Vowel formants example

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Getting started

R packages

In R, you need to install (once) any R software package (aka library) that you want to use, before you load it with the library() function each time that you run a script or RMarkdown file.

This code will check whether or not you have those packages, and if not, will install them and load the packages.

```
if(!require("tidyverse")) install.packages("tidyverse")
if(!require("ggpubr")) install.packages("ggpubr")
if(!require("devtools")) install.packages("devtools")
library(devtools)
if(!require("ggConvexHull")) devtools::install_github("cmartin/ggConvexHull")
```

Normally, once a package is already installed, you simply load it with the library() function, like this:

```
library(tidyverse)
library(ggpubr)
library(ggConvexHull)
```

The tidyverse package will install several R packages including:

- ggplot for creating nice looking plots
- dplyr for manipulating data easily

We are going to additionally use ggpubr package because it is helpful in making professional looking plots.

And the ggConvexHull package, which extends the <code>geom_polyon()</code> function in the ggplot package, so that we can add a convex hull around our vowel polygon data. This package is available via GitHub and hence the devtools package.

Load our vowel data

Let's load the vowel formants data from our measurements in class.

First download it from the shared Google sheets as a CSV file.

I renamed my downloaded file to data.csv to remove the spaces in the filename (you don't have to) and I saved it in the same directory as this README.Rmd file. If you want to get the current working directory in RStudio (or R) you can use this command:

```
getwd()
```

```
## [1] "/Users/stiv/GitHub/APY313/case_studies/formants"
```

In RStudio, I set the working directory to the directory that contains this script. In this folder with the script, I also put the downloaded vowels data.

Make your life easier and put both files in the same folder!

You can set the working directory a la the link above or you can also do it manually with the setwd() function, e.g.:

```
# setwd('/Users/stiv/GitHub/APY313/case_studies/formants')
```

Let's load the data that's in the same directory as this script.

```
df <- read_csv('data.csv')
# If you want the data in a different directory, you can give `read_csv()` the full path! E.g.:
# df <- read_csv('/Users/stiv/Downloads/data.csv')</pre>
```

With the read_csv() function we read the CSV file – a comma delimited text file that represents tabular (i.e. table) data as rows and columns.

The read_csv() function reads the file into R as a data frame, essentially a table!¹

Have a look at the raw data

Let's have a look at the data. The function structure str() shows the data structure of the loaded data frame. It tells you what the columns are, what each column's data type is (e.g. chr means the rows in that column include characters; num means they include numbers) – followed by human rows there are and examples of the first few rows.

```
str(df)
```

```
## spc_tbl_ [35 x 10] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
## $ ID : num [1:35] 1 1 1 1 1 2 2 2 2 2 2 ...
## $ Word : chr [1:35] "heed" "hayed" "hawed" "who'd" ...
## $ Vowel : chr [1:35] "i" "e" "a" "u" ...
## $ F0 : num [1:35] 120 115 115 122 119 180 181 177 201 185 ...
## $ F1 : num [1:35] 319 418 558 317 457 383 503 785 383 544 ...
## $ F2 : num [1:35] 2522 2119 1044 874 1044 ...
```

 $^{^{1}}$ It's actuall a "tibble", which is tidy verse's version of the data frame, but that's not important for now.

```
##
    $ F3
            : num [1:35] 3299 3631 2677 2668 2587 ...
    $ Sex
##
            : chr [1:35] "M" "M" "M" "M" ...
##
            : chr [1:35] "English" "English" "English" "English" ...
    $ Height: num [1:35] 69 69 69 69 69 62 62 62 62 ...
##
##
    - attr(*, "spec")=
##
     .. cols(
##
          ID = col_double(),
     . .
          Word = col_character(),
##
##
          Vowel = col_character(),
##
          F0 = col_double(),
##
          F1 = col_double(),
          F2 = col_double(),
##
##
          F3 = col_double(),
          Sex = col_character(),
##
##
          L1 = col_character(),
##
          Height = col_double()
##
     ..)
    - attr(*, "problems")=<externalptr>
```

