 0) r += p; while (r >= p) r -= p;
               return r;
       long long pow(long long u, long long v, long long n) {
   long long res = 1;
   while (v) {
      if (v & 1) res = mul(res, u , n);
      u = mul(u, u, n);
      v >>= 1;
}
               return res;
        bool rabin(long long n) {
               if (n < 2) return 0;
if (n == 2) return 1;
long long s = 0, m = n - 1;
while (m % 2 == 0) {</pre>
                      m >>= 1;
              }
// 1 - 0.9 ^ 40
for (int it = 1; it <= 40; it++) {
   long long u = random(n - 2) + 2;
   long long f = pow(u, m, n);
   if (f == 1 || f == n - 1) continue;
   for (int i = 1; i < s; i++) {
      f = mul(f, f, n);
      if (f == 1) return 0;
      if (f == n - 1) break;
   }
}</pre>
                       if (f != n - 1) return 0;
               return 1;
       x = f(x, n);
y = f(f(y, n), n);
p = __gcd(abs(x - y), n);
               return p;
       if (n > 1) ans[n]++;
               if (rabin(n)) {
               long long p = 0;
while (p == 0 || p == n) {
    p = findfactor(n);
               pollard_rho(n / p);
pollard_rho(p);
int main() {
    long long n;
        cin >> n;
PollardRho f(n);
        forliard in (ii),
for (auto x : f.ans) {
    cout << x.first << " " << x.second << end);</pre>
```

```
Let m, n, a, b be any interger. Let g = gcd(m, n). x % m = a x % n = b if (a % g == b % g): it has unique solution modulo lcm(n, m) else: no solution
 g = u * m + v * n

x = (a * v * n + b * u * m) / g
 Eigen Decomposition
 D = diagonal matrix, D_i_i is eigenvector qi
 Generating function
 1 / ((1-ax)^{(k+1)}) = sum_(0->INF)_{a^n * C(n+k, k) * x^n}
 Partition Generating function : PI: (1 / (1 - x ^k)) p(n)=p(n-1)+p(n-2)-p(n-5)-p(n-7)+p(n-12)+p(n-15)-p(n-22)-\dots p_k = k * (3k - 1) / 2 with k = 1, -1, 2, -2, 3, -3, \dots
 Center of mass + green theorem
Center or mass + green theorem  (\mathbf{x} = 1/6A + \mathbf{sum}_{-}(0 - \mathbf{y} - 1)_{-} ( (\mathbf{x}_{-}\mathbf{i} + \mathbf{x}_{-}\mathbf{i} + 1) + (\mathbf{x}_{-}\mathbf{i} + \mathbf{y}_{-}\mathbf{i} + 1 - \mathbf{x}_{-}\mathbf{i} + 1 + \mathbf{y}_{-}\mathbf{i}) \}   Cy = 1/6A + \mathbf{sum}_{-}(0 - \mathbf{y} - 1)_{-} \{ (\mathbf{y}_{-}\mathbf{i} + \mathbf{y}_{-}\mathbf{i} + 1) + (\mathbf{x}_{-}\mathbf{i} + \mathbf{y}_{-}\mathbf{i} + 1 - \mathbf{x}_{-}\mathbf{i} + 1 + \mathbf{y}_{-}\mathbf{i}) \}   A = 1/2 + \mathbf{sum}_{-}(0 - \mathbf{y} - 1)_{-} \{ (\mathbf{x}_{-}\mathbf{i} + \mathbf{y}_{-}\mathbf{i} + 1 - \mathbf{x}_{-}\mathbf{i} + 1 + \mathbf{y}_{-}\mathbf{i}) \}   Green: C_{-}intergral (Pdx + Qdy) = 2D_{-}intergral (dQ/dx - dP/dy) dxdy 
 Fn = 276601605(691504013^n - 308495997^n)[10^9 + 9]
 SQRT for loop
for (int i = 1, la; i <= n; i = la + 1) {
    la = n / (n / i);</pre>
         //n / x yields the same value for i <= x <= la.
Mobius inversion if g(n) = sum_(d|n)_f(d) with n >= 1 then f(n) = sum_(d|n)_mu(d)*g(n/d) with n >= 1
Dual graph Euler formula: V - E + F = 2 in dual graph: V <=> F in complement dual graph: (removed egdes in the original => edges in dual):
         a connected component is equivalent to a face in dual
Pell equation
Peli equation x^2 - ny^2 = 1 x1, y1 is the minimal solution x_k+1 = x_1+x_k + n+y_1+y_k y_k+1 = x_1+y_k + y_1+x_k
 Burnside lemma
 G: finite group acts on set X
X_g: set of elements fixed by g
 Number of orbits: |X/G| = 1/|G| * sum_(g in G)_|X_g|
Given 3 mutually tangent circles. Find inner circle (touching all 3) and outer circle (touching all 3).

The radius is given by:
k4 = |k1 + k2 + k3 +- 2*sqrt(k1*k2 + k2*k3 + k3*k1)|
where ki = 1/ri
Minus --> Outer
Plus --> Inner
    If 1 circle --> line, change ki to 0 --> k4 = k1 + k2 +- 2*sqrt(k1*k2)
 Hacken Bush Green Hacken Bush: subtree of u: g(u) = SUMXOR\{g(v)\} + 1 with v is a child of
 u
RB Hacken Bush:
 a. subtree of u: g(u) = SUM_{f(g(v))} with v is a child of u if color of \{u, v\} is blue: f(x) = (x+i) / 2^{(i-1)} with smallest i >= 1 such that x + i > 1
 if color of \{u, v\} is red: f(x) = (x-i) / 2^{(i-1)} with smallest i \ge 1 such that x - i < -1
 that x - i < -1
b. Loop: find 2 nearest 2 points where segment change color, cut the rest in
 the value of loop is sum of the 2 segments.
```

```
Prufer sequence
a. Get prufer code of a tree
- Find a leaf of lowest label x, connect to y. Remove x, add y to the sequence
- Repeat until we are left with 2 nodes
b. Construct a tree
- Let the first element is X, find a node which doesn't appear in the sequence L
- Add edge X, L
- Remove X
```

1.6 Cubic

```
const double EPS = le-6;
struct Result {
    int n; // Number of solutions
    double x[3]; // Solutions
};
Result solve_cubic(double a, double b, double c, double d) {
    long double al = b/a, a2 = c/a, a3 = d/a;
    long double p = (a1*a1 - 3*a2)/9.0, sq = -2*sqrt(q);
    long double r = (2*a1*a1*a1 - 9*a1*a2 + 27*a3)/54.0;
    double z = r*r-q*q*q, theta;
    Result s;
    if(z <= EPS) {
        s.n = 3; theta = acos(r/sqrt(q*q*q));
        s.x[0] = sq*cos(theta/3.0) - a1/3.0;
        s.x[1] = sq*cos((theta*2.0*PI)/3.0) - a1/3.0;
        s.x[2] = sq*cos((theta*4.0*PI)/3.0) - a1/3.0;
}
else {
        s.n = 1; s.x[0] = pow(sqrt(z)*fabs(r),1/3.0);
        s.x[0] += q/s.x[0]; s.x[0] *= (r < 0) ? 1 : -1;
        s.x[0] -= a1/3.0;
}
return s;
}</pre>
```

1.7 PythagoreTriple

2 String

2.1 Suffix Array

