

Bayesian modeling... and how to use brain data to arbitrate between models of cognition

Valentin Wyart

LNC² / Inserm & Ecole Normale Supérieure
Université PSL, Paris, France

valentin.wyart@ens.fr

What is Bayesian modeling?

Bayesian modeling can mean two things:

Meaning **A**:

Bayes rule as model of cognition under uncertainty

or

Meaning **B**:

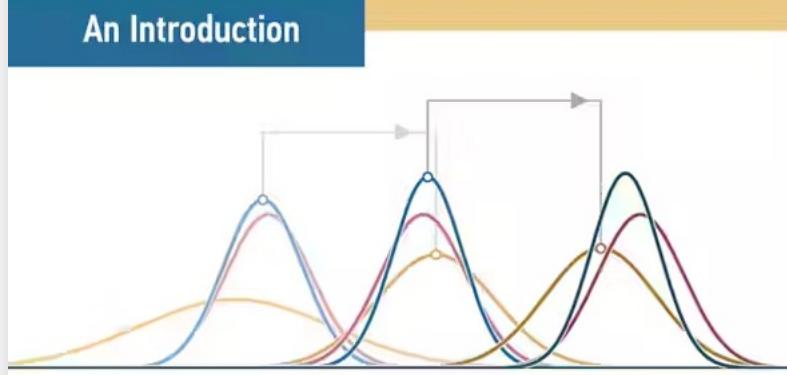
Bayesian inference as machine learning framework
for the fitting of cognitive models and the estimation
of their free parameters

Today I will mean **A**!

What is Bayesian modeling?

Bayesian Models of Perception and Action

An Introduction



The diagram shows three overlapping bell-shaped curves on a horizontal axis. A blue curve is labeled 'Posterior' with a blue dot at its peak. A red curve is labeled 'Likelihood' with a red dot at its peak. An orange curve is labeled 'Prior' with an orange dot at its peak. Arrows point from the labels to their respective curves. The curves are colored blue, red, and orange.

Wei Ji Ma
Konrad Paul Kording
Daniel Goldreich

Bayes rule:

$$\frac{p(\text{hyp}|\text{obs})}{\text{Posterior}} \propto \frac{p(\text{obs}|\text{hyp})}{\text{Likelihood}} \cdot \frac{p(\text{hyp})}{\text{Prior}}$$

What is Bayesian modeling?

Most of the decisions that matter are uncertain.

perceptual



eat strange fruit?

hyp
fruit is edible

financial



buy new crypto?

hyp
crypto will rise

political



vote Macron?

hyp
???

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**stomach
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**savings
gone**

hyp
???

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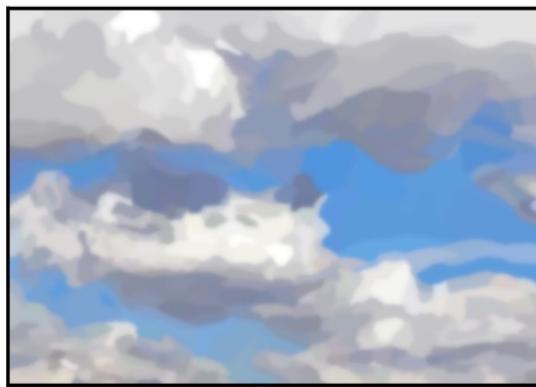
vote Macron?

**stomach
pain**

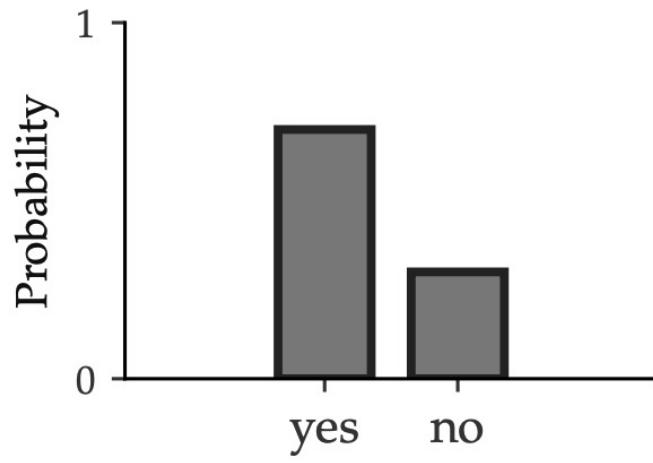
**savings
gone**

**big piles
of trash**

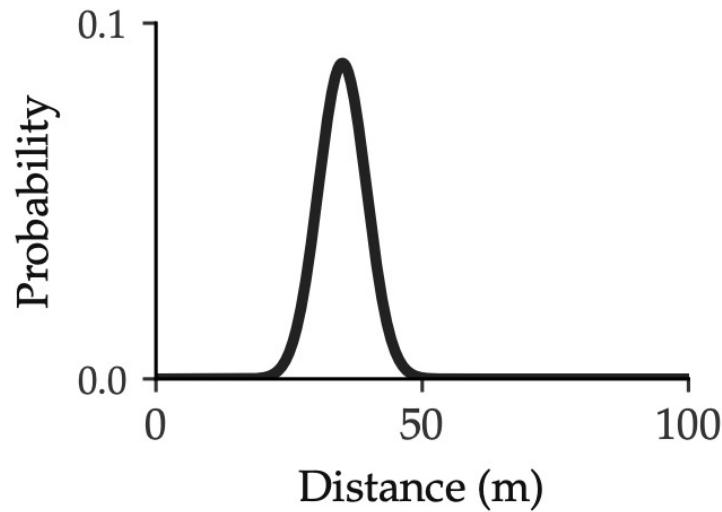
What is Bayesian modeling?



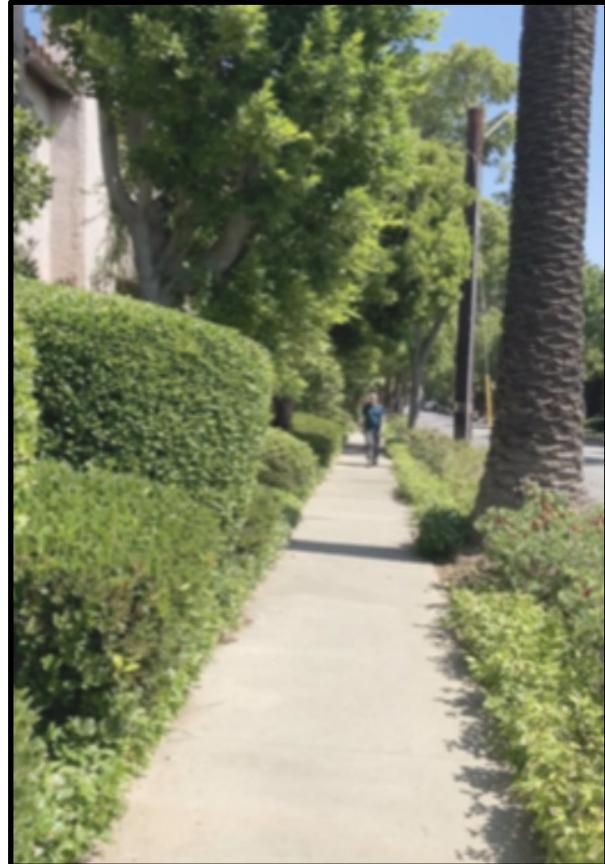
$p(\text{it is going to rain} \mid \text{cloudy sky})$



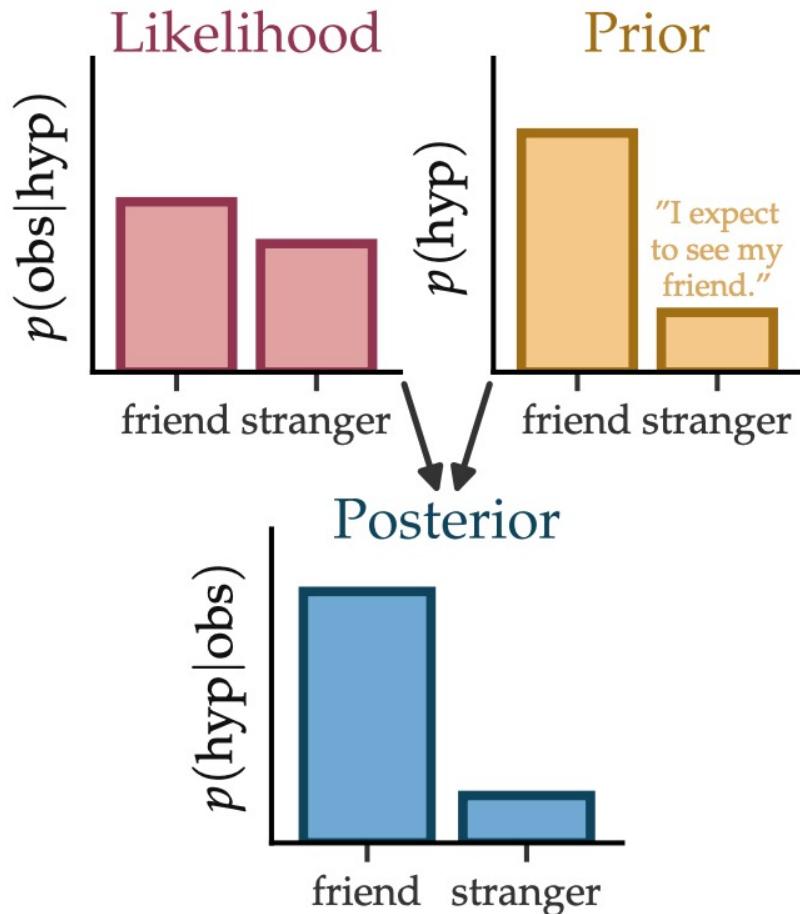
$p(\text{distance to car} \mid \text{visual image})$



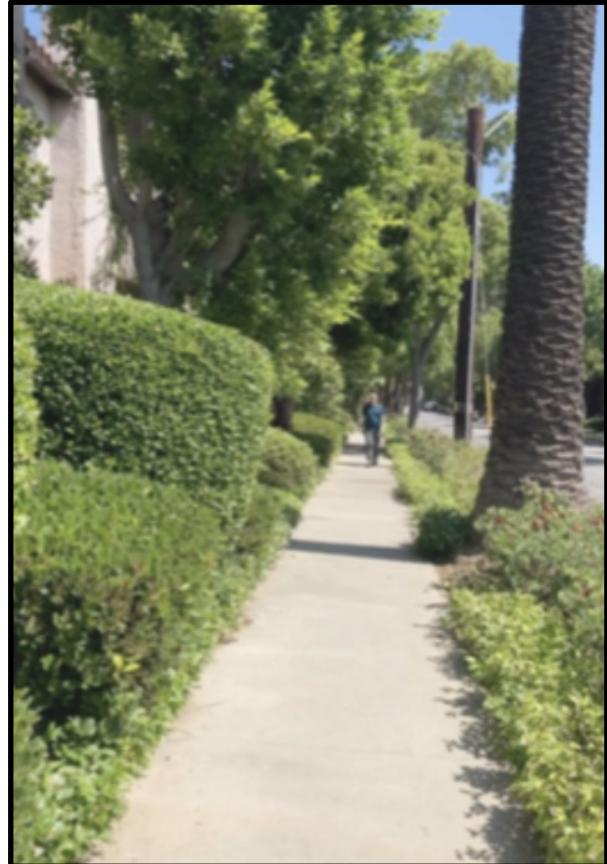
What is Bayesian modeling?



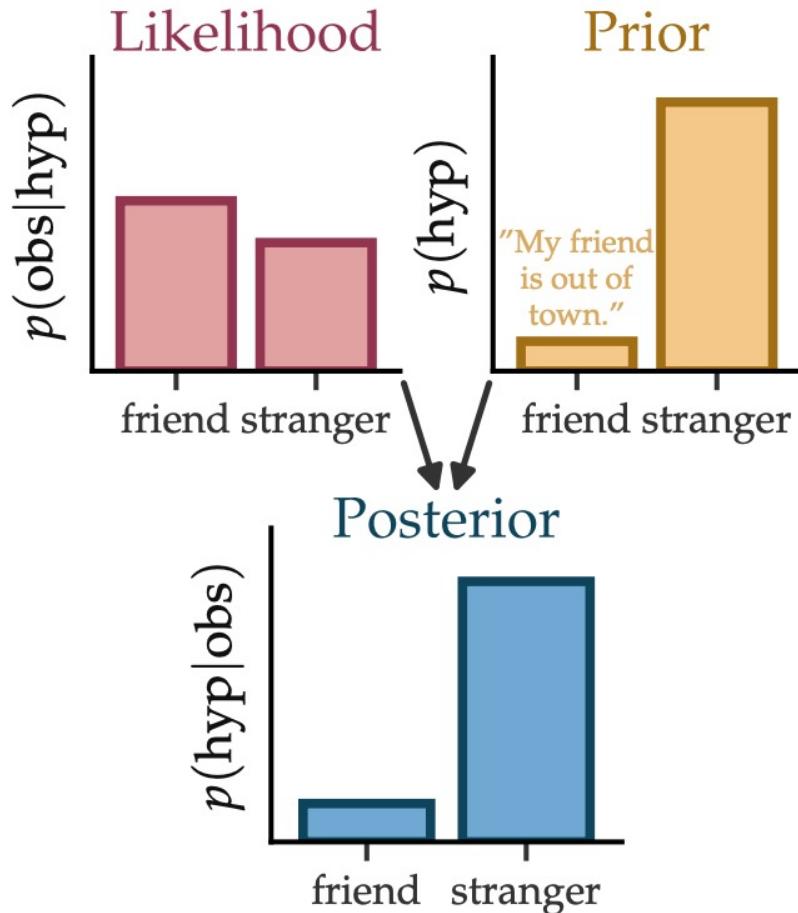
$p(\text{this is my friend})$



What is Bayesian modeling?



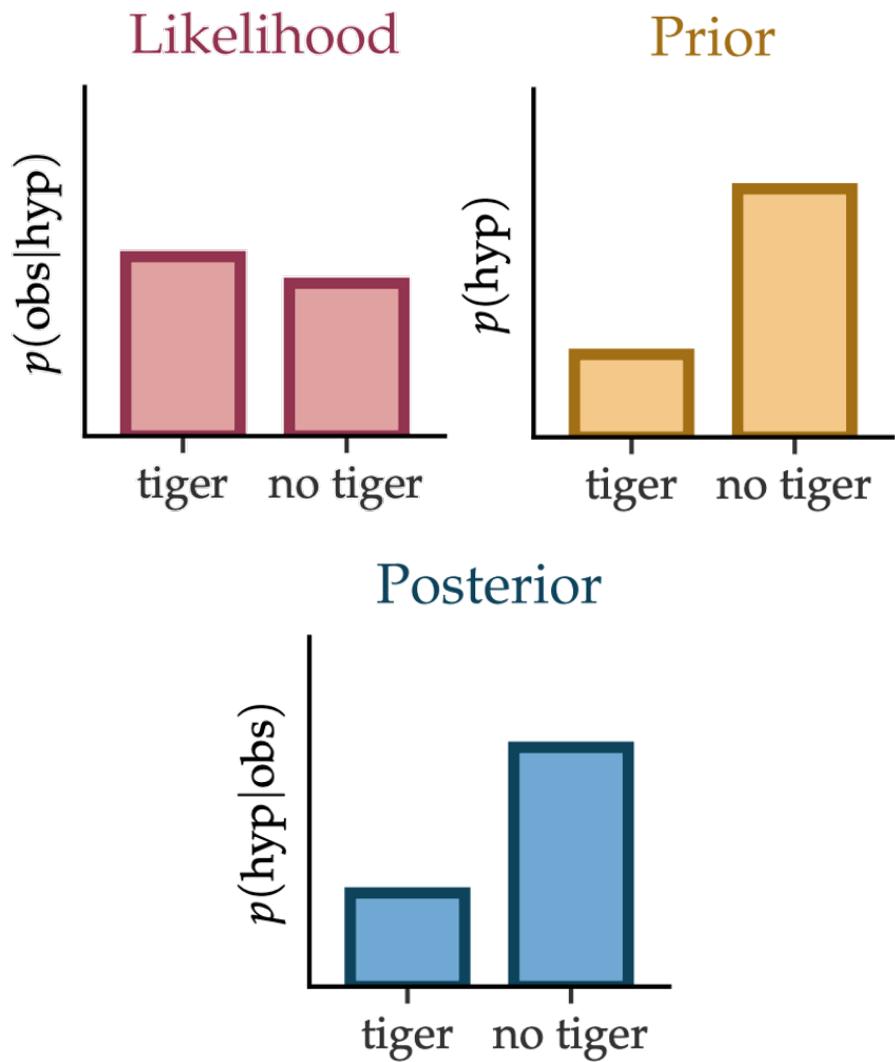
$p(\text{this is my friend})$



What is Bayesian modeling?



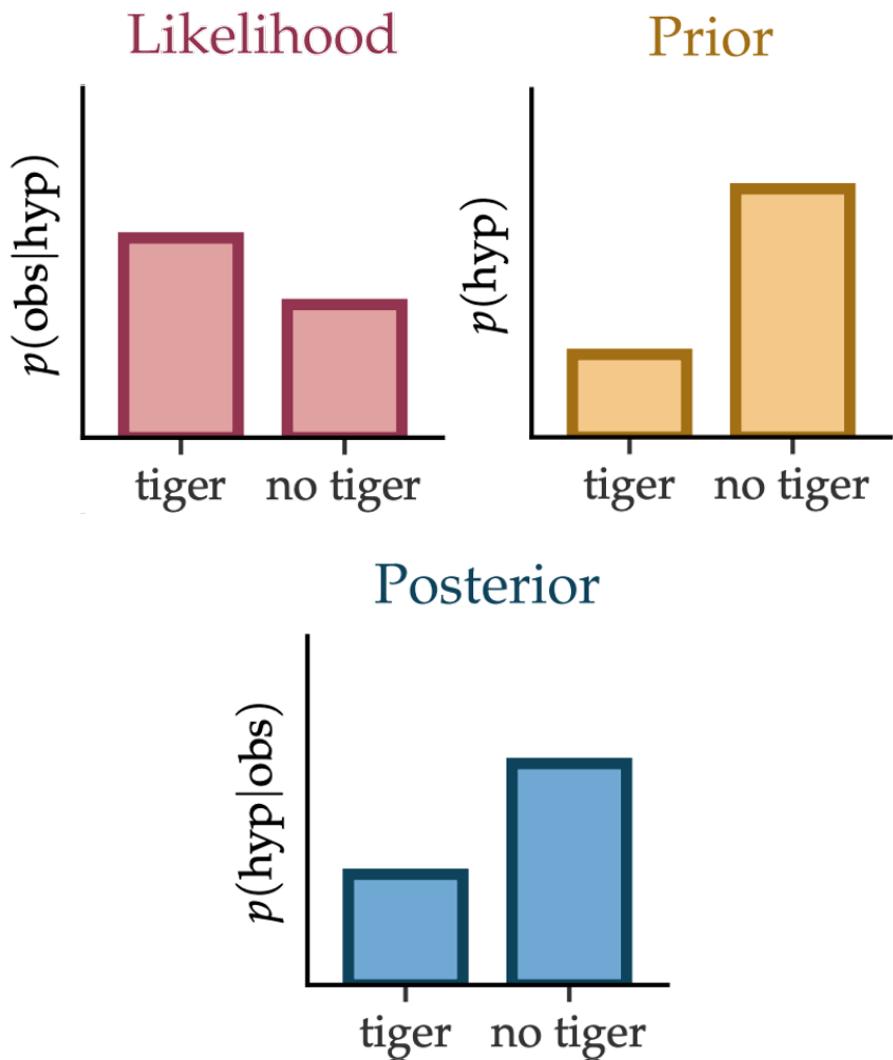
$p(\text{tiger in the bush})$



What is Bayesian modeling?



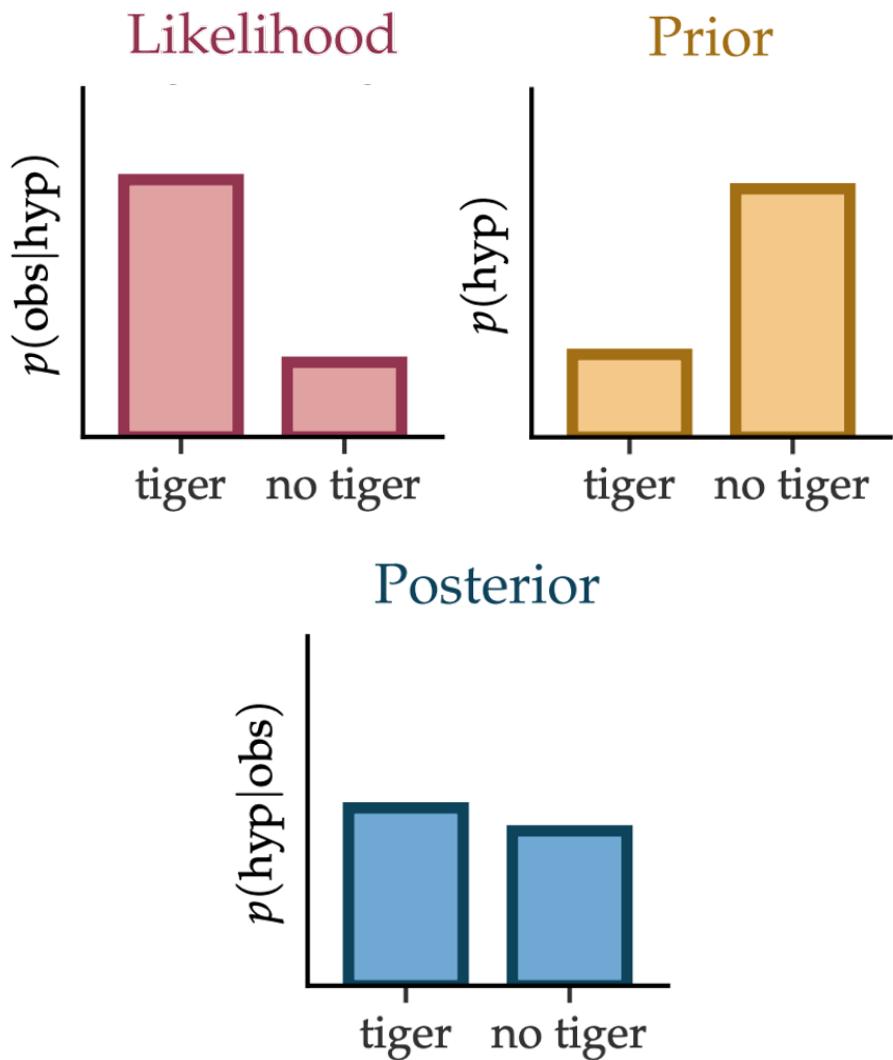
$p(\text{tiger in the bush})$



What is Bayesian modeling?

