

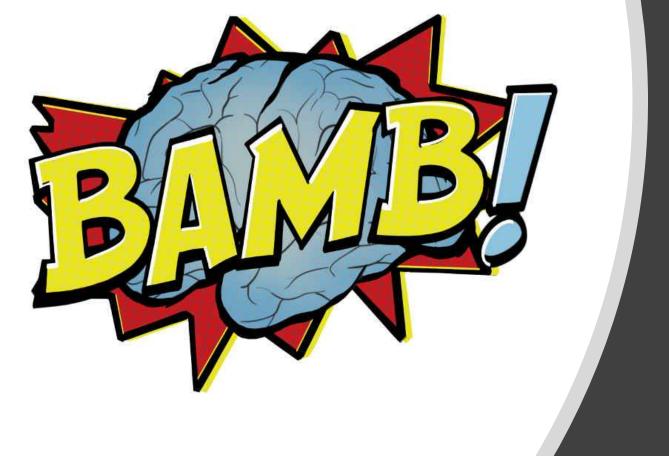
## Introduction to modelling of behavioral data

BAMB! 2023 Summer School Lecture 1A – Alex Hyafil

## Life cycle of a modelling project

Our goal for today: cover all the steps involved in a modelling project using a toy model example

- ✓ Defining a model
- ✓ Simulating a model
- ✓ Fitting a model to behavioral data
- ✓ Validating the model against the data
- ✓ Comparing various models on a dataset
- ✓ Checking the validity of the model selection process



Part I
Defining your
model
(a 5-step guide)

BAMB! Summer School Lecture I

## 1. Start from a question



(about the brain)

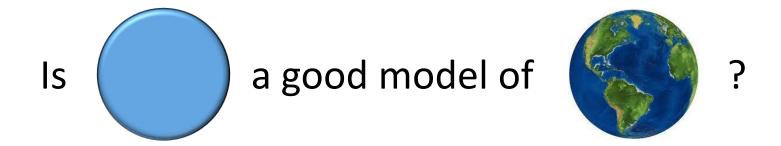
One model = One hypothesis



#### 2. Define your modelling objectives

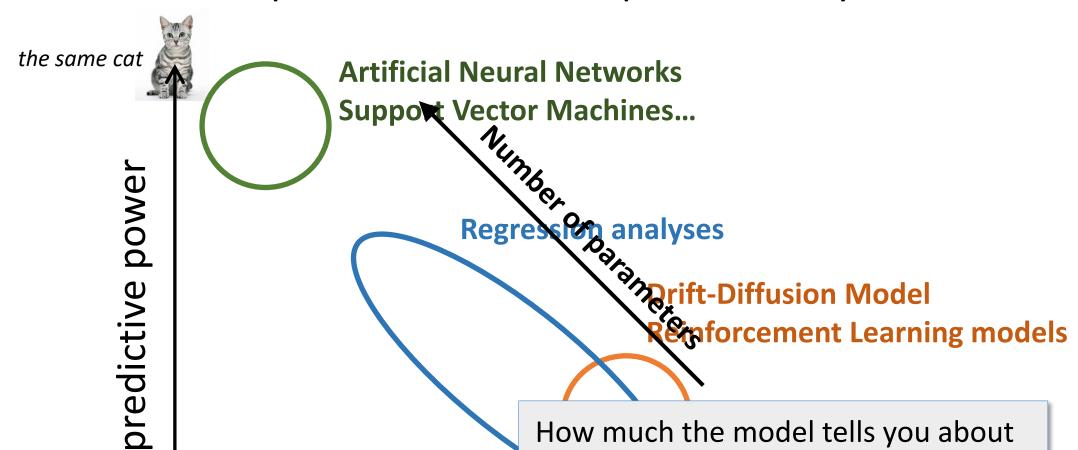
"All models are wrong, some are useful."