```
#include <bits/stdc++.h>
using namespace std;

struct SuffixArray {
    static const int N = 100010;

    int n;
    char *s;
    int sa[N], tmp[N], pos[N];
    int len, cnt[N], lcp[N];

    SuffixArray(char *t) {
        s = t;
        n = strlen(s + 1);
        buildSA();
    }

bool cmp(int u, int v) {
        if (pos[u] != pos[v]) {
            return pos[u] < pos[v];
        }
    return (u + len <= n && v + len <= n) ? pos[u + len] < pos[v + len] :
            u > v;
    }

void radix(int delta) {
        memset(cnt, 0, sizeof cnt);
        for (int i = 1; i < n; i++) {
            cnt[i + delta <= n ? pos[i + delta] : 0]++;
        }
    for (int i = n; i > 0; i--) {
            int id = sa[i];
            tmp[cnt[id + delta <= n ? pos[id + delta] : 0]--] = id;
    }
}</pre>
```

```
for (int i = 1; i <= n; i++) {
    sa[i] = tmp[i];</pre>
      void buildSA() {
   for (int i = 1; i <= n; i++) {
     sa[i] = i;
     pos[i] = s[i];
}</pre>
              while (1) {
                     radix(len);
radix(0);
tmp[1] = 1;
                     for (int i = 2; i <= n; i++) {
   tmp[i] = tmp[i - 1] + cmp(sa[i - 1], sa[i]);</pre>
                     for (int i = 1; i <= n; i++) {
    pos[sa[i]] = tmp[i];</pre>
                     if (tmp[n] == n) {
    break;
                     len <<= 1;</pre>
              len = 0:
             for (int i = 1; i <= n; i++) {
   if (pos[i] == n) {</pre>
                            continue:
                     int j = sa[pos[i] + 1];
while (s[i + len] == s[j + len]) {
                            len++;
                    lcp[pos[i]] = len;
if (len) {
                            len--;
            }
     }
1:
```

2.2 Aho Corasick

```
struct AhoCorasick {
   const int N = 30030;
         int fail[N];
        int to[N][26];
int ending[N];
        AhoCorasick() {
                sz = 1;
        int add(const string &s) {
                 int node = 1;
for (int i = 0; i < s.size(); ++i) {
    if (!to[node][s[i] - 'a']) {
        to[node][s[i] - 'a'] = ++sz;
}</pre>
                         node = to[node][s[i] - 'a'];
                   ending[node] = true;
                 return node;
        void push() {
                d push() {
    queue<int> 0;
    0.push(1);
    fail[1] = 1;
    while (!Q.empty()) {
        int u = 0.front(); Q.pop();
        for (int i = 0; i < 26; ++i) {
            int &v = to[u][i];
            if (!v) {</pre>
                                  if (!v) {
   v = u == 1 ? 1 : to[fail[u]][i];
                                  v = u == 1 ? 1 : to[rair[u]][1];
} else {
    fail[v] = u == 1 ? 1 : to[fail[u]][i];
    ending[v] |= ending[fail[v]];
    Q.push(v);
                        }
               }
      }
```

2.3 Z algorithm

```
vector<int> calcZ(const string &s) {
  int L = 0, R = 0;
  int n = s.size();
  vector<int> Z(n);
  Z[0] = n;
  for (int i = 1; i < n; i++) {
    if (i > R) {
        L = R = i;
        while (R < n && s[R] == s[R - L]) R++;
        Z[i] = R - L; R--;
    }
  else
    {
    int k = i - L;
}</pre>
```

```
if (Z[k] < R - i + 1) Z[i] = Z[k];
else
{
    L = i;
    while (R < n && s[R] == s[R - L]) R++;
    Z[i] = R - L; R--;
}
return Z;
}</pre>
```

2.4 Manacher

2.5 Suffix Automaton

```
//set last = 0 everytime we add new string
struct SuffixAutomaton {
    static const int N = 100000;
    static const int CHARACTER = 26;
    int suf[N * 2], nxt[N * 2][CHARACTER], cnt, last, len[N * 2];

SuffixAutomaton() {
        memset(suf, -1, sizeof suf);
        memset(nxt, -1, sizeof nxt);
        memset(nxt, -1, sizeof nxt);
        memset(len, 0, sizeof len);
        last = cnt = 0;
}

int getNode(int last, int u) {
        int q = nxt[last][u];
        if (len[last] + 1 == len[q]) {
            return q;
        }
        int clone = ++cnt;
        len[clone] = len[last] + 1;
        for (int i = 0; i < CHARACTER; i++) {
            nxt[clone][i] = nxt[q][i];
        }
        while (last != -1 && nxt[last][u] == q) {
            nxt[last][u] = clone;
        last = suf[last];
        }
        void add(int u) {
        if (nxt[last][u] = -1) {
            int newNode = ++cnt;
            len[newNode] = len[last] + 1;
            while (last != -1 && nxt[last][u] == -1) {
                nxt[last][u] = newNode;
                last = suf[last];
        }
        if (last == -1) {
            suf[newNode] = 0;
            last = newNode;
            return;
        }
        suf[newNode] = getNode(last, u);
        last = newNode;
        return;
      }
    }
};
</pre>
```

2.7 Palindromic Tree

```
const int N = 1e5, SIZE = 26;
int s[N], len[N], link[N], to[N][SIZE], depth[N];
int n, last, sz;

void init() {
    s[n++] = -1;
    link[0] = 1;
    len[1] = -1;
    sz = 2;
}

int get_link(int v) {
    while (s[n - len[v] - 2] != s[n - 1]) v = link[v];
    return v;
}

int add_letter(int c) {
    s[n++] = c;
    last = get_link(last);
    if (!to[last][c]) {
        len [sz] = len[last] + 2;
        link[sz] = to[get_link(link[last])][c];
        to[last][c] = sz++;
    }
    last = to[last][c];
    return len[last];
}
```

3 Combinatorial optimization

4 Geometry

4.1 Geometry

```
double cosa = cos(alpha), sina = sin(alpha);
return Point(x * cosa - y * sina, x * sina + y * cosa);
double angle (Point a, Point o, Point b) { // min of directed angle AOB & BOA
         a = a - o; b = b - o;
return acos((a * b) / sqrt(a.norm()) / sqrt(b.norm()));
double directed_angle(Point a, Point o, Point b) { // angle AOB, in range [0,
         }
}// Distance from p to Line ab (closest Point --> c)
double distToLine(Point p, Point a, Point b, Point &c) {
   Point ap = p - a, ab = b - a;
   double u = (ap * ab) / ab.norm();
   c = a + (ab * u);
   return (p-c).len();
}
}
}// Distance from p to segment ab (closest Point --> c)
double distToLineSegment (Point p, Point a, Point b, Point &c) {
   Point ap = p - a, ab = b - a;
   double u = (ap + ab) / ab.norm();
   if (u < 0.0) {
        c = Point(a.x, a.y);
        return (p - a).len();
   }
}</pre>
         }
if (u > 1.0) {
    c = Point(b.x, b.y);
    return (p - b).len();
         return distToLine(p, a, b, c);
// NOTE: WILL NOT WORK WHEN a = b = 0.
         Line(Point A, Point B) : A(A), B(B) {
    a = B.y - A.y;
    b = A.x - B.x;
    c = - (a * A.x + b * A.y);
         Line(Point P, double m) {
                 a = -m; b = 1;

