

# Prepare Your Data

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#### Content outline

- Data quality
- Major tasks in Data preprocessing

# Data quality

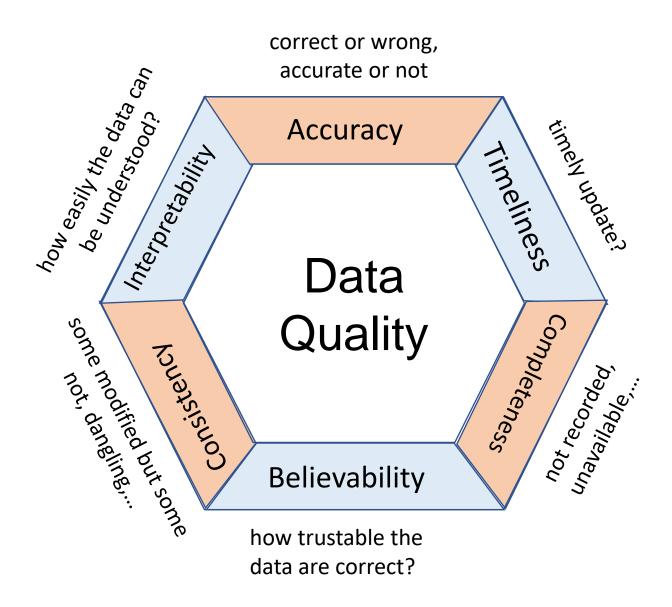
### An example of data analytics



- A branch manager analyzes the sales data by inspecting the company's data warehouse to include the necessary attributes.
- HOWEVER, the data being considered has many problems
  - Information needed for the analysis has not been recorded.
  - Many errors and unusual values for some transactions have been reported.

Inaccurate, incomplete, and inconsistent data are commonplace properties of large real-world databases and data warehouses

## Measures of data quality

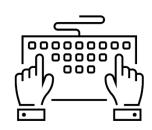


### Data accuracy

Inaccurate data means having incorrect attribute values.

Incorrect values submitted for mandatory fields

- E.g., negative weight, inappropriate range of ages, etc.
- Disguised missing data: many users have the same birthday, e.g., Jan 01





Faulty data collection instruments

Data transmission errors due to technology limitations



• E.g., limited buffer size for coordinating synchronized data transfer



Incorrect data may also result from inconsistencies

#### Data completeness

- The attributes of interest may not always be available or contain only aggregate data.
  - E.g., study the shopping habits in festive seasons while only the annual sales are available
- Many causes are leading to missing data.
  - Equipment malfunction
  - Some records are deleted due to inconsistency with other records.
  - Data is not entered due to misunderstanding.
  - Certain data may not be considered vital at the time of entry.
  - The recording of data history may have been overlooked.

#### Data consistency

- Inconsistencies in naming conventions or data codes
  - E.g., USA vs. US, alternative name (Bill Clinton vs. William Clinton), author name in reference: Li Fei-Fei vs. Fei-Fei, L.
- Incompatible formats for input fields
  - E.g., datetime format (dd/mm/yy vs. mm/dd/yy), rating scale ([1..5] vs. [1..10]), decimal and thousand separators
- Duplicate tuples also require data cleaning.

#### Data timeliness

- Suppose you are overseeing the data of monthly sales
- For a while after each month, the data stored is incomplete.
  - Several sales representatives fail to submit their sales records on time at the end of the month.
  - There are also some corrections and adjustments flowing in after the month's end.
- However, once all the data is received, it is correct.
- The month-end data are not updated in a timely fashion, harming the data quality.

## Believability and Interpretability

 Suppose that a database, at one point, had several errors, all of which have since been corrected.



Believability: how trustily is the data correct?

 E.g., the past errors had caused many problems for sales department users → they no longer trust the data



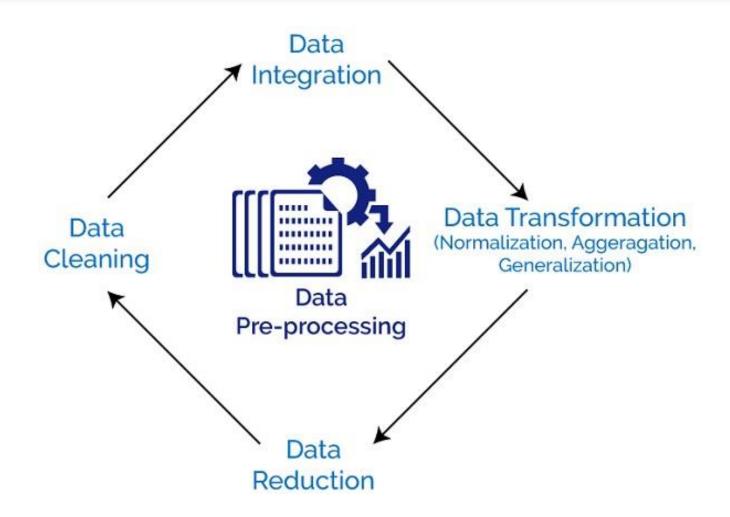
Interpretability: how easily is the data interpreted?

