

Observe that we did not compute the partial derivative with respect to w because it does not yield any useful information due to the presence of the term $\|w\|_2$ (as opposed to $\|w\|_2^2$). Our minimization problem is reduced to: find

$$\begin{aligned}
 & \inf_{w, \|w\| \leq 1} \left(w^\top \left(\sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right) + \gamma \|w\|_2 - \gamma \right) \\
 &= -\gamma - \gamma \inf_{w, \|w\| \leq 1} \left(-w^\top \frac{1}{\gamma} \left(\sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right) + \|-w\|_2 \right) \\
 &= \begin{cases} -\gamma & \text{if } \left\| \frac{1}{\gamma} \left(\sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right) \right\|_2^D \leq 1 \\ -\infty & \text{otherwise} \end{cases} \quad \text{by Example 50.8(6)} \\
 &= \begin{cases} -\gamma & \text{if } \left\| \sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right\|_2 \leq \gamma \\ -\infty & \text{otherwise.} \end{cases} \quad \text{since } \|\cdot\|_2^D = \|\cdot\|_2 \text{ and } \gamma > 0
 \end{aligned}$$

It is immediately verified that the above formula is still correct if $\gamma = 0$. Therefore

$$G(\lambda, \mu, \gamma) = \begin{cases} -\gamma & \text{if } \left\| \sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right\|_2 \leq \gamma \\