The function head() shows us the first few rows, so we can have an idea of its contents.

head(df)

```
## # A tibble: 6 x 10
##
        ID Word Vowel
                                  F1
                                         F2
                                               F3 Sex
                                                                  Height
                            F0
                                                         L1
##
     <dbl> <chr> <chr> <dbl>
                               <dbl>
                                     <dbl>
                                            <dbl> <chr> <chr>
                                                                   <dbl>
## 1
         1 heed i
                           120
                                 319
                                      2522
                                             3299 M
                                                         English
                                                                      69
## 2
         1 hayed e
                           115
                                 418
                                      2119
                                             3631 M
                                                         English
                                                                      69
## 3
                                                                      69
         1 hawed a
                           115
                                 558
                                      1044
                                             2677 M
                                                         English
                                                         English
                                                                      69
         1 who'd u
                           122
                                 317
                                        874
                                             2668 M
## 5
         1 hoed
                 0
                           119
                                 457
                                      1044
                                             2587 M
                                                         English
                                                                      69
## 6
         2 heed i
                           180
                                 383
                                      2756
                                             3159 F
                                                         English
                                                                      62
```

The function tail() gives us the last few rows.

tail(df)

```
## # A tibble: 6 x 10
                                         F2
                                               F3 Sex
##
        ID Word Vowel
                            F0
                                  F1
                                                         L1
                                                                  Height
##
     <dbl> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <chr> <chr>
                                                                   <dbl>
## 1
         6 hoed o
                          122
                                 385
                                        963
                                             2952 M
                                                         English
                                                                      62
## 2
         7 heed
                          180.
                                2756
                                      3616
                                             3930 <NA>
                                                                      68
                 i
                                                         spanish
## 3
         7 hayed e
                          180.
                                2756
                                      3343
                                             3972 <NA>
                                                         spanish
                                                                      68
## 4
         7 hawed a
                          179.
                                1204
                                       2819
                                             4056 <NA>
                                                                      68
                                                         spanish
## 5
         7 who'd u
                          198.
                                1393
                                       2798
                                             4098 <NA>
                                                         spanish
                                                                      68
         7 hoed o
                          184.
                                1037
                                      2693
                                             3700 <NA>
                                                         spanish
                                                                      68
```

We can also simply ask for the dimensions of the data frame (table!) with the dim() function. This tells us the number of **rows** (i.e. observations) by the number of **columns** (i.e. variables).

dim(df)

```
## [1] 35 10
```

Recall from class that every data has a data type. We can ask R to tell us the data type with the class() function:

```
class(df)
```

```
## [1] "spec_tbl_df" "tbl_df" "tbl" "data.frame"
```

Or if you want to know the data type of a specific column in the table.

```
class(df$ID)
```

```
## [1] "numeric"
```

The \$ in R is used to access specific columns! You can access each column by its name, e.g.:

df\$Word

```
[1]
       "heed"
                "haved" "hawed" "who'd" "hoed"
                                                 "heed"
                                                         "haved"
                                                                 "hawed" "who'd"
                "heed"
## [10]
       "hoed"
                        "hayed" "hawed" "whod"
                                                 "hoed"
                                                         "heed"
                                                                 "heyed" "hawed"
## [19] "who'd" "hoed"
                        "heed"
                                "hayed" "hawed" "who'd" "hoed"
## [28] "hawed" "who'd" "hoed"
                                "heed"
                                         "hayed" "hawed" "who'd" "hoed"
```

Working with the data

Overview

Above we had a quick look at the raw data, which you can also do directly with RStudio by clicking on the dataframe in the Environment tab.

There are lots of ways of doing preliminary data analysis and one great way is to visualize the data!

Recall our discussion of how the International Phonetic Alphabet (IPA) vowel chart looks – head faces left, vertical access is the jaw's height (closed to open) and the horizontal access is the position of the tongue (front to back in the mouth).

Single speaker

Let's look at one speaker in our sample. This is where the data manipulation R package dplyr comes in handy! We will talk about how to use these functions in class.