c = -((a * P.x) + (b * P.y));
         double f(Point A) {
   return a*A.x + b*A.y + c;
bool areParallel(Line 11, Line 12) {
    return cmp(11.a*12.b, 11.b*12.a) == 0;
        l areIntersect(Line 11, Line 12, Point &p) {
   if (areParallel(11, 12)) return false;
   double dx = 11.b+12.c - 12.b+11.c;
   double dy = 11.c+12.a - 12.c+11.a;
   double d = 11.a+12.b - 12.a+11.b;
   p = Point(dx/d, dy/d);
          return true;
}
void closestPoint(Line 1, Point p, Point &ans) {
   if (fabs(l.b) < EPS) {
      ans.x = -(l.c) / l.a; ans.y = p.y;
      return;
}</pre>
         if (fabs(1.a) < EPS) {
    ans.x = p.x; ans.y = -(1.c) / 1.b;
    return;</pre>
         Line perp(1.b, -1.a, - (1.b*p.x - 1.a*p.y));
areIntersect(1, perp, ans);
void reflectionPoint(Line 1, Point p, Point &ans) {
         Point b;
closestPoint(1, p, b);
ans = p + (b - p) * 2;
}
struct Circle : Point {
    double r;
    Circle(double x = 0, double y = 0, double r = 0) : Point(x, y), r(r) {}
    Circle(Point p, double r) : Point(p), r(r) {}
    bool contains(Point p) { return (*this - p).len() <= r + EPS; }</pre>
 // Find common tangents to 2 circles
       Tested:
- http://codeforces.com/gym/100803/ - H
       Helper method
// Helper method
void tangents(Point c, double r1, double r2, vector<Line> & ans) {
    double r = r2 - r1;
    double z = sqr(c.x) + sqr(c.y);
    double d = z - sqr(r);
    if (d < -EPS) return;
    d = sqrt(flas)(d));
    Line 1((c.x * r + c.y * d) / z,
        (c.y * r - c.x * d) / z,
        r);</pre>
         ans.push_back(1);
}
// Actual method: returns vector containing all common tangents
vector<Line> tangents(Circle a, Circle b) {
   vector<Line> ans; ans.clear();
   for (int i=-1; i<=1; i+=2)
        for (int j=-1; j<=1; j+=2)
        tangents(b-a, a.r*i, b.r*j, ans);
   for(int i = 0; i < ans.size(); ++i)</pre>
```

```
ans[i].c -= ans[i].a * a.x + ans[i].b * a.y;
             ans[1].c == ans[1].d ^ a.x r ans[1].c = vectors[intex per; for(int i = 0; i < (int) ans.size(); ++i) {
   bool ok = true; for(int j = 0; j < i; ++j)  
   if (areSame(ret[j], ans[i])) {
                                                           k = false;
                           if (ok) ret.push_back(ans[i]);
               return ret;
   // Circle & line intersection
vector<Point> intersection(Line 1, Circle cir) {
   double r = cir.r, a = 1.a, b = 1.b, c = 1.c + 1.a*cir.x + 1.b*cir.y;
             vector<Point> res;
double x0 = -a*c/(a*a+b*b), y0 = -b*c/(a*a+b*b);
if (c*c > r*r*(a*a+b*b)+EPS) return res;
else if (fabs(c*c - r*r*(a*a+b*b)) < EPS) {
    res.push_back(Point(x0, y0) + Point(cir.x, cir.y));
    return res;</pre>
                vector<Point> res;
                          e {
    double d = r*r - c*c/(a*a+b*b);
    double mult = sqrt (d / (a*a+b*b));
    double ax,ay,bx,by;
    ax = x0 + b * mult;
    bx = x0 - b * mult;
    by = y0 - a * mult;
    by = y0 + a * mult;
    res.push_back(Point(ax, ay) + Point(cir.x, cir.y));
    res.push_back(Point(bx, by) + Point(cir.x, cir.y));
    return res;
               else {
  // helper functions for commonCircleArea
double cir_area_solve(double a, double b, double c) {
    return acos((a*a + b*b - c*c) / 2 / a / b);
 }
double cir_area_cut(double a, double r) {
  double s1 = a * r * r / 2;
  double s2 = sin(a) * r * r / 2;
  return s1 - s2;
 double commonCircleArea(Circle c1, Circle c2) { //return the common area of
             ble commonCircleArea(Circle c1, Circle c2) { //return the co
    two circle

if (c1.r < c2.r) swap(c1, c2);
double d = (c1 - c2).len();
if (d + c2.r <= c1.r + EPS) return c2.r*c2.r*M_PI;
if (d >= c1.r + c2.r - EPS) return 0.0;
double a1 = cir_area_solve(d, c1.r, c2.r);
double a2 = cir_area_solve(d, c2.r, c1.r);
return cir_area_cut(a1*2, c1.r) + cir_area_cut(a2*2, c2.r);
 }
}// Check if 2 circle intersects. Return true if 2 circles touch
bool areIntersect(Circle u, Circle v) {
    if (cmp((u - v).len(), u.r + v.r) > 0) return false;
    if (cmp((u - v).len() + v.r, u.r) < 0) return false;
    if (cmp((u - v).len() + u.r, v.r) < 0) return false;
    return true;</pre>
 }
// If 2 circle touches, will return 2 (same) points
// If 2 circle are same --> be careful
vector<Point> circleIntersect(Circle u, Circle v) {
    vector<Point> res;
    if (!areIntersect(u, v)) return res;
    double d = (u - v).len();
    double alpha = acos((u.r * u.r + d*d - v.r * v.r) / 2.0 / u.r / d);
              Point p1 = (v - u).rotate(alpha);
Point p2 = (v - u).rotate(-alpha);
res.push_back(p1 / p1.len() * u.r + u);
res.push_back(p2 / p2.len() * u.r + u);
 Point centroid(Polygon p) {
              tcentroid(Polygon p) {
    Point c(o, 0);
    double scale = 6.0 + signed_area(p);
    for (int i = 0; i < p.size(); i++) {
        int j = (i+1) * p.size();
        c = c + (p[i]+p[j]) + (p[i].x + p[j].y - p[j].x + p[i].y);
    }
}</pre>
              return c / scale;
 // Cut a polygon with a line. Returns one half.
// To return the other half, reverse the direction of Line 1 (by negating 1.a , 1.b)
 , 1.b)
// The line must be formed using 2 points
Polygon polygon_cut(const Polygon& P, Line 1) {
    Polygon Q;
    for(int i = 0; i < P.size(); ++i) {
        Point A = P[i], B = (i == P.size()-1) ? P[0] : P[i+1];
        if (ccw(1.A, 1.B, A) != -1) Q.push_back(A);
        if (ccw(1.A, 1.B, A)*ccw(1.A, 1.B, B) < 0) {
            Point p; areIntersect (Line(A, B), 1, p);
            Q.push_back(p);
        }
}</pre>
               return 0:
  }
// Find intersection of 2 convex polygons
// Find intersection of 2 convex polygons
// Helper method
bool intersect lpt(Point a, Point b,
    Point c, Point d, Point &r) {
    double D = (b - a) % (d - c);
    if (cmp(D, 0) == 0) return false;
    double t = ((c - a) % (d - c)) / D;
    double s = -((a - c) % (b - a)) / D;
    r = a + (b - a) * t;
    return cmp(t, 0) >= 0 && cmp(t, 1) <= 0 && cmp(s, 0) >= 0 && cmp(s, 1) <=</pre>
 }
Polygon convex_intersect(Polygon P, Polygon Q) {
   const int n = P.size(), m = Q.size();
   int a = 0, b = 0, aa = 0, ba = 0;
   enum { Pin, Qin, Unknown } in = Unknown;
   Polygon R;
```

