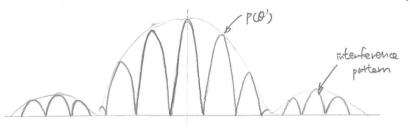


(i) if D~O, for normal incident light with wavelingth & (making long-term exposure) light sources A and B can be viewed as monochromatic light sources that have identical initial phase. photon number flux density at 0=0' on the screen

$$\frac{\cos(kx - \omega t + \phi_0)}{\text{Ea: electric field contributed}} + \frac{\cos(k(x + \Delta x) - \omega t + \phi_0)}{\text{Eb}}^2$$

auto-correlation. (long-term average over time is: 1) auto-correlation

= $\cos^2(kx - \omega t + \phi_0) + \cos^2(k(x+\Delta x) - \omega t + \phi_0) + 2\cos(kx - \omega t + \phi_0)\cos(k(x+\Delta x) - \omega t + \phi_0)$



cross-comelation using trigonometric identity: $\cos\theta\cos\varphi = \frac{1}{2}\left(\cos(\theta-\varphi) + \cos(\theta+\varphi)\right)$ cos (kax) + cos(zkx-zwt+zφo+kax) long-term time average is 0

27 · BsinO =mT. → m=1.3.5, ----0~型产

Amplitude equal to 1. At the minimum (05(kax) =-1 this cross-complation tom (together with the factor 2) can cancel the contribution of the auto-correlation

when D is not neglegibly small, the amplitude of the electric field contributed by each of the two slits is modulated by the factor $\frac{\sin(\pm kD\sin\theta')}{\pm k\sin\theta'}$, and corries an extra phase offset $\pm kD\sin\theta'$. Since the phase offsets are idential, the calculation of the intertenence pattern is not affected. The amplitude modulation can be expressed as a envelope factor P(O) in the final interference puttern:

(photon number flux dusity) Intertenence puttern can be

contribution of cross-cornelation larm

U= B = slit squantity

unit of expressed by $\frac{I(O')}{A} = P(O') \left[1 + \cos\left(\frac{2\pi}{\lambda}BO'\right) \right] = P(O') \left[1 + \cos\left(2\pi uO'\right) \right]$ wavelegger contribution of outo-conduction terms. As compared to choose-cornelation terms outo-cornelation terms outo-cornelation terms outo-cornelation terms outo-cornelation terms.

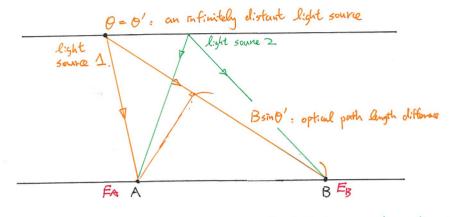
how bright is each of the light sounce

auto-comelation terms are less sonsita to angle of emengence O

when P(O') and u are known, making two independent measurements of I(O') (i.e., at two different O'positions) will allow unambiguously determining O' and A

Directly measuring the electric field strength $E_0 \cos (kx - \omega t + \phi_0)$ instead of photon number density, i.e., directly measuring $\{E_B = \cos (kx - \omega t + \phi_0)\}$ $\{E_B = \cos (k(x + \delta x)) - \omega t + \phi_0\}$ Then use correlator to evaluate $\{E_B^{-1}\}$, $\{E_B^{-1}\}$, $\{E_B^{-1}\}$, $\{E_B^{-1}\}$ or clenotes long-term time average.

Radio Interferometry



- (ii) when there is only one infinitely distant, monochromatic light source, the (EAEB) is exactly the same with the case of double slit
- (iii) When there are two light sources, denoted as light sources 1 and 2, then $E_B = E_B^{(1)} + E_B^{(2)}$ $E_B = E_B^{(1)} + E_B^{(2)}$

 $\langle (E_A + E_B) \rangle = \langle E_A^{(1)^2} \rangle + \langle E_B^{(2)} \rangle + \langle 2E_A^{(2)} E_B^{(2)} \rangle - interference pattern of source 1 alone .$ $<math>+ \langle E_A^{(2)^2} \rangle + \langle E_B^{(2)^2} \rangle + \langle 2E_A^{(2)} E_B^{(2)} \rangle - interference pattern of source 2 alone .$

+ < 2 EA EA > + < 2 EA EB > + < 2 EB EB > + < 2 EB EB > + < 2 EB EB >

if the two sources are not correlated, then the phase of these cross-term will rank randomly over time. In this case, the time overage of these cross-term over time is zero

Acoherent source
thermal noise is also acoherent source, of which the
expectation value is 0, but the noot-mean-square is
positively definite.

If we only look at the cross-correlation terms.

So a mefficient to describe how bright is the source

(EAEB) & \(\sum_{i=0}^{\infty} P(\theta_i) \) \(A_i \) (os (2\pi u \theta') \)

generalizing from descrete sources to continuous sources.