The dplyr package has several functions that allow us to filter() rows and to select() columns (among many other useful things!).

Let's filter out a single speaker and plot their vowels. You can set the ID to yourself!

```
single_speaker <- df %>% filter(ID == 5)
```

Above, we have saved the output of filtering by ID == 1 (read "subject ID equals one") to a new data frame and named it single_speaker. Let's have a look.

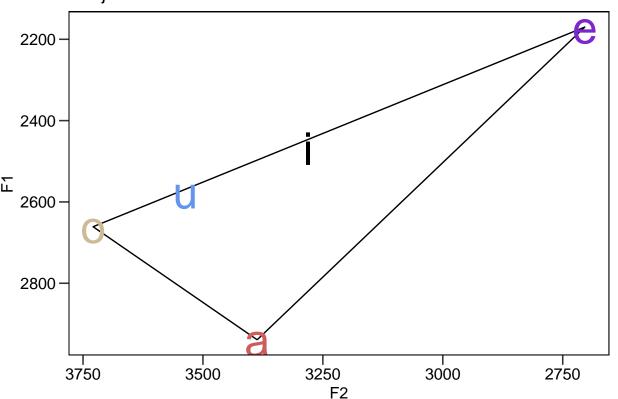
single_speaker

```
## # A tibble: 5 x 10
##
        ID Word Vowel
                           F0
                                  F1
                                        F2
                                               F3 Sex
                                                         T.1
                                                                 Height
##
     <dbl> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <chr> <chr>
                                                                   <dbl>
## 1
         5 heed i
                          169.
                                2469
                                      3281
                                             3772 M
                                                         Spanish
                                                                      67
                                2170
                                                         Spanish
                                                                      67
## 2
         5 hayed e
                          142.
                                      2704
                                             3750 M
                                             4583 M
                                                                      67
## 3
                          133.
                                2939
                                      3387
                                                         Spanish
         5 hawed a
## 4
         5 who'd u
                                2576
                                      3537
                                             4220 M
                                                         Spanish
                                                                      67
                          144.
## 5
         5 hoed o
                          127.
                                2661
                                      3729
                                             4583 M
                                                         Spanish
                                                                      67
```

Now let's plot Subject ID 1's vowel formant values for F1 and F2.

```
ggplot(single_speaker, aes(x = F2, y = F1, color = Vowel)) +
  geom_convexhull(alpha = 0, colour = "black") +
  geom_text(aes(label = Vowel), size = 12) +
  scale_x_reverse() +
  scale_y_reverse() +
  coord_cartesian() +
  theme_pubr(border = TRUE, legend = "none") +
  theme(axis.ticks.length = unit(.25, "cm")) +
  scale_color_manual(
   name = "Vowel",
   values = c(
      "a" = "indianred",
      "i" = "black",
      "u" = "cornflowerblue",
      "o" = "wheat3",
      "e" = "purple3"
   )
  ) +
  ggtitle('Subject ID 1')
```

Subject ID 1



summary(df)

```
##
         ID
                   Word
                                     Vowel
                                                           FO
## Min.
               Length:35
                                                     Min. :115.0
         :1
                                  Length:35
   1st Qu.:2
               Class : character
                                  Class : character
                                                     1st Qu.:123.5
               Mode :character
                                  Mode :character
  Median:4
                                                     Median :142.3
## Mean
                                                     Mean
                                                           :154.9
```

```
3rd Qu.:6
                                                        3rd Qu.:182.4
##
    Max.
          :7
                                                        Max.
                                                                :207.0
##
          F1
                            F2
                                            F3
                                                         Sex
##
   Min.
           : 124.0
                      Min.
                             : 874
                                     Min.
                                             :2307
                                                     Length:35
##
    1st Qu.: 344.5
                      1st Qu.:1208
                                     1st Qu.:2824
                                                     Class : character
##
    Median : 461.0
                      Median:2268
                                     Median:3104
                                                     Mode :character
    Mean
          : 925.0
                      Mean
                            :2132
                                     Mean
                                            :3287
##
                      3rd Qu.:2818
    3rd Qu.:1120.5
##
                                     3rd Qu.:3736
           :2939.0
##
    Max.
                      Max.
                             :3729
                                     Max.
                                             :4583
##
         L1
                            Height
##
   Length:35
                       Min.
                               :62.00
##
    Class : character
                        1st Qu.:62.00
                        Median :67.00
##
    Mode :character
##
                        Mean
                               :66.43
##
                        3rd Qu.:69.00
##
                        Max.
                               :70.00
```