```
int al = (a+n-1) % n, bl = (b+m-1) % m;
double C = (P[a] - P[ai]) % (Q[b] - Q[bi]);
double A = (P[ai] - Q[b]) % (P[a] - Q[b]);
double B = (Q[bi] - P[a]) % (Q[b] - P[ai]);
               double B = (V[DI] - r[a]) * (V[DI] - r[a]),
point r;
if (intersect_lpt(P[al], P[a], Q[bl], Q[b], r)) {
   if (in == Unknown) aa = ba = 0;
   R.push_back(r);
   in = B > 0 ? Pin : A > 0 ? Qin : in;
               if (B > 0) { if (in == Qin) R.push_back(Q[b]); b = (b+1)%m; ++ba;
                                     { if (in == Pin) R.push_back(P[a]); a = (a+1)%n; ++aa;
        } while ( (aa < n || ba < m) && aa < 2*n && ba < 2*m );
if (in == Unknown) {
   if (in_convex(Q, P[0])) return P;
   if (in_convex(P, Q[0])) return Q;</pre>
 }
// Find the diameter of polygon.
// Rotating callipers
double convex_diameter(Polygon pt) {
    const int n = pt.size();
    int is = 0, js = 0;
    for (int i = 1; i < n; ++i) {
        if (pt[i].y > pt[is].y) is = i;
        if (pt[i].y < pt[js].y) js = i;
    }
}</pre>
        double maxd = (pt[is]-pt[js]).norm();
int i, maxi, j, maxj;
i = maxi = is;
j = maxj = js;
do {
              {
    int jj = j+1; if (jj == n) jj = 0;
    if ((pt[i] - pt[j]).norm() > (pt[i] - pt[j]).norm()) j = (j+1) % n;
    else i = (i+1) % n;
    if ((pt[i]-pt[j]).norm() > maxd) {
        --vd = (pt[i]-pt[j]).norm();
    }
                     maxd = (pt[i]-pt[j]).norm();
maxi = i; maxj = j;
         } while (i != is || j != js);
return maxd; /* farthest pair is (maxi, maxj). */
 }
// Check if we can form triangle with edges x, y, z.
bool isSquare(long long x) { /* */ }
bool isIntegerCoordinates(int x, int y, int z) {
   long long s=(long long) (x+y+z)*(x+y-z)*(x+z-y)*(y+z-x);
   return (s%4==0 && isSquare(s/4));
       Given non-intersecting polygon.
   // I = number of integer points strictly Inside // B = number of points on sides of polygon // S = I + B/2 - 1
return c:
```

```
}
int res = 0;
for (int i = 0; i < n; i++) {
    Point v = a[i], w = a[i == n - 1 ? 0 : i + 1];
    if (cmp(v.x, w.x) == 0) continue;
    if (v.x > w.x) swap(v, w);
    if (u.x < v.x - EPS) continue;
    if (u.x > w.x - EPS) continue;
    res ^= (cmp((u - v) % (w - v), 0) >= 0);
}
return res;
```

5 Numerical algorithms

5.1 Gauus Elimination

5.2 Simplex Algorithm

```
/**
 * minimize c^T * x
 * subject to Ax <= b
 * and x >= 0
 * The input matrix a will have the following form
 * 0 c c c c c
 * b A A A A A
 * b A A A A A
 * b A A A A A
 * b A A A A A
 * b B A A A A A
 * b B A B A A A
 * b B A B A A A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
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 * b B A B A B A
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 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
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 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B A B A
 * b B A B B B
 * int m = (int) a [0] size() - 1;

**cotor

**Cotor
```

```
}
if (x == -1) break;
int y = -1;
for (int j = 1; j <= m; j++) {
        if (a[x][j] < -EPS && (y == -1 || a[x][j] < a[x][y])) {
            y = j;
}
if (y == -1) return vector<ld>(); // infeasible
pivot(x, y);
}
while (1) {
    int y = -1;
    for (int j = 1; j <= m; j++) {
        if (a[0][j] > EPS && (y == -1 || a[0][j] > a[0][y])) {
            y = j;
    }
}
if (y == -1) break;
int x = -1;
for (int i = 1; i <= n; i++) {
        if (a[i][y] > EPS && (x == -1 || a[i][0] / a[i][y] < a[x][0]
            / a[x][y])) {
        x = i;
    }
}
if (x == -1) return vector<ld>(); // unbounded
pivot(x, y);
}
vector<ld> ans(m + 1);
for (int i = 1; i <= n; i++) {
        if (left[i] <= m) ans[left[i]] = a[i][0];
}
ans[0] = -a[0][0];
return ans;
}
</pre>
```

5.3 NTT

```
//Foly Invert: R(2n) = 2R(n) - R(n) ^2 * F where R(z) = invert F(z) //Foly Sqrt: 2 * S(2n) = S(n) + F * S(n) ^-1 const int MOD = 998244353;
struct NTT {
   int base = 1;
          int maxBase = 0;
int root = 2;
vector<int> w = {0, 1};
vector<int> rev = {0, 1};
          vector<int> rev = {0, 1}
NTT () {
   int u = MOD - 1;
   while (u % 2 == 0) {
      u >>= 1;
      maxBase++;
}
                     while (power(root, 1 << maxBase) != 1 || power(root, 1 << (maxBase -
1)) == 1) root++;</pre>
           void ensure(int curBase) {
                     a ensure(int curBase) {
    assert(curBase <= maxBase);
    if (curBase <= base) return;
    rev.resize(1 << curBase);
    for (int i = 0; i < (1 << curBase);
        rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (curBase - 1));
    }
}</pre>
                     }
w.resize(1 << curBase);
for (; base < curBase; base++) {
   int wc = power(root, 1 << (maxBase - base - 1));
   for (int i = 1 << (base - 1); i < (1 << base); i++) {
      w[i << 1] = w[i];
      w[i << 1 | 1] = mul(w[i], wc);
   }
}</pre>
           void fft(vector<int> &a) {
                     int re(vector(int) & a) {
   int n = a.size();
   int curBase = 0;
   while (1 << curBase) < n) curBase++;
   int shift = base - curBase;
   for (int i = 0; i < n; i++) {
      if (i < (rev[i] >> shift)) swap(a[i], a[rev[i] >> shift]);
   }
}
                    for (int k = 1; k < n; k <<= 1) {
   for (int i = 0; i < k; i++) {
      for (int j = i; j < n; j += k * 2) {
        int foo = a[j];
        int bar = mul(a[j + k], w[i + k]);
        a[j] = add(foo, bar);
        a[j + k] = sub(foo, bar);
}</pre>
           vector<int> mult(vector<int> a, vector<int> b) {
  int nResult = a.size() + b.size() - 1;
  int curBase = 0;
  while ((1 << curBase) < nResult) curBase++;</pre>
                     int n = 1 << curBase;
a.resize(n), b.resize(n);
fft(a);</pre>
                       fft(b):
                      int invN = inv(n);
for (int i = 0; i < n; i++) {
    a[i] = mul(mul(a[i], b[i]), invN);</pre>
                         reverse(a.begin() + 1, a.end());
                      fft(a);
a.resize(nResult);
                      return a:
```

vector<int> polyInv(vector<int> r, vector<int> f) {

