## 3.1. MOTIVATIONS: LINEAR COMBINATIONS, LINEAR INDEPENDENCE, RANK59

This system has no solution since there is no point simultaneously contained in all three planes; see Figure 3.4.

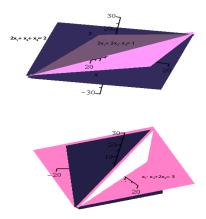


Figure 3.4: The linear system  $x_1 + 2x_2 - x_3 = 1$ ,  $2x_1 + x_2 + x_3 = 2$ ,  $x_1 - x_2 + 2x_3 = 3$  has no solution.

Finally, the planes corresponding to the system

$$x_1 + 2x_2 - x_3 = 3$$
$$2x_1 + x_2 + x_3 = 3$$
$$x_1 - x_2 + 2x_3 = 0,$$

are illustrated in Figure 3.5.

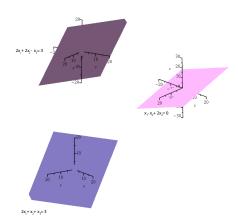


Figure 3.5: The planes defined by the equations  $x_1 + 2x_2 - x_3 = 3$ ,  $2x_1 + x_2 + x_3 = 3$ , and  $x_1 - x_2 + 2x_3 = 0$ .