

1. Examination time: 14:00-16:00.
2. Submission time: Please start to submit your source code by Tsinghua Web Learning (网络学堂) at least before 16:10. The submission site will be closed at 16:10. You may also submit your source code by USB drive to our TA if you cannot access internet. Please NOTE that late submissions are NOT accepted.
3. Submission requirement: Please follow the rules for our homework submission.

1. Segment tree (Credits 65%)

In computer science, a segment tree also known as a statistic tree is a tree data structure used for storing information about intervals, or segments [1]. It allows querying which of the stored segments contain a given point. For example, given the following segments: $[0, 3)$, $[2, 5)$, $[3, 7)$, $[5, 8)$, $[2, 8)$, $[8, 9)$, $[8, 18)$, $[12, 18)$, a query on point 3 returns the following segments: $[2, 5)$, $[3, 7)$, $[2, 8)$.

A segment tree T is a binary tree. Its leaves correspond to the elementary intervals in an ordered way: the leftmost leaf corresponds to the leftmost interval, and so on. The internal nodes of T correspond to intervals that are the union of elementary intervals: the interval $Int(N)$ corresponding to node N is the union of the intervals corresponding to the leaves of the tree rooted at N . Each node in T corresponds to the segments that span through its interval, but do not span through the interval of its parent. It is popular to implement a segment tree using an array due to its high efficiency. Attached is a sample implementation of the segment tree. Please improve the segment tree according to the following requirements:

(1) After calling `tree.search(3);` in `main.cpp`, there are 3 overlapping segments. Add a member variable named "`segIDs_`" in class `SegmentTree` to store the overlapping segments' ids. Then use stream operator overloading (`std::cout << tree << std::endl;`) to print the ids of the overlapping segments. Please note that each time

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function `tree.search` is called, `segIDs_` should be cleared first to store the new results. (10%)

(2) Using the added variable `segIDs_`, implement a member function to count the number of overlapping intervals for a given query point: `std::cout << tree.count(3) << std::endl;` (10%)

(3) Instead of adding member variables (`segIDs_`), implement a function object to obtain the ids of the overlapping segments. You may add new member functions if needed. A suggested format of using the function object is as follows: `void SegmentTree::search(const int& point, BaseFuncObj& callBackFunObjIds) const;` Then the ids could be printed by `cout << callBackFunObj << endl;`. (10%)

(4) Implement two more function objects. One is for directly counting the number of overlapping segments; the other is for immediately (as soon as the matched segment is found) printing the matched overlapping segments to standard output (prints the segment's `start_`, `end_` and `id_`, 每找到一个匹配就及时打印匹配信息). Using **polymorphism**, make all the three function objects work together with the following single search function:

```
void SegmentTree::search(const int& point, BaseFuncObj& callBackFunObj) const;
Moreover, the three function objects could also be printed by cout << callBackFunObj << endl;.
```

(20%)

(5) Make templates named `TSegmentTree` and `TNode`, which accept different types of "start_ and end_" (i.e. `long`), and different types of `id_` (i.e. `string`). Test the templates using the above-mentioned `long` and `string` types. (15%)

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2. Code reuse (Credits 35%)

From Wikipedia, the definition of a trie is as follows: "In computer science, a trie, also called digital tree and sometimes radix tree or prefix (前缀) tree (as they can be searched by prefixes), is an ordered tree data structure that is used to store a dynamic set or associative array where the keys are usually strings (以字符串为查询关键字)."

Read the given source code of a basic trie implementation and try to understand the code. Then write a subclass named `MyTrie` of the base class `BaseTrie` by **public inheritance**. The goal is to reuse the searching functions in class `BaseTrie` to search for all the strings stored in the trie structure matching a given prefix (在 trie 结构中搜索匹配某个前缀的所有字符串).

Requirements:

- (1) Write `MyTrie.h` and `MyTrie.cpp` for subclass (子类) `MyTrie` (check `main.cpp` for the required interfaces); (10%)
- (2) Add new code into `main.cpp` to test class `MyTrie`:
 - (a) Randomly generate 15 character strings of 8 alphabets (a~z) in length (随机生成 15 个字符串, 每个字符串长度为 8 个字符, 且由字母 a 至 z 组成). Insert the 15 character strings into the object of `MyTrie`, with each string corresponding to a different integer key value (每个字符串对应不同整数键值); (5%)
 - (b) Search all the character strings starting with a given prefix string (e.g. "a", "b", "c"), and print the strings to visually check (通过打印信息检查结果的正确性) that results are correct. (5%)
- (3) Write the destructors to avoid memory leaks (you may modify class `BaseTrie` if needed). (5%)

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(4) Use Adapter design pattern to implement another class named SuffixTrie, which adapts MyTrie for searching suffix strings (搜索匹配某个后缀的所有字符串). Randomly generate the character strings, and use a given suffix string for testing the correctness of the design. (10%)