COMP 5700/6700/6706 Software Process Spring 2017

Outcomes Primary: To give you exposure to Test Driven Development

Background

We have been constructing code in class that implements the Student's t distribution based on the following equations:

$$prob = \begin{cases} if \ tails == 1: \left(\frac{\Gamma\left(\frac{n+1}{2}\right)}{\Gamma\left(\frac{n}{2}\right)\sqrt{n\pi}}\right) \int_{-\infty}^{t} \left(1 + \frac{u^2}{n}\right)^{-\left(\frac{n+1}{2}\right)} du \\ if \ tails == 2: \left(\frac{\Gamma\left(\frac{n+1}{2}\right)}{\Gamma\left(\frac{n}{2}\right)\sqrt{n\pi}}\right) \int_{-t}^{t} \left(1 + \frac{u^2}{n}\right)^{-\left(\frac{n+1}{2}\right)} du \end{cases}$$

Working in collaboration with our customer, we packaged our code in a class named "Sample" having the following public interface methods:

We determined that we needed to modularize the implementation of p, so we identified additional private support methods:

```
gamma(x)
calculateConstant(n)
f(u, n)
integrate(lowBound, highBound, n, f)
```

The accompanying files, Sample.py and SampleTest.py, contain code and corresponding tests for all the methods except integrate.

Use TDD to construct the method that performs the integration, integrate.

integrate calculates the area under the curve for the equation, $\left(1+\frac{u^2}{n}\right)^{-\left(\frac{n-2}{2}\right)}$

(Note that f implements the equation for you. You do not need to construct it.). Please implement integrate using Simpson's Rule for numerical integration. The algorithm is given in Python-like pseudocode below:

Note: epsilon may have to be adjusted to provide the desired amount of accuracy

The algorithm divides the curve into ${\tt s}$ slices and calculates the area of each slice based on a quadratic interpolation of points along the top of the curve. It then doubles the number of slices and recalculates the area. If the two calculations are not close enough in value – where "close enough" is defined by the value of epsilon – the number of slices is doubled and the area recalculated. This proceeds until the two values are within the prescribed error tolerance.

It isn't important to understand the mathematics underlying how the area is calculated. But, it is important to understand statement 8 in the pseudocode above. The number of terms to tally in statement 8 depends on how many times the curve is sliced, with each term having a coefficient of 1, 2, or 4. To illustrate this, suppose lowbound=0, highBound=16, and s=4. The value of n is unimportant for purposes of this discussion. The value of Statement 8 would be calculated as

```
simpsonNew = (4/3)*(f(0,n)+4f(4,n)+2f(8,n)+4f(12,n)+f(16,n))
```

If we were to double s to 8, Statement 8 would be calculated as

```
simpsonNew = (2/3) * (f(0,n)+4f(2,n)+2f(4,n)+4f(6,n)+2f(8,n)+4f(10,n)+2f(12,n)+4f(14,n)+f(16,n))
```

Note that the number of terms will be s+1. The beginning and final term have a coefficient of 1. The second, fourth, sixth, etc. term have a coefficient of 4. The third, fifth, seven, etc. term have a coefficient of 2.

Hints

- You'll see from the p method how integrate should be invoked. Notice that one of the parameters to integrate is a function.
- integrate may be tricky to test if you start by using $\left(1 + \frac{u^2}{n}\right)^{-\left(\frac{n+1}{2}\right)}$ in your initial TDD cycles. Consider using a size of the size of the

initial TDD cycles. Consider using a simpler integral, one that you know the result. In case you've forgotten your calculus, below are some sample functions and the result you should expect when integrating from 0 to t:

function	value of t	value of n	expected result		
<pre>def f(u, n): return u</pre>	1.0	doesn't matter	1/2		
<pre>def f(u, n): return u**2</pre>	1.0	doesn't matter	1/3		
<pre>def f(u, n): return u**6</pre>	1.0	doesn't matter	1/7		
<pre>def f(u, n): return u**100</pre>	1.0	doesn't matter	1/101		

Guidelines

- This effort is to be done on an individual basis. The code should be original.
 DO NOT use code from the Internet.
- Please accomplish this assignment as follows:
 - o Install the TDD plugin
 - o Copy Sample.py into your PyCharm Edu "softwareprocess" directory.
 - o Copy SampleTest.py into your test directory.
 - o Commit both files to your local git repository.
 - o Implement integrate() using TDD. Ensure you use the "red light" and "green light" buttons, not the "run" button.
 - When you are satisfied your assignment is complete, push your workspace to GitHub.

Grading Rubric	TDD	git log shows evidence of TDD git log shows some evidence of TDD git log shows little to no evidence of TDD Code is not available	+10 +5 +0 +0
	Tests	Passes all tests for p Fails one or more tests for p Code is not available	+10 +0 +0
	Algorithm	Code is not available	10
	, agontiiii	 integrate() fully implements the specified algorithm: Simpson's Rule <u>and</u> Convergent approach 	+10
		 integrate() produces a correct result, but partially implements the algorithm. Examples: Implements Simpson's rule, but doesn't adjust the number of slices (e.g., uses a fixed number of slices) 	+5

Uses some other method to calculate the area of each slice.
 integrate() is not functional, is missing, or is obviously incomplete.

Delivery

The submission conforms to instructions and can be tested without modification.

The submission was pushed to GitHub but must be modified to test
The submission was not pushed to GitHub.

+5

The submission was not pushed to GitHub.

+6

score = TDD + Tests + Algorithm + Delivery = max(40)

Extra Information

Selected values of the t-distribution are shown in the table below:

		p(a)=	0.6	0.7	0.85	0.9	0.95	0.975	0.99	0.995
		p(a/2)=	0.2	0.4	0.7	0.8	0.9	0.95	0.98	0.99
degrees of freedom	1		0.3249	0.7265	1.9626	3.0777	6.3138	12.7062	31.8205	63.6567
	2		0.2887	0.6172	1.3862	1.8856	2.9200	4.3027	6.9646	9.9248
	3		0.2767	0.5844	1.2498	1.6377	2.3534	3.1824	4.5407	5.8409
	4		0.2707	0.5686	1.1896	1.5332	2.1318	2.7764	3.7469	4.6041
	5		0.2672	0.5594	1.1558	1.4759	2.0150	2.5706	3.3649	4.0321
	6		0.2648	0.5534	1.1342	1.4398	1.9432	2.4469	3.1427	3.7074
	7		0.2632	0.5491	1.1192	1.4149	1.8946	2.3646	2.9980	3.4995
	8		0.2619	0.5459	1.1081	1.3968	1.8595	2.3060	2.8965	3.3554
	9		0.2610	0.5435	1.0997	1.3830	1.8331	2.2622	2.8214	3.2498
	10		0.2602	0.5415	1.0931	1.3722	1.8125	2.2281	2.7638	3.1693
	15		0.2579	0.5357	1.0735	1.3406	1.7531	2.1314	2.6025	2.9467
	20		0.2567	0.5329	1.0640	1.3253	1.7247	2.0860	2.5280	2.8453
	30		0.2556	0.5300	1.0547	1.3104	1.6973	2.0423	2.4573	2.7500

The table gives the one- and two-tailed probabilities for value of t at various degrees of freedom. For example, suppose we want to find the probability where t=1.1342 and degrees of freedom=6. Go along the row designed as "6" and find 1.1342. The top of column where 1.1342 was found gives the probabilities. "p(a)" indicates the probability for one tail and "p(a/2)" indicates the probability for two tails. Given this, the one-tailed probability is 0.85 and the two-tailed probability is 0.7.