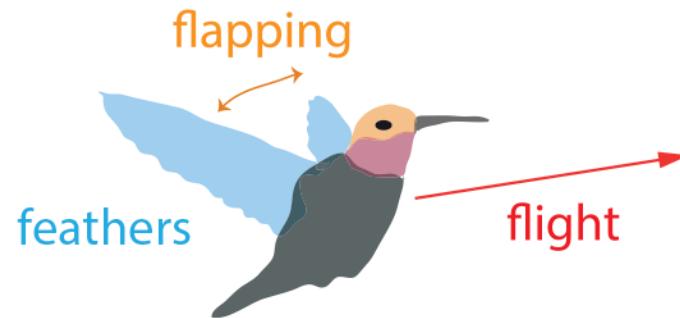
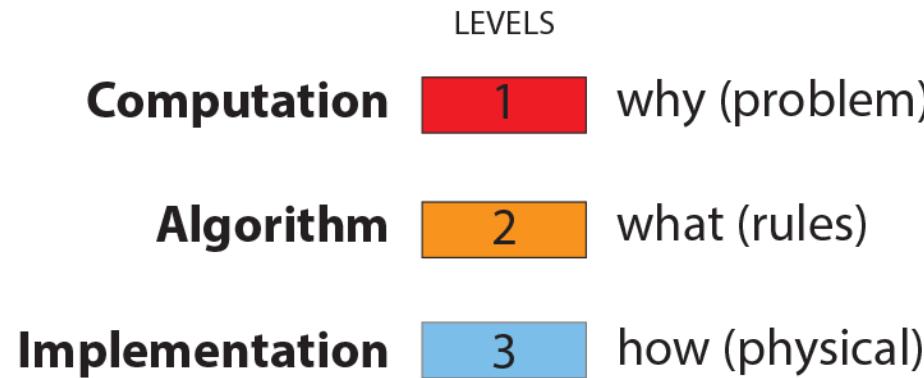


$p(\text{tiger in the bush})$



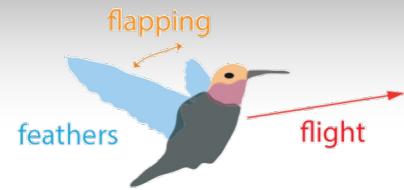
Flavors of Bayesian modeling

Marr's multi-level analysis of cognition



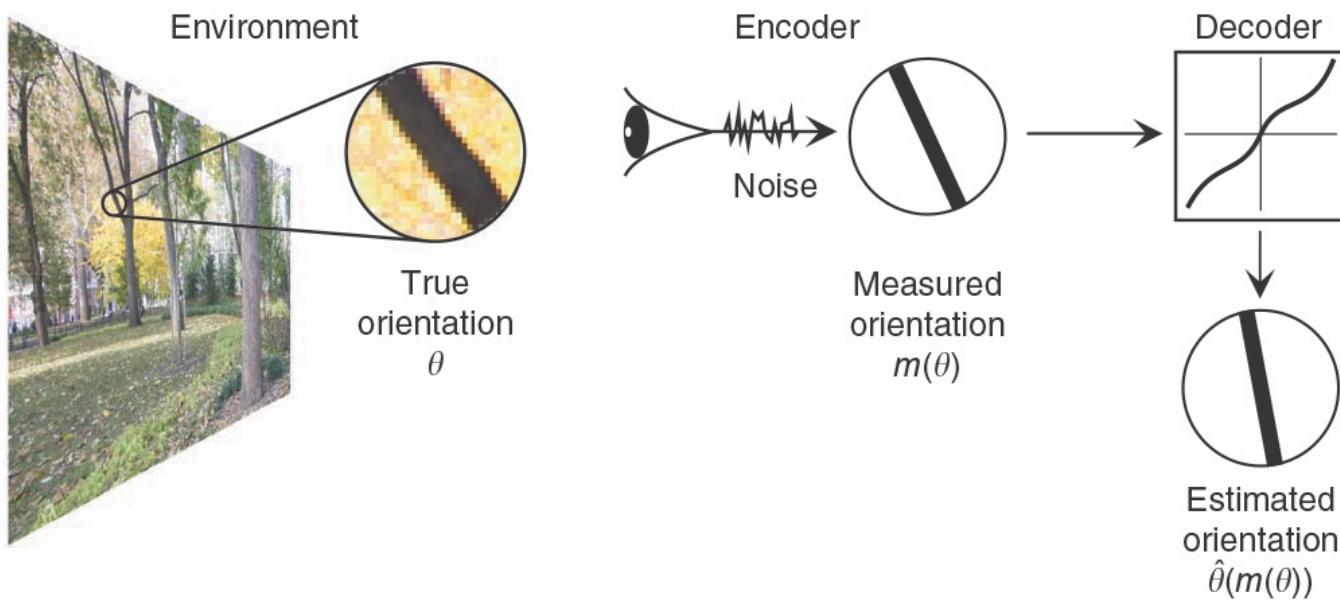
Krakauer et al. (2016) *Neuron*

Neuroscience needs behavior: correcting a reductionist bias



Bayesian models as statistical computations

They define the (Bayes-)optimal solution to dealing with probabilistic uncertainty

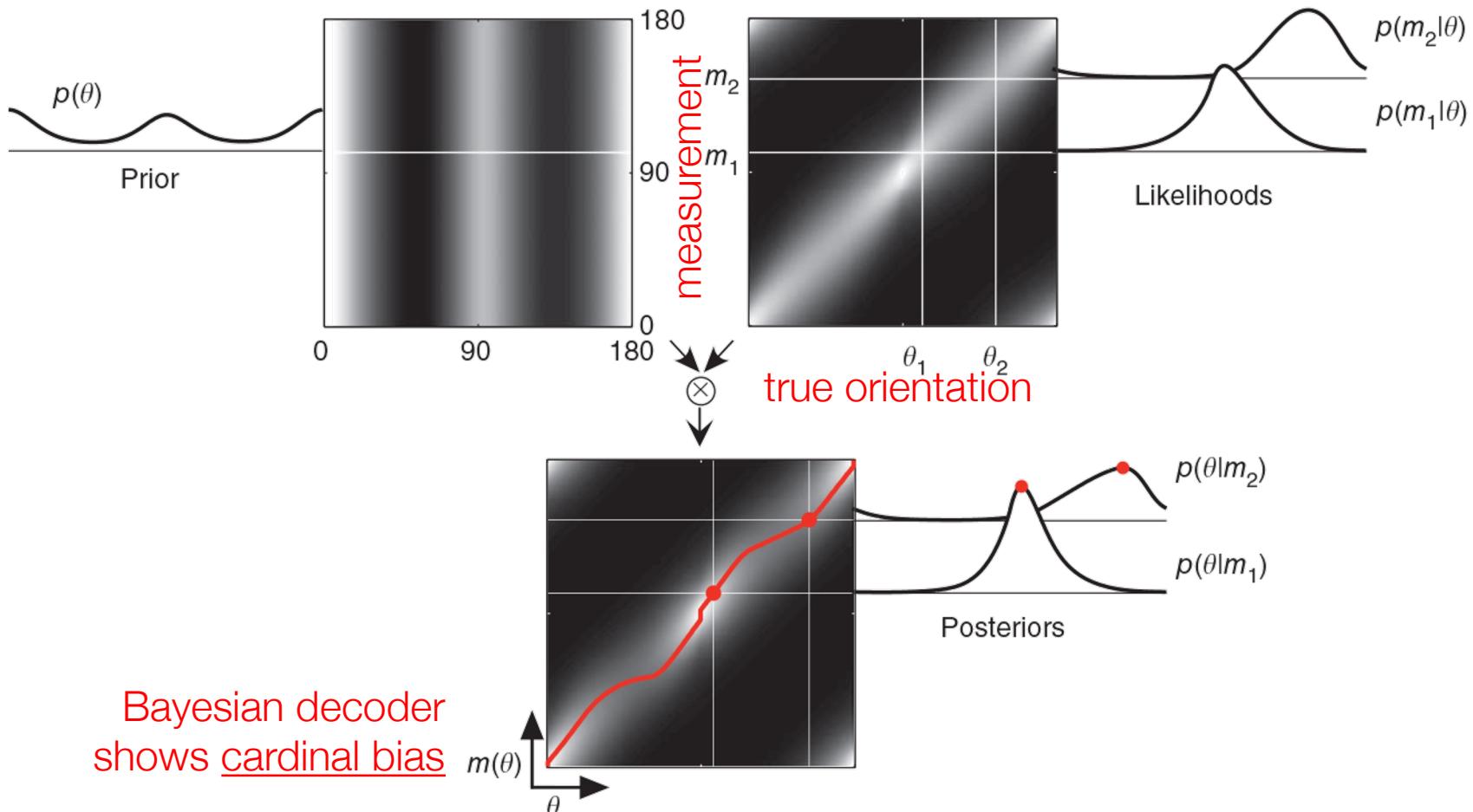
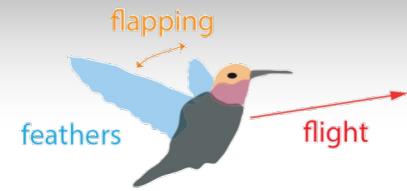


Girshick et al. (2011) *Nature Neuroscience*

Cardinal rules: orientation perception reflects knowledge of environmental statistics

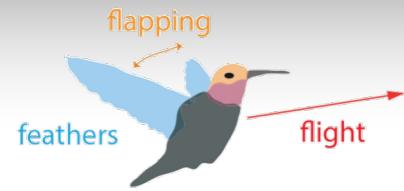
Bayesian models as statistical computations

1

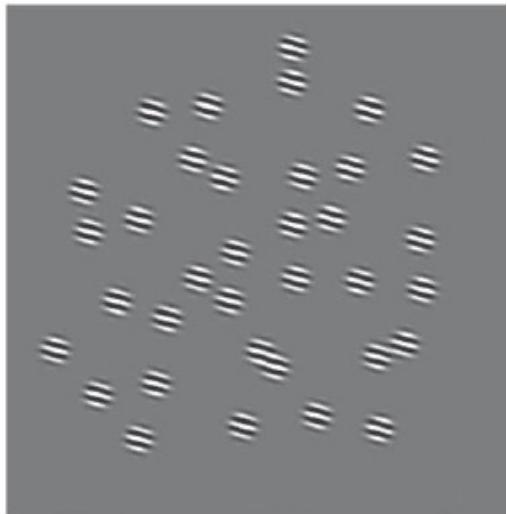


Girshick et al. (2011) *Nature Neuroscience*

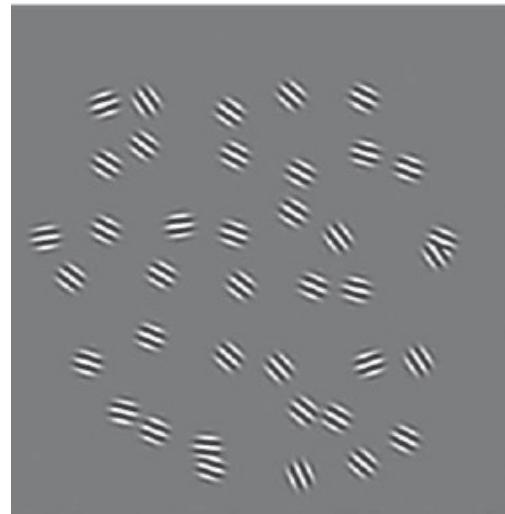
Cardinal rules: orientation perception reflects knowledge of environmental statistics



low-noise stimulus



high-noise stimulus



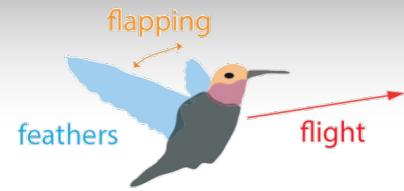
Is the right stimulus tilted counter-clockwise or clockwise relative to the left stimulus?

Girshick et al. (2011) *Nature Neuroscience*

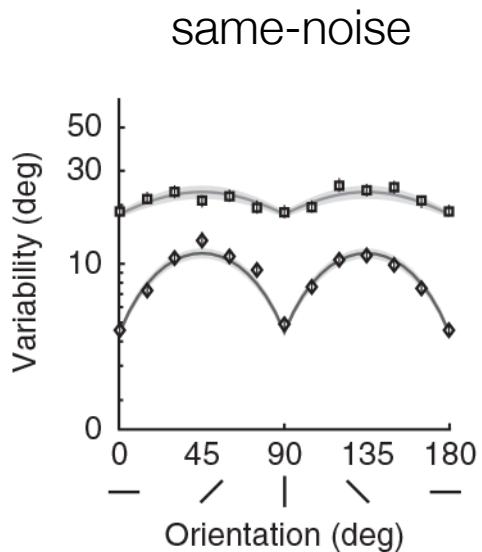
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Bayesian models as statistical computations

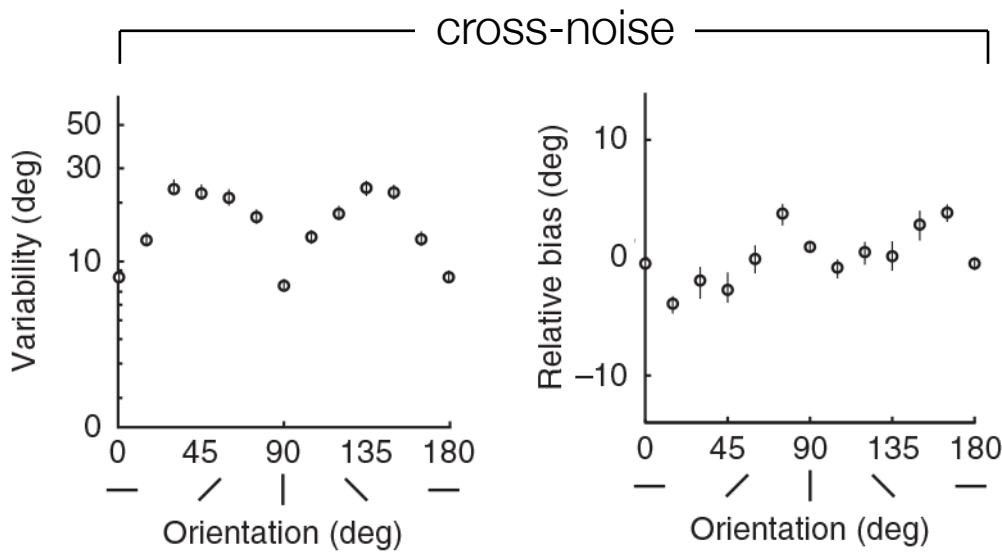
1



measure variability
in orientation perception

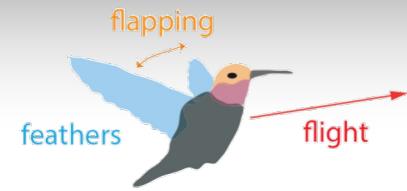


measure prior
distribution

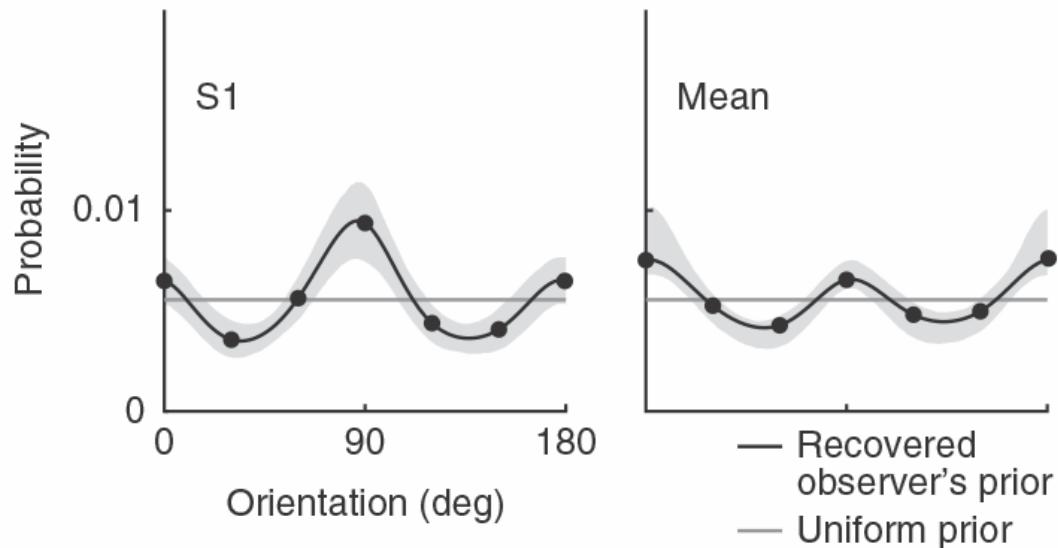


Girshick et al. (2011) *Nature Neuroscience*

Cardinal rules: orientation perception reflects knowledge of environmental statistics



estimated prior distribution
from subject data

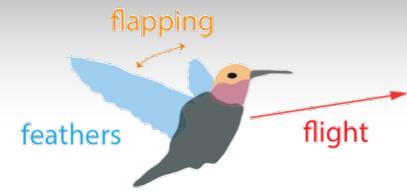


Girshick et al. (2011) *Nature Neuroscience*

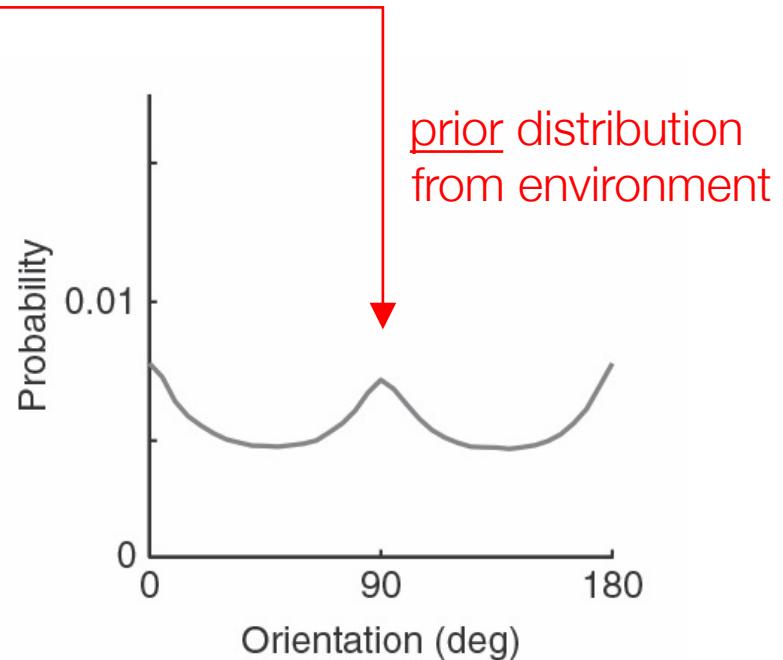
Cardinal rules: orientation perception reflects knowledge of environmental statistics

Bayesian models as statistical computations

1



natural image database
oriented edge detection

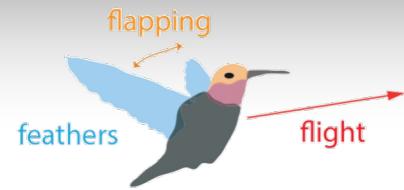


Girshick et al. (2011) *Nature Neuroscience*

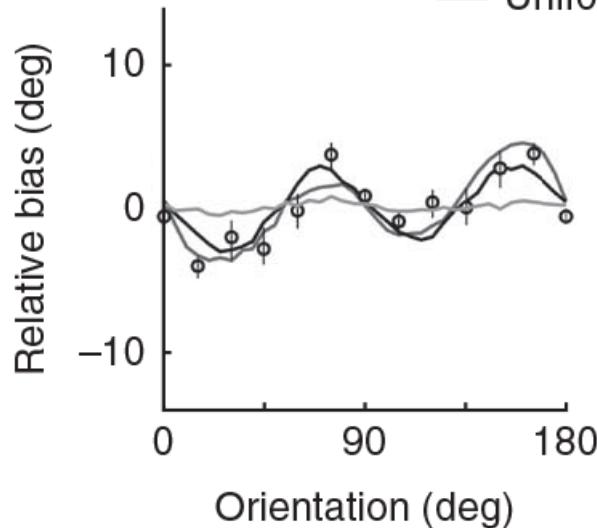
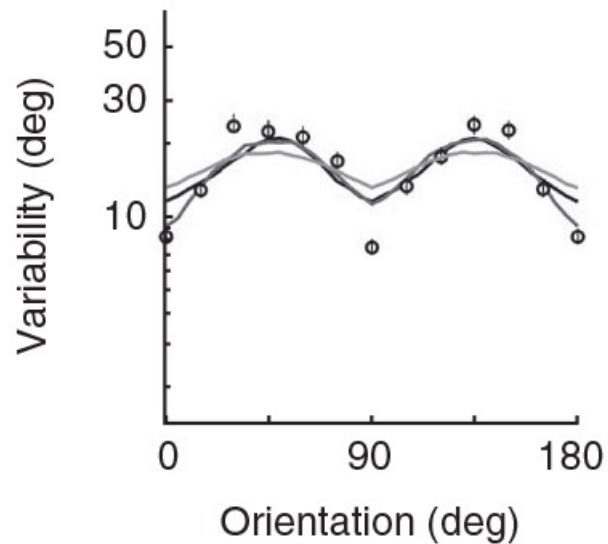
Cardinal rules: orientation perception reflects knowledge of environmental statistics

Bayesian models as statistical computations

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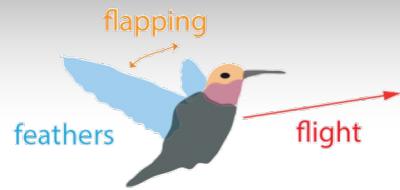


compare human bias to
Bayesian decoder bias
(model predictions)



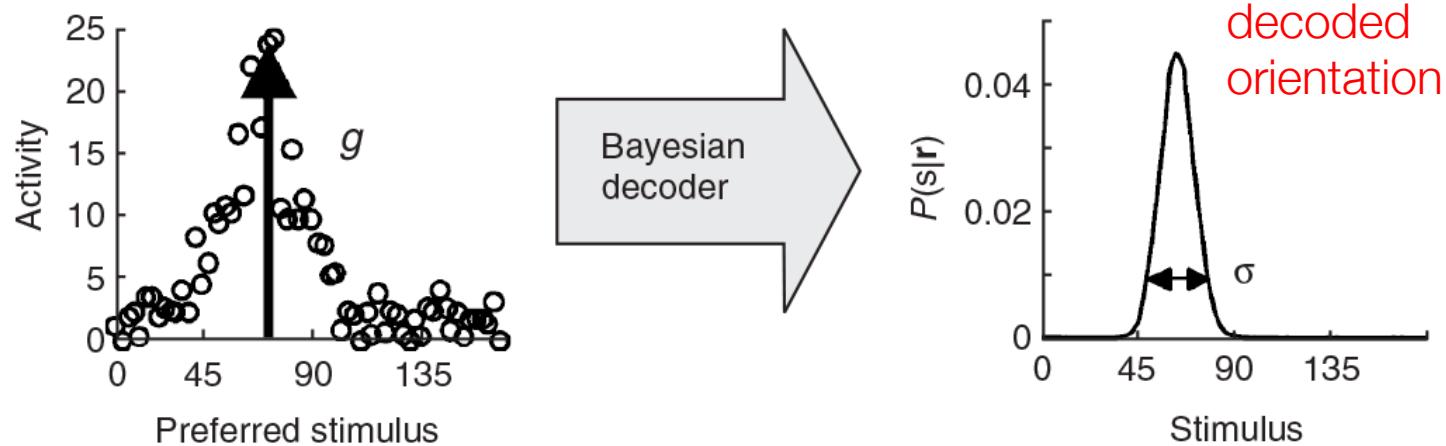
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Cardinal rules: orientation perception reflects knowledge of environmental statistics



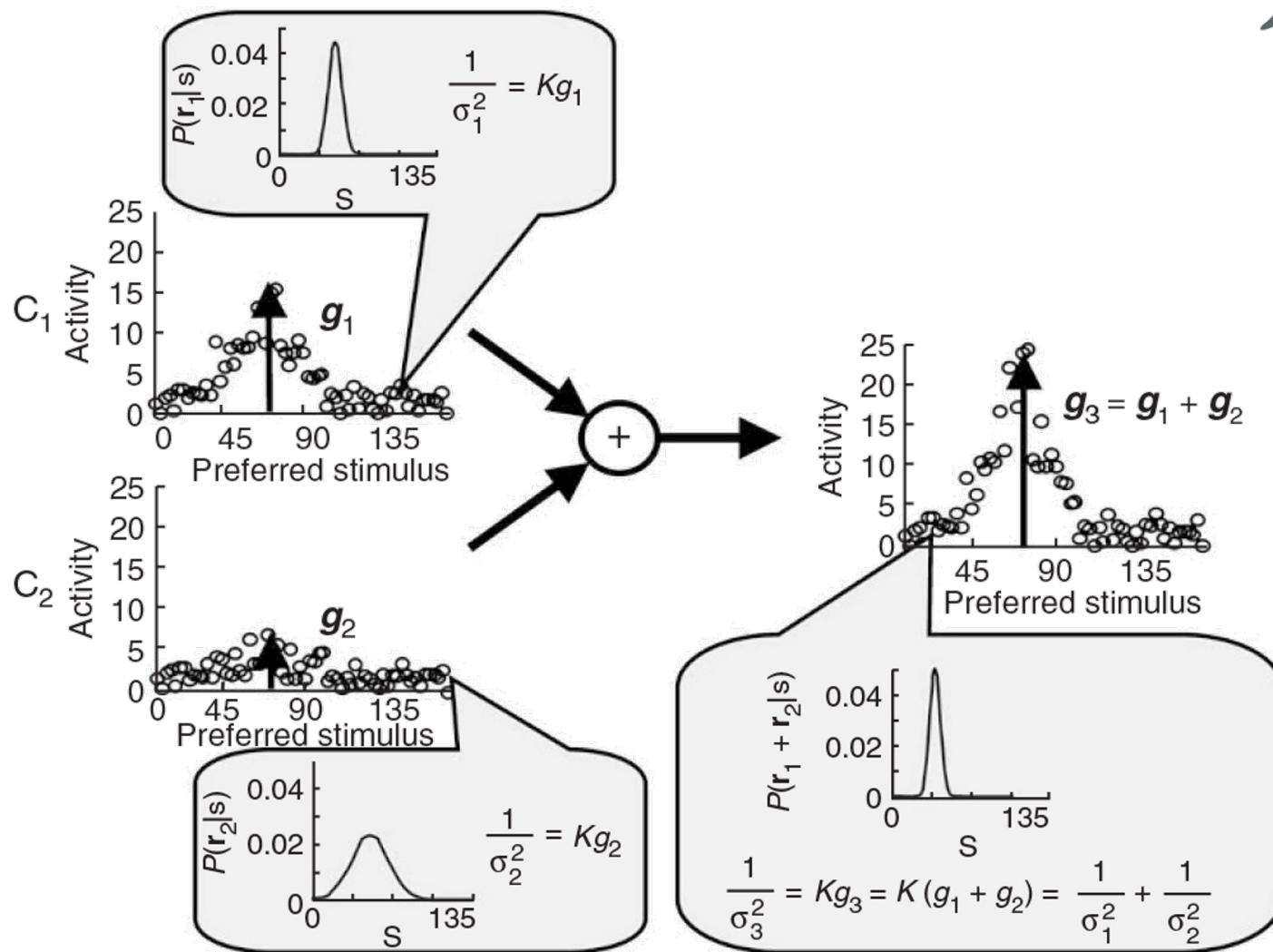
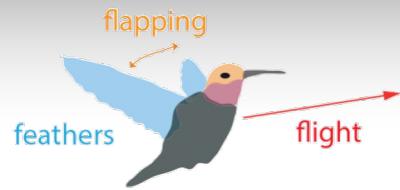
Bayesian models as neural mechanisms