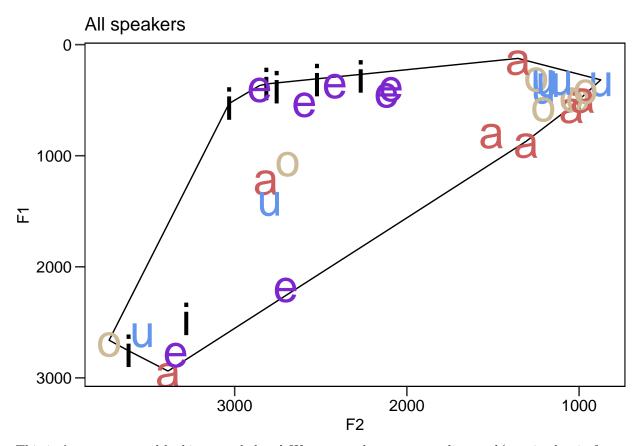
All speakers

Let's plot all of the F1 and F2 formants in our sample and see what they look like. We use the ggplot() function with lots of other functions. This is complicated – do not worry, we will go through this mess in class.

```
ggplot(df, aes(x = F2, y = F1, color = Vowel)) +
 geom_convexhull(alpha = 0, colour = "purple") +
  scale_x_reverse() +
  scale_y_reverse() +
    coord_cartesian() +
  theme_pubr(border = TRUE, legend = "none") +
  theme(axis.ticks.length = unit(.25, "cm")) +
  scale_color_manual(
   name = "Vowel",
   values = c(
      "a" = "indianred",
      "i" = "black",
      "u" = "cornflowerblue",
      "o" = "wheat3",
      "e" = "purple3"
    )
  ) +
  ggtitle('All speakers')
```

All speakers 1000 2000 3000 F2

```
ggplot(df, aes(x = F2, y = F1, color = Vowel)) +
  geom_convexhull(alpha = 0, colour = "black") +
  geom_text(aes(label = Vowel), size = 12) +
  scale_x_reverse() +
  scale_y_reverse() +
  coord_cartesian() +
  theme_pubr(border = TRUE, legend = "none") +
  theme(axis.ticks.length = unit(.25, "cm")) +
  scale_color_manual(
    name = "Vowel",
    values = c(
      "a" = "indianred",
      "i" = "black",
      "u" = "cornflowerblue",
      "o" = "wheat3",
      "e" = "purple3"
    )
  ) +
  ggtitle('All speakers')
```



This isn't a very normal looking vowel chart! We seem to have some outliers and/or mistakes in formant measurements, e.g., the "e" vowel in the bottom left corner is way too high in terms of F1 and F2 frequencies.

Filter out outliers

If we have outliers in our data, we can filter them out for exploratory purposes. For example, perhaps we find some data points (observations) that are missing data or perhaps some mistakes were made in the data collection. (Note that you should never remove outliers in real scientific experiments!)

First, let's check that all subjects have recorded all five vowels.

This code is a bit complex, but we will discuss it in class. By using dplyr we can "pipe" data frames (table data) into functions and manipulate the data.