George Box, 1976





## Predictive power vs. interpretability



How precisely the model predicts actual behaviour

interpretability

the **structure** of data, i.e. cognitive

processes at work



#### A dual perspective on model evaluation

Outperforming other models on quantitative measures for how well the model explains the data Capturing some *qualitative*properties of the data revealed by
model-free analysis
(e.g. psychometric curve)

Relative criterion



Absolute criterion



We want our model to pass both tests



#### Setting your modelling on firm experimental ground

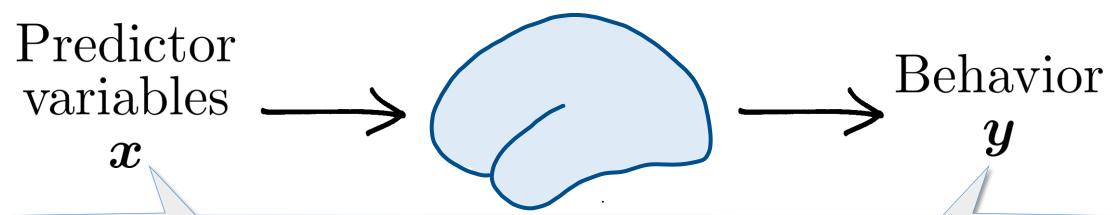
Modelling does **not** spare looking for an experimental paradigm where models generate different *conceptual* predictions. Otherwise it is unlikely modelling can be of any help.

Modelling as **support** to standard analyses rather instead of standard analyses.

A good modelling won't save a bad paradigm!



## 3. Define your input and output variables



Called independent variable, regressors, covariates, explanatory variables ...:

- Stimuli
- Experimental conditions
- History of stimuli, choices, outcomes, ...
- Peripheral marker (SCR, ECG, pupil dilation, ...)
- Neural marker (alpha power, ROI activity,...)

- ...

able, target variable ...:

;



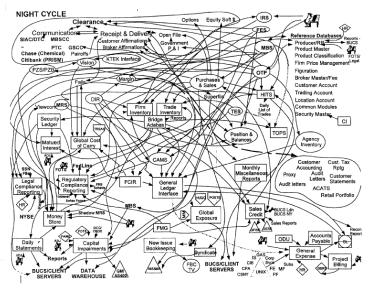
#### Selecting output variables

- The output variables should be sensitive to the process under study (sure)
- Include more than one variable if they offer complimentary views on the process under study (e.g choice & RT in speeded perceptual tasks)

#### input variables = variables of interest + control variables

#### Should I include this control variable?

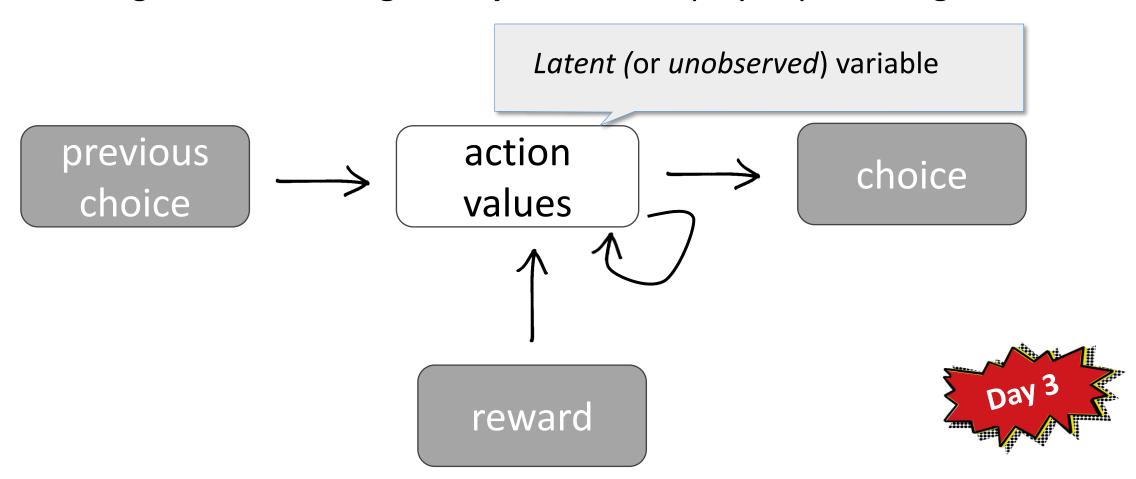
- <u>always</u> when the *control* variable is correlated with the variable of interest
  - -> regressing *out* the effect of control regressors