 E.g., the data use many accounting codes → the sales department does not know how to figure out

#### Data quality is subjective

- Data quality depends on the intended use of the data.
- Two users may assess the quality of a database differently.
- Consider a database in which some customer addresses are outdated or incorrect, yet overall, 80% of them are accurate.
  - A marketing analyst considers the database to be accurate enough for target marketing purposes.
  - However, a sales manager may consider the data inaccurate.

# Major tasks in Data preprocessing





# Data cleaning

## How to handle missing data?



#### Ignore the tuple

- Usually done when class label is missing
- Not effective when the percentage of missing values per attribute varies considerably

#### Fill in the missing value manually



Tedious and infeasible





- A global constant, e.g., "unknown" or a new class
- The attribute mean (for all samples of the same class)
- The most probable value: Bayesian approach or decision tree

## How to handle noisy data?

#### Binning and smoothing

- First sort data and partition into (equal-frequency) bins
- Then smooth each bin by its mean, median, or boundary, etc.

#### Regression

Smooth by fitting the data into regression functions

#### Clustering

Detect and remove outliers

#### **Hybrid**

Suspicious values are detected by computers and checked by human

# Binning and smoothing: An example

Consider the following sorted data points

15 21 21 24 25 28 34

Partition into equal-frequency bins

Bin 1: 15 21 Bin 2: 21 24

25

Smooth the bins

Bin 1: 8 Bin 1: 9 9

Bin 2: 21 21 21 Bin 2: 22 22 22

Bin 3: 29 29 29 Bin 3: 28 28 28

By medians

4 15 Bin 1: 4

28

34

Bin 2: 21 21 24

Bin 3: 25 25 34

By bin boundaries

Bin 3:

By means



# Data integration

#### Entity identification problem

- Entity identification problem arises during integration.
- Identify real world entities from multiple data sources
  - Differences in representation, scaling, or encoding
  - E.g., metric units in British system and other systems, currencies, grading scheme between schools, time format, etc.
- Matching attributes from one database to another following the ontological structure.
  - An attribute in one system is recorded at, say, a lower abstraction level than the "same" attribute in another.
  - E.g., "Total sales" may refer to one branch or to all stores in a region.
- Careful integration helps improve mining speed and quality.

## How to handle redundancy?

- Redundant data often occur when integrating databases.
- Object identification: The same attribute or object may have different names in various databases.
  - E.g., the occupation information may be stored in column "job" of the first database and column "career" of the second database.
- Derivable data: An attribute is derived from other attributes.
  - E.g., the annual revenue is the sum of monthly revenues.

# $\chi^2$ statistic for correlation analysis

- Suppose attribute A has c distinct values and attribute B has r distinct value. There are n data tuples.
- Let  $(A_i, B_j)$  denote the joint event that  $A = a_i$  and  $B = b_j$ .
- $\chi^2$  statistic tests the hypothesis that A and B are independent

$$\chi^{2} = \sum_{i=1}^{c} \sum_{j=1}^{r} \frac{\left(o_{ij} - e_{ij}\right)^{2}}{e_{ij}}$$

- $o_{ij}$ : observed frequency (i.e., actual count) of  $(A = a_i, B = b_j)$
- $e_{ij}$ : expected frequency of  $(A_i, B_j)$   $e_{ij} = \frac{count(A=a_i) \times count(B=b_j)}{n}$
- The larger  $\chi^2$  value, the more likely the variables are related.

# $\chi^2$ statistic: An example

Consider the below a contingency table

	male	female	Total
fiction	250 (90)	200 (360)	450
$non\_fiction$	50 (210)	1000 (840)	1050
Total	300	1200	1500

(Numbers in parenthesis are expected counts calculated based on the data distribution in the two categories)

Are gender and preferred\_reading correlated?

$$\chi^2 = \frac{(250 - 90)^2}{90} + \frac{(50 - 210)^2}{210} + \frac{(200 - 360)^2}{360} + \frac{(1000 - 840)^2}{840} = 507.93$$

- Two attributes are (strongly) correlated for the given group of people
- However, correlation does not imply causality.
  - # of hospitals and # of car-theft in a city are correlated
  - However, both are causally linked to the third variable population.