Here we group by ID, i.e., we group each subjects responses into their own groups, and then we count (by "summarizing") how many rows (n()) function) are in each group – and we do so by creating a new column called vowels.

```
df %>% group_by(ID) %>% summarize(vowels = n())
```

```
##
   # A tibble: 7 x 2
##
         ID vowels
              <int>
##
     <dbl>
## 1
          1
                  5
## 2
          2
                  5
## 3
          3
                  5
## 4
          4
                  5
          5
                  5
## 5
## 6
          6
                  5
## 7
          7
                  5
```

We will pretend that subject ID 2 does not have 5 observations. What we can do is remove that subject from our data set like this:

```
temp <- df %>% filter(ID != 5)
```

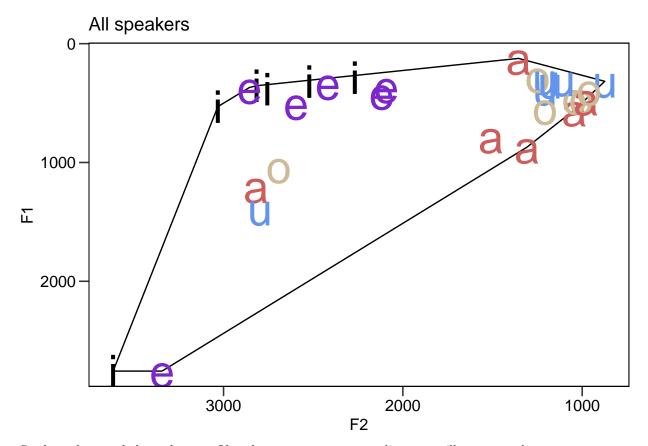
We saved the new data frame in a "temporary" data frame, so that we still have the full data in the df data frame.

Now let's revisualize what's left. We can use the same code we used above.

7

5 u

```
ggplot(temp, aes(x = F2, y = F1, color = Vowel)) +
  geom_convexhull(alpha = 0, colour = "black") +
  geom_text(aes(label = Vowel), size = 12) +
  scale_x_reverse() +
  scale_y_reverse() +
  coord_cartesian() +
  theme_pubr(border = TRUE, legend = "none") +
  theme(axis.ticks.length = unit(.25, "cm")) +
  scale_color_manual(
   name = "Vowel",
   values = c(
      "a" = "indianred",
      "i" = "black",
      "u" = "cornflowerblue",
      "o" = "wheat3",
      "e" = "purple3"
   )
  ) +
  ggtitle('All speakers')
```

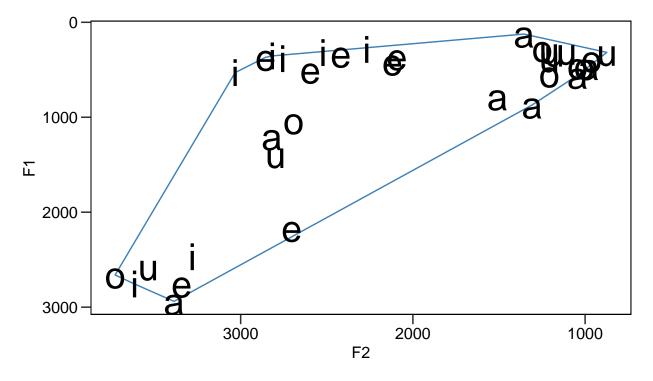


See how the vowel chart changes. If we have great or more outliers, we will see more change.

For each speaker, we can add the vowel polygon lines.

```
ggplot(df, aes(x = F2, y = F1)) +
  geom_convexhull(alpha = 0, aes(colour = ID)) +
  geom_text(aes(label = Vowel), size = 10) +
  scale_x_reverse() +
  scale_y_reverse() +
  coord_cartesian() +
  theme_pubr(border = TRUE) +
  theme(axis.ticks.length = unit(.25, "cm"))
```



