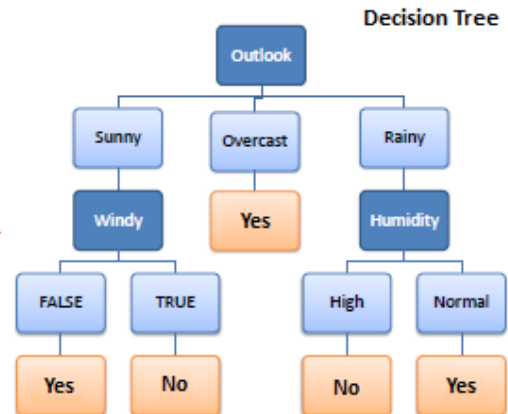


Predictors				Target
Outlook	Temp	Humidity	Windy	Play Golf
Rainy	Hot	High	False	No
Rainy	Hot	High	True	No
Overcast	Hot	High	False	Yes
Sunny	Mild	High	False	Yes
Sunny	Cool	Normal	False	Yes
Sunny	Cool	Normal	True	No
Overcast	Cool	Normal	True	Yes
Rainy	Mild	High	False	No
Rainy	Cool	Normal	False	Yes
Sunny	Mild	Normal	False	Yes
Rainy	Mild	Normal	True	Yes
Overcast	Mild	High	True	Yes
Overcast	Hot	Normal	False	Yes
Sunny	Mild	High	True	No



$$E(S) = \sum_{i=1}^c -p_i \log_2 p_i$$

Play Golf	
Yes	No
9	5



Entropy(PlayGolf) = Entropy(5,9)  
 = Entropy(0.36, 0.64)  
 = - (0.36 log<sub>2</sub> 0.36) - (0.64 log<sub>2</sub> 0.64)  
 = 0.94

$$E(T, X) = \sum_{c \in X} P(c)E(c)$$

		Play Golf		
		Yes	No	
Outlook	Sunny	3	2	5
	Overcast	4	0	4
	Rainy	2	3	5
				14



$$\begin{aligned}
 E(\text{PlayGolf}, \text{Outlook}) &= P(\text{Sunny}) \cdot E(3,2) + P(\text{Overcast}) \cdot E(4,0) + P(\text{Rainy}) \cdot E(2,3) \\
 &= (5/14) \cdot 0.971 + (4/14) \cdot 0.0 + (5/14) \cdot 0.971 \\
 &= 0.693
 \end{aligned}$$

$$\begin{aligned}
 \text{Entropy}(\text{PlayGolf}) &= \text{Entropy}(5,9) \\
 &= \text{Entropy}(0.36, 0.64) \\
 &= - (0.36 \log_2 0.36) - (0.64 \log_2 0.64) \\
 &= 0.94
 \end{aligned}$$

		Play Golf	
		Yes	No
Outlook	Sunny	3	2
	Overcast	4	0
	Rainy	2	3
		Gain = 0.247	

		Play Golf	
		Yes	No
Temp.	Hot	2	2
	Mild	4	2
	Cool	3	1
		Gain = 0.029	

		Play Golf	
		Yes	No
Humidity	High	3	4
	Normal	6	1
		Gain = 0.152	

		Play Golf	
		Yes	No
Windy	False	6	2
	True	3	3
		Gain = 0.048	

$$Gain(T, X) = Entropy(T) - Entropy(T, X)$$

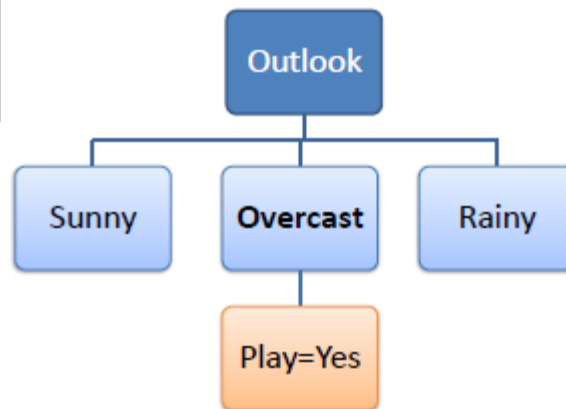
$$G(\text{PlayGolf}, \text{Outlook}) = E(\text{PlayGolf}) - E(\text{PlayGolf}, \text{Outlook})$$

$$= 0.940 - 0.693 = 0.247$$

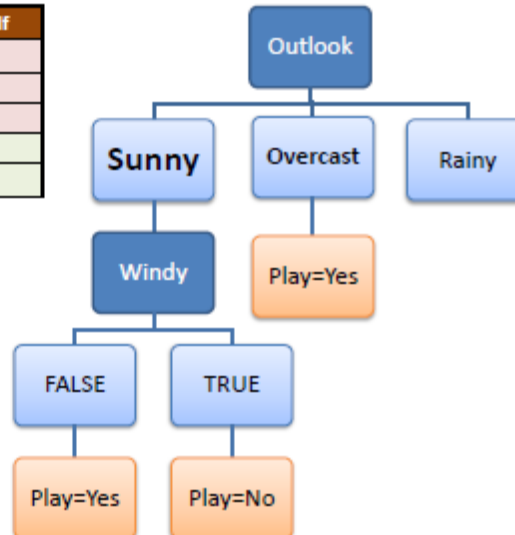
		Play Golf	
		Yes	No
Outlook	Sunny	3	2
	Overcast	4	0
	Rainy	2	3
Gain = 0.247			

		Outlook	Temp	Humidity	Windy	Play Golf
Outlook	Sunny	Sunny	Mild	High	FALSE	Yes
		Sunny	Cool	Normal	FALSE	Yes
		Sunny	Cool	Normal	TRUE	No
		Sunny	Mild	Normal	FALSE	Yes
		Sunny	Mild	High	TRUE	No
	Overcast	Overcast	Hot	High	FALSE	Yes
		Overcast	Cool	Normal	TRUE	Yes
		Overcast	Mild	High	TRUE	Yes
		Overcast	Hot	Normal	FALSE	Yes
	Rainy	Rainy	Hot	High	FALSE	No
		Rainy	Hot	High	TRUE	No
		Rainy	Mild	High	FALSE	No
		Rainy	Cool	Normal	FALSE	Yes
		Rainy	Mild	Normal	TRUE	Yes

Temp	Humidity	Windy	Play Golf
Hot	High	FALSE	Yes
Cool	Normal	TRUE	Yes
Mild	High	TRUE	Yes
Hot	Normal	FALSE	Yes



Temp	Humidity	Windy	Play Golf
Mild	High	FALSE	Yes
Cool	Normal	FALSE	Yes
Mild	Normal	FALSE	Yes
Cool	Normal	TRUE	No
Mild	High	TRUE	No



$R_1$ : IF (Outlook=Sunny) AND (Windy=FALSE) THEN Play=Yes

$R_2$ : IF (Outlook=Sunny) AND (Windy=TRUE) THEN Play=No

$R_3$ : IF (Outlook=Overcast) THEN Play=Yes

$R_4$ : IF (Outlook=Rainy) AND (Humidity=High) THEN Play=No

$R_5$ : IF (Outlook=Rain) AND (Humidity=Normal) THEN Play=Yes