They define possible physical implementations of Bayesian inference by populations of neurons



Bayesian models as neural mechanisms

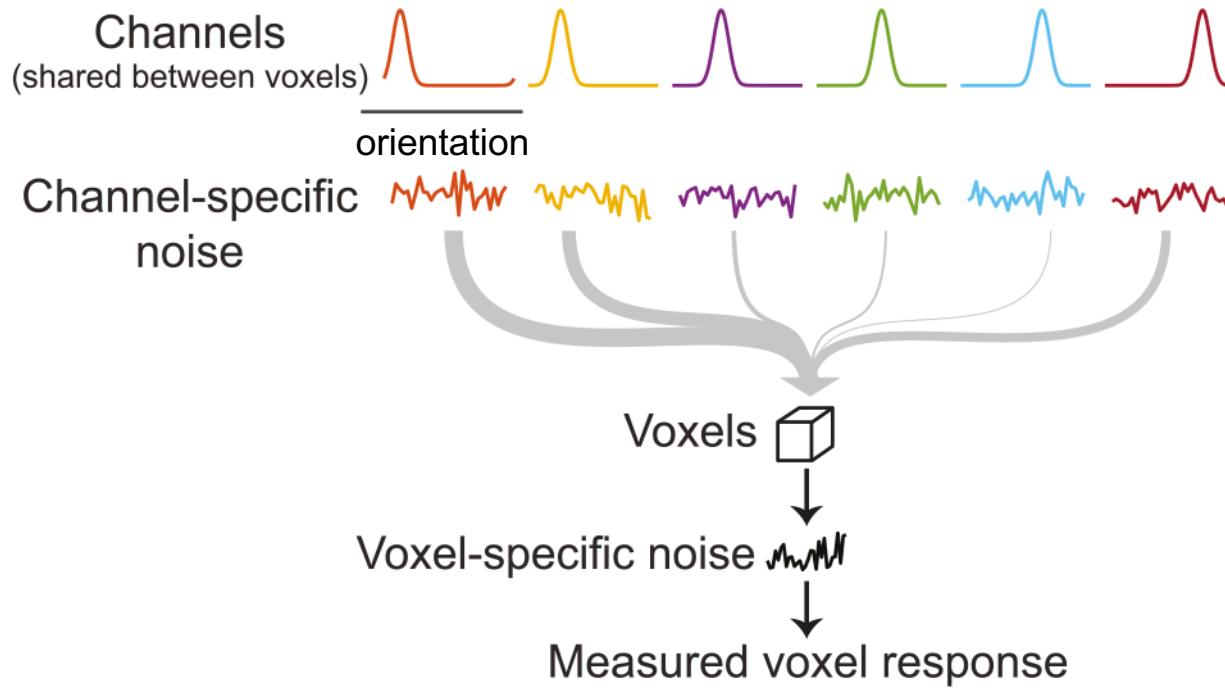
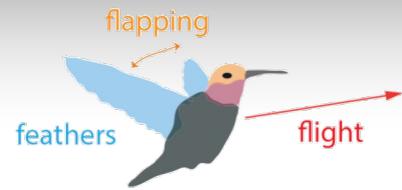
3



Ma et al. (2006) *Nature Neuroscience*
Bayesian inference with probabilistic population codes

Bayesian models as neural mechanisms

3

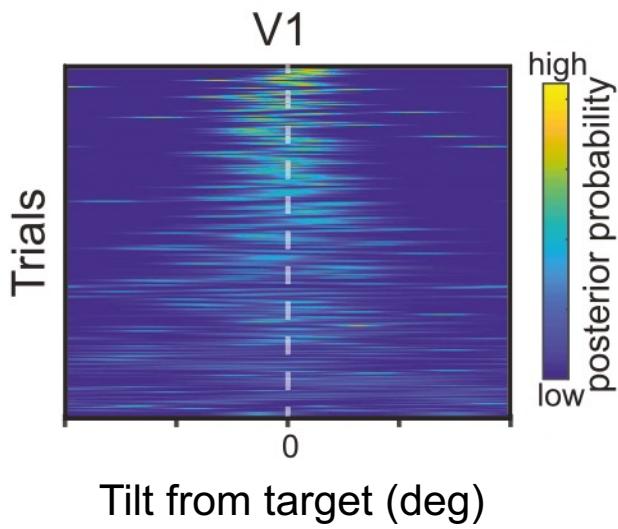
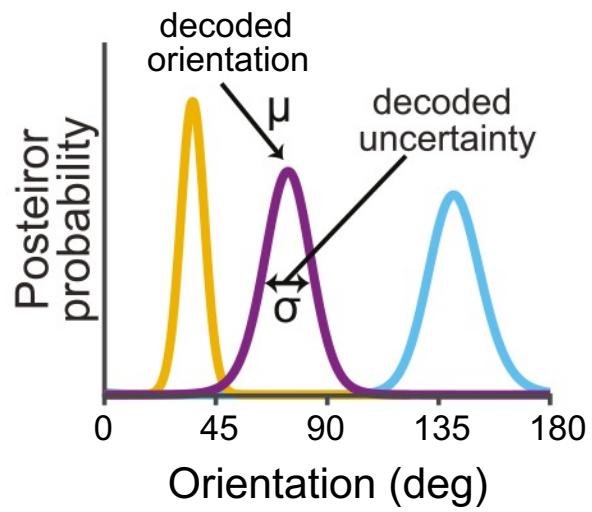
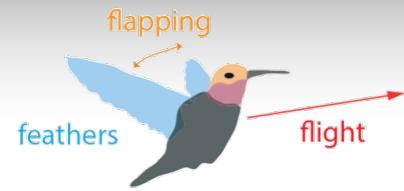


Geurts et al. (2022) *Nature Human Behaviour*

Subjective confidence reflects representation of Bayesian probability in cortex

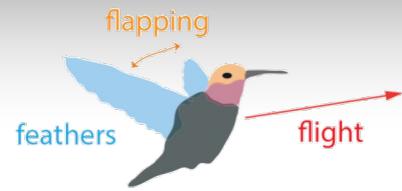
Bayesian models as neural mechanisms

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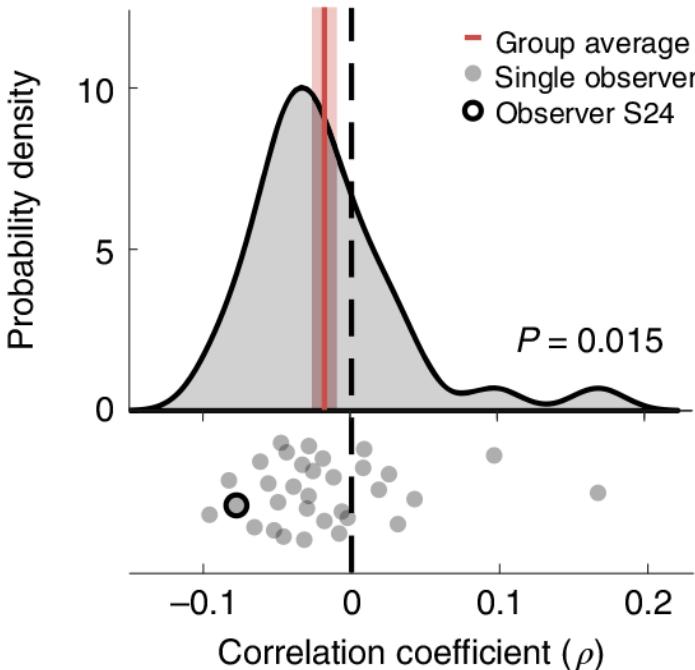
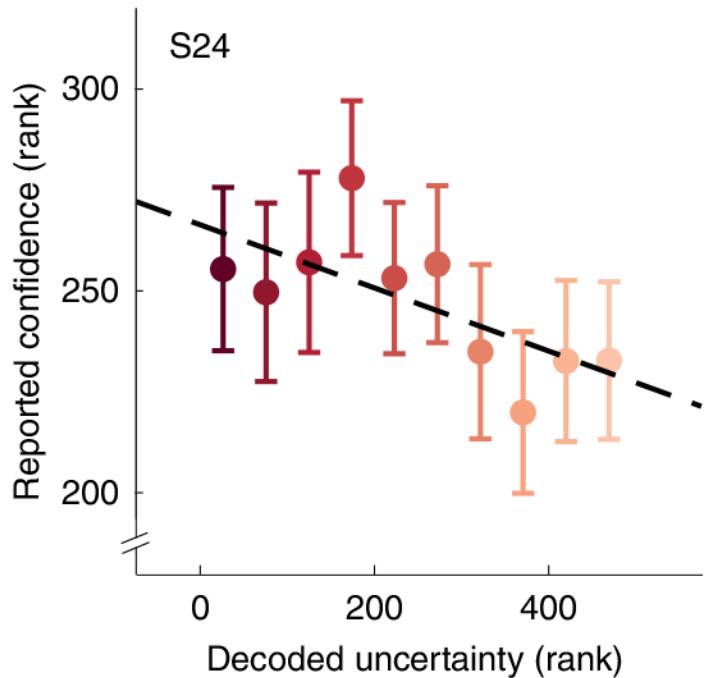


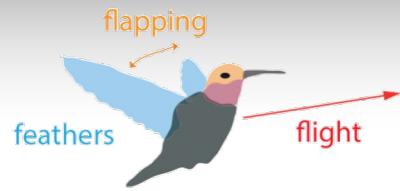
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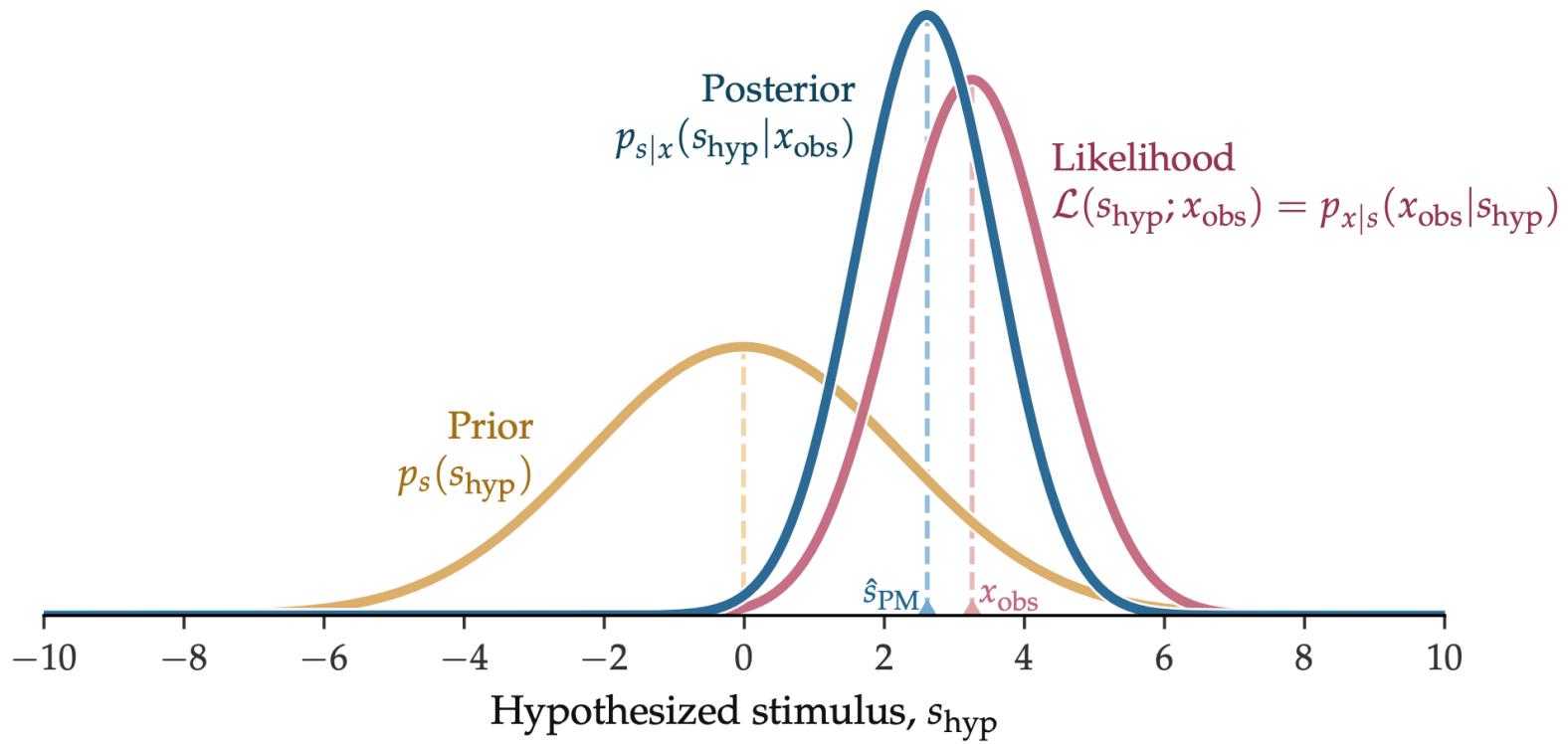
negative relation between Bayesian uncertainty and reported confidence





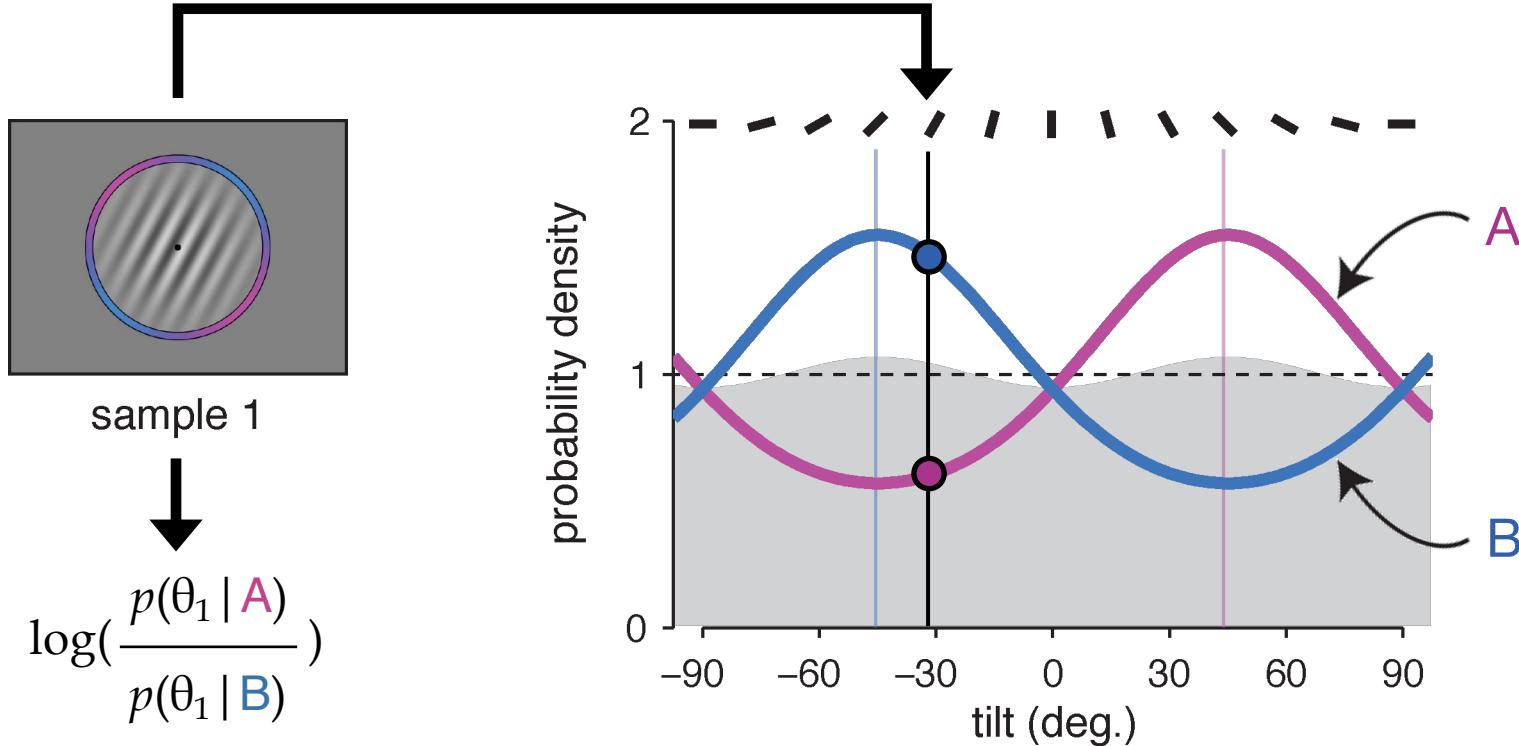
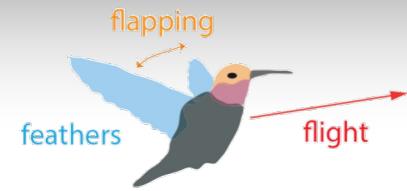
Bayesian models as cognitive algorithms

They define update rules for combining uncertain prior knowledge with uncertain evidence



Bayesian models as cognitive algorithms

2

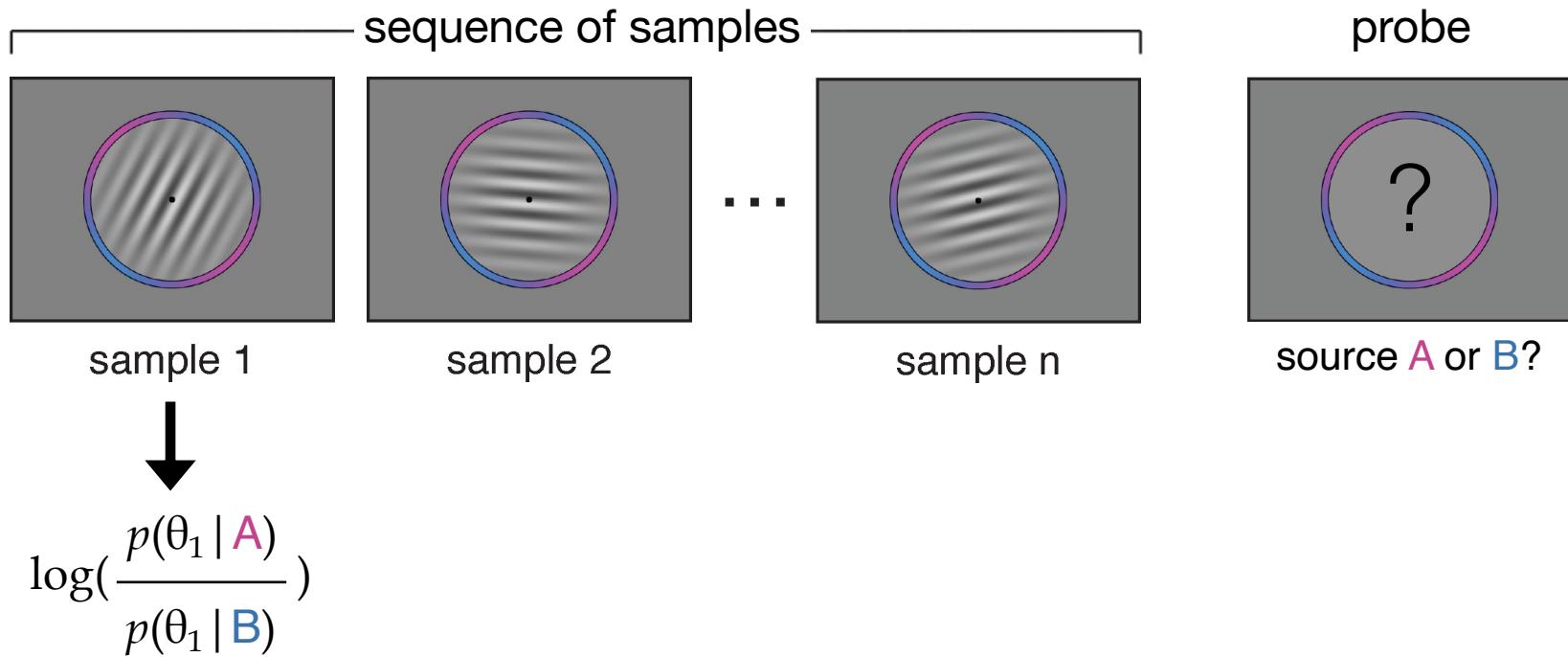
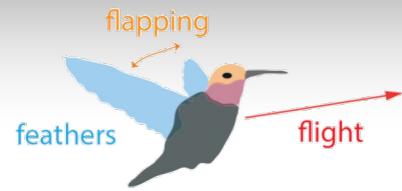


Drugowitsch, Wyart et al. (2016) *Neuron*

Computational precision of inference as critical source of human choice suboptimality

Bayesian models as cognitive algorithms

2

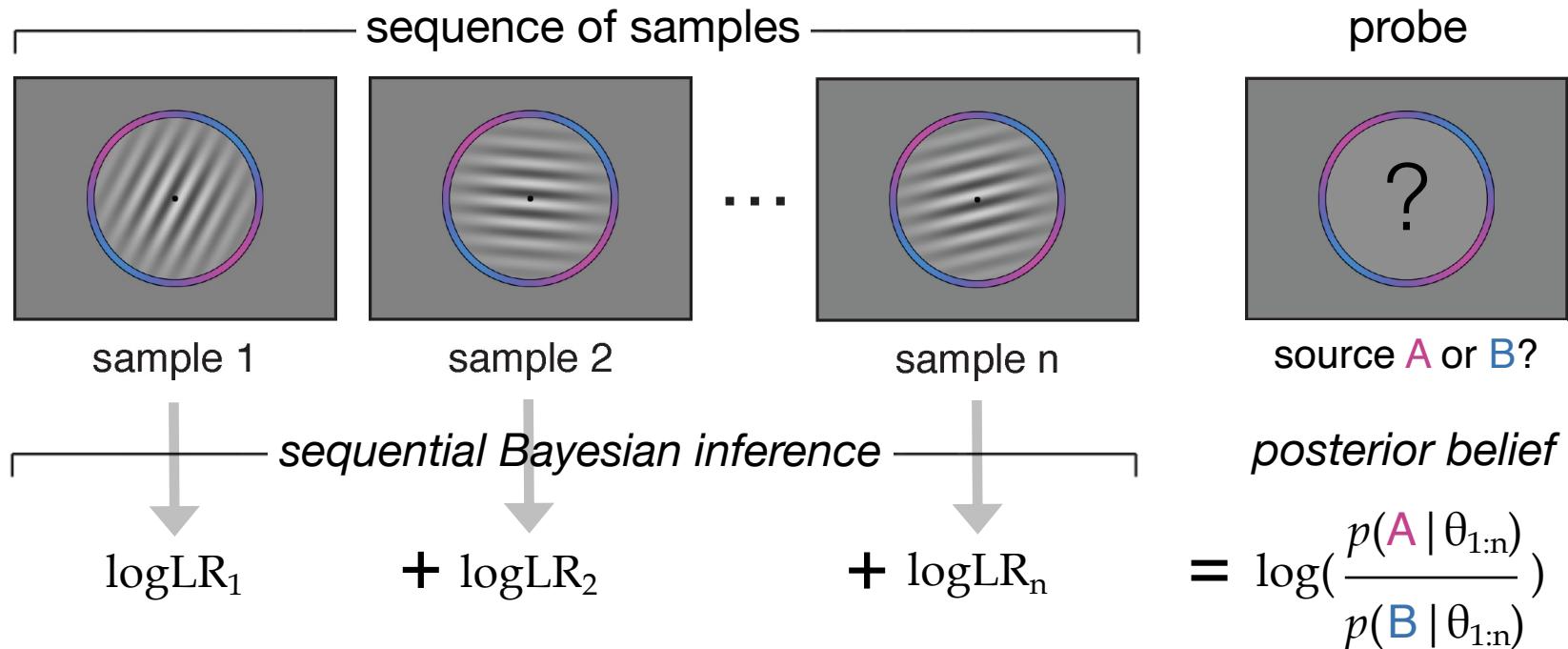
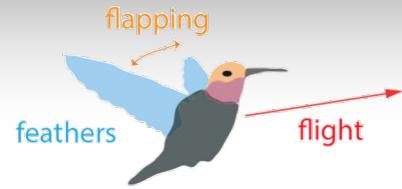