- If it is not correlated with the variable of interest, adding the control variable can have two opposite effects:
  - if it has a strong influence on behavior, more variance is explained so the parameter for the variable of interest will be more precisely evaluated
  - If the influence is weak and the number of trials is low, more regressors may lead to *overfitting*, so poorer estimation

## 4. Define your model as a box diagram

The diagram isolates cognitive processes at play in producing behavior



#### 5. Convert the diagram into a statistical model

- We need to formalize our model by moving from a conceptual description to a computational level
- Formalization allows:
  - *Model estimation*: compare *parameters* in different conditions, populations; infer *latent variable* to look for their neural substrate (e.g. model-based fMRI)
  - *Model validation and comparison*: can one model account for subject behavior? Better than others?
  - *Model predictions*: formalization allows to make specific predictions (both qualitative and quantitative) that often are difficult to formulate directly from a conceptual description.



#### A statistical description of behavior

$$p(m{y}|m{x}) = f_{\mathcal{M}}(m{y}; m{x}, m{ heta})$$
Parameters (properties of neural system), e.g. learning rate, sensitivity to motion, etc.

previous action values choice reward

Turning arrows into (deterministic/stochastic) equations

action values:

$$V_k^{(t+1)} = V_k^{(t)} + \lambda (reward - V_k^{(t)})$$

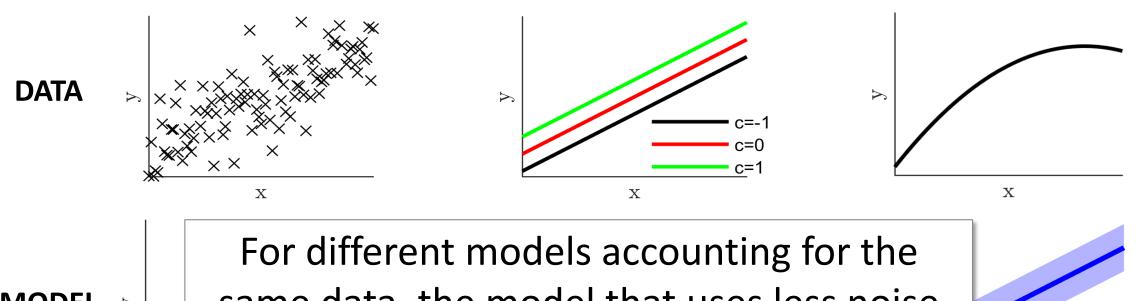
choice:

$$p(choice = k) = e^{V_k^{(t)}} / \sum_{l} e^{V_l^{(t)}}$$

## What's that noise (in the model)?

'Noise' = all that cannot be accounted for by the deterministic part of the model:

- Neural noise: low level variability in neural circuits / behavior (sensory, decision, motor...)
- Factors not taken into account in the model (fluctuation in response bias, attention ...)
- **Model imperfections**: any systematic bias between the model predicted response and subject behavior that the model cannot accomodate



MODEL

For different models accounting for the same data, the model that uses less noise explains the most structure in the data



 $\mathbf{X}$ 

#### On the importance of simulating your model



<u>Before</u> fitting your model to data, simulate it (with various parameter sets) to **develop intuitions** about its behavior and understand how it is affected by the choice of parameters.