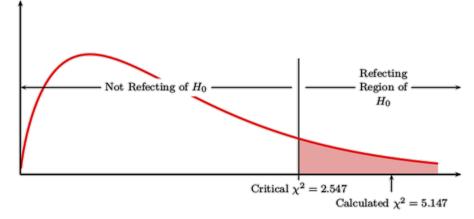
# $\chi^2$ statistic: Degrees of freedom

• The test is based on a significance level with a degrees of freedom

(DOF)  $(r - 1) \times (c - 1)$ .

If the hypothesis is denied,

A and B are statistically correlated.



Degrees of	Probability Probability										
Freedom	0.95	0.90	0.80	0.70	0.50	0.30	0.20	0.10	0.05	0.01	0.001
1	0.004	0.02	0.06	0.15	0.46	1.07	1.64	2.71	3.84	6.64	10.83
2	0.10	0.21	0.45	0.71	1.39	2.41	3.22	4.60	5.99	9.21	13.82
3	0.35	0.58	1.01	1.42	2.37	3.66	4.64	6.25	7.82	11.34	16.27
4	0.71	1.06	1.65	2.20	3.36	4.88	5.99	7.78	9.49	13.28	18.47
5	1.14	1.61	2.34	3.00	4.35	6.06	7.29	9.24	11.07	15.09	20.52
6	1.63	2.20	3.07	3.83	5.35	7.23	8.56	10.64	12.59	16.81	22.46
7	2.17	2.83	3.82	4.67	6.35	8.38	9.80	12.02	14.07	18.48	24.32
8	2.73	3.49	4.59	5.53	7.34	9.52	11.03	13.36	15.51	20.09	26.12
9	3.32	4.17	5.38	6.39	8.34	10.66	12.24	14.68	16.92	21.67	27.88
10	3.94	4.86	6.18	7.27	9.34	11.78	13.44	15.99	18.31	23.21	29.59
	Non-significant Non-significant						S	ignificant			

#### Pearson correlation coefficient

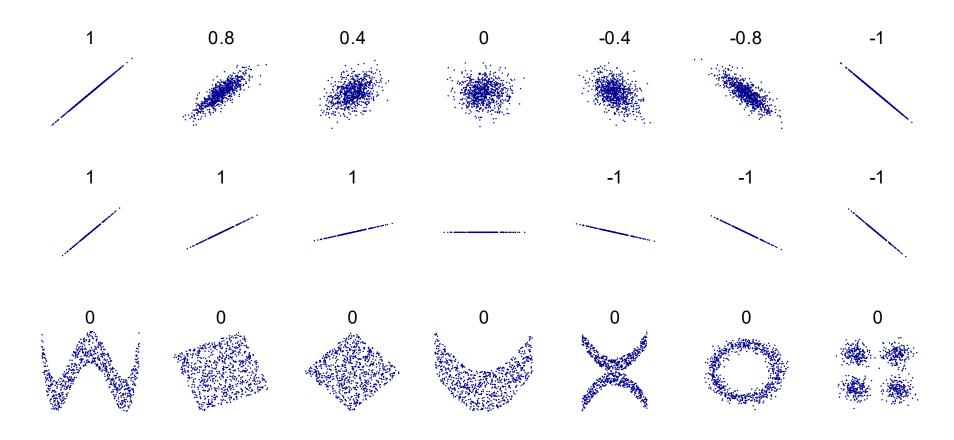
- Consider two numeric attributes A and B, and a set of n observations  $\{(a_1,b_1),...,(a_n,b_n)\}.$
- Pearson's product moment coefficient

$$r_{A,B} = \frac{\sum_{i=1}^{n} (a_i - \bar{A})(b_i - \bar{B})}{n\sigma_A \sigma_B} = \frac{(\sum_{i=1}^{n} a_i b_i) - n\bar{A}\bar{B}}{n\sigma_A \sigma_B}$$

- $\bar{A}$ ,  $\bar{B}$ ,  $\sigma_A$ ,  $\sigma_B$ : means and standard deviations of A and B, respectively
- $\Sigma a_i b_i$ : sum of the AB cross-product