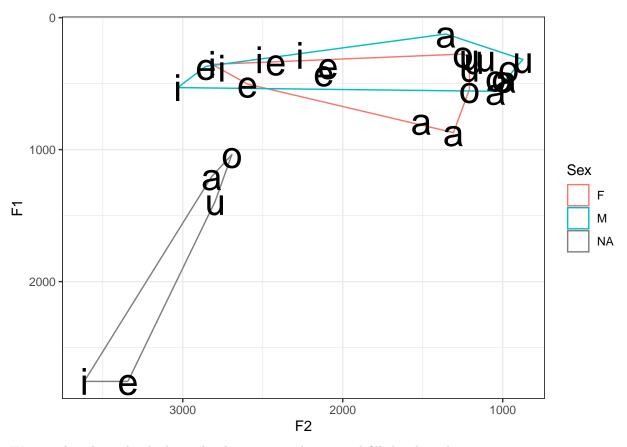


Analyses

Phonetic differences by sex

Let's plot individual vowel polygons by the reported sex of the speaker. As we expect from the literature on phonetic differences between male and female speech, the vowel polygon of the women in our sample displays greater acoustic range than the men.

```
temp <- df %>% filter(ID != 5)
ggplot(temp, aes(x = F2, y = F1)) +
  geom_convexhull(alpha = 0, aes(colour = Sex)) +
  geom_text(aes(label = Vowel), size = 10) +
  scale_x_reverse() +
  scale_y_reverse() +
  coord_cartesian() +
  theme_pubr(border = TRUE) +
  theme(axis.ticks.length = unit(.25, "cm")) +
  theme_bw()
```

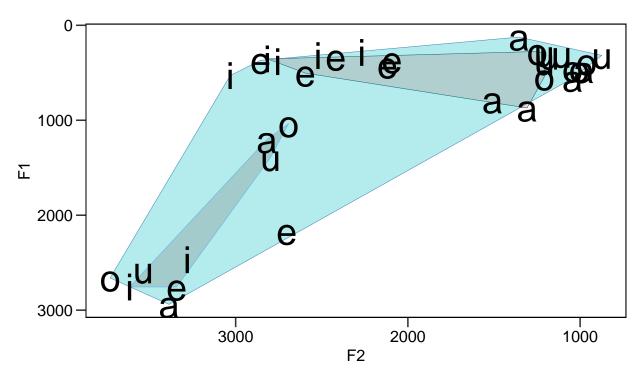


We can also plot individual vowel polygon spaces by sex and filled in by color.

```
ggplot(df, aes(x = F2, y = F1)) +
  geom_convexhull(alpha = 0.3, lwd = 0, aes(colour = ID, fill = Sex)) +
  geom_text(aes(label = Vowel), size = 10) +
  scale_x_reverse() +
  scale_y_reverse() +
  coord_cartesian() +
  theme_pubr(border = TRUE) +
  theme(axis.ticks.length = unit(.25, "cm"))
```

Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
i Please use `linewidth` instead.





Differences in pitch

Recall that we also recorded our F0 – our fundamental frequency, which we perceive as our pitch. This is in the F0 column of our data frame:

head(df)

```
## # A tibble: 6 x 10
##
        ID Word Vowel
                            F0
                                   F1
                                         F2
                                                F3 Sex
                                                                   Height
                                                          L1
##
     <dbl> <chr> <chr> <dbl>
                               <dbl>
                                      <dbl>
                                             <dbl> <chr>
                                                         <chr>
                                                                    <dbl>
## 1
         1 heed
                           120
                                  319
                                       2522
                                              3299 M
                                                          English
                                                                       69
## 2
                                                          English
                                                                       69
         1 hayed e
                           115
                                  418
                                       2119
                                              3631 M
                                                          English
## 3
                                                                       69
         1 hawed a
                           115
                                  558
                                       1044
                                              2677 M
                                        874
                                                          English
                                                                       69
         1 who'd u
                           122
                                  317
                                              2668 M
                                                          English
## 5
         1 hoed
                           119
                                  457
                                       1044
                                              2587 M
                                                                       69
         2 heed
                           180
                                  383
                                       2756
                                             3159 F
                                                          English
```

Again, we access any column in the data frame with the \$ operator with the name of the column as the suffix, e.g. let's get all values (aka observations, rows) of F0:

df\$F0

```
## [1] 120.0 115.0 115.0 122.0 119.0 180.0 181.0 177.0 201.0 185.0 201.0 203.0 ## [13] 205.0 207.0 206.0 126.0 127.0 124.0 126.0 124.0 169.3 142.3 132.9 143.6 ## [25] 127.3 122.0 133.0 120.0 123.0 122.0 180.4 180.2 179.3 198.4 183.8
```