#### Preparing for tutorial part 1

- Standard 2AFC motion discrimination task (left vs right)
- Stimulus evidence is varied across 9 levels
- In half of trials, brain area X is experimentally deactivated
- A reduction in performance is observed in those trials

Is it due to deteriorated sensory processing or to sensory-unrelated effects (lapses)?



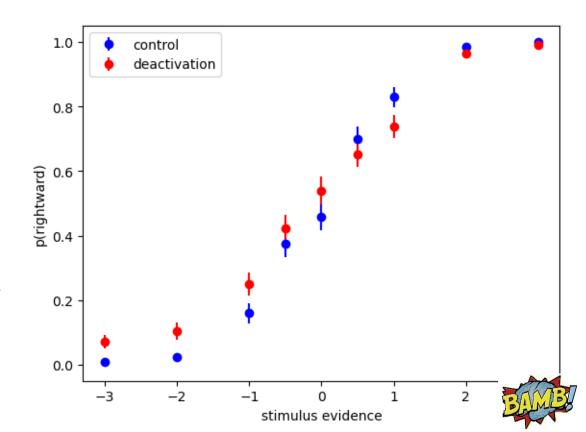
#### Defining the models

#### 1. Scientific question:

"Does deactivating brain area X deteriorate sensory processing or provoke sensory-unrelated effects (lapses)?" -> Two models

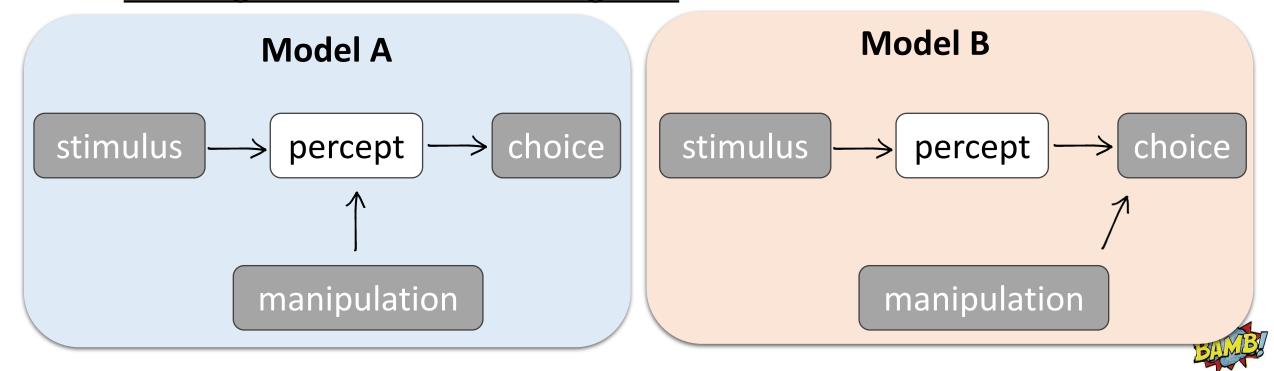
#### 2. Modelling objectives:

- which of two models representing each hypothesis better accounts for the data? (relative criterion)
- does the favored model reproduces the change in the psychometric curve during deactivation? (absolute criterion)



## Defining the models (cont'd)

- 3. Defining input and output variables:
  - output variable: choice (binary)
  - input variables: stimulus evidence, manipulation (+control variables?)
- 4. Defining the models as box diagrams:

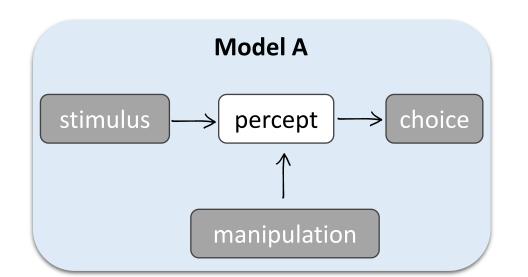


## Defining the models (cont'd)

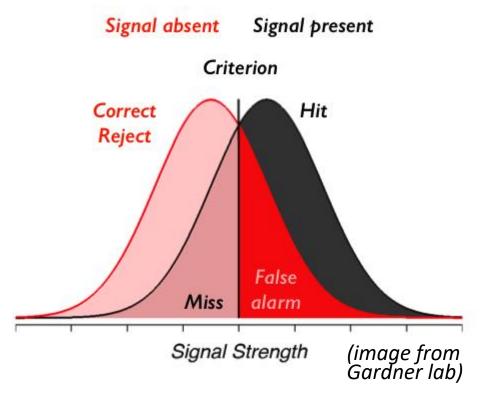
#### 5. Convert model A to statistical model:

percept: 
$$\hat{s} = s + \epsilon$$

 $\epsilon$  sensory noise drawn from zero-mean Gaussian, variance  $\sigma_d^2$  in deactivation trials,  $\sigma_m^2$  in control trials choice: Right if  $\hat{s}>0$ , Left otherwise



#### Signal detection theory





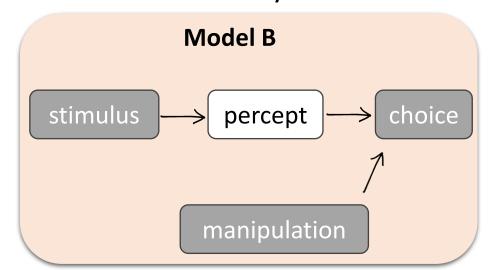
## Defining the models (cont'd)

#### 5. Convert model B to statistical model:

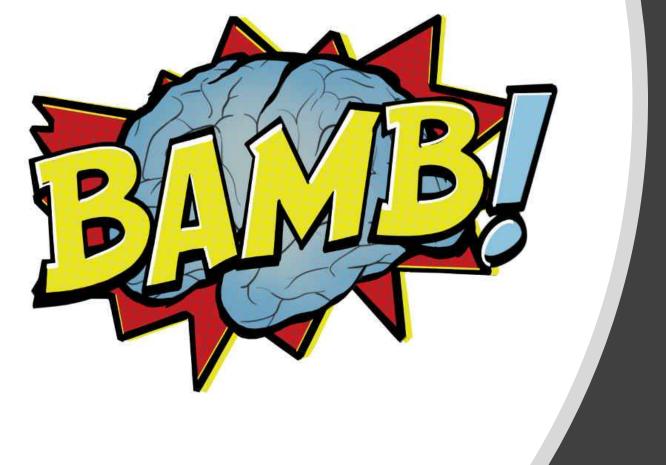
percept:  $\hat{s} = s + \epsilon$ 

 $m{\epsilon}$  sensory noise drawn from zero-mean Gaussian, variance  $\sigma_d^2$  in all trials

choice: Right if  $\hat{s} > 0$ , Left otherwise (with probability 1- $\lambda$ ) randomly chosen between Right and Left (with probability  $\lambda$ )







# Part II Fitting your model to data

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#### Parameter estimation (aka inference)

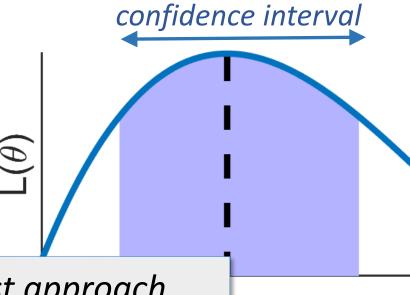
Inference: 
$$(oldsymbol{X}, oldsymbol{Y}) = \{(oldsymbol{x}_1, oldsymbol{y}_1), ..., (oldsymbol{x}_n, oldsymbol{y}_n)\} \longrightarrow$$

We want the parameters with better match between *model* behavior and *observed* behavior.