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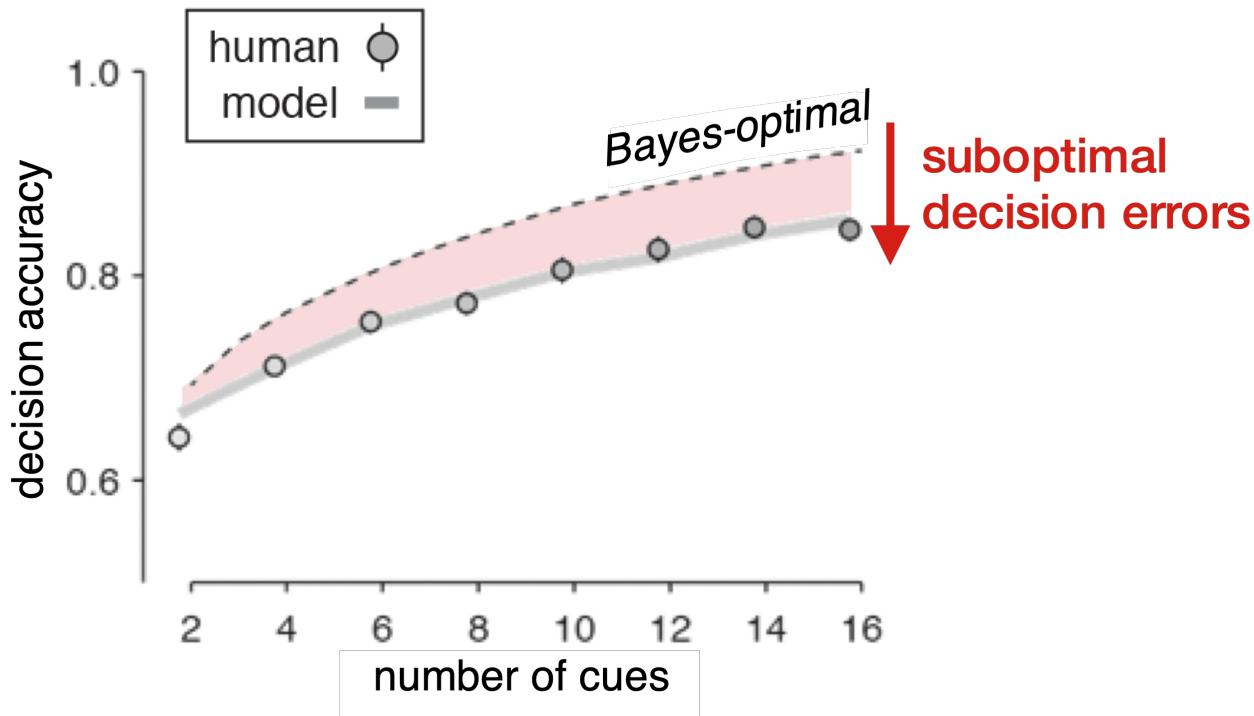
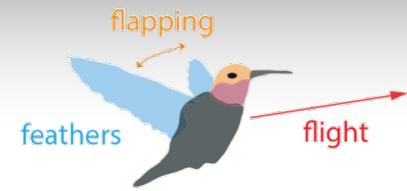


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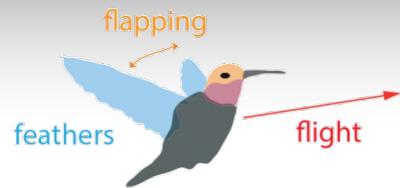
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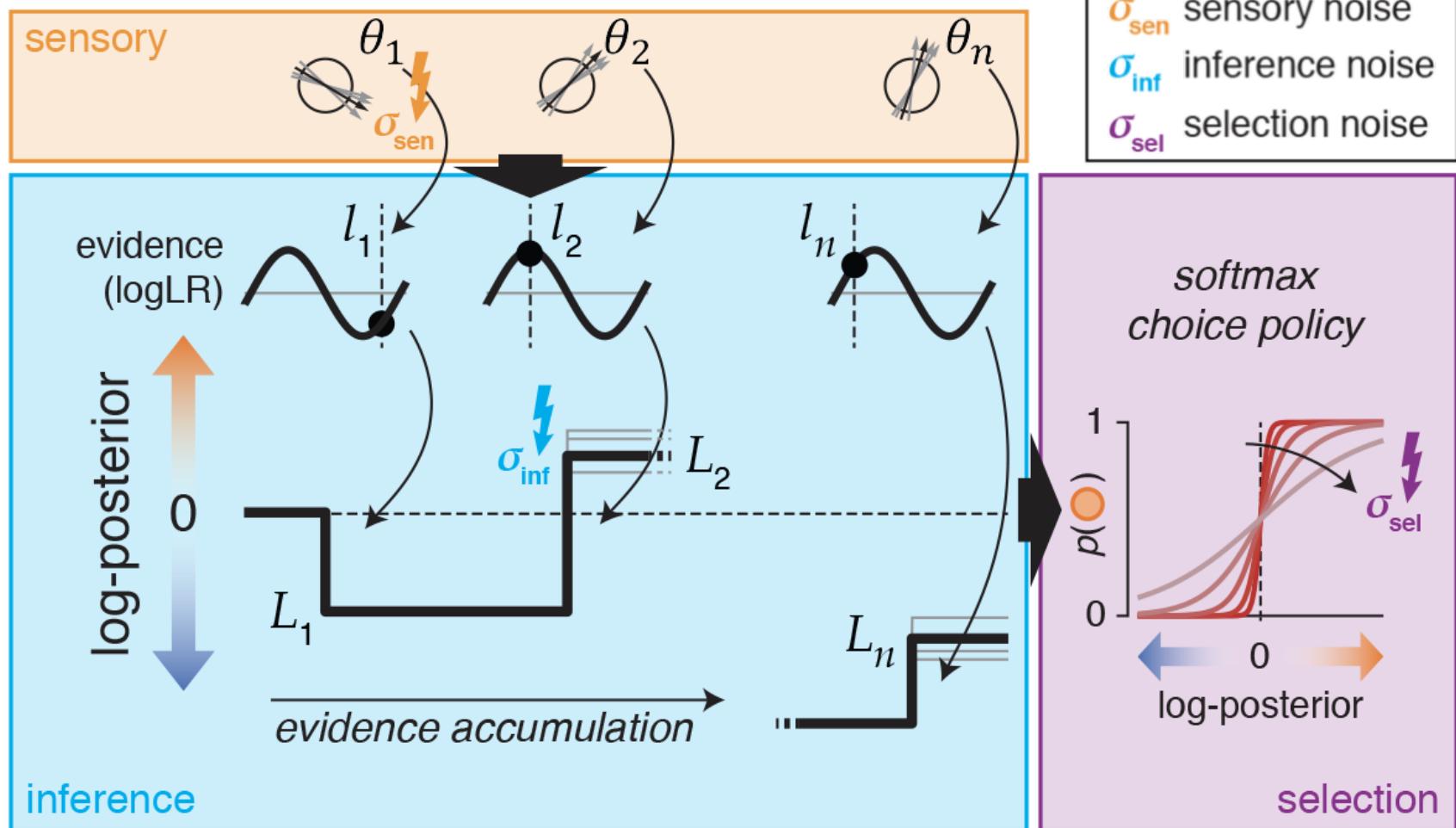


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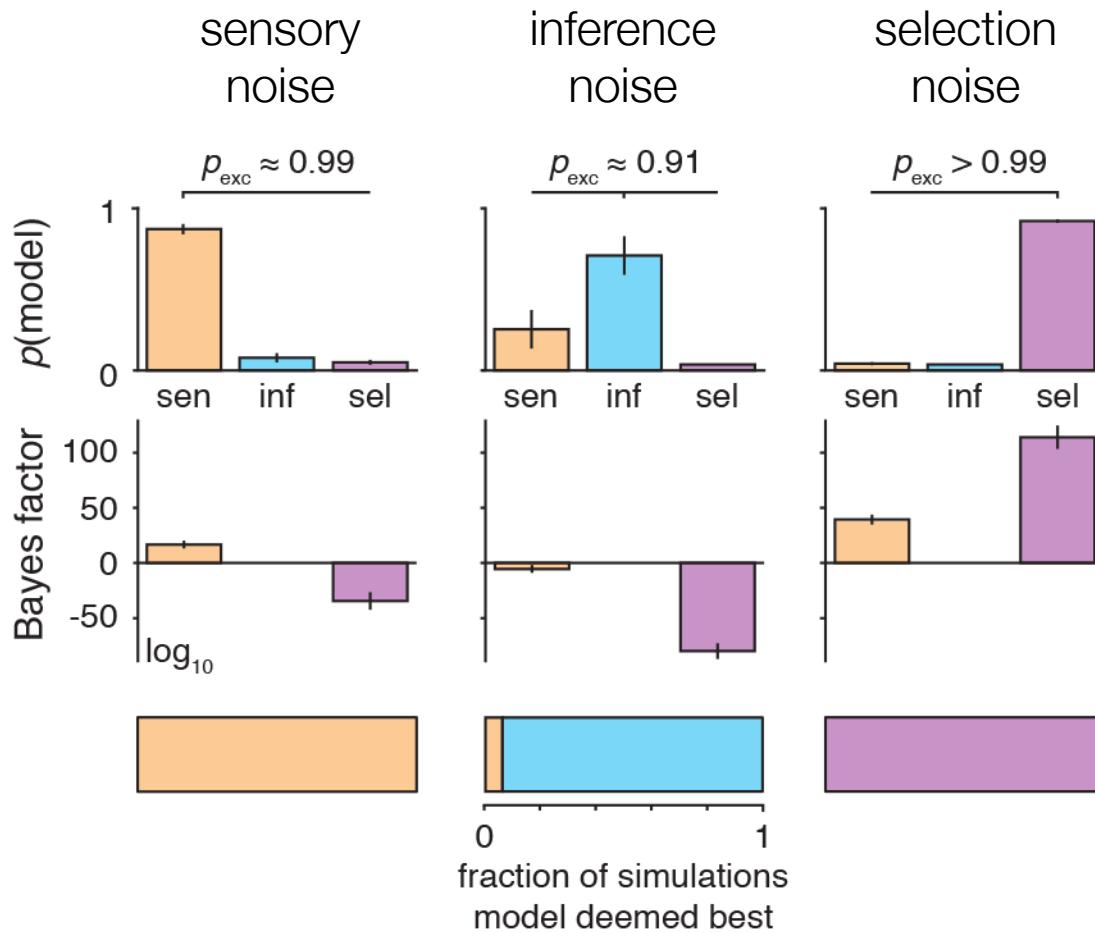
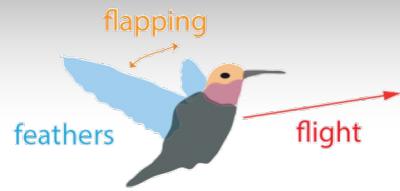
suboptimal Bayesian inference model

Drugowitsch, Wyart et al. (2016) *Neuron*

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Bayesian models as cognitive algorithms

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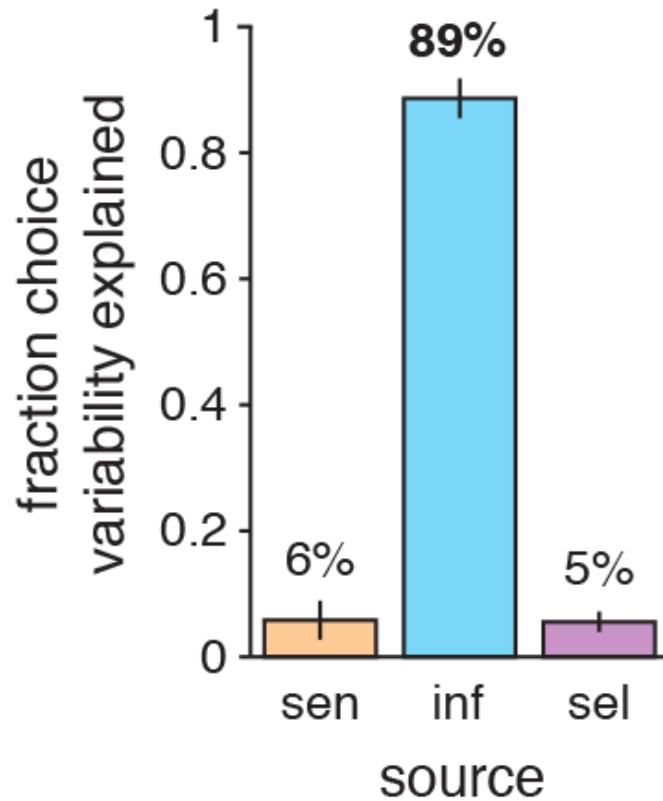
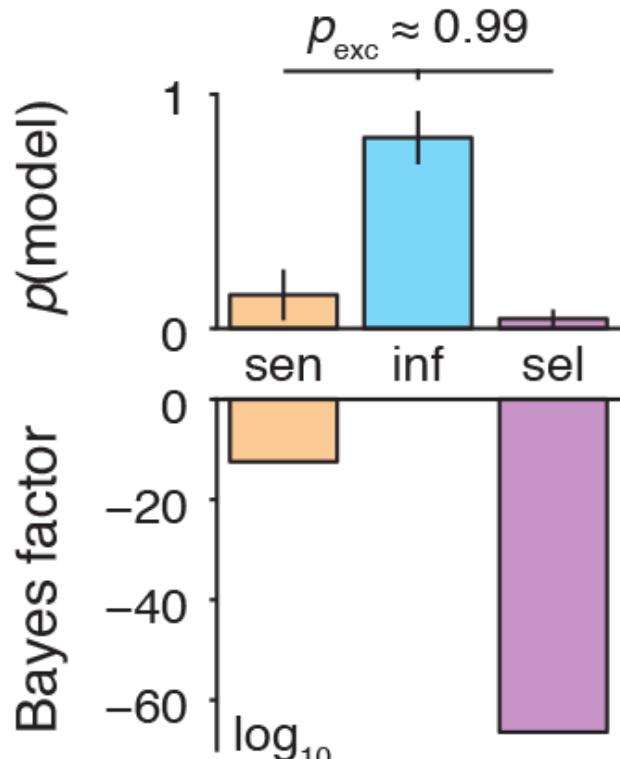
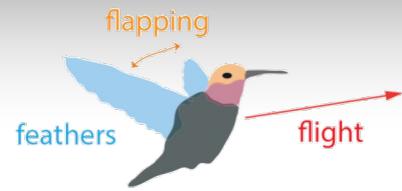


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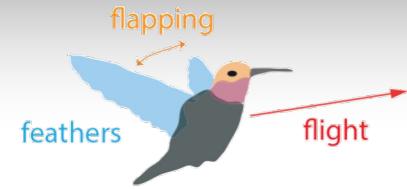
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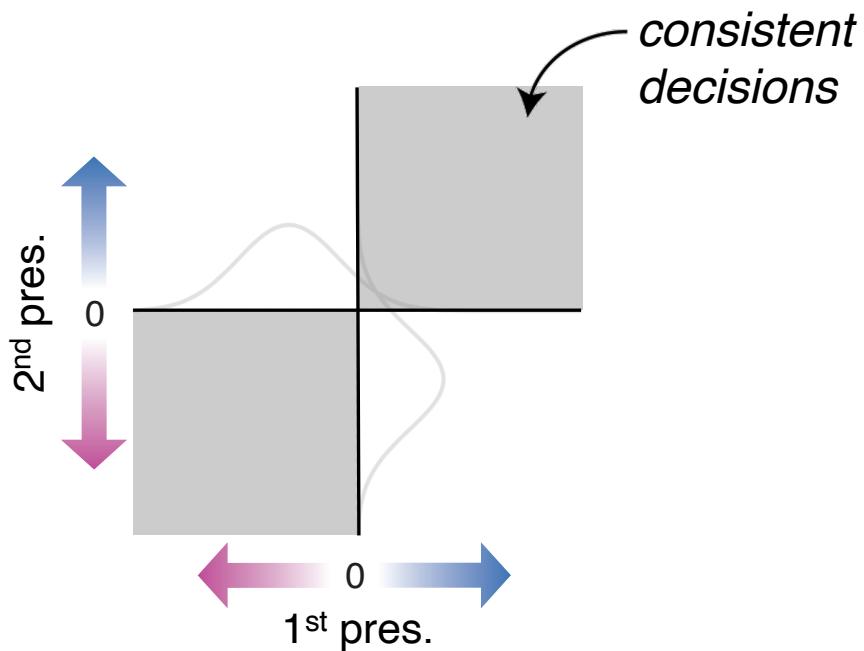


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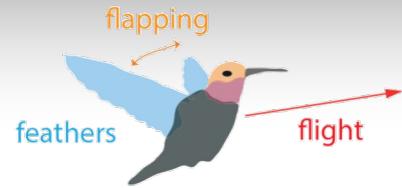


Bayes-optimal models can be used to quantify and qualify suboptimal human inferences



Drugowitsch, Wyart et al. (2016) *Neuron*

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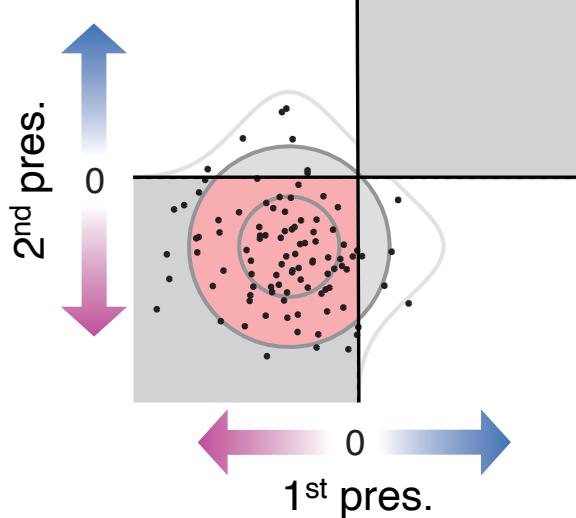


Bayes-optimal models can be used to quantify and qualify suboptimal human inferences

variable inference

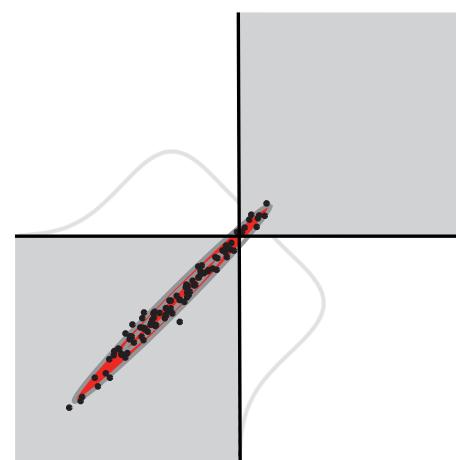
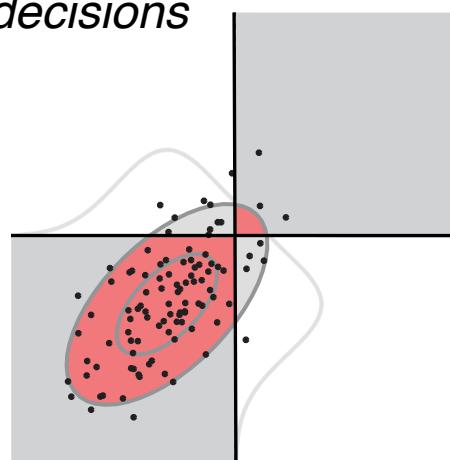
less consistent

consistent decisions



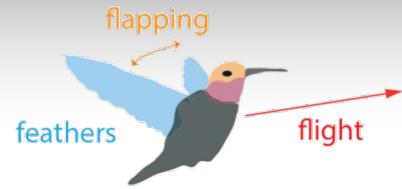
biased inference

more consistent

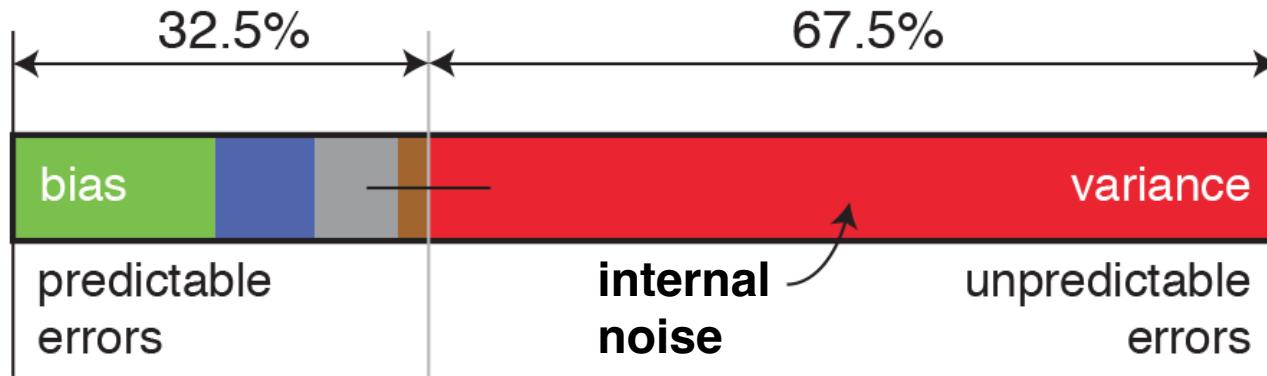


Drugowitsch, Wyart et al. (2016) *Neuron*

Computational precision of inference as critical source of human choice suboptimality

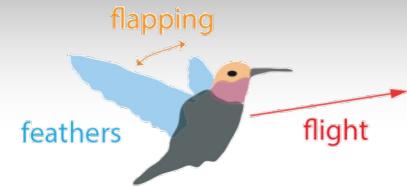


Bayes-optimal models can be used to quantify and qualify suboptimal human inferences



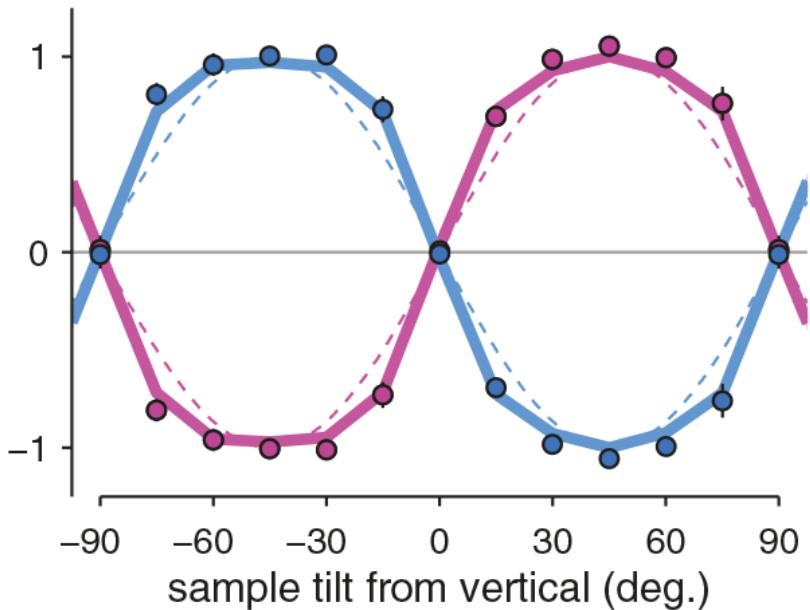
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Computational precision of inference as critical source of human choice suboptimality