```
vector<int> foo = mult(r, f);
    foo.resize(f.size());
    foo[0] = sub(2, foo[0]);
    for (int i = 1; i < foo.size(); i++) {
        foo[i] = sub(0, foo[i]);
    }
    vector<int> res = mult(r, foo);
    res.resize(f.size());
    return res;
}

vector<int> polySqrt(vector<int> s, vector<int> invS, vector<int> f) {
        vector<int> res = mult(f, invS);
        res.resize(f.size());
        for (int i = 0; i < s.size(); i++) {
             res[i] = add(res[i], s[i]);
        }
        for (int i = 0; i < res.size(); i++) {
             res[i] = mul(res[i], INV_2);
        }
        return res;
}

vector<int> getSqrt(vector<int> c, int sz) {
        vector<int> sqrtC = {1}, invSqrtC = {1}; //change this if c[0] != 1
        for (int k = 1; k < (1 < sz); k <<= 1) {
             vector<int> bar = sqrtC;
             bar.resize(bar.size() * 2, 0);
             vector<int> tempinv = polyInv(invSqrtC, bar);
             sqrtC = polySqrt(sqrtC, tempInv, foo);
             invSqrtC = polyInv(invSqrtC, sqrtC);
        }
        return sqrtC;
}

vector<int> getInv(vector<int> c, int sz) {
             vector<int> res = {INV_2}; // change this if c[0] != 2
             for (int k = 1; k < (1 < sz); k <<= 1) {
                  vector<int> res = {INV_2}; // change this if c[0] != 2
                  for (int k = 1; k < (1 < sz); k <<= 1) {
                  vector<int> res = polyInv(res, foo);
                  res = polyInv(res, foo);
                  return res;
}
```

5.4 FFT

5.5 Bitwise FFT

5.6 FFT chemthan

```
#define double long double
namespace FFT {
    const int maxf = 1 << 17;</pre>
     cp operator - (const cp& rhs) const {
                    return cp(x - rhs.x, y - rhs.y);
             cp operator * (const cp& rhs) const {
   return cp(x * rhs.x - y * rhs.y, x * rhs.y + y * rhs.x);
             cp operator !() const {
       } rts[maxf + 1];
      cp fa[maxf], fb[maxf];
cp fc[maxf], fd[maxf];
       int bitrev[maxf];
      int bitrev(maxf);
void fftinit() {
   int k = 0; while ((1 << k) < maxf) k++;
   bitrev[0] = 0;
   for (int i = 1; i < maxf; i++) {
      bitrev[i] = bitrev[i >> 1] >> 1 | ((i & 1) << k - 1);
   }
}</pre>
             }
double PI = acos((double) -1.0);
rts[0] = rts[maxf] = cp(1, 0);
for (int i = 1; i + i <= maxf; i++) {
    rts[i] = cp(cos(i * 2 * PI / maxf), sin(i * 2 * PI / maxf));</pre>
             for (int i = maxf / 2 + 1; i < maxf; i++) {
   rts[i] = !rts[maxf - i];</pre>
       y
woid dft(cp a[], int n, int sign) {
    static int isinit;
    if (!isinit) {
        isinit = 1;
}
              int d = 0; while ((1 << d) * n != maxf) d++;</pre>
             for (int i = 0; i < n; i++) {
   if (i < (bitrev[i] >> d)) {
      swap(a[i], a[bitrev[i] >> d]);
}
```

```
}
              }
for (int len = 2; len <= n; len <<= 1) {
    int delta = maxf / len * sign;
    for (int i = 0; i < n; i += len) {
        cp *x = a + i, *y = a + i + (len >> 1), *w = sign > 0 ? rts :
            rts + maxf;
    for (int k = 0; k + k < len; k++) {
        cp z = *y * *w;
        *y = *x - z, *x = *x + z;
        x++, y++, w += delta;
    }
}</pre>
                          }
              fif (sign < 0) {
   for (int i = 0; i < n; i++) {
      a[i].x /= n;
      a[i].y /= n;
}</pre>
              }
 }
void multiply(int a[], int b[], int na, int nb, long long c[]) {
    int n = na + nb - 1; while (n != (n & -n)) n += n & -n;
    for (int i = 0; i < n; i++) fa[i] = fb[i] = cp();
    for (int i = 0; i < na; i++) fa[i] = cp[a[i]);
    for (int i = 0; i < nb; i++) fb[i] = cp[a[i]);
    dft(fa, n, 1), dft(fb, n, 1);
    for (int i = 0; i < n; i++) fa[i] = fa[i] * fb[i];
    dft(fa, n, -1);
    for (int i = 0; i < n; i++) c[i] = (long long) floor(fa[i].x + 0.5);
}</pre>
}
dft(fc, n, -1), dft(fd, n, -1);
for (int i = 0; i < n; i++) {
  long long u = ((long long) floor(fc[i].x + 0.5)) % mod;
  long long v = ((long long) floor(fd[i].x + 0.5)) % mod;
  long long w = ((long long) floor(fd[i].y + 0.5)) % mod;
  c[i] = ((u << 15) + v + (w << 30)) % mod;
}</pre>
   vector<int> multiply(vector<int> a, vector<int> b, int mod = (int) 1e9 +
               static int fa[maxf], fb[maxf], fc[maxf];
int na = a.size(), nb = b.size();
for (int i = 0; i < na; i++) fa[i] = a[i];
for (int i = 0; i < nb; i++) fb[i] = b[i];
multiply(fa, fb, na, nb, fc, mod);
int k = na + nb - 1;
vector<int> res(k);
for (int i = 0; i < k; i++) res[i] = fc[i];
return res;</pre>
```

5.7 Interpolation

```
#include <bits/stdc++.h>
using namespace std;

/*
   * Complexity: O(Nlog(mod), N)
   */
#define IP Interpolation
namespace Interpolation {
    const int mod = (int) le9 + 7;
    const int maxn = le5 + 5;
    int a[maxn];
    int fac(maxn);
    int prf(maxn);
    int fpow(int n, int k) {
        int r = 1;
        for (; k; k >>= 1) {
            if (k & 1) r = (long long) r * n % mod;
            n = (long long) n * n % mod;
        }
        return r;
    }
    void upd(int u, int v) {
        a[u] = v;
    }
    void build() {
        fac[0] = ifac[0] = 1;
        for (int i = 1; i < maxn; i++) {
            fac[i] = (long long) fac[i - 1] * i % mod;
            ifac[i] = fpow(fac[i], mod - 2);
        }
    // Calculate P(x) of degree k - 1, k values form 1 to k
    //P(i) = a[i]
    int calc(int x, int k) {
        prf[0] = suf[k + 1] = 1;
    }
}</pre>
```

5.8 Binary vector space

6 Graph algorithms

6.1 Bridges and Articulations

6.2 Bipartite Maximum Matching