-> Optimize measure of how plausible would the experimental data be if the model were to be true, i.e. maximize **likelihood**:

$$L(\boldsymbol{\theta}) = p(\boldsymbol{Y}|\boldsymbol{X}, \boldsymbol{\theta})$$

That's the frequentist approach



#### Maximum likelihood estimation

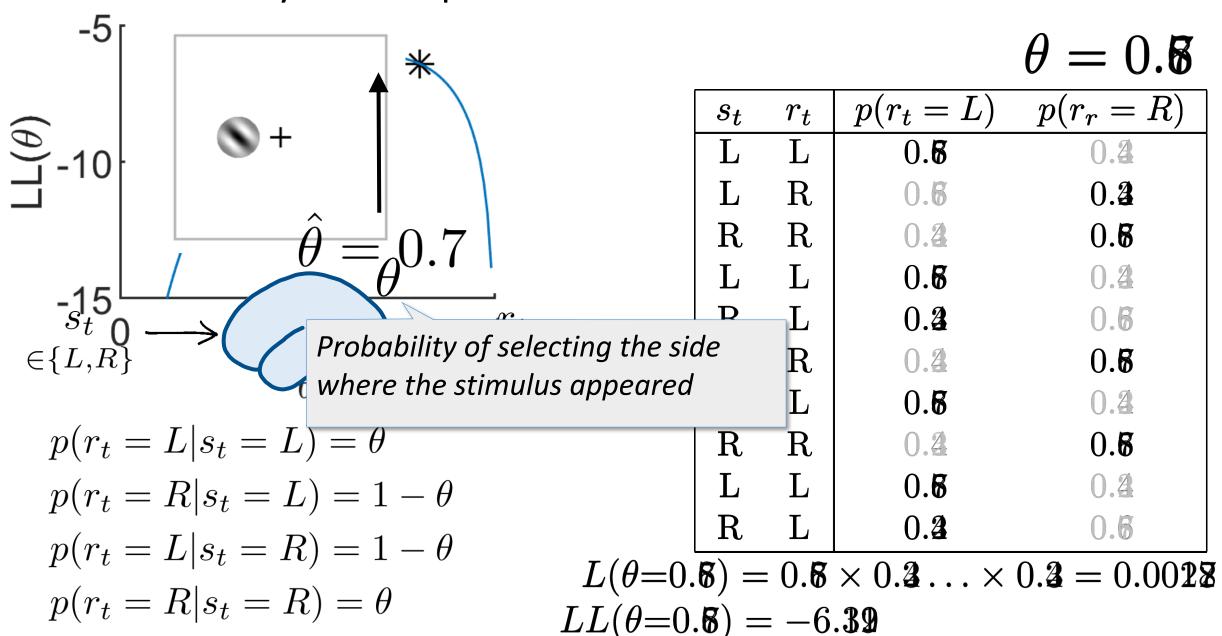
$$\hat{\boldsymbol{\theta}}_{ML} = arg \max_{\boldsymbol{\theta}} L(\boldsymbol{\theta})$$
 | log-likelihood (LLH)   
 $\hat{\boldsymbol{\theta}}_{ML} = arg \max_{\boldsymbol{\theta}} \log L(\boldsymbol{\theta}) = arg \max_{\boldsymbol{\theta}} LL(\boldsymbol{\theta})$ 

If behavior is independent across trials, LLH turns into sum of terms:

$$L(m{ heta}) = p(m{Y}|m{X}, m{ heta})$$
 The sum is more practical to deal with for analytical and numerical reasons 
$$LL(m{ heta}) = \log p(m{y}_1|m{x}_1, m{ heta}) + ... + \log p(m{y}_n|m{x}_n, m{ heta}) \\ = \log f_{\mathcal{M}}(m{y}_1; m{x}_1, m{ heta}) + ... + \log f_{\mathcal{M}}(m{y}_n; m{x}_n, m{ heta})$$



#### Toy example: 2 AFC detection task



#### References

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