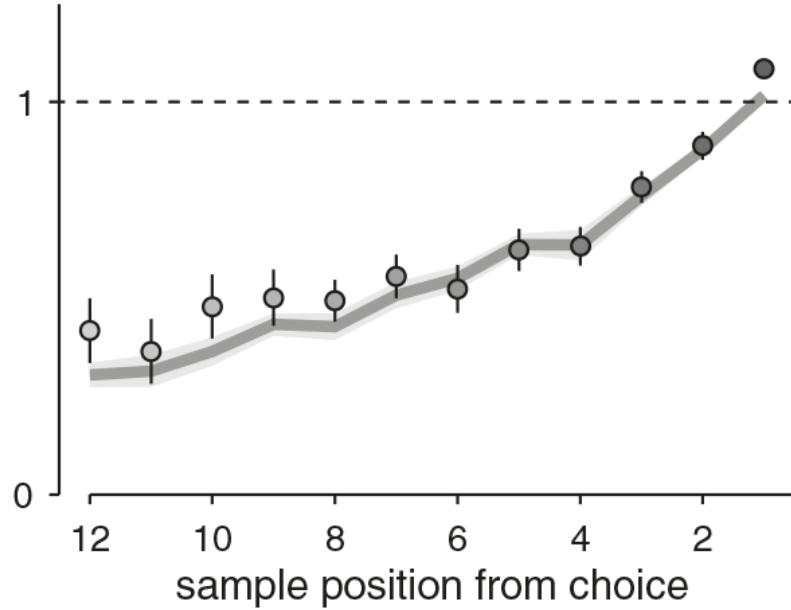


Bayes-optimal models can be used to quantify and qualify suboptimal human inferences

subjective likelihood function

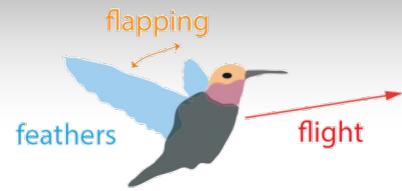


temporal weighting kernel



Drugowitsch, Wyart et al. (2016) *Neuron*

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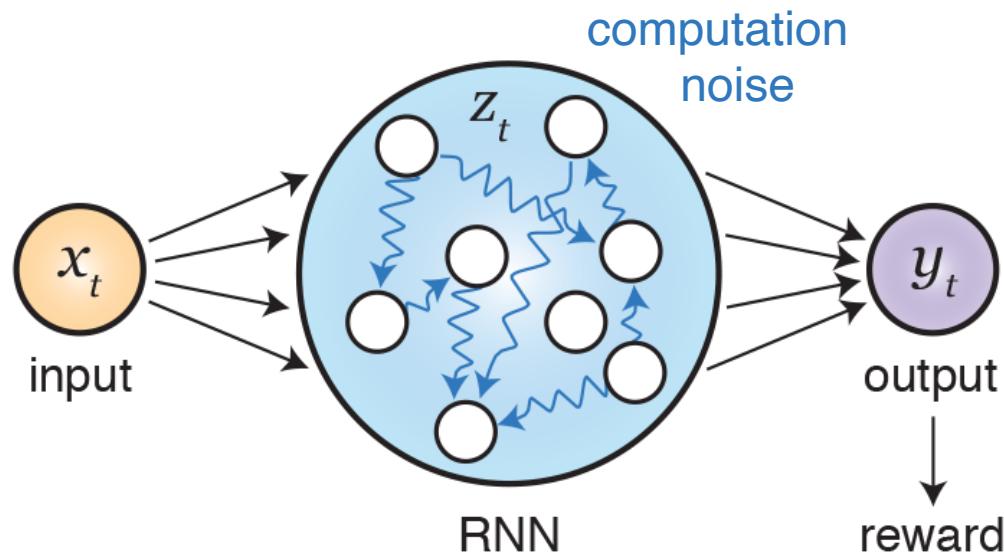
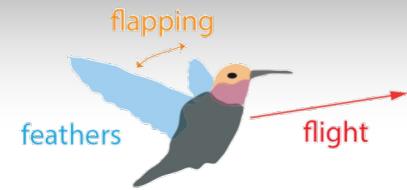


Charles Findling

Geneva University



Findling and Wyart (2020) *bioRxiv*
Computation noise promotes training-free adaptation to uncertainty in RNNs



network dynamics

$$\hat{z}_t = W \cdot z_{t-1} + U \cdot x_t + b$$

$$z_t = \sigma_z(\mathcal{N}(\hat{z}_t, \sigma))$$

objective function

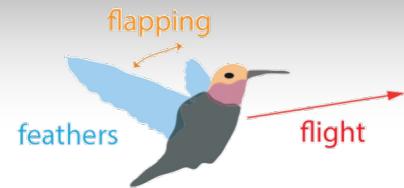
$$y_t = \sigma_y(V \cdot z_t)$$

$$L(U, V, W, b) = \mathbb{E}^\pi[r]$$

computation noise level

Bayesian models as cognitive algorithms

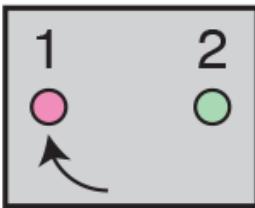
2



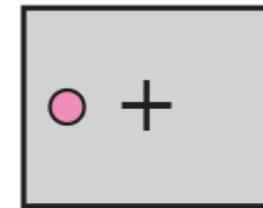
training



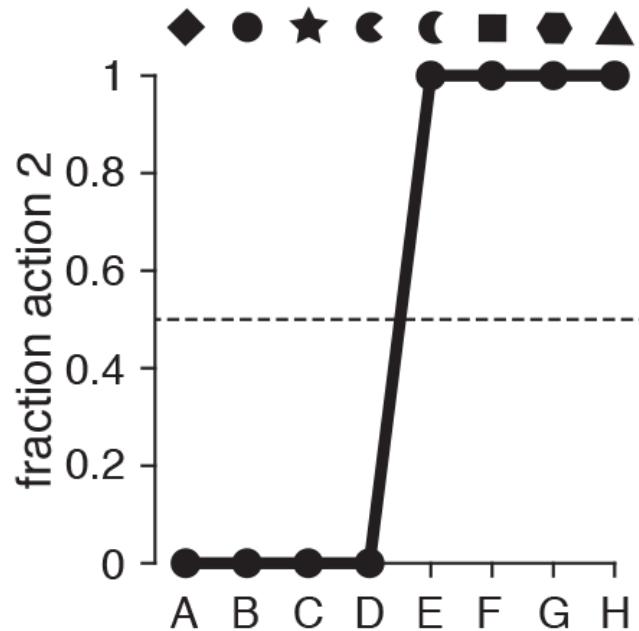
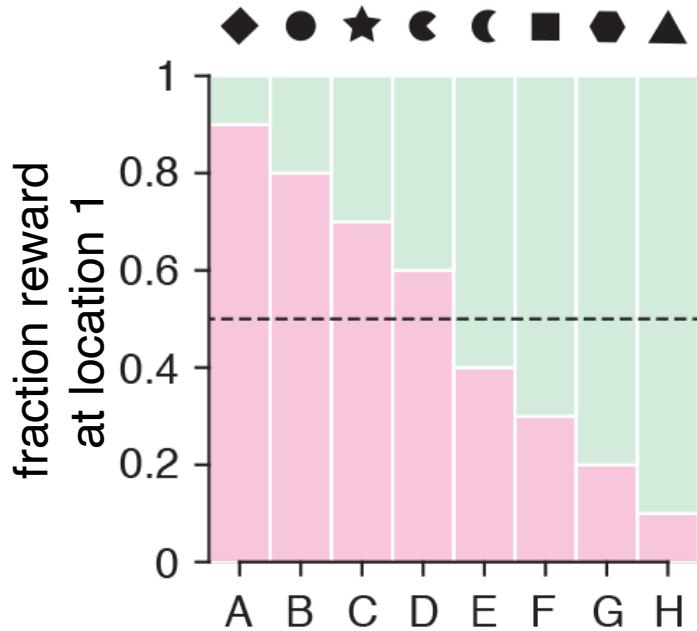
choice



outcome



after training

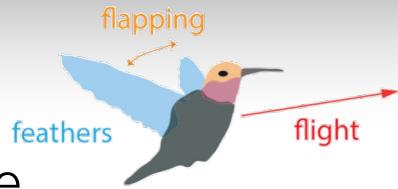


Findling and Wyart (2020) *bioRxiv*

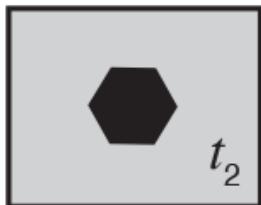
Computation noise promotes training-free adaptation to uncertainty in RNNs

Bayesian models as cognitive algorithms

2



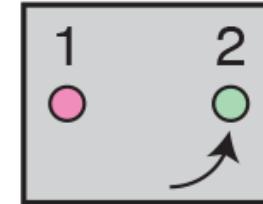
test



...

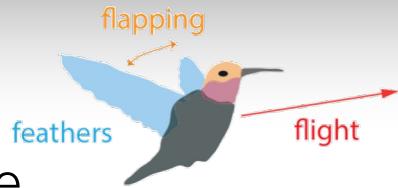


choice

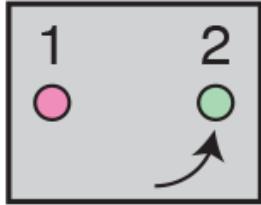


Findling and Wyart (2020) *bioRxiv*

Computation noise promotes training-free adaptation to uncertainty in RNNs

**test** t_1  t_2

...

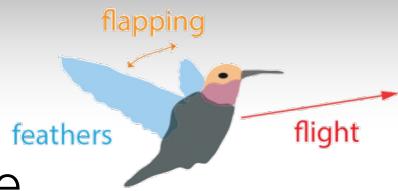
 t_n **choice** $\log LR_1$ $+ \log LR_2$ $+ \log LR_n$ $= \log PR$

log-likelihood
odds ratio

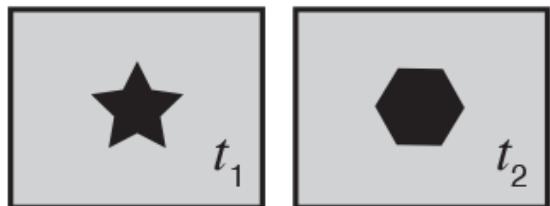
log-posterior
odds ratio

Bayesian models as cognitive algorithms

2

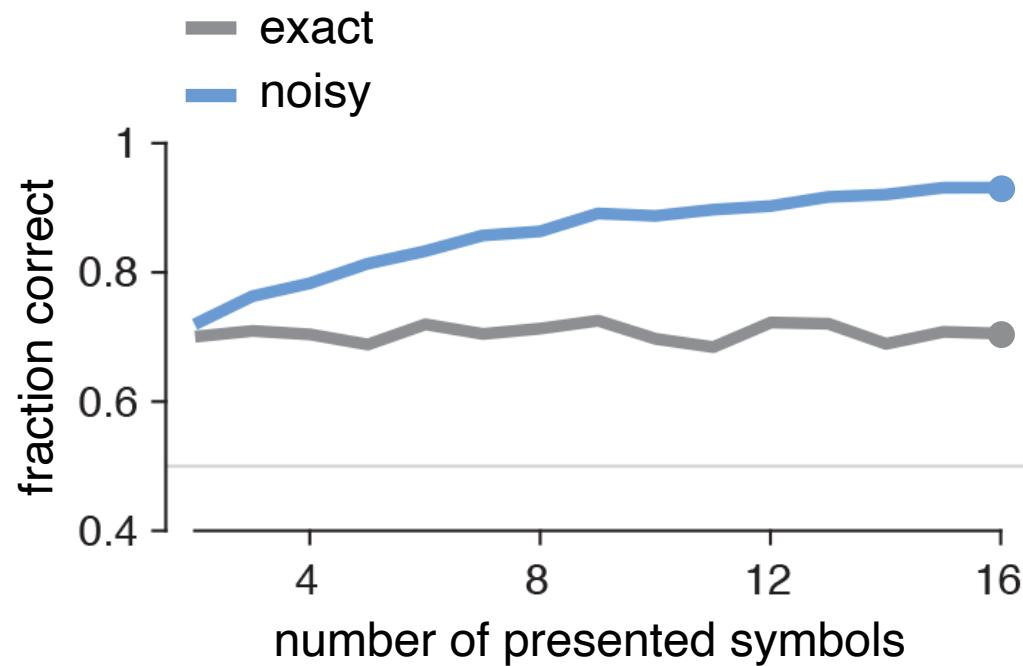
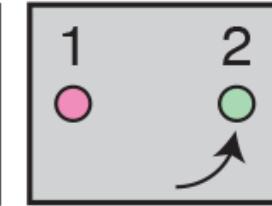


test



...

choice

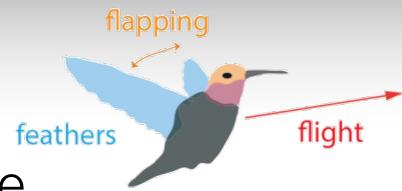


Findling and Wyart (2020) *bioRxiv*

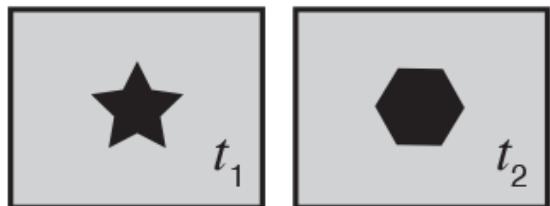
Computation noise promotes training-free adaptation to uncertainty in RNNs

Bayesian models as cognitive algorithms

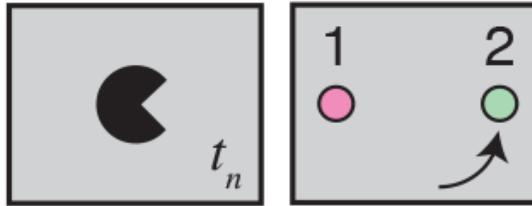
2



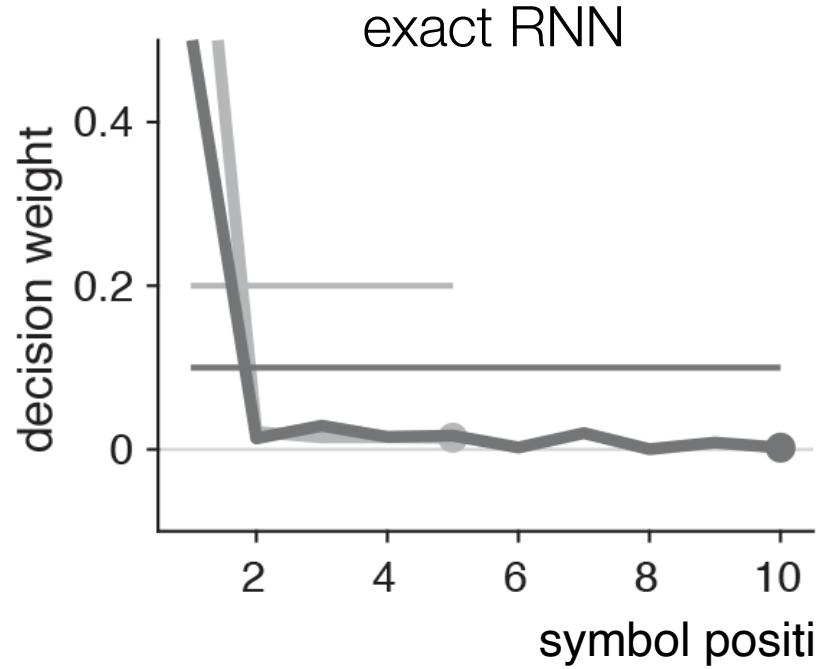
test



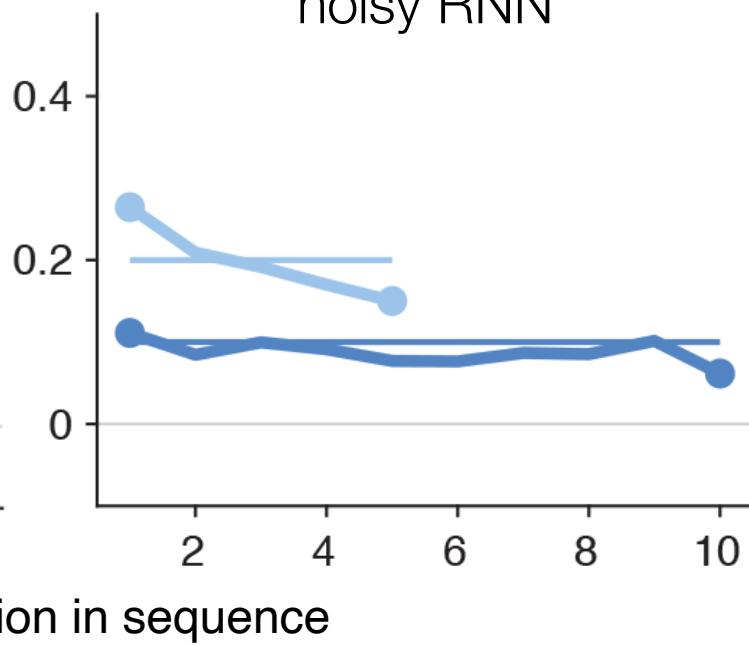
choice



exact RNN

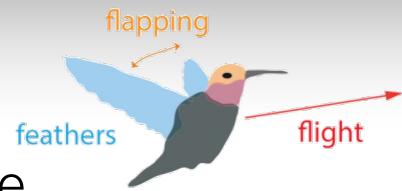


noisy RNN



Findling and Wyart (2020) *bioRxiv*

Computation noise promotes training-free adaptation to uncertainty in RNNs



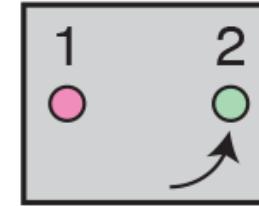
test



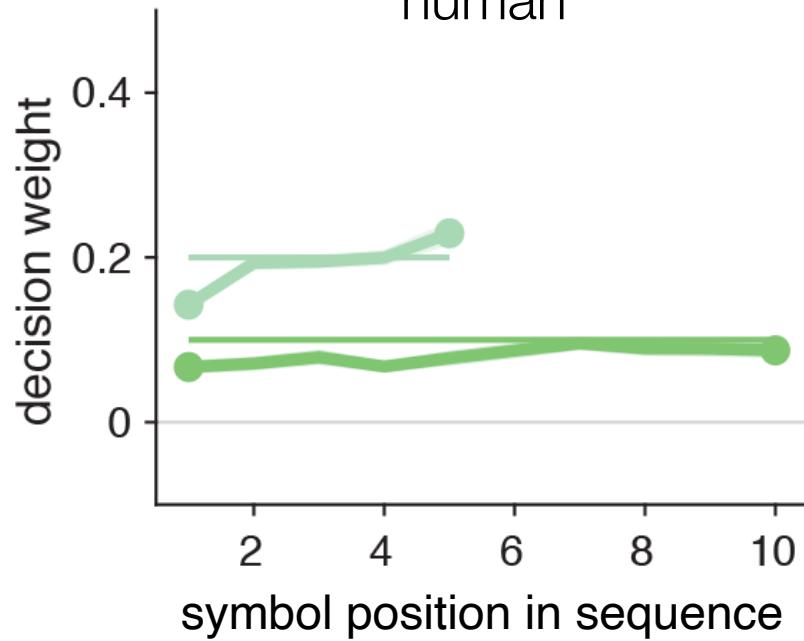
...

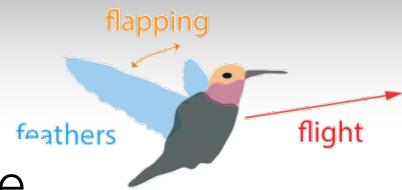


choice

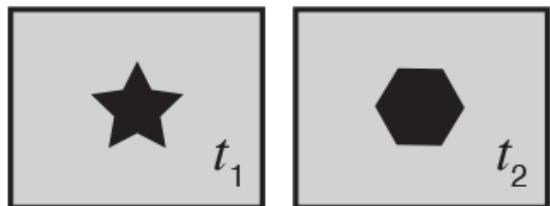


human

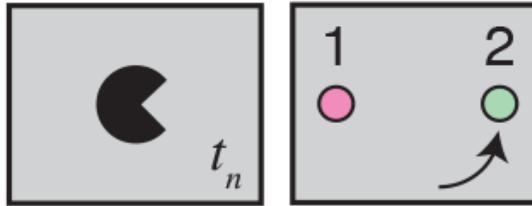




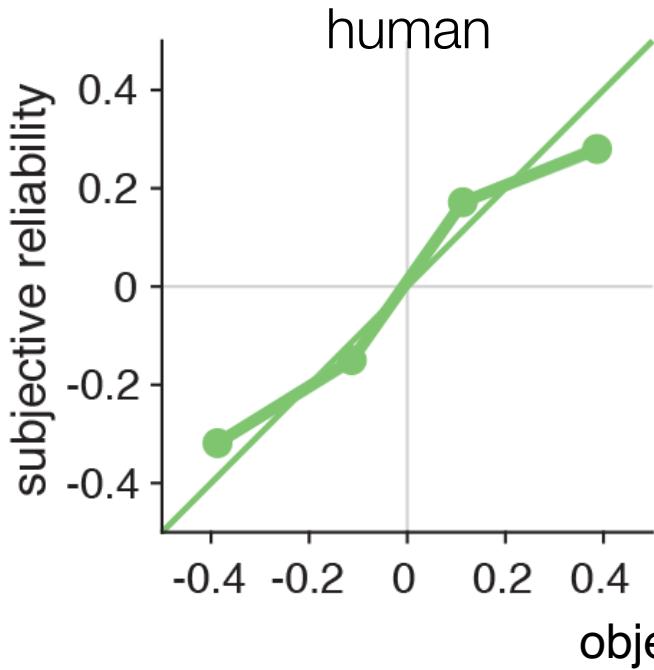
test



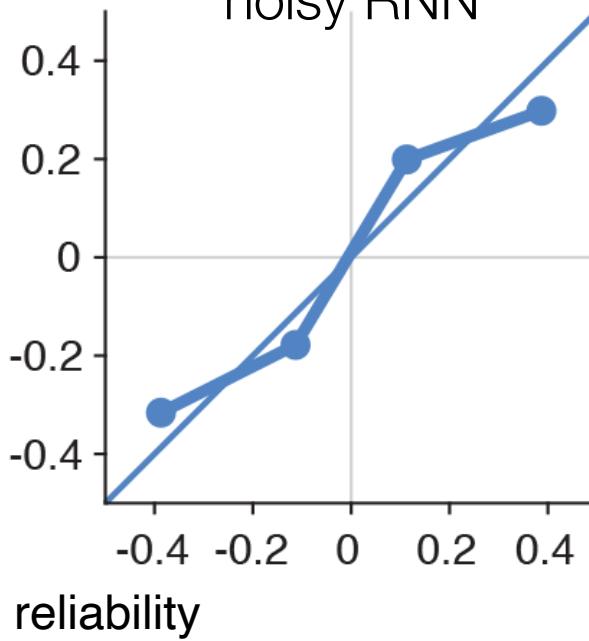
choice



human



noisy RNN



Why Bayesian modeling?

Bayesian models provide the normative solution to dealing with probabilistic uncertainty

Bayesian models have behavioral signatures (such as the reliability-dependent weighting of evidence) that can be looked for in behavior

Bayesian models can be used to explain apparent biases (such as the cardinal bias) as rational

Bayesian models can be leveraged to quantify and qualify suboptimal inferences

Beyond brain mapping

What kind of cognitive neuroscientist are you?

Goal A: understand how the brain works

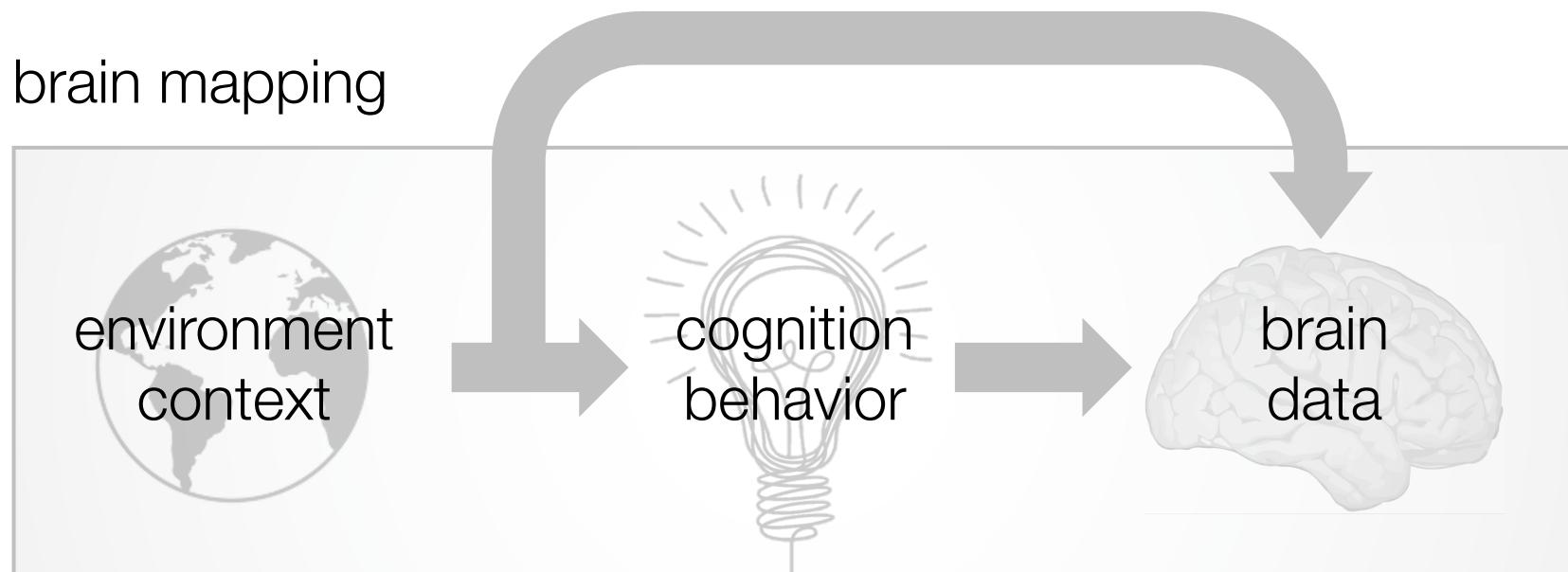
Goal B: understand cognition and behavior



Beyond brain mapping

Brain mapping treats brain data as the dependent variable (to be explained).