If there is a way to manually add an $\frac{1}{2}\pi$ phase to EB, (denoting phase shifted ase as EB) $(EA + EB')^2 = \left(\cos(kx - \omega t + \phi_0) + \cos(k(x + \Delta A) - \omega t + \phi_0 + \Xi')\right)^2$

 $= \left(\cos\left(kx - \omega t + \phi_0\right) + \cos\left(k(x + \Delta x) - \omega t + \phi_0\right)\cos\frac{\pi t}{2} - \sin\left(k(x + \Delta x) - \omega t + \phi_0\right)\sin\frac{\pi t}{2}\right)$

= $\cos^2(kx - \omega t + \beta) + \sin^2(k(x + \Delta x) - \omega t + \beta) - 2\cos(kx - \omega t + \beta) \sin(k(x + \Delta x) - \omega t + \beta)$

using trigonometric identity $(050 sin \varphi = \frac{1}{2} \left(sin(0+\varphi) - sin(0-\varphi) \right)$

 $sin(2kx-2at+2\phi_0+k\Delta x)$ - $sin(k\Delta x)$ long-term average is 0 sine correlation

generalizing from descrete sources to continuous sources

we can combine these measurements to yield the complex visibility

The outputs of cosine/sine comelators are the real/imaginary parts of the complex visibility. A complex visibility includes two independent mensurements. The flux clensity and position of a single point-source can be determined by one complex visibility.

Imaging: the ruversion from (FAFB) to P(O)A(O)

if we can vary the value of a continuously (i.e., changing the separation of the fun radio detectors), then we can make a complete fourier transform of P(O)A(O). In this case, ranging can be a simple inverse Fourier transform. Otherwis, we obtain incomplete samplings that requires a more compliate(3)

$$A(0) = \delta(\theta - \theta')$$

⇒ output of rosine correlator

complex gath $g \int P(\theta) S(\theta - \theta') \cos(2\pi u \theta) d\theta$ outsibuted by atmospheric and instrumental $= g P(\theta') \cos(2\pi u \theta')$ for any u effects.

similarly, the output of sine comelator is 9P(0') sin (27,40')

complex visibility = 9 P(0') (cos(2TUO') + i sin(2TUO'))

= 9 P(0') e 2 EUO', phase

uncalibrated visibility amplitude (e.g., in unit of volts)

Summary: for a point source, visibility amplitude does not vary with [4].

For a fixed source location O', phase depends linearly on U,

We can regard 27 U as the rate for the phase to vary with O'.

With a longer baseline length [4], phase will vary more rapidly with O'

1D linear radio intertenentes

Light source

Sin 01 = 11 sin 02

atmospheric attenuation e - Yorkin

N = nearly independent of frequency

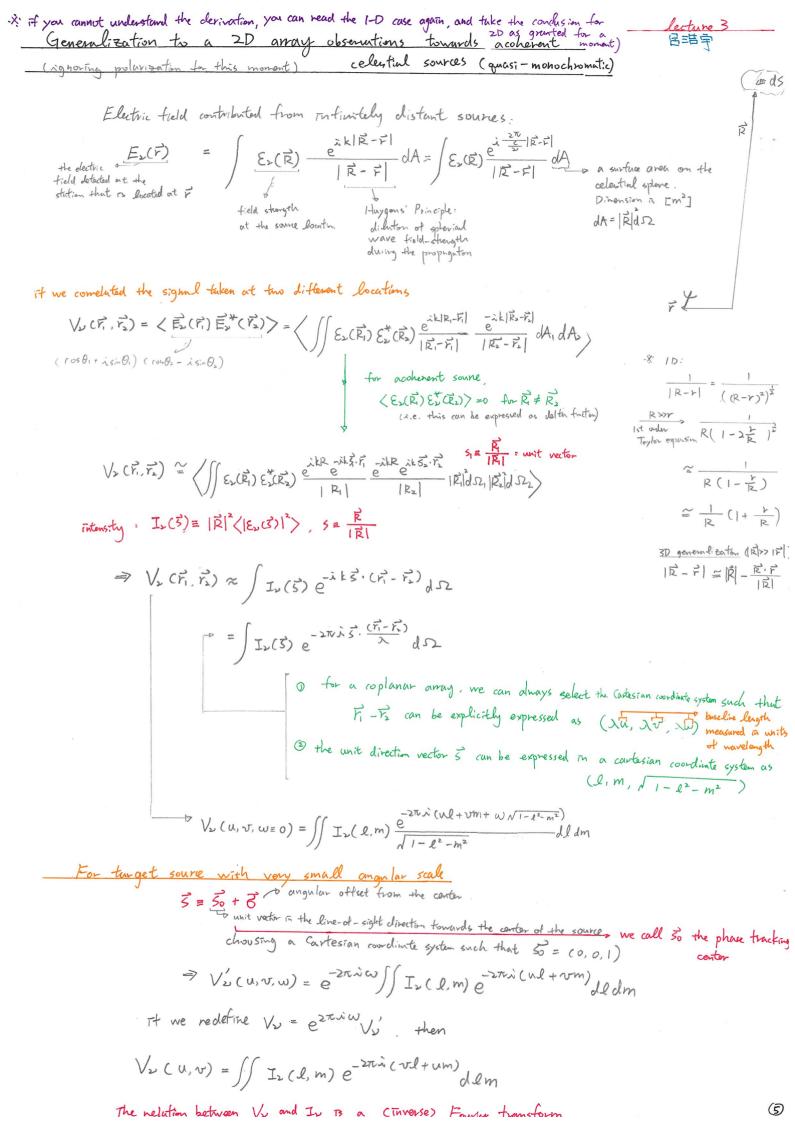
changing optical path length

A Y BY CY

Dy

Correlator

UAB, UAC, UAD, UBC, UBD, UCD, --The total number of inclipendut buseline is $\frac{1}{2}N(N-1)$ When designing an array, the less redundant is the sampling Unit (i.e. less repeats of the measurements at the sampling that the sampling construction.



The nelation between V2 and I2