We can also use various R functions on columns. For example, you can summarize numerical values from a column with the summary() function!

```
summary(df$F0)
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
                      142.3
##
     115.0
             123.5
                              154.9
                                       182.4
                                               207.0
Perhaps we want to summarize the F0 by sex? In "base R":
# Get a column by name
df$F0
  [1] 120.0 115.0 115.0 122.0 119.0 180.0 181.0 177.0 201.0 185.0 201.0 203.0
## [13] 205.0 207.0 206.0 126.0 127.0 124.0 126.0 124.0 169.3 142.3 132.9 143.6
## [25] 127.3 122.0 133.0 120.0 123.0 122.0 180.4 180.2 179.3 198.4 183.8
# Get rows by filtering the contents of a colum; here by "sex is F(emale)"
df[df$Sex == "F",]
## # A tibble: 15 x 10
##
         ID Word Vowel
                            F0
                                  F1
                                         F2
                                               F3 Sex
                                                         L1
                                                                 Height
##
      <dbl> <chr> <chr> <dbl> <dbl>
                                     <dbl> <dbl> <chr> <chr>
                                                                   <dbl>
##
                                       2756
                                             3159 F
    1
          2 heed i
                           180
                                 383
                                                         English
                                                                     62
##
    2
          2 hayed e
                           181
                                 503
                                       2596
                                             2937 F
                                                         English
                                                                     62
##
    3
          2 hawed a
                           177
                                 785
                                       1509
                                             2817 F
                                                         English
                                                                     62
                                       1208
##
    4
          2 who'd u
                           201
                                 383
                                             2837 F
                                                         English
                                                                     62
##
    5
          2 hoed o
                           185
                                 544
                                       1208
                                             2817 F
                                                         English
                                                                     62
    6
                           201
                                       2816
                                             3392 F
##
          3 heed i
                                 354
                                                        English
                                                                     67
##
   7
          3 hayed e
                           203
                                 335
                                       2419
                                             2995 F
                                                         English
                                                                     67
##
   8
          3 hawed a
                           205
                                 871
                                       1308
                                             3074 F
                                                         English
                                                                     67
                           207
                                       1209
                                             3034 F
##
   9
          3 whod
                                 296
                                                         English
                                                                     67
## 10
          3 hoed
                           206
                                 276
                                      1249
                                             2975 F
                                                         English
                                                                     67
                  0
## 11
         NA <NA>
                   <NA>
                            NA
                                  NA
                                         NA
                                               NA <NA>
                                                         <NA>
                                                                     NA
## 12
         NA <NA>
                                               NA <NA>
                                                         <NA>
                   <NA>
                            NA
                                  NA
                                         NA
                                                                     NA
## 13
         NA <NA>
                   <NA>
                            NA
                                  NA
                                         NA
                                               NA <NA>
                                                         <NA>
                                                                     NA
## 14
         NA <NA>
                   <NA>
                            NA
                                  NA
                                         NA
                                               NA <NA>
                                                         <NA>
                                                                     NA
## 15
         NA <NA>
                  <NA>
                            NA
                                  NA
                                         NA
                                               NA <NA>
                                                         <NA>
                                                                     NA
# Get just the contents of the column we want by the filter -- ugh this is painful!
df[df$Sex == "F", ]$F0
## [1] 180 181 177 201 185 201 203 205 207 206 NA NA NA NA NA
# Now let's summarize that mess
summary(df[df$Sex == "F", ]$F0)
##
      Min. 1st Qu. Median
                               Mean 3rd Qu.
                                                Max.
                                                         NA's
##
     177.0
             182.0
                      201.0
                              194.6
                                       204.5
                                               207.0
                                                            5
# And the men
summary(df[df$Sex == "M", ]$F0)
##
      Min. 1st Qu. Median
                               Mean 3rd Qu.
                                                         NA's
                                                Max.
     115.0
##
             121.5
                      124.0
                              127.7
                                       128.7
                                               169.3
                                                            5
```

Men in the sample have on average lower pitch.