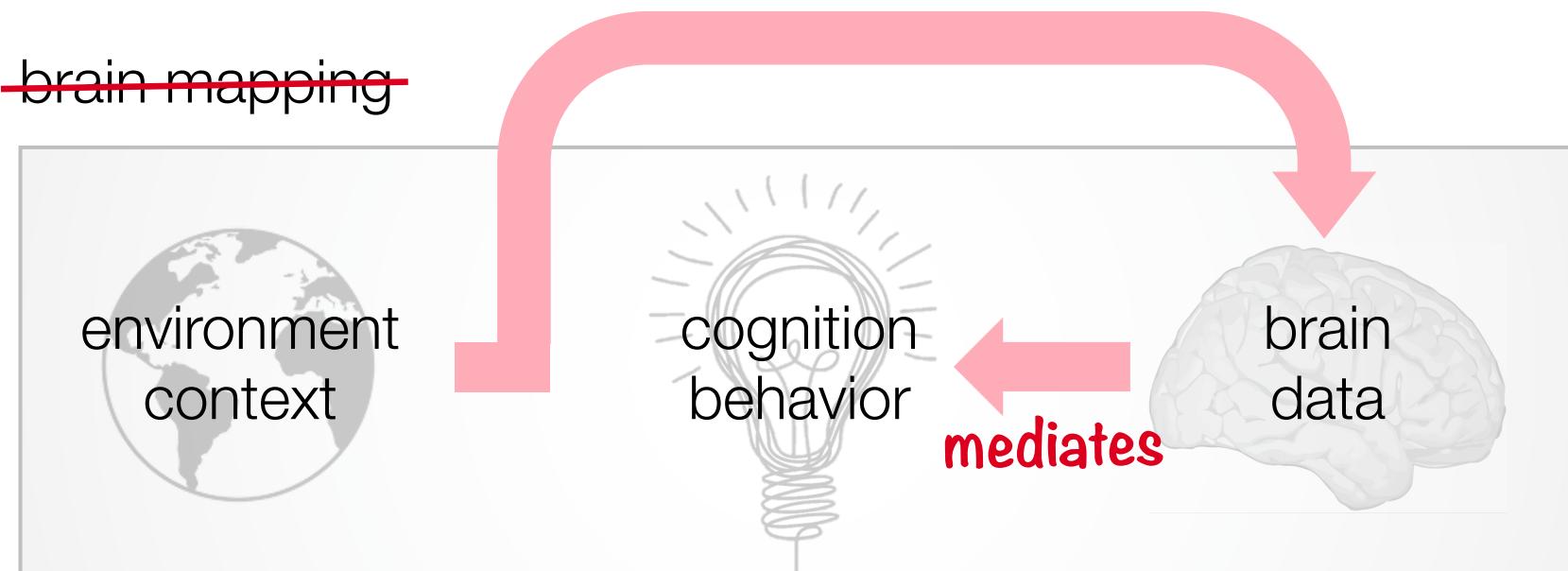
But brain data should rather be seen as mediating cognition and behavior.



Beyond brain mapping

Brain mapping treats brain data as the dependent variable (to be explained).

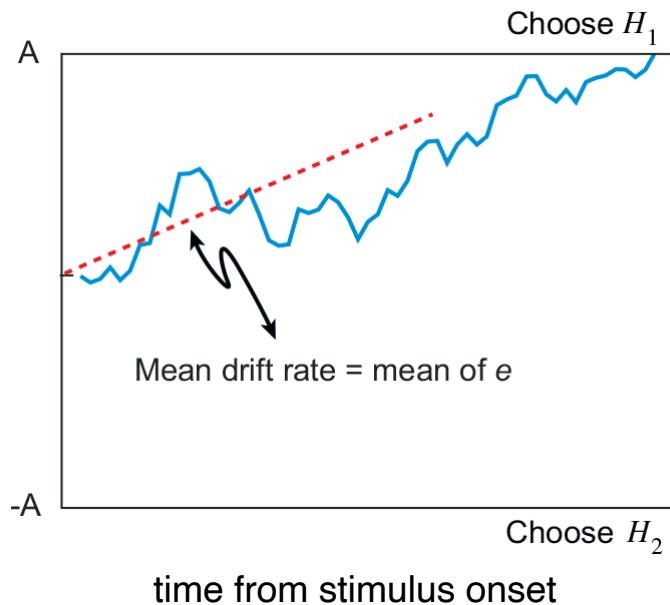
But brain data should rather be seen as mediating cognition and behavior.



Beyond brain mapping

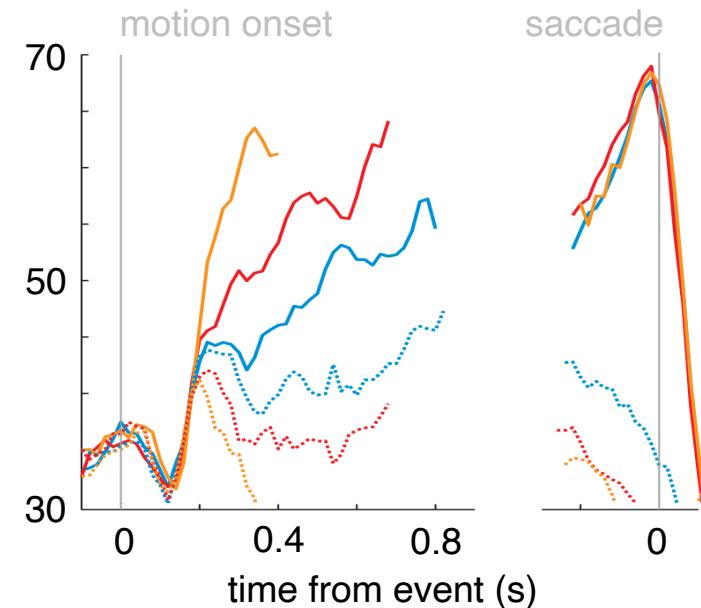
drift-diffusion model
(algorithm)

2



LIP spiking activity
(implementation)

3



Beyond brain mapping

If you are a neuroscientist, then you want 3
but you need to know 2 first.

If you are a cognitive scientist, then you want 2
but you can use 3 to validate 2.

In both cases, studying which **algorithm** is used
is necessary to look for its **implementation**.

Beyond brain mapping



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COMMENTARY

The Primacy of Behavioral Research for Understanding the Brain

Yael Niv

Department of Psychology and Neuroscience Institute, Princeton University

Understanding the brain requires us to answer both *what* the brain does, and *how* it does it. Using a series of examples, I make the case that behavior is often more useful than neuroscientific measurements for answering the first question.¹ Moreover, I show that even for “how” questions that pertain to neural mechanism, a well-crafted behavioral paradigm can offer deeper insight and stronger constraints on computational and mechanistic models than do many highly challenging (and very expensive) neural studies. I conclude that purely behavioral research is essential for understanding the brain—especially its cognitive functions—contrary to the opinion of prominent funding bodies and some scientific journals, who erroneously place neural data on a pedestal and consider behavior to be subsidiary.

Keywords: behavioral experiments, cognition, neuroscience, priorities

In an era of increasingly precise methods for measuring and perturbing neurons in the brain, it often seems that with more neural data, we will soon make untold breakthroughs in understanding the brain. Such anticipation has heralded neuroscience-data-focused projects such as the Brain Initiative and the Human Connectome Project. The focus on neural measurement has been accompanied by the demotion of animal and human behavioral research—the mainstays of psychology from where understanding of the brain and behavior have sprung since the discipline was founded.

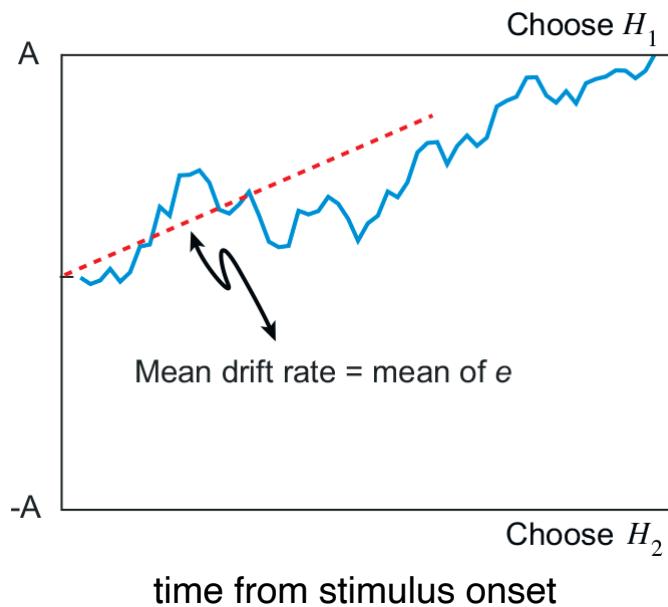
looking at single neurons, or even their ensembles, is like attempting to understand why people in Australia drive on the left side of the road from examination of their DNA. Neural firing patterns are the wrong level for investigating many pressing questions in neuroscience. Even if we could measure all the neurons in the brain with arbitrary precision, without an incisive behavioral paradigm we would not be able to answer many neuroscientific questions. Indeed, the insights about the brain that my lab has gleaned from our own research have almost all come from behavioral data, which explains

Beyond brain mapping

Example: decision as accumulation-to-bound

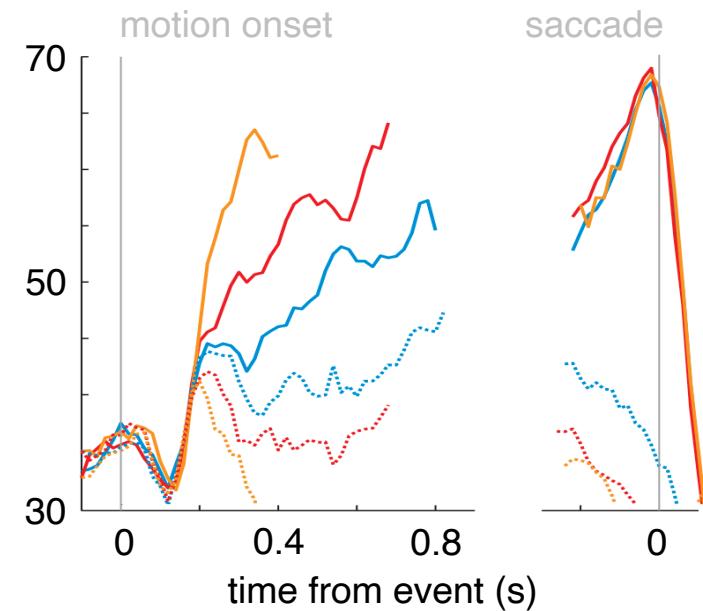
algorithm

Ratcliff (1978)
Psychological Review



implementation

Roitman and Shadlen (2002)
Journal of Neuroscience



Beyond brain mapping

Behavior alone can inform about the algorithms used by the brain to solve complex tasks.

Brain data can be used as additional observables for understanding cognition and behavior.

Case studies where we have used this approach for understanding human decision-making with different types of brain data.

Case study 1: covert bound on decision-making

Tarryn Balsdon
Glasgow University



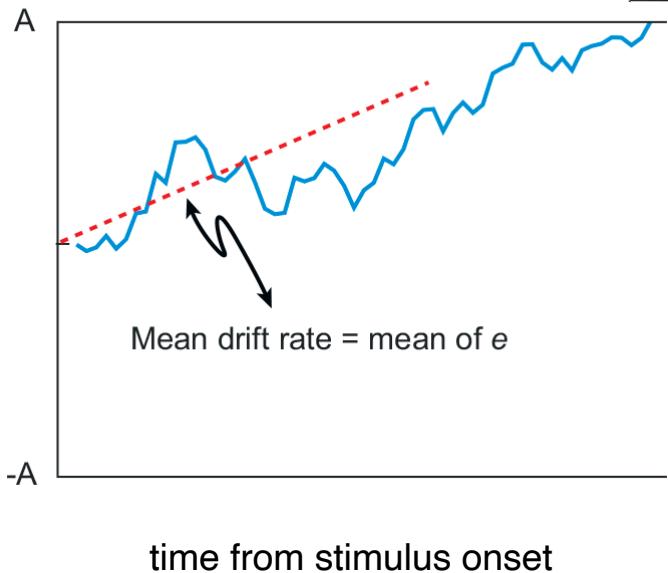
Pascal Mamassian
Ecole Normale Supérieure



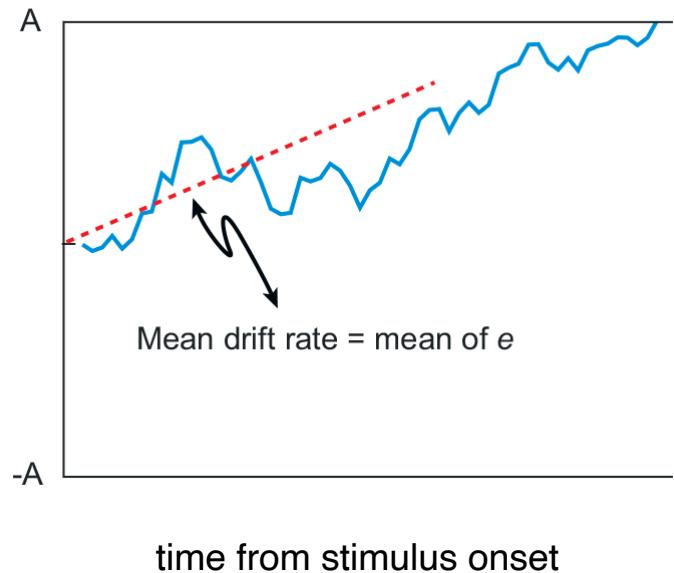
Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making

motor response
overt decision bound



mental commitment
covert decision bound



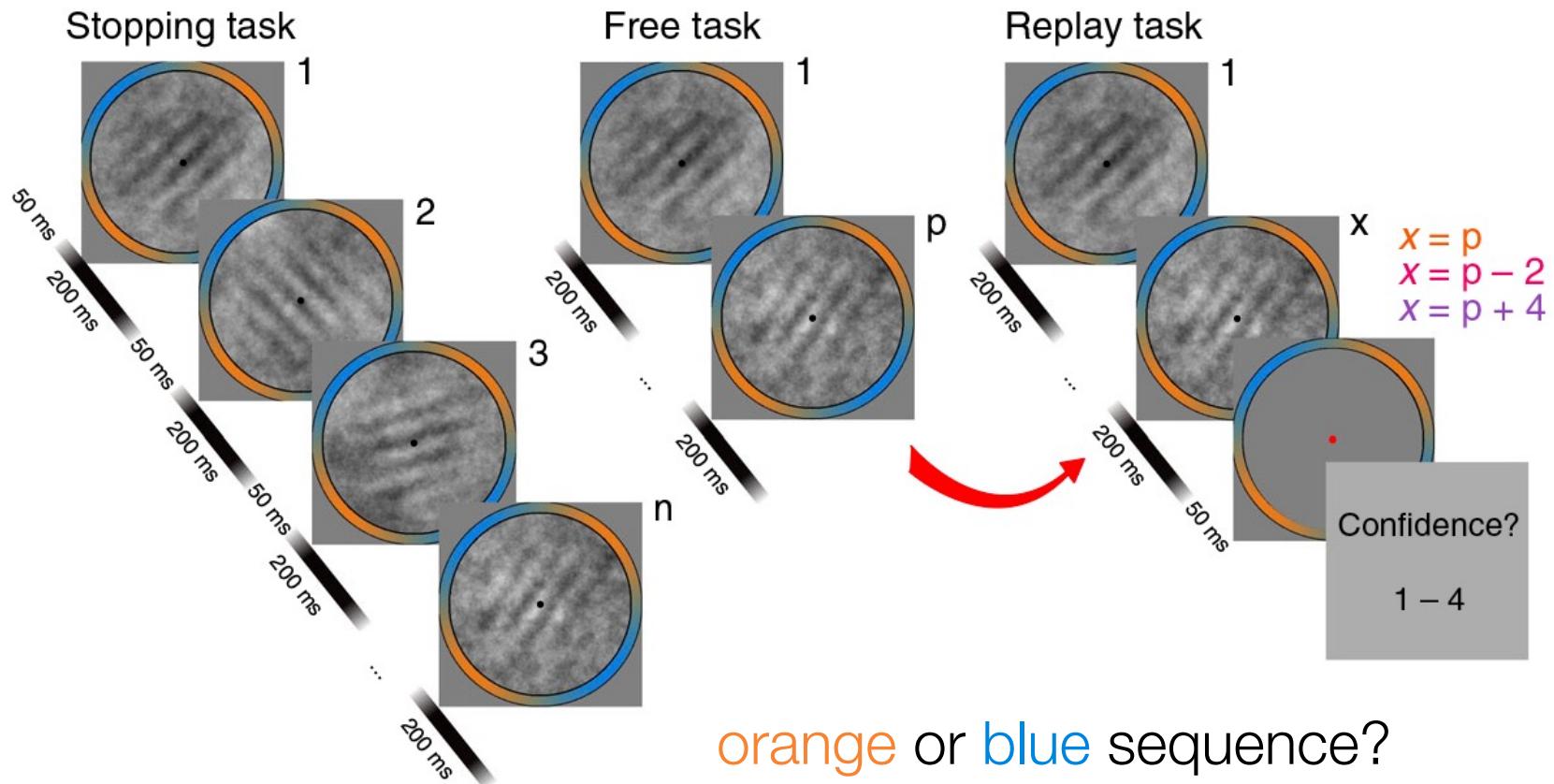
Case study 1: covert bound on decision-making

Brain data: pupil dilation



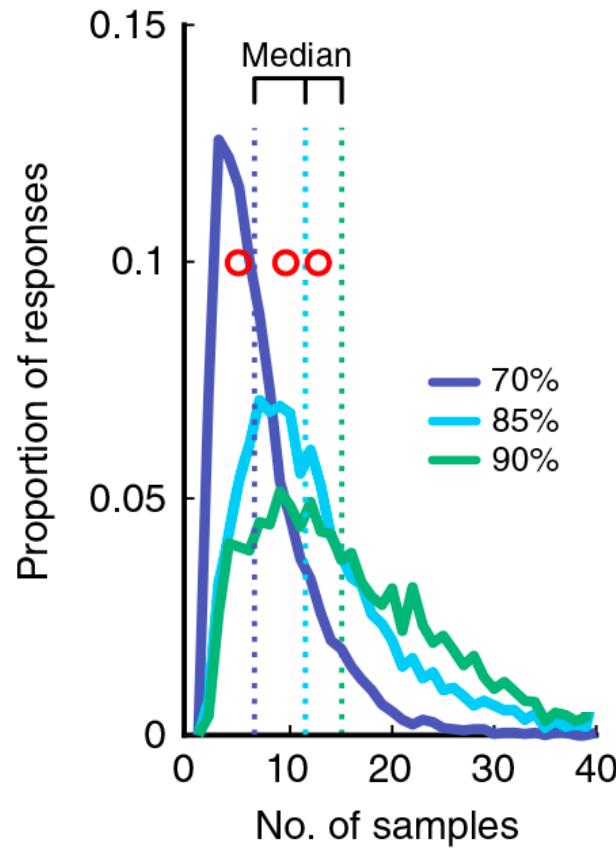
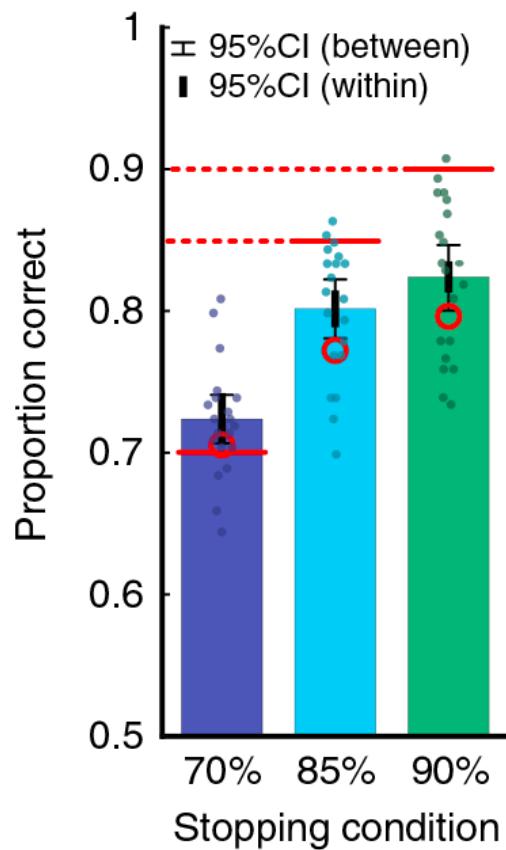
Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making



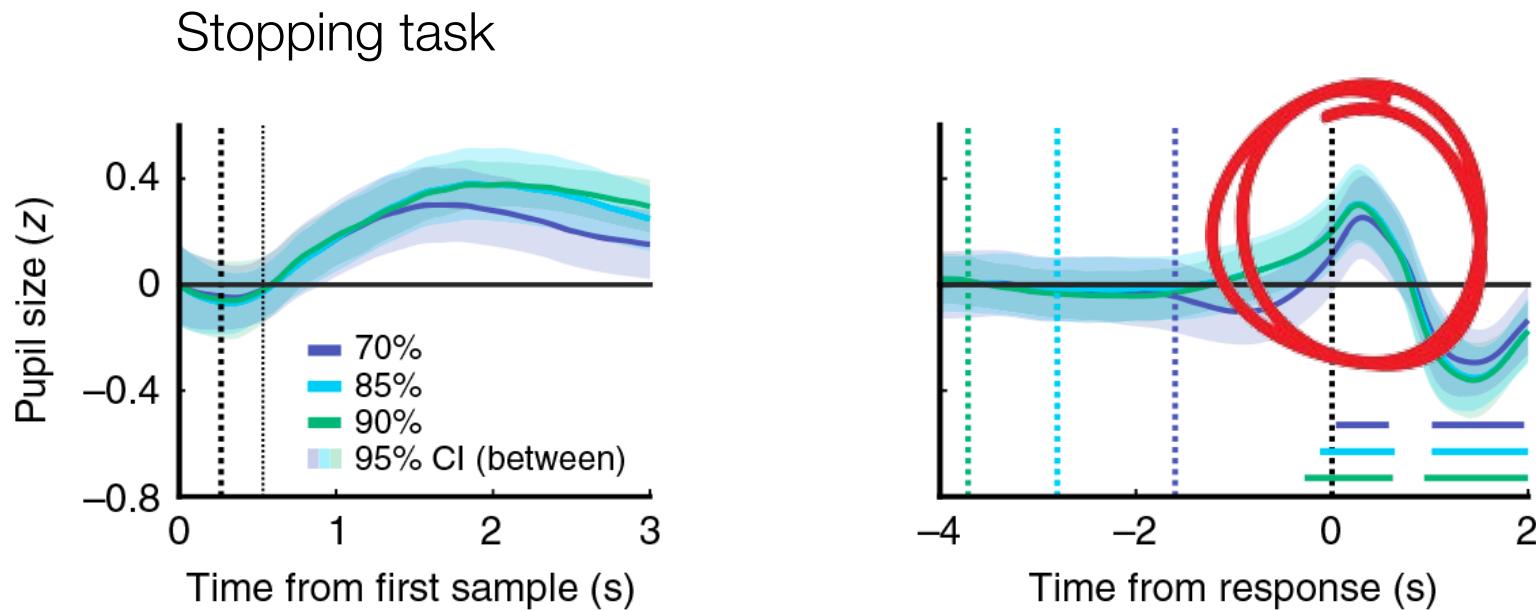
Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making



