

# COMP9417 - Machine Learning

## Tutorial: Tree Learning

### Question 1. Expressiveness of Trees

Give decision trees to represent the following Boolean functions, where the variables  $A, B, C$  and  $D$  have values  $\mathbf{t}$  or  $\mathbf{f}$ , and the class value is either `True` or `False`. Can you observe any effect of the increasing complexity of the functions on the form of their expression as decision trees ?

- (a)  $A \wedge \neg B$
- (b)  $A \vee [B \wedge C]$
- (c)  $A \text{ XOR } B$
- (d)  $[A \wedge B] \vee [C \wedge D]$

### Question 2. Decision Tree Learning

- (a) Assume we learn a decision tree to predict class  $Y$  given attributes  $A, B$  and  $C$  from the following training set, with no pruning.

$A$	$B$	$C$	$Y$
0	0	0	0
0	0	1	0
0	0	1	0
0	1	0	0
0	1	1	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	0	1
1	1	1	0
1	1	1	1

What would be the training set error for this dataset ? Express your answer as the number of examples out of twelve that would be misclassified.

- (b) One nice feature of decision tree learners is that they can learn trees to do *multi-class* classification, i.e., where the problem is to learn to classify each instance into exactly one of  $k > 2$  classes. Suppose a decision tree is to be learned on an arbitrary set of data where each instance has a discrete class value in one of  $k > 2$  classes. What is the maximum training set error, expressed as a fraction, that any dataset could have ?

### Question 3. ID3 Algorithm

Here is small dataset for a two-class prediction task. There are 4 attributes, and the class is in the

rightmost column (homeworld). Look at the examples. Can you guess which attribute(s) will be most predictive of the class ?

species	rebel	age	ability	homeworld
pearl	yes	6000	regeneration	no
bismuth	yes	8000	regeneration	no
pearl	no	6000	weapon-summoning	no
garnet	yes	5000	regeneration	no
amethyst	no	6000	shapeshifting	no
amethyst	yes	5000	shapeshifting	no
garnet	yes	6000	weapon-summoning	no
diamond	no	6000	regeneration	yes
diamond	no	8000	regeneration	yes
amethyst	no	5000	shapeshifting	yes
pearl	no	8000	shapeshifting	yes
jasper	no	6000	weapon-summoning	yes

You probably guessed that attributes 3 and 4 were not very predictive of the class, which is true. However, you might be surprised to learn that attribute “species” has higher information gain than attribute “rebel”. Why is this ?

Suppose you are told the following: for attribute “species” the Information Gain is 0.52 and *Split Information* is 2.46, whereas for attribute “rebel” the Information Gain is 0.48 and *Split Information* is 0.98.

Which attribute would the decision-tree learning algorithm select as the split when using the *Gain Ratio* criterion instead of Information Gain ? Is Gain Ratio a better criterion than Information Gain in this case ?

#### Question 4. Working with Decision Trees

In `utils.py` you will find the implementation of the function `visualize_classifier` which allows us to visualise any classifier that has a `predict` method. You can use this function as a black box throughout. The `sklearn.datasets.make_blobs` function gives us a quick way to create toy data for classification. In the following we’ll create a 3 class classification problem:

```

1 from sklearn.datasets import make_blobs
2 X, y = make_blobs(n_samples=120,                                # total number of samples
3                  centers=[[0,0], [0,2], [-2,1]],                # cluster centers of the 3 classes
4                  random_state=123,                             # reproducibility
5                  cluster_std=0.6)                              # how spread out are the samples
6                  from their center
7 plt.scatter(X[:, 0], X[:, 1], c=y, s=50)                       # scatter with color=label
8 plt.show()
```

- Use `sklearn.neighbors.KNeighborsClassifier` and `sklearn.tree.DecisionTreeClassifier` objects to demonstrate the `visualize_classifier` function. Explain the differences between the decision boundaries of the two classifiers.
- Another way to visualise a tree can be done by running:

```

1 from sklearn import tree
2
3 fig, axes = plt.subplots(1, 1, figsize = (3,3), dpi=300)
4 tree.plot_tree(modell,                                     # fitted decision tree
5               feature_names=['f1', 'f2'],                  # names for features
```

```
6 class_names=['t1', 't2', 't3'], # names for class labels
7 filled=True)
8 plt.show()
9
```

Explain what is going on in the resulting plot. What do the colors represent? What does the `value` argument tell us? What about `entropy`?

(c) Generate data using the following code:

```
1 X, y = make_blobs(n_samples=500,
2                   centers=[[0,0], [0,2], [-2,1], [-2,2], [3,3], [1,-2]],
3                   random_state=123,
4                   cluster_std=0.6)
5
```

Then fit a decision tree (using information gain for splits) with `max_depth` set to  $1, 2, \dots, 12$  and visualize the classifier (use a  $3 \times 4$  grid). What do you observe? Why do you think decision trees are described as performing 'recursive partitioning'?