```
struct BipartiteGraph {
   vector< vector<int> > a;
```

```
vector<int> match;
          vector<bool> was:
        BipartiteGraph(int m, int n) {
                 // zero-indexed
this->m = m; this->n = n;
a.resize(m);
match.assign(n, -1);
                 was.assign(n, false);
        void addEdge(int u, int v) {
    a[u].push_back(v);
       bool dfs(int u) {
  for (int v : a[u]) if (!was[v]) {
    was[v] = true;
    if (match[v] == -1 || dfs(match[v])) {
        match[v] = u;
    }
}
                 return false:
        int maximumMatching() {
                 vector<int> buffer;
for (int i = 0; i < m; ++i) buffer.push_back(i);
bool stop = false;
int ans = 0;</pre>
                         ++ans;
stop = false;
buffer[i] = buffer.back();
buffer.pop_back();
                  } while (!stop);
        vector<int> konig() {
    // returns minimum vertex cover, run this after maximumMatching()
    vector<bool> matched(m);
    for (int i = 0; i < n; ++i) {
        if (match[i] != -1) matched[match[i]] = true;
    }
}</pre>
                  queue<int> 0;
                 queterinty 0;
was.assign(m + n, false);
for (int i = 0; i < m; ++i) {
    if (!matched[i]) {
        was[i] = true;
    }
}</pre>
                while (!Q.empty()) {
   int u = Q.front(); Q.pop();
   for (int v : a[u]) if (!was[m + v]) {
      was[m + v] = true;
      if (match[v] != -1 && !was[match[v]]) {
            was[match[v]] = true;
            Q.push(match[v]);
      }
                 }
                 vector<int> res;
for (int i = 0; i < m; ++i) {
    if (!was[i]) res.push_back(i);
}</pre>
                  for (int i = m; i < m + n; ++i) {
   if (was[i]) res.push_back(i);</pre>
                 return res;
};
```

6.3 General Matching

```
/*
    * Complexity: O(E*sqrt(V))
    * Indexing from 1
*/
struct Blossom {
    static const int MAXV = 1e3 + 5;
    static const int MAXE = 1e6 + 5;
    int n, E, 1st[MAXV], next[MAXE], adj[MAXE];
    int nxt[MAXV], mat[MAXV], dad[MAXV], col[MAXV];
    int que[MAXV], qh, qt;
    int vis[MAXV], act[MAXV];
    int tis[MAXV], act[maxV];
    int vis[maxV], act[maxV], act[max
```

```
int lca(int u, int v) {
           tag++;
for(;; swap(u, v)) {
          tag++;
for(;; swap(u, v)) {
    if (u) {
        if (vis[u = dad[u]] == tag) {
            return u;
        }
}
                               vis[u] = tag;
u = nxt[mat[u]];
                    }
           }
}
void blossom(int u, int v, int g) {
    while (dad[u] != g) {
        nxt[u] = v;
        if (col[mat[u]] == 2) {
            col[mat[u]] = 1;
            que[++qt] = mat[u];
        }
}
                     if (u == dad[u]) dad[u] = g;
if (mat[u] == dad[mat[u]]) dad[mat[u]] = g;
v = mat[u];
u = nxt[v];
}
int augument(int s) {
   for (int i = 1; i <= n; i++) {
      col[i] = 0;
      dad[i] = i;
}</pre>
          }
qh = 0; que[qt = 1] = s; col[s] = 1;
for (int u, v, i; qh < qt; ) {
    act[u = que[++qh]] = 1;
    for (i = lst[u];i; i = next[i]) {
      v = adj[i];
      if (col[v] = 0) {
         nxt[v] = u;
      col[v] = 2;
      if (!mat[v]) {
            for (', v, v, v, u) }</pre>
                                                        for (; v; v = u) {
    u = mat[nxt[v]];
    mat[v] = nxt[v];
    mat[nxt[v]] = v;
                                                        return 1;
                                             col[mat[v]] = 1;
que[++qt] = mat[v];
                                  else if (dad[u] != dad[v] && col[v] == 1) {
                                            int g = lca(u, v);

blossom(u, v, g);

blossom(v, u, g);

for (int j = 1; j <= n; j++) {

    dad[j] = dad[dad[j]];
                     }
            return 0;
int maxmat() {
   for (int i = 1; i <= n; i++) {
      if (!mat[i]) {
        total += augument(i);
}</pre>
                    }
           return total;
```

6.4 Dinic Flow

```
const int V = le5;
const int INF = le9;
struct Flow {
    vector(sint) adj[V];
    int to[V], c[V], f[V];
    int n, s, t, cnt;
    int d[V];
    int cur[V];
    Flow(int n, int s, int t) {
        this=>n = n;
        this=>s = s;
        this=>t = t;
        cnt = 0;
}

int addEdge(int u, int v, int _c) {
        to[cnt] = v, c[cnt] = [0;
        adj[u].push_back(cnt++);
        to[ent] = u, c[cnt] = 0, f[cnt] = 0;
        adj[v].push_back(cnt++);
}

bool bfs() {
    for (int i = 0; i < n; i++) d[i] = -1;
    d[s] = 0;
    queue(int>);
    while (!q.empty()) {
        int u = q.front();
        q.posh(s);
    while (!q.empty()) {
        int v = to[id];
        if (d[v] = -1 && f[id] < c[id]) {
            d[v] = d[u] + 1;
            q.push(v);
        }
    }
    return d[t] != -1;
}
int dfs(int u, int res) {
    if (u = t) return res;</pre>
```

```
for (int &it = cur[u]; it < adj[u].size(); it++) {
    int id = adj[u][it];
    int v = to[id];
    if (id)v == d[u] + 1 && f[id] < c[id]) {
        int foo = dfs(v, min(c[id] - f[id], res));
        if (ffoo) {
            f[id] += foo;
            f[id] += foo;
            return foo;
        }
    }
    return 0;
}

int maxFlow() {
    int res = 0;
    while (bfs()) {
        for (int i = 0; i < n; i++) cur[i] = 0;
        while (1) {
            int foo = dfs(s, INF);
            if (!foo) break;
            res += foo;
    }
}
return res;
}
</pre>
```

6.5 Min Cost-Max Flow