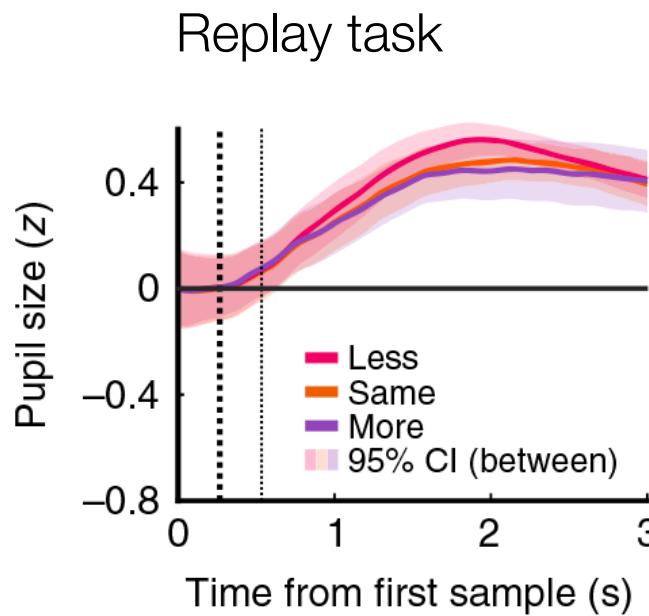
Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making



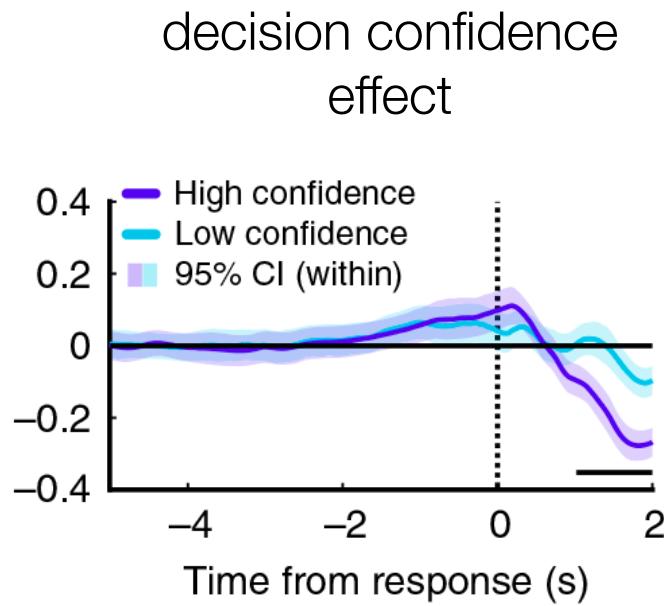
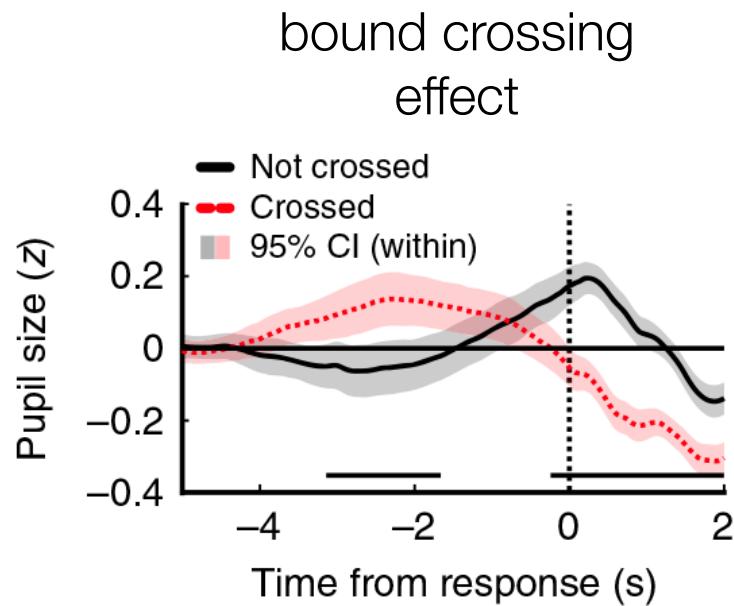
Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making



Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making



Balsdon, Wyart and Mamassian (2020) *Nature Communications*
Confidence controls perceptual evidence accumulation

Case study 1: covert bound on decision-making

Pupil dilation reveals a covert bound on decision-making (not directly visible from behavior).

Understanding the origin of pupil dilation is not needed to draw this conclusion.

Pupil dilation is used to refine cognitive models of decision-making, not to map pupillary correlates of decision-making.

Case study 2: effect of controllability on decision-making

Aurélien Weiss

PhD student



Marion Rouault

Brain Institute, Paris



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

Case study 2: effect of controllability on decision-making



C- condition

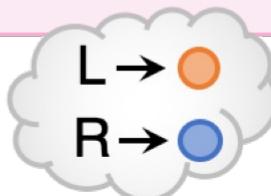
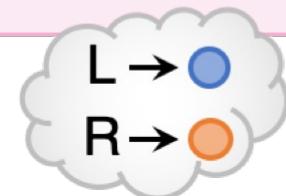
instruction: track drawn category

passive sampling
not controllable

C+ condition

instruction: press ●-drawing key

active sampling
controllable



Case study 2: effect of controllability on decision-making

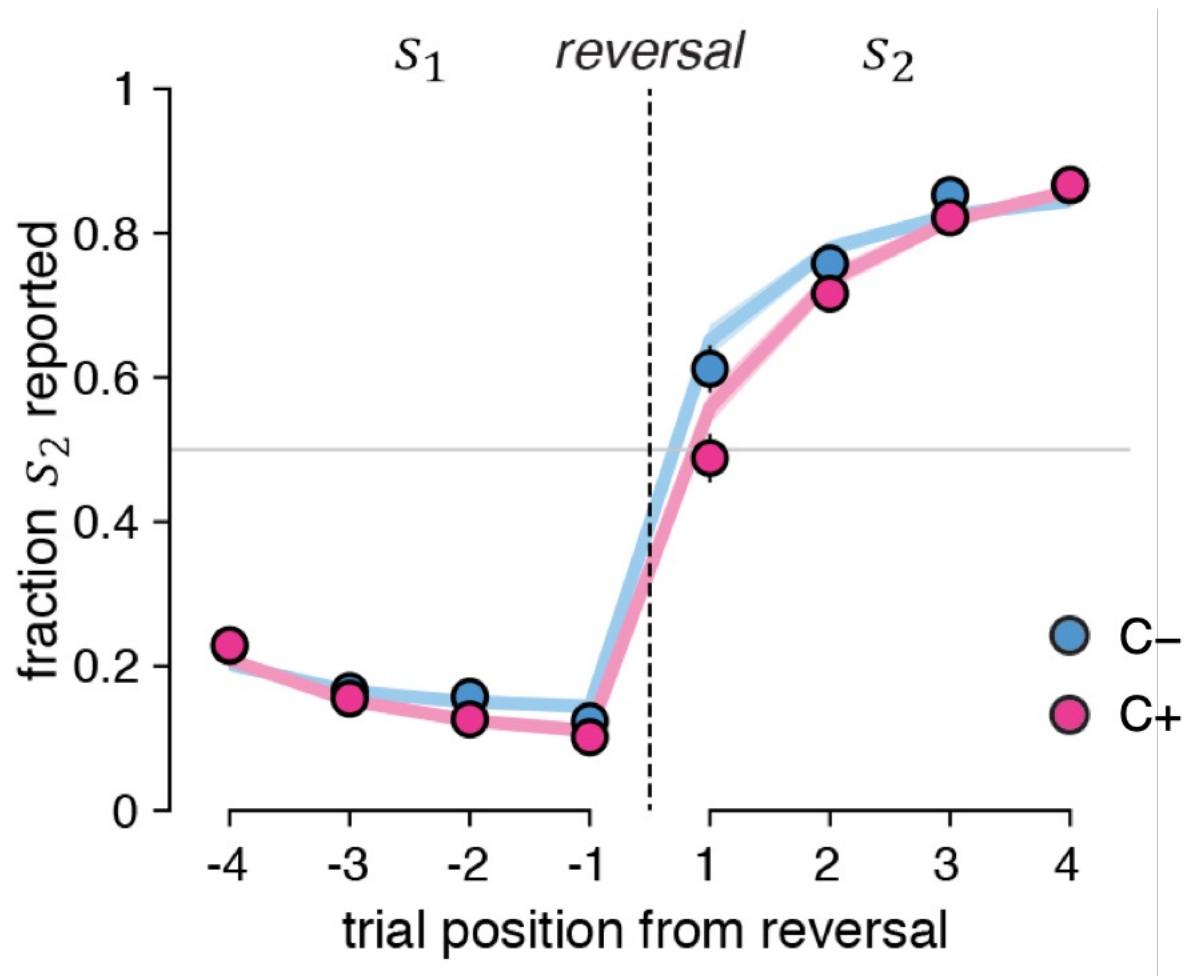
Brain data: MEG activity



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

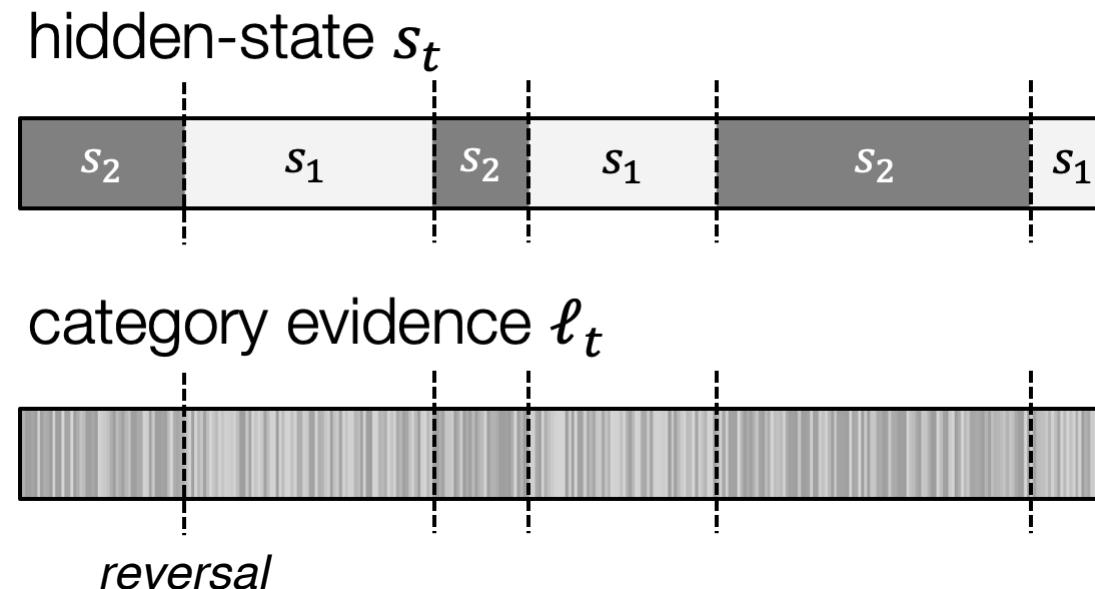
Case study 2: effect of controllability on decision-making



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

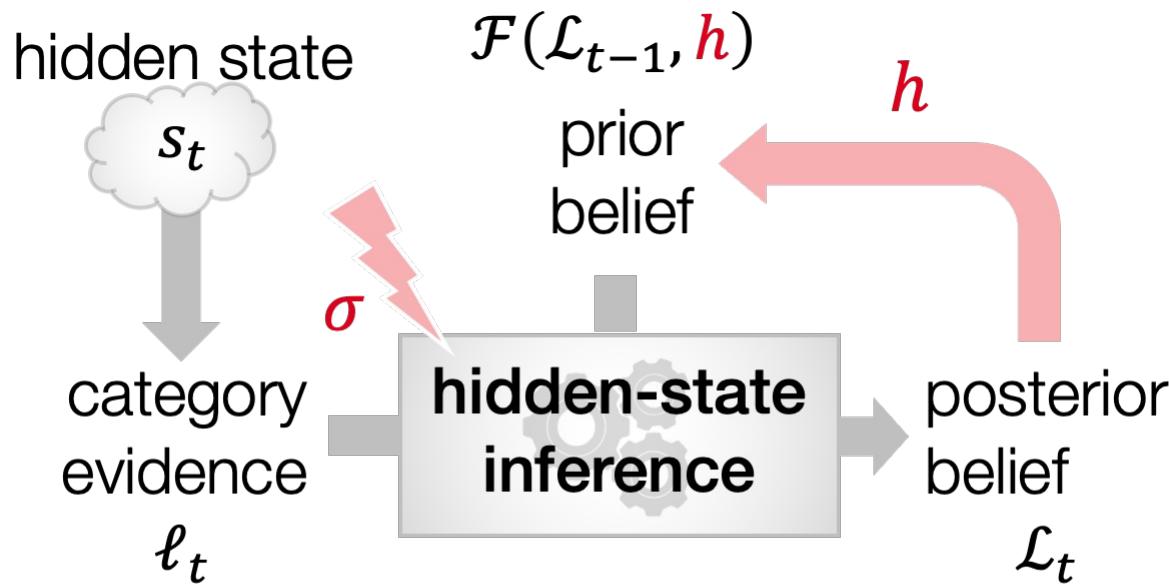
Case study 2: effect of controllability on decision-making



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

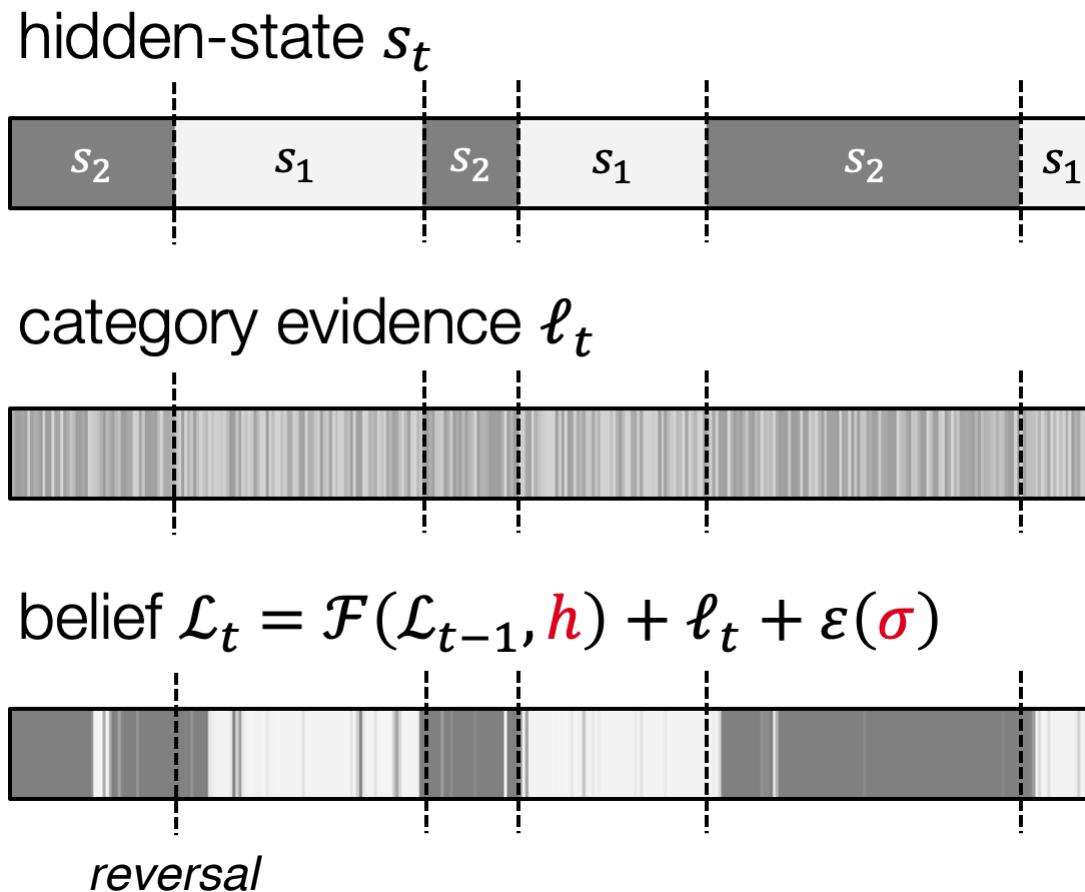
Case study 2: effect of controllability on decision-making



h = perceived reversal rate

σ = computation noise

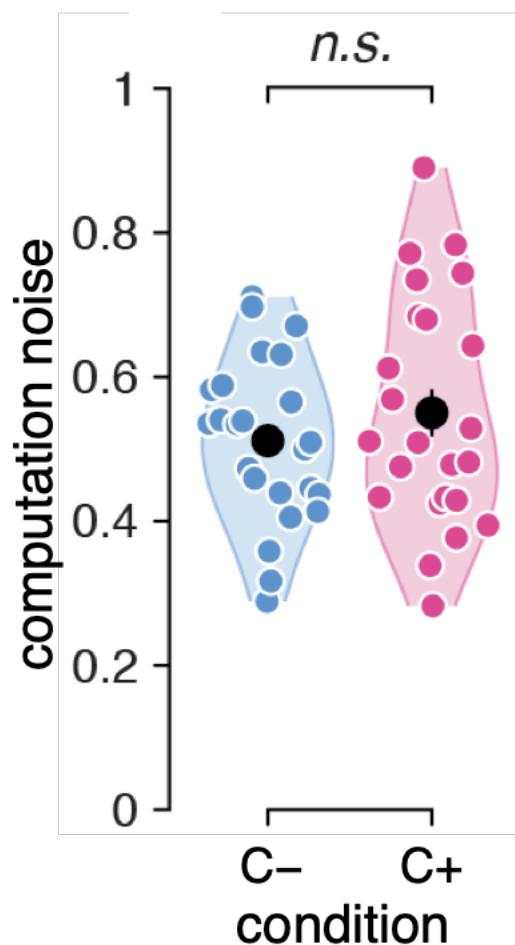
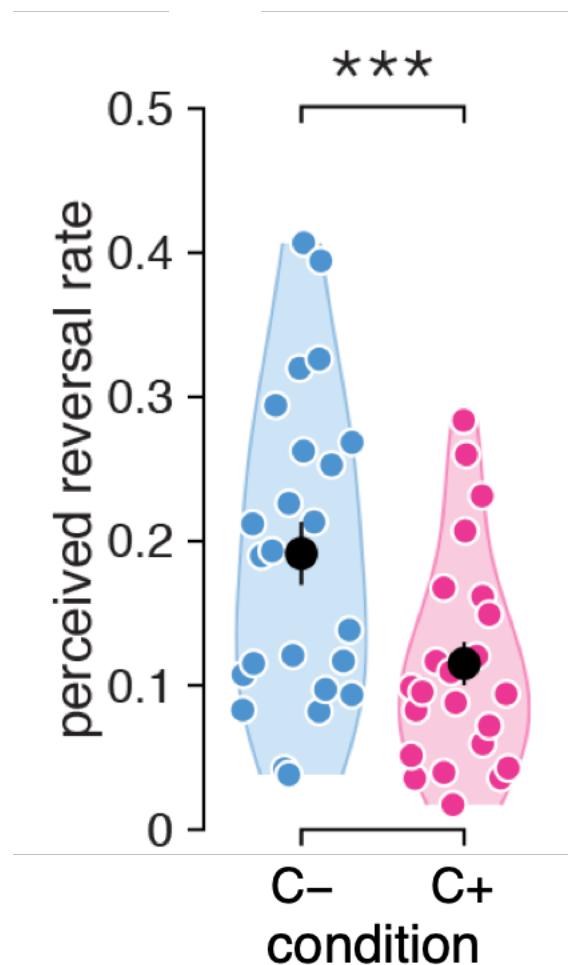
Case study 2: effect of controllability on decision-making



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

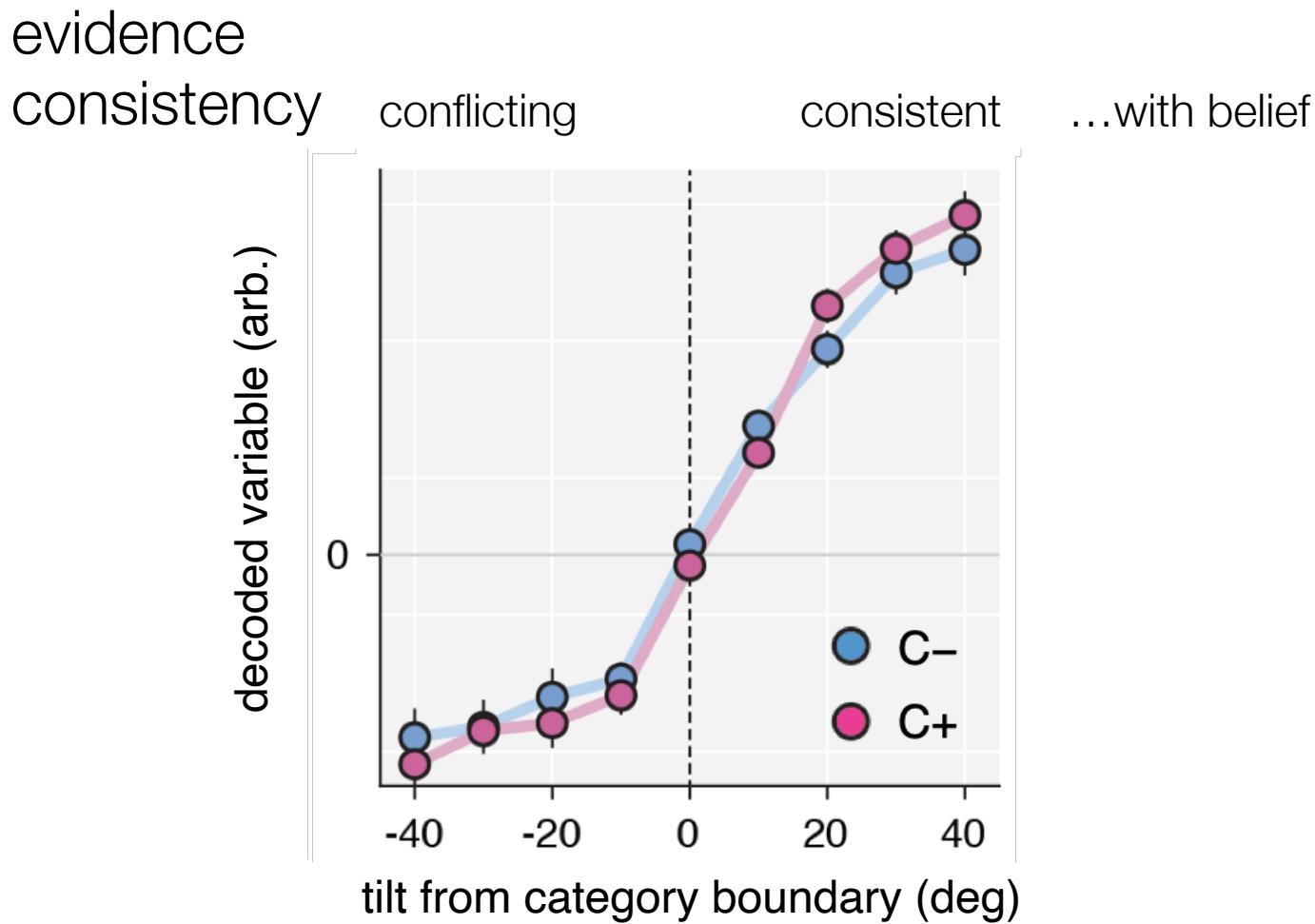
Case study 2: effect of controllability on decision-making