$-1 \leftarrow r_{A,B}$	$r_{A,B}=0$	$r_{A,B} \rightarrow 1$		
Negative correlation	A and B are independent	Positive correlation		

#### Pearson correlation coefficient



Several sets of (x, y) points, with the Pearson correlation coefficient of x and y for each set. The correlation reflects the noisiness and direction of a linear relationship (top row), but not the slope of that relationship (middle), nor many aspects of nonlinear relationships (bottom). N.B.: the figure in the center has a slope of 0 but in that case the correlation coefficient is undefined because the variance of Y is zero. (Wikipedia)

# Covariance analysis

The covariance between A and B is defined as

$$Cov(A,B) = \frac{\sum_{i=1}^{n} (a_i - \bar{A})(b_i - \bar{B})}{n} = E(A \cdot B) - \bar{A}\bar{B}$$

• where  $E(A) = \bar{A} = \frac{\sum_{i=1}^n a_i}{n}$  and  $E(B) = \bar{B} = \frac{\sum_{i=1}^n b_i}{n}$  are the expected values of A and B

Cov(A, B) > 0	Cov(A, B) < 0	Cov(A,B)=0
Positive covariance	Negative covariance	A and B are independent

• Covariance vs. correlation:  $r_{A,B} = \frac{Cov(A,B)}{\sigma_A \sigma_B}$ 

## Covariance analysis: An example

 If the stocks are affected by the same industry trends, will their prices rise or fall together?

Stock Prices for AllElectronics and HighTech

Time point	AllElectronics	HighTech
t1	6	20
t2	5	10
t3	4	14
t4	3	5
t5	2	5

• 
$$E(AllElectronics) = \frac{6+5+4+3+2}{5} = \frac{20}{5} = $4$$

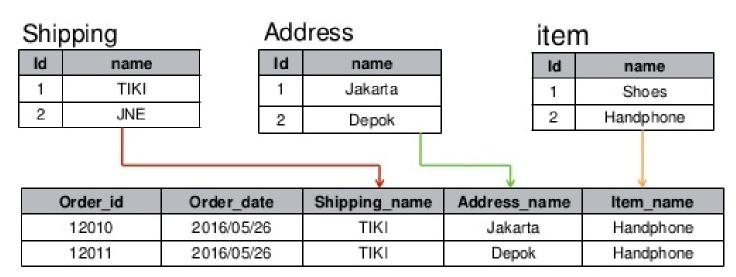
• 
$$E(HighTech) = \frac{20+10+14+5+5}{5} = \frac{54}{5} = $10.80$$

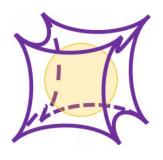
• 
$$Cov(AllElectronics, HighTech) = \frac{6 \times 20 + 5 \times 10 + 4 \times 14 + 3 \times 5 + 2 \times 5}{5} - 4 \times 10.80 = 7$$

 Therefore, a positive covariance indicates that stock prices for both companies rise together

## **Tuple duplication**

- Duplication should also be detected at the tuple level.
  - E.g., two or more identical tuples for a given unique data entry case.
- The use of denormalized tables (often done to improve performance by avoiding joins operation) is also a reason.
  - E.g., a purchase order database contains a purchaser's name and address instead of a key to this information in a purchaser database

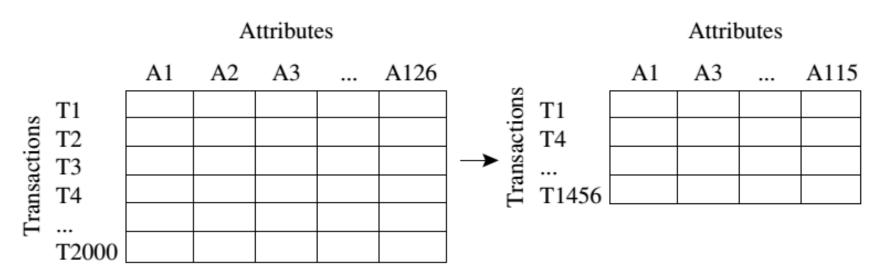




# Data reduction

## Why data reduction?

- A data collection stores terabytes of data → complex data analysis on the entire dataset may take a long time.
- Data reduction reduces the dataset in volume to achieve (almost) the same analytical results.



## Why data reduction?



Avoid the curse of dimensionality



Reduce time and space required in data mining



Eliminate irrelevant features and reduce noise



Allow easier visualization

#### Data reduction techniques

#### **Dimensionality reduction**

 Data encoding schemes are applied for a compressed representation of the original data.