```
act Flow {
    static const int V = 100000;
    int head[V], to[V], c[V], cost[V], f[V], nxt[V], h[V], par[V], inQueue[V]
                       ];
         l;
int s, t, n, cnt;
queue <int> q;
Flow (int n, int s, int t) {
    this->n = n;
    this->s = s;
    this->t = t;
    cnt = 0;
                  cnt = 0;
for (int i= 0; i < n; i++) {
  head[i] = -1;
  inQueue[i] = 0;</pre>
         pair<int, int> maxFlow () {
   int res = 0, minCost = 0;
   while (1) {
                            le (1) {
for (int i = 0; i < n; i++) {
   par[i] = -1;
   h[i] = 2e9;</pre>
                            }
h[s] = 0;
q.push(s);
inQueue[s] = 1;
while (!q.empty()) {
   int u = q.front();
   q.pop();
   inQueue[u] = 0;
                                     inqueue[u] = 0;
for (int id = head[u]; id != -1; id = nxt[id]) {
   int v = to[id];
   if (h[v] > h[u] + cost[id] && f[id] < c[id]) {
      h[v] = h[u] + cost[id];
      par[v] = id;
   if (!inqueue[v]) {
      inqueue[v] = 1;
      q.push(v);
   }</pre>
                                     }
                             if (par[t] == -1) {
    break;
                             int x = t;
                            int x = t;
int now = 2e9;
while (x != s) {
   int id = par[x];
   now = min(now, c[id] - f[id]);
   x = to[id ^ 1];
                                     t;
le (x != s) {
   int id = par[x];
   minCost += cost[id] * now;
   f[id] += now;
   f[id ^ 1] -= now;
   x = to[id ^ 1];
                             res += now:
                  return make_pair(res, minCost);
};
```

6.6 Bounded Feasible Flow

```
struct BoundedFlow {
  int low[N][N], high[N][N];
  int c[N][N];
  int f[N][N];
```

6.7 Hungarian Algorithm

```
truct BipartiteGraph {
    const int INF = le9;

    vector<vector<int> > c; // cost matrix
    vector<int> fx, fy; // potentials
    vector<int> matchX, matchY; // corresponding vertex
    vector<int> trace; // last vertex from the left side
    vector<int> trace; // last vertex from the tree && the corresponding node
    queue<int> Q; // queue used for BFS

int n; // assume that |L| = |R| = n
    int start; // current root of the tree
    int finish; // leaf node of the augmenting path

BipartiteGraph(int n) {
        this->n = n;
            c = vector<vector<int> > (n + 1, vector<int> > (n + 1, INF));
        fx = fy = matchX = matchY = trace = d = arg = vector<int> (n + 1);
    }

void addEdge(int u, int v, int cost) { c[u][v] = min(c[u][v], cost); }
    int cost(int u, int v) { return c[u][v] - fx[u] - fy[v]; }

void initBFS(int root) {
        start = root;
        Q = queue(int>(); Q.push(start);
        for (int i = 1; i <= n; ++i) {
            trace(i] = 0;
            d[i] = cost(start, i);
            arg[i] = start;
        }
    }

int findPath() {
        while (!Q.empty()) {
            int w = cost(u, v);
            if (w = 0) {
                trace[v] = u;
                if (matchY[v]) = 0) return v;
                  Q.push(matchY[v]);
            }
            if (d[v] > w) d[v] = w, arg[v] = u;
        }
        return 0;
}

void enlarge() {
```

6.8 Undirected mincut

```
* Find minimum cut in undirected weighted graph * Complexity: O(V^3)
#define SW StoerWagner
#define cap_t int
namespace StoerWagner {
      int n;
vector<vector<cap_t> > graph;
      vector<int> cut;
      void init(int _n) {
            n = _n;
qraph = vector<vector<cap_t>>(n, vector<cap_t>(n, 0));
      }
woid addEdge(int a, int b, cap_t w) {
    if (a == b) return;
    graph[a][b] += w;
    graph[b][a] += w;
      pair<cap_t, pair<int, int> > stMinCut(vector<int> &active) {
            t = s;
s = cur;
v[cur] = 1;
                   for (auto j : active) key[j] += graph[cur][j];
            return make_pair(key[s], make_pair(s, t));
      cap_t solve() {
  cap_t res = numeric_limits <cap_t>::max();
  vector<vector<int>> grps;
            vector<vector<int>> grps;
vector<int>> active;
cut.resize(n);
for (int i = 0; i < n; i++) grps.emplace_back(1, i);
for (int i = 0; i < n; i++) active.push_back(i);
while (active.size() >= 2) {
    auto stcut = stMinCut (active);
    if (stcut.first < res) {
        res = stcut.first;
        fill(cut.begin(), cut.end(), 0);
        for (auto v : grps[stcut.second.first]) cut[v] = 1;
}</pre>
```

6.9 Eulerian Path/Circuit

```
struct EulerianGraph {
    vector< vector< pair<int, int> >> a;
    int num_edges;

EulerianGraph(int n) {
        a.resize(n + 1);
        num_edges = 0;
}

void add_edge(int u, int v, bool undirected = true) {
        a[u].push_back(make_pair(v, num_edges));
        if (undirected) a[v].push_back(make_pair(u, num_edges));
        num_edges++;
}

vector<int> get_eulerian_path() {
        vector<br/>int> path, s;
        vector<br/>vector<br/>int> path, s;
        vector<br/>int> path, s;
        vector<br/>int path, s;
```

6.10 2-SAT

7 Data structures

7.1 Treap

```
class Treap {
       struct Node {
             int key;
uint32_t prior;
bool rev_lazy;
              int size;
              inline int size(Node *x) { return x ? x->size : 0; }
       void push(Node *x) {
   if (x && x->rev_lazy) {
      x->rev_lazy = false;
      swap(x->l, x->r);
      if (x->l) x->l->rev_lazy ^= true;
      if (x->r) x->r->rev_lazy ^= true;
}
       }
       inline void update(Node *x) {
                     x \rightarrow size = size(x \rightarrow 1) + size(x \rightarrow r) + 1;
       void join(Node *&t, Node *l, Node *r) {
   push(l);  push(r);
   if (!l || !r)
        t = l ? l : r;
   else if (1->prior < r->prior)
        join(l->r, 1->r, r), t = l;
}
                      join(r->1, 1, r->1), t = r;
       void splitByKey(Node *v, int x, Node* &1, Node* &r) {
   if (!v) return void(l = r = nullptr);
               push(v);
                      splitByKey(v->r, x, v->r, r), 1 = v;
                      splitByKey(v->1, x, 1, v->1), r = v;
              update(v);
       void splitByIndex(Node *v, int x, Node* &1, Node* &r) {
   if (!v) return void(1 = r = nullptr);
   push(v);
   int index = size(v->1) + 1;
   if (index < x)</pre>
                      splitByIndex(v->r, x - index, v->r, r), l = v;
             esse
    splitByIndex(v->1, x, 1, v->1), r = v;
update(v);
       void show(Node *x) {
             if (!x) return;
              push(x);
show(x->1);
cerr << x->key << '';
              show(x->r);
       Node *root;
Node *1, *m, *r;
       Treap() { root = NULL; }

Treap() { delete root; }

int size() { return size(root); }
       int insert(int x) {
              insert(int x) {
splitByKey(root, x, 1, m);
splitByKey(m, x + 1, m, r);
int ans = 0;
if (!m) m = new Node(x), ans = size(l) + 1;
join(l, 1, m);
join(root, l, r);
              return ans;
              erase(int x) {
    splitByKey(root, x, 1, m);
    splitByKey(m, x + 1, m, r);
    int ans = 0;
    if (m) {
        ans = size(l) + 1;
    }
}
                     delete m;
                join(root, l, r);
              return ans:
```