Pitch versus height

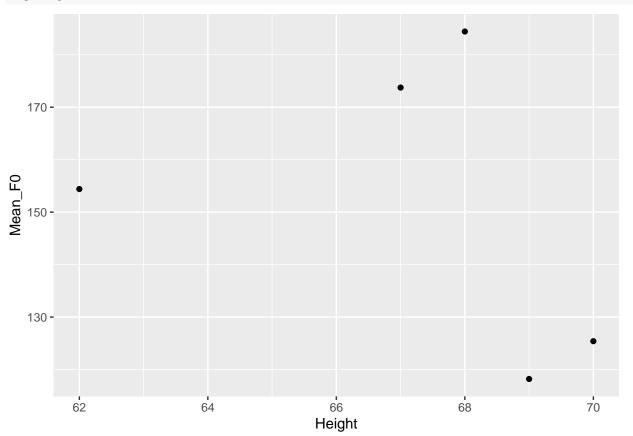
Lastly, let's see if there is a correlation between one's height and one's F0.

First, let's get the data we want by "grouping" the height variable and summarizing the mean F0 for each by height.

```
tmp <- df %>% group_by(Height) %>% summarize(Mean_F0 = mean(F0))
```

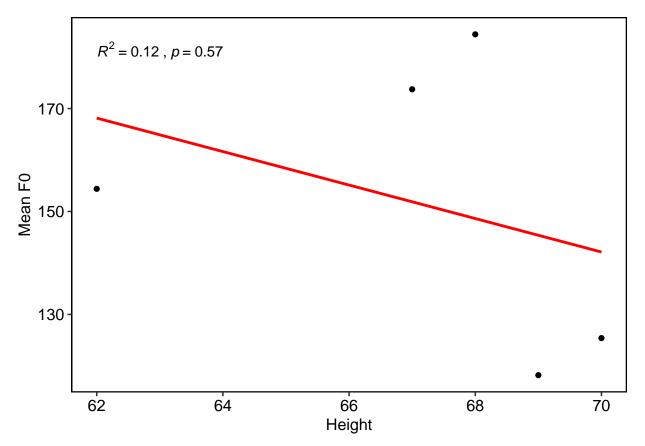
Now let's plot the results as a linear regression.

```
ggplot(tmp, aes(x=Height, y=Mean_F0)) +
geom_point()
```



```
ggplot(tmp, aes(Height, Mean_F0)) +
  geom_point(colour = "black", alpha = 1) +
  xlab("Height") +
  ylab("Mean F0") +
  theme_pubr(border = TRUE, margin = TRUE) +
  geom_smooth(method = "lm", se = FALSE, colour = "red") +
  ggpubr::stat_cor(aes(label = paste(..rr.label.., ..p.label.., sep = "~~,~~")))
```

```
## Warning: The dot-dot notation (`..rr.label..`) was deprecated in ggplot2 3.4.0.
## i Please use `after_stat(rr.label)` instead.
## `geom_smooth()` using formula = 'y ~ x'
```



And indeed it looks like as one gets taller, their pitch on average gets lower.

We can also get the model statistics directly from the data with these functions.

```
model1 <- lm(Mean_F0 ~ Height, data = tmp)
summary(model1)</pre>
```

```
##
## Call:
## lm(formula = Mean_F0 ~ Height, data = tmp)
##
## Residuals:
##
        1
               2
                      3
                             4
                                    5
   -13.75 21.86
                  35.79 -27.18 -16.72
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                369.826
                           339.506
                                      1.089
                                               0.356
                 -3.253
                             5.048
                                    -0.644
                                               0.565
##
  Height
## Residual standard error: 31.44 on 3 degrees of freedom
## Multiple R-squared: 0.1216, Adjusted R-squared: -0.1712
## F-statistic: 0.4153 on 1 and 3 DF, p-value: 0.5652
```