#### Numerosity reduction

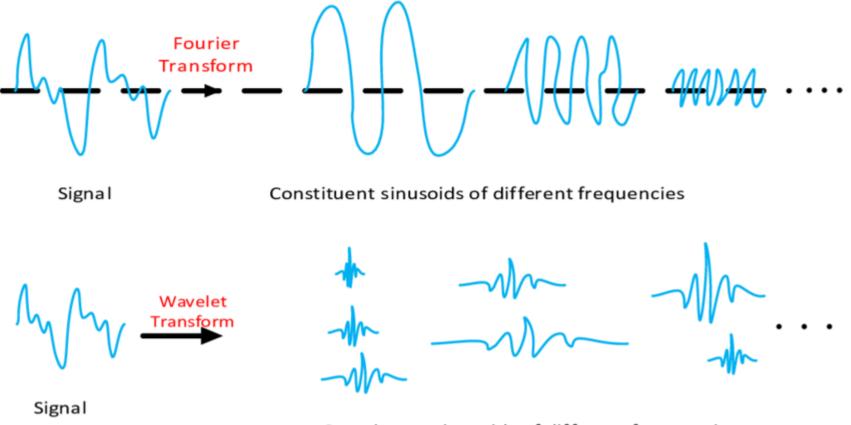
 Data volume is reduced by choosing alternative, smaller forms of data representation

#### Data compression

The data is encoded using fewer bits than the original representation.

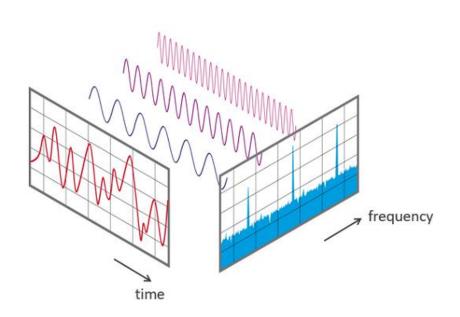
#### Mathematical transform

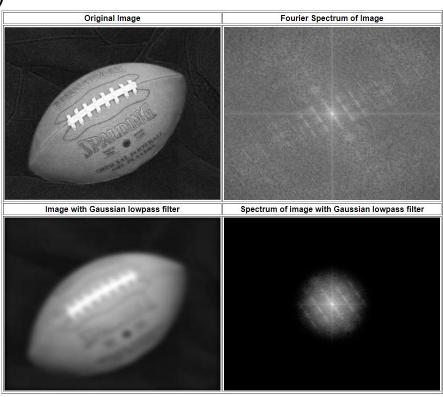
 Map the data to a new space and store only a small fraction of the strongest of the signal coefficients



#### Mathematical transform: DFT

- Discrete Fourier transform: decompose a function in time domain into the frequency one
  - E.g., decompose an audio wave in the time domain into its constituent frequencies and volume (amplitude)





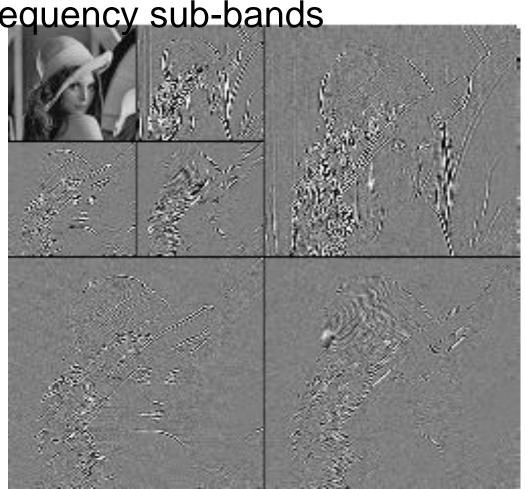
#### Mathematical transform: Wavelet

 Wavelet transform: decompose a (n-dimensional) signal into different frequency sub-bands