```
void insertAt(int pos, int x) {
    splitByIndex(root, pos, l, r);
    join(l, l, new Node(x));
    join(root, l, r);
}

void eraseAt(int x) {
    splitByIndex(root, x, l, m);
    splitByIndex(m, 2, m, r);
    delete m;
    join(root, l, r);
}

void updateAt(int pos, int newValue) {
    eraseAt(pos);
    insertAt(pos, newValue);
}

int valueAt(int pos) {
    splitByIndex(root, pos, l, m);
    splitByIndex(m, 2, m, r);
    int res = m->key;
    join(l, l, m);
    join(root, l, r);
    return res;
}

void reverse(int from, int to) {
    splitByIndex(m, to - from + 2, m, r);
    m->rev_lazy '= 1;
    join(l, l, m);
    join(root, l, r);
}

void show() {
    cerr << "Size = " << size() << " ";
    cerr << "]\n";
}</pre>
```

7.2 Big Integer

```
typedef vector<int> bigInt;
 const int BASE = 1000;
const int LENGTH = 3;
// * Refine function
bigInt& fix(bigInt &a) {
   a.push_back(0);
   for (int i = 0; i + 1 < a.size(); ++i) {
        a[i + 1] += a[i] / BASE; a[i] %= BASE;
        if (a[i] < 0) a[i] += BASE, --a[i + 1];
}</pre>
           while (a.size() > 1 && a.back() == 0) a.pop_back();
  // * Constructors
// * Constructors
bigInt big(int x) {
  bigInt result;
  while (x > 0) {
    result push_back(x % BASE);
    x /= BASE;
          return result;
bigInt big(string s) {
   bigInt result(s.size() / LENGTH + 1);
   for (int i = 0; i < s.size(); ++i) {
      int pos = (s.size() - i - 1) / LENGTH;
      result[pos] = result[pos] * 10 + s[i] - '0';
}</pre>
          return fix(result), result;
 // * Compare operators
int compare(bigInt &a, bigInt &b) {
   if (a.size() != b.size()) return (int)a.size() - (int)b.size();
   for (int i = (int) a.size() - 1; i >= 0; --i)
      if (a[i] != b[i]) return a[i] - b[i];
   return 0;
 \texttt{\#define} \ \ \texttt{DEFINE\_OPERATOR}(x) \ \ \textbf{bool operator} \ \ x \ \ (\texttt{bigInt \&a, bigInt \&b)} \ \ \{ \ \ \textbf{return} \ \ 
#define DEFINE_OPERATOR(X)
compare(a, b) x 0; }
DEFINE_OPERATOR(==)
DEFINE_OPERATOR(=)
DEFINE_OPERATOR(>)
DEFINE_OPERATOR(>)
DEFINE_OPERATOR(>=)
DEFINE_OPERATOR(<==)
 #undef DEFINE_OPERATOR
 // * Arithmetic operators
void operator += (bigInt &a, bigInt b) {
   a.resize(max(a.size(), b.size()));
   for (int i = 0; i < b.size(); ++i)
      a[i] += b[i];
   fix(a);</pre>
 fix(a);
```

7.3 Convex Hull IT

```
struct Line {
       long long a, b; // y = ax + b
Line(long long a = 0, long long b = -INF): a(a), b(b) {}
long long eval(long long x) {
             return a * x +
};
struct Node (
       Line line;
int 1, r;
Node *left, *right;
       \label{eq:node_node_node} Node(\mbox{int } 1, \mbox{ int } r): \mbox{$1(1)$, $r(r)$, $left(NULL)$, $right(NULL)$, $line()$ $\{\}$}
      return;
                    int mid = valueX[1 + r >> 1];
if (AB.eval(mid) < CD.eval(mid))
    line = CD, left->update(i, j, AB);
                           line = AB, right->update(i, j, CD);
             left->update(i, j, newLine);
right->update(i, j, newLine);
       long long getMax(int i) {
   if (1 == r) return line.eval(valueX[i]);
   if (i <= (1 + r >> 1)) return max(line.eval(valueX[i]), left->getMax(
             return max(line.eval(valueX[i]), right->getMax(i));
};
Node* build(int 1, int r) {
  Node *x = new Node(1, r);
  if (1 == r) return x;
  x>>left = build(1, 1 + r >> 1);
  x>right = build((1 + r >> 1) + 1, r);
}
       return x;
```

7.4 Link Cut Tree

```
// to change it to sum weight of child in root>u
// comment all update on w and return x->s instead
struct node_t {
   node_t *p, *l, *r;
   int size, rev;
   int s, w;
   node_t() : p(0), l(0), r(0), size(1), rev(0), s(1), w(1) {}
};
 int
          isrt(node_t* x) {
return !(x->p) || (x->p->1 != x && x->p->r != x);
int left(node_t* x) {
    return x->p->1 == x;
void setchild(node_t* x, node_t* p, int 1) {
    (1 ? p->1 : p->r) = x;
    if (x) x->p = p;
void push(node_t* x) {
   node_t* u = x->l;
   node_t* v = x->r;
   if (x->rev) {
      if (u) swap(u->l, u->r), u->rev ^= 1;
      if (v) swap(v->l, v->r), v->rev ^= 1;
      x->rev = 0;
}
int size(node_t* x) {
    return x ? x->size : 0;
int sum(node_t* x) {
    return x ? x->s : 0;
void pull(node_t* x) {
    x->size = size(x->1) + 1 + size(x->r);
    x->s = sum(x->1) + x->w + sum(x->r);
void rotate(node_t* x) {
  node_t *p = x->p, *g = p->p;
  int l = left(x);
  setchild(1 ? x->r : x->1, p, l);
  if (list(p)) setchild(x, g, left(p));
}
          else x->p = g;
setchild(p, x, !1);
pull(p);
node_t* splay(node_t* x) {
   push(x);
   while (!isrt(x)) {
                    node_t * p = x > p, *g = p > p;
if (g) push(g);
push(p), push(x);
if (lisrt(p)) rotate(left(x) != left(p) ? x : p);
                    rotate(x);
           pull(x);
          return x:
node_t* access(node_t* x) {
   node_t* z = 0;
```

```
for (node_t* y = x; y; y = y->p) {
    splay(y);
    y->w += sum(y->r);
    y->r = z;
    y->w -= sum(y->r);
              pull(z = y);
        return z;
void link(node_t* x, node_t* p) {
  access(x), access(p);
  x->p = p;
  p->w += sum(x);
void cut(node_t* x) {
   access(x);
   x->1->p = 0, x->1 = 0;
   pull(x);
void makeroot(node_t* x) {
       access(x);
x->rev ^= 1;
swap(x->1, x->r);
node_t* findroot(node_t* x) {
        access(x);
while (x->1) push(x), x = x->1;
        push(x);
return splay(x);
node_t* lca(node_t* x, node_t* y) {
   if (findroot(x) != findroot(y)) return 0;
        access(x);
        return access(y);
int connect(node_t* x, node_t* y) {
   if (x == y) return 1;
   access(x), access(y);
   return x->p != 0;
int treequery(node_t* x) {
   access(x);
        return x->w;
```

8 Miscellaneous

8.1 RNG

mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
//use mt19937_64 if we want 64-bit number