Weiss et al. (2021) *Nature Comm.*

Interacting with volatile environments stabilizes hidden-state inference

Case study 2: effect of controllability on decision-making

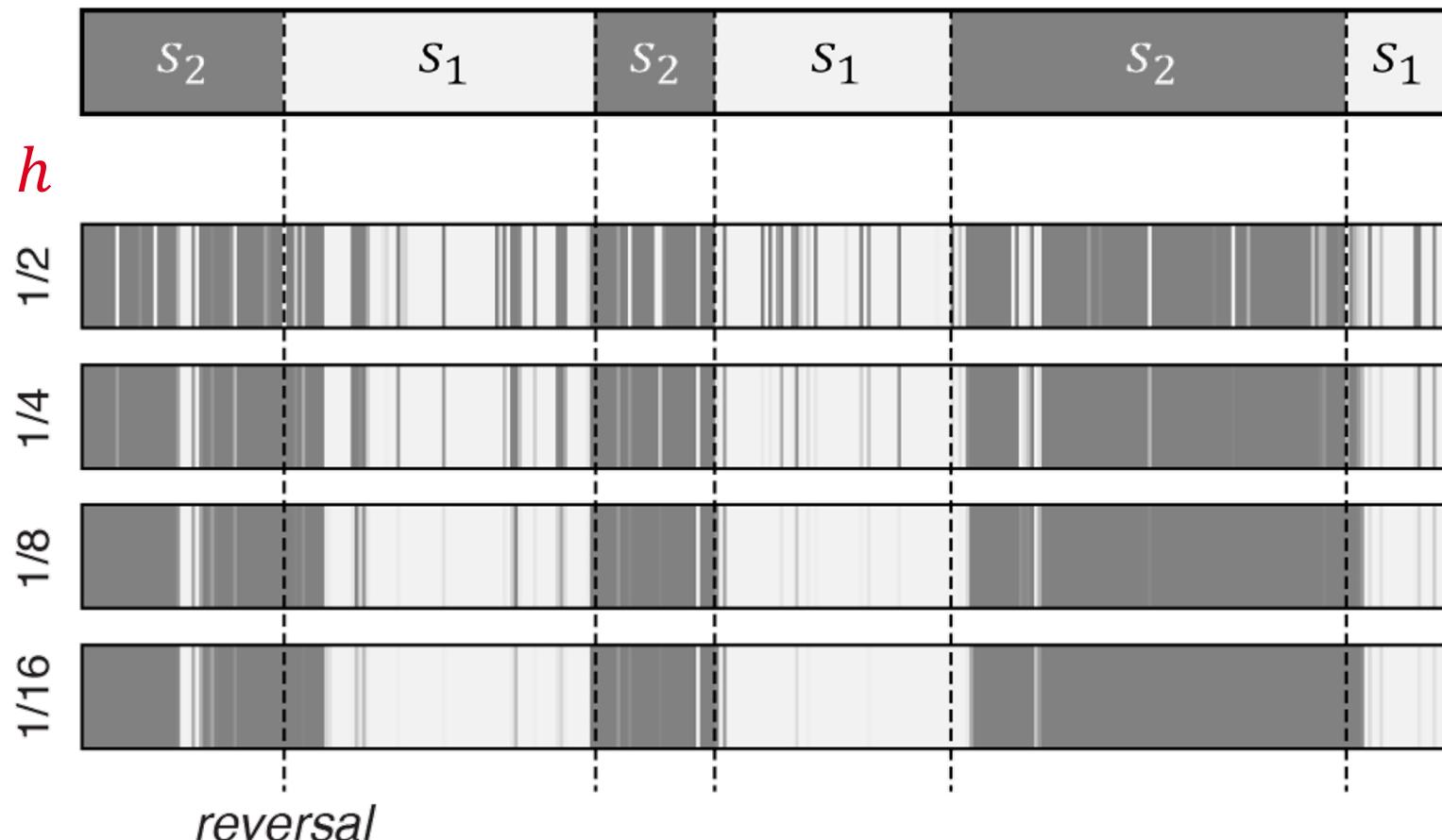


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Interacting with volatile environments stabilizes hidden-state inference

Case study 2: effect of controllability on decision-making

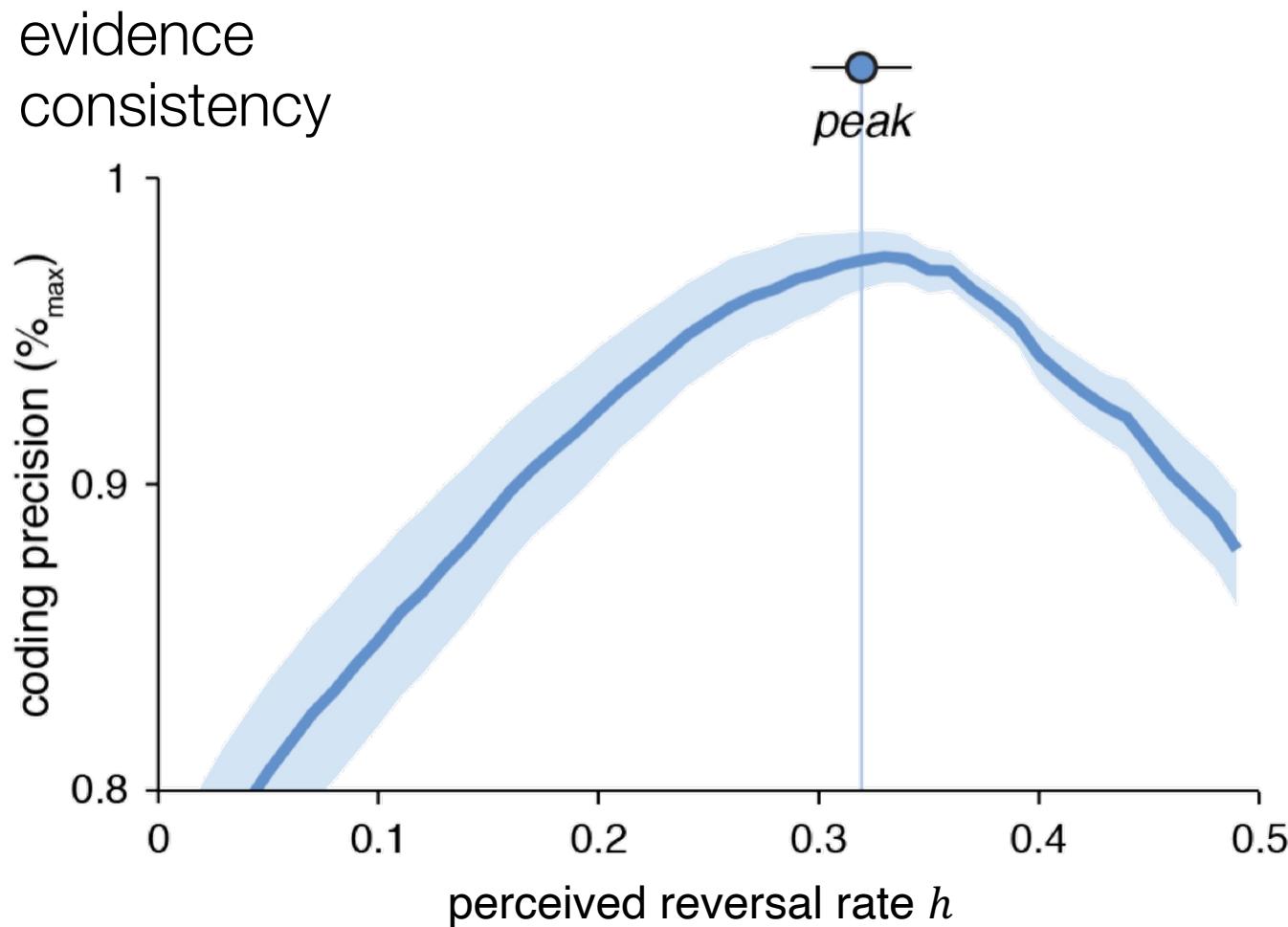
$$\text{belief } \mathcal{L}_t = \mathcal{F}(\mathcal{L}_{t-1}, \textcolor{red}{h}) + \ell_t + \varepsilon(\sigma)$$



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

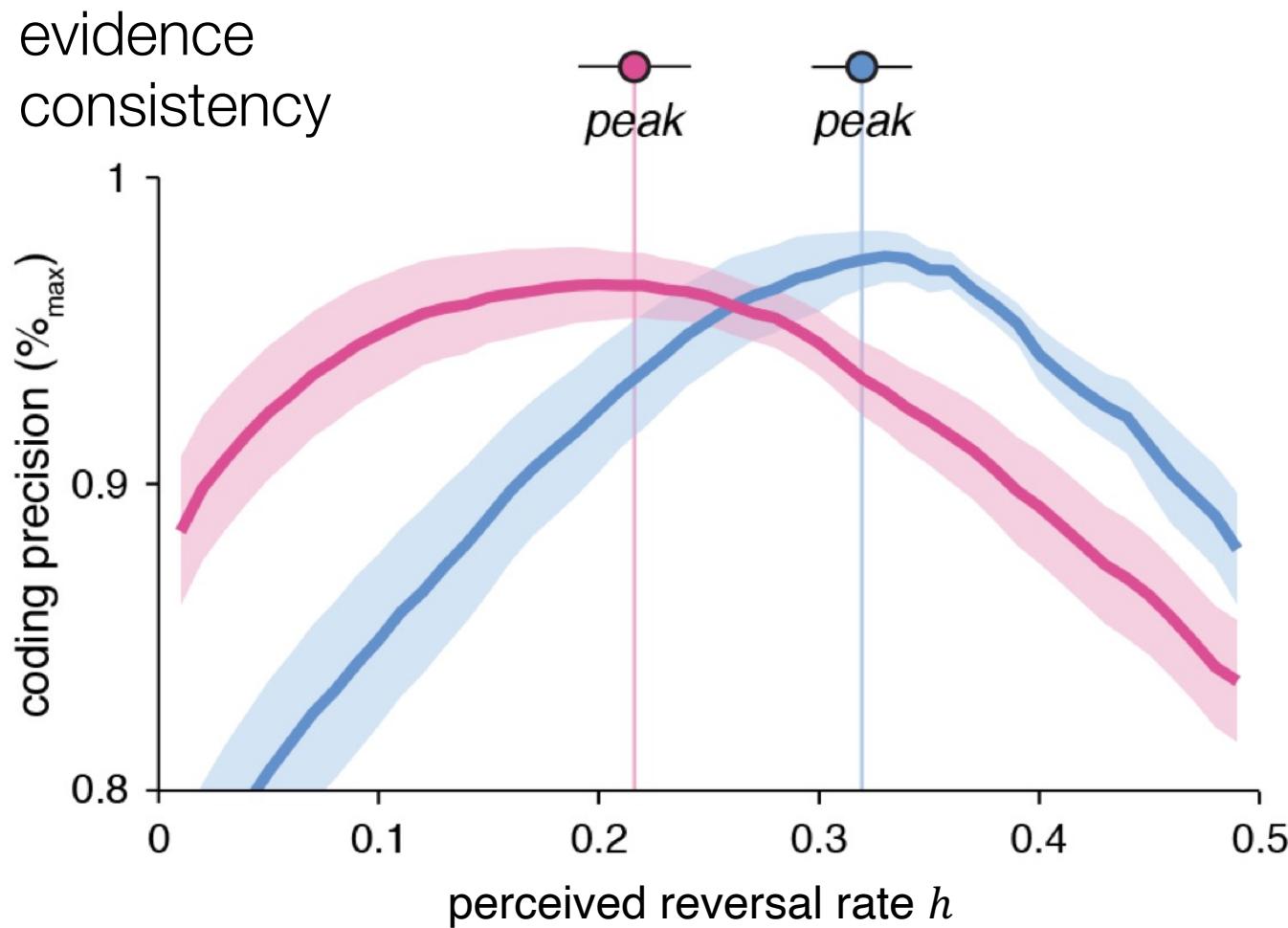
Case study 2: effect of controllability on decision-making



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

Case study 2: effect of controllability on decision-making



Weiss et al. (2021) *Nature Communications*

Interacting with volatile environments stabilizes hidden-state inference

Case study 2: effect of controllability on decision-making

MEG activity patterns support a specific effect of controllability on decision-making.

Mapping the source of MEG activity is not needed to draw this conclusion.

MEG activity is used to fit a parameter of hidden-state inference, not to map the MEG correlates of decision-making.

Beyond brain mapping

Is this approach perfectly conclusive? **NO**

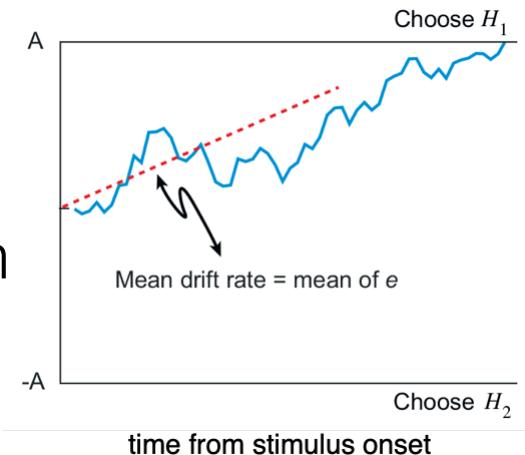
Brain data, as any type of data, provide empirical and partial support for a cognitive hypothesis.

Is this approach different from brain mapping? **YES**

It treats brain data not as a special type of data (to be explained), but as an additional observable for understanding cognition and behavior.

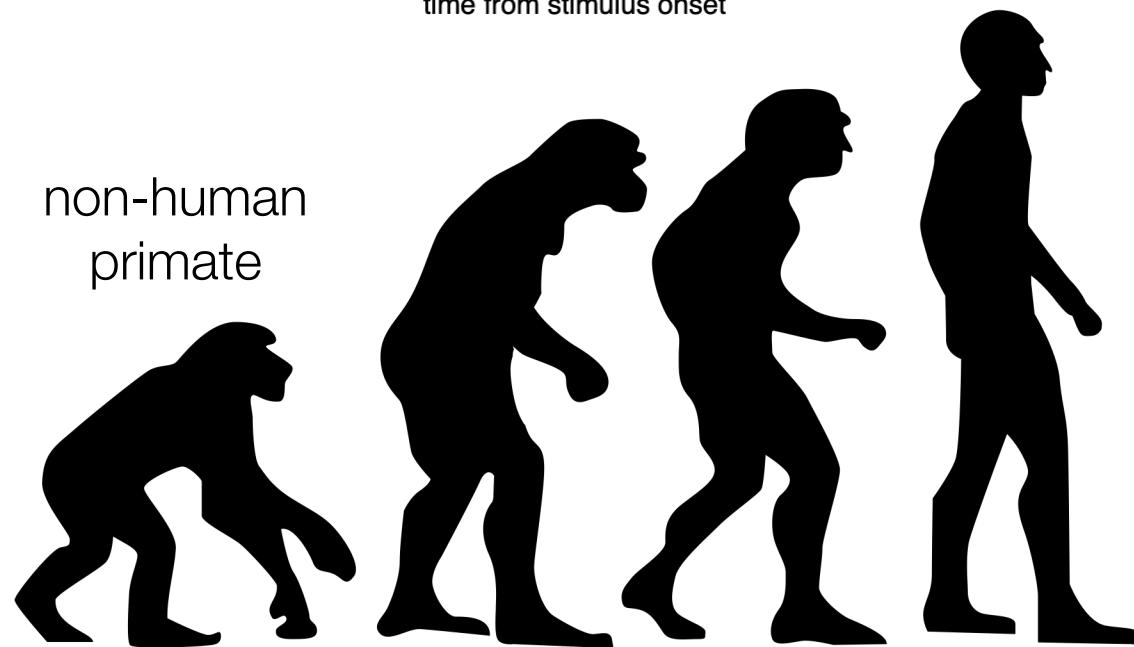
Beyond brain mapping

2
algorithm

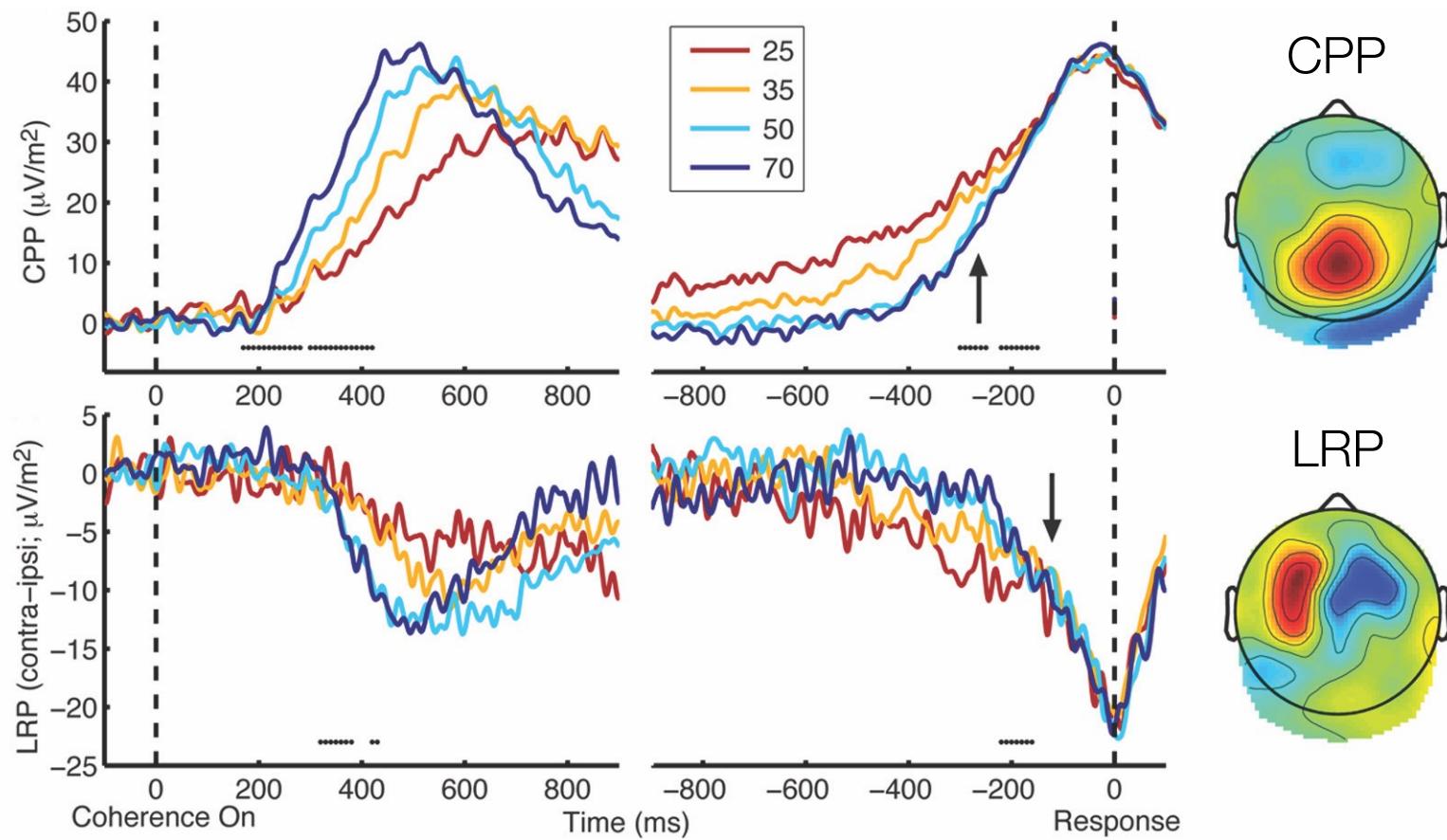


human

non-human
primate

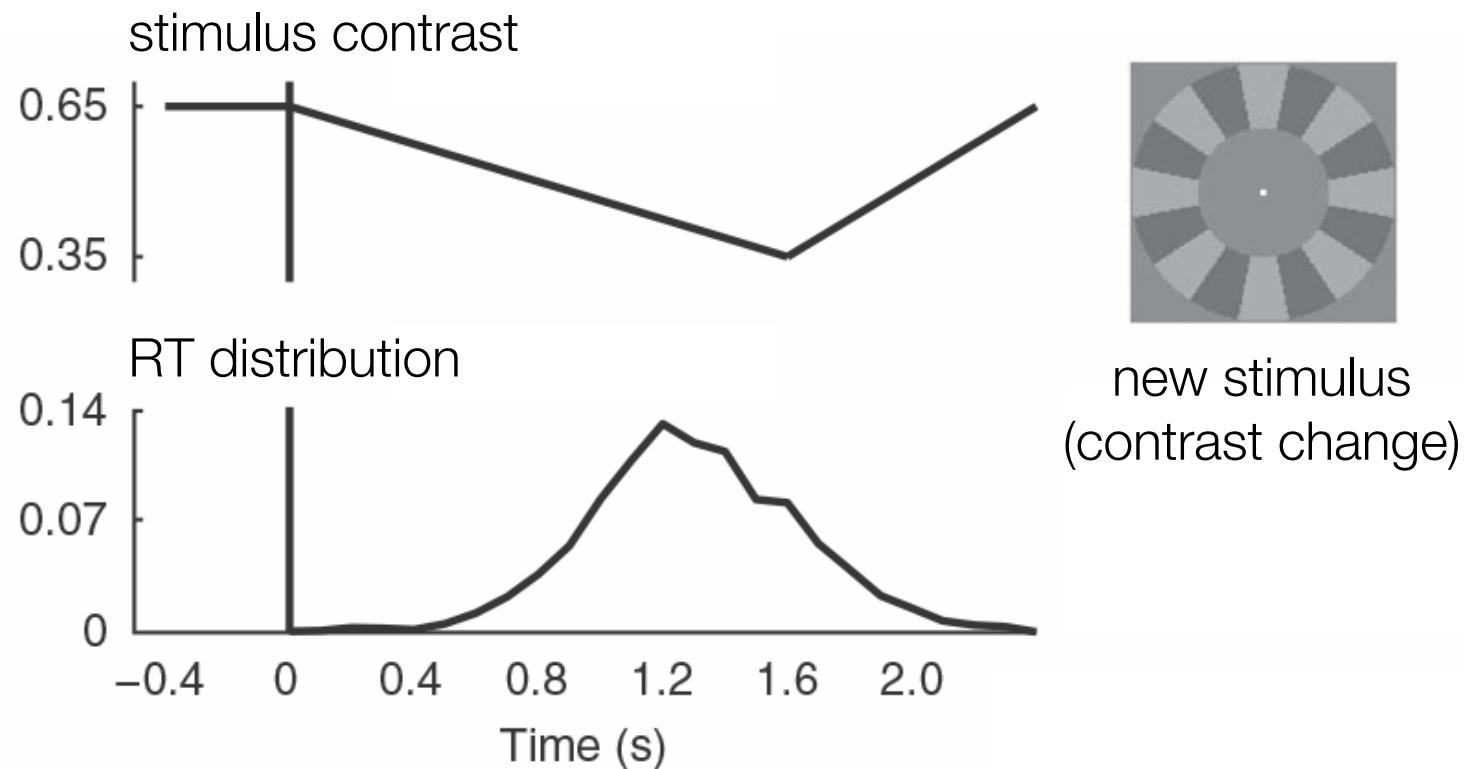


Beyond brain mapping



Kelly and O'Connell (2013) *Journal of Neuroscience*
Internal and external influences on the rate of sensory evidence accumulation

Beyond brain mapping

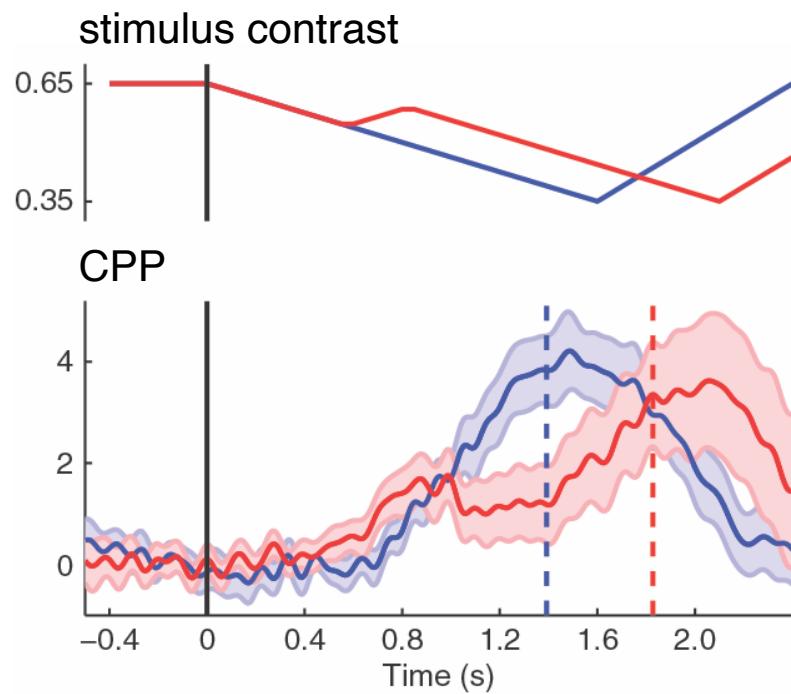


O'Connell et al. (2012) *Nature Neuroscience*

A supramodal accumulation-to-bound signal that determines perceptual decisions

Beyond brain mapping

button press
overt decision bound



O'Connell et al. (2012) *Nature Neuroscience*

A supramodal accumulation-to-bound signal that determines perceptual decisions

Beyond brain mapping

Practical requirements:

1. implement cognitive hypotheses in terms of
competing algorithms
2. develop experimental tasks where competing
algorithms make distinct predictions
3. use brain data not as dependent variables, but
for arbitrating between competing algorithms

**There is much more to cognitive neuroscience
than brain mapping and reverse inferences.**

Bayesian modeling... and how to use brain data to arbitrate between models of cognition

Valentin Wyart

LNC² / Inserm & Ecole Normale Supérieure
Université PSL, Paris, France

valentin.wyart@ens.fr