 Preserve relative distance between objects at different levels of resolution

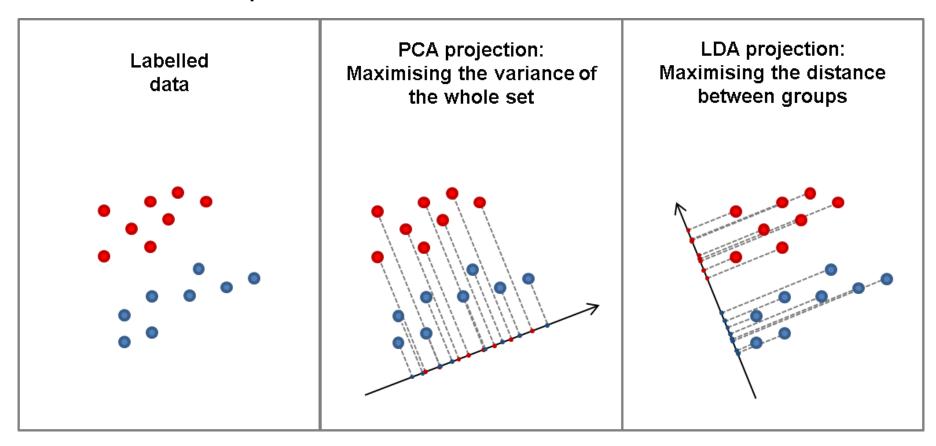
 Allow natural clusters to become more distinguishable

Used for image compression



## Subspace transform

 PCA and LDA both look for linear combinations of variables which best explain the data.

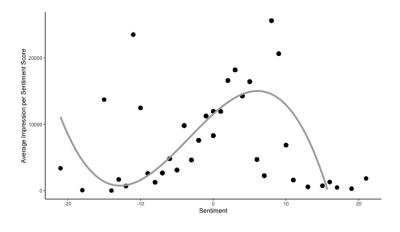


#### Attribute subset selection

- A way to remove redundant and/or irrelevant attributes
  - The purchase price of a product already includes the amount of sales tax paid → redundant
  - Predicting a student's GPA does not require his full name → irrelevant
- There are  $2^d$  possible attribute combinations of d attributes.

## Parametric numerosity reduction

Parametric methods stores only the model's parameters,
while discarding the original data (except possible outliers)

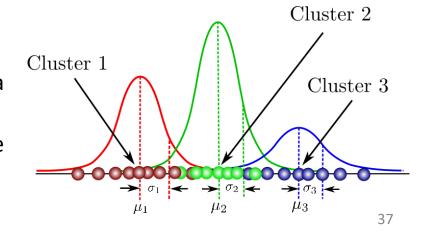


#### **Regression analysis**

- The parameters are estimated to give a "best fit" of the data
- The best fit is evaluated by using the least squares method or other criteria

#### Gaussian mixture model

- All data points are assumed to come from a mixture of Gaussian distributions
- The best fit is estimated by using the Expectation-Maximization algorithm.



## Non-parametric numerosity reduction

- Non-parametric methods do not assume models.
- A histogram divides the data into buckets and stores the average sum for each bucket
- Equal-width (distance) binning
  - Divide the range into N intervals of equal width, W = (B A)/N
    - where A and B are the lowest and highest values of the attribute
  - Outliers may dominate presentation, skewed data is not handled well
- Equal-depth (frequency) binning
  - Divide the range into N intervals, each containing approximately same number of samples → good data scaling

# Equal-frequency binning

## Histogram analysis: An example

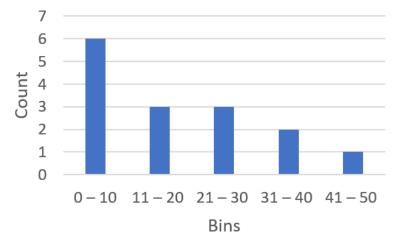
· Consider the values aside

Equal-width binning

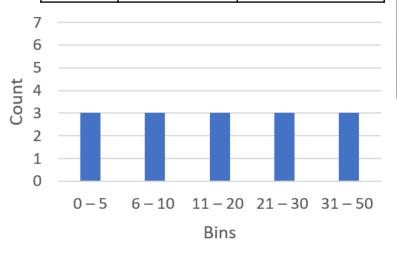
0, 2, 5, 8, 8, 10, 15, 15, 20, 25, 25, 30, 35, 40, 49

Partition the above data into 5 bins

	Bin range	Values
Bin 1	0 – 10	0, 2, 5, 8, 8, 10
Bin 2	11 – 20	15, 15, 20
Bin 3	21 – 30	25, 25, 30
Bin 4	31 – 40	35, 40
Bin 5	41 – 50	49

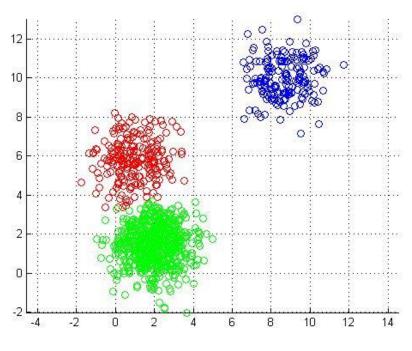


	Bin range	Values
Bin 1	0 – 5	0, 2, 5
Bin 2	6 – 10	8, 8, 10
Bin 3	11 – 20	15, 15, 20
Bin 4	21 – 30	25, 25, 30
Bin 5	31 – 50	35, 40, 49

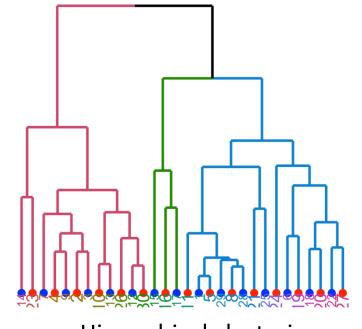


## Clustering

- Partition the data into clusters based on similarity, and store cluster representation (e.g., centroid and diameter) only
- Very effective if data is clustered but not if data is "smeared"



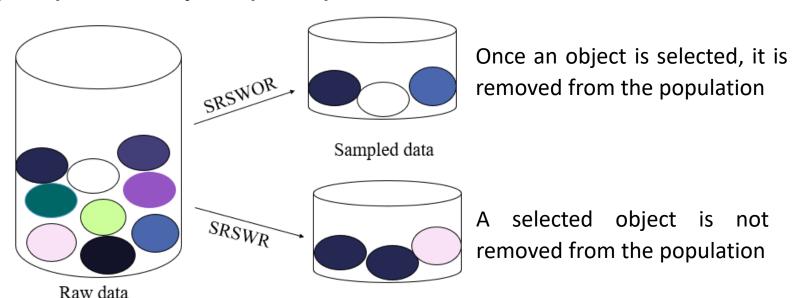
Distance-based clustering



Hierarchical clustering

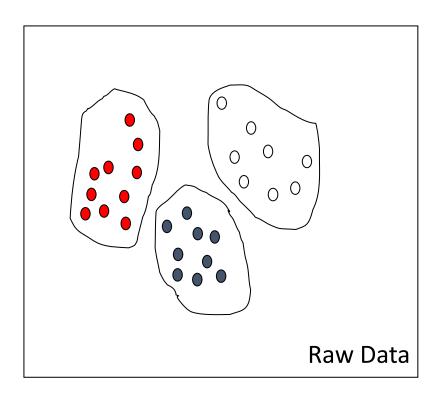
## Random sampling

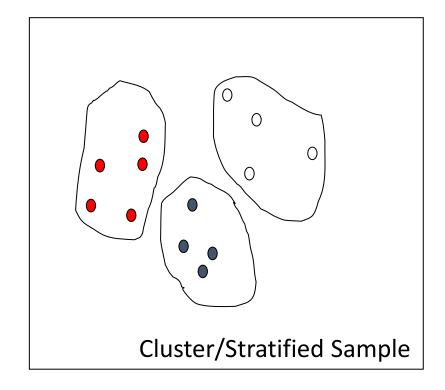
- Choose a representative subset s of the whole dataset D
- Allow a mining algorithm to run in complexity that is potentially sub-linear to the size of the data
- Simple random sampling: any item can be selected with an equal probability → poor performance in skewed data



## Stratified random sampling

 Partition the dataset and draw samples from each partition proportionally → good for skewed data





# Sampling: An example

#### Startified sample

(according to age)

T38	youth
T256	youth
T307	youth
T391	youth
T96	middle_aged
T117	middle_aged
T138	middle_aged
T263	middle_aged
T290	middle_aged
T308	middle_aged
T326	middle_aged
T387	middle_aged
T69	senior
T284	senior

T38	youth
T391	youth
T117	middle_aged
T138	middle_aged
T290	middle_aged
T326	middle_aged
T69	senior

T901

T201

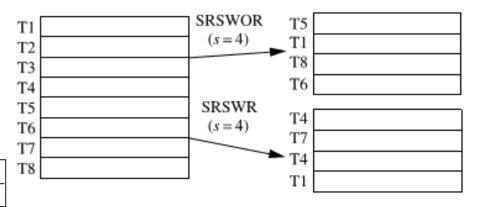
T101

T1

T2

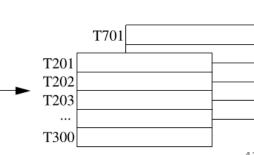
T3

T100

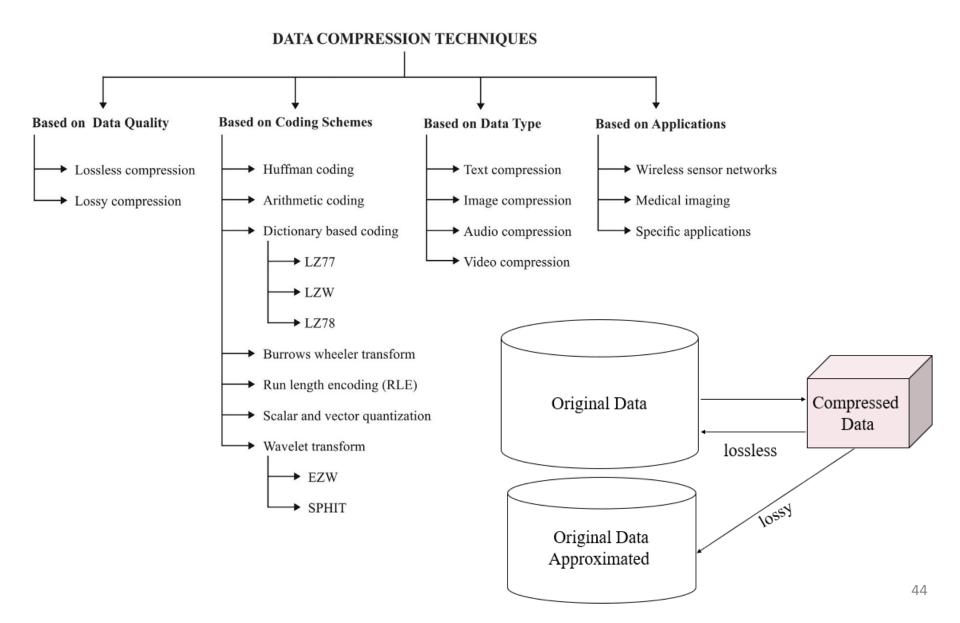


#### Cluster sample (s = 2)

T701 T201



# Data compression





# Data transformation

## Data normalization

- Let A be a numeric attribute with n observed values,  $v_1, \dots, v_n$
- Min-max normalization

$$v_i' = \frac{v_i - min_A}{max_A - min_A} (new\_max_A - new\_min_A) + new\_min_A$$

- where  $max_A$ ,  $new_max_A$ ,  $min_A$  and  $new_min_A$  are the original and modified maximum and minimum values of attribute A, respectively.
- Decimal scaling:  $v_i' = \frac{v_i}{10^j}$ 
  - where j is the smallest integer such that  $\max(|v_i'|) < 1$
  - Move the decimal point of values of A, in which the number of decimal points moved depends on the maximum absolute value of A

## Data normalization

- Z-score normalization:  $v_i' = \frac{v_i \mu_A}{\sigma_A}$ 
  - Where  $\mu_A$  and  $\sigma_A$  are the mean and standard deviation, respectively, of attribute A
- A variation that is more robust to outliers: replace  $\sigma_A$  by mean absolute deviation of A

$$s_A = \frac{1}{n}(|v_1 - \mu_A| + |v_2 - \mu_A| + \dots + |v_n - \mu_A|)$$

## Data normalization: An example

Consider the following sorted points

```
4 8 15 21 21 24 25 28 34
```

Perform min-max normalization to the new range [-1, 1]

```
• min = 4, max = 34, new_min = -1, new_max = 1
```

```
-1 -0.733 -0.267 0.133 0.133 0.333 0.4 0.6 1
```

Perform decimal scaling normalization

```
• max = 34 \rightarrow j = 2
```

```
0.04 0.08 0.15 0.21 0.21 0.24 0.25 0.28 0.34
```

Perform Z-score normalization

```
• mean = 20, std = 8.994
```

-1.779 -1.334 -0.556 0.111 0.111 0.445 0.556 0.889 1.557

### Data discretization

- The range of a continuous attribute is divided into intervals, whose labels are used to replace actual data values.
- It aims to reduce data size or prepare for further analysis.
- Typical methods can be applied recursively, such as clustering and histogram-binning.

## References

 Jiawei Han, Micheline Kamber, and Jian Pei, 2011. Data Mining: Concepts and Techniques (3rd ed.). Morgan Kaufmann Publishers Inc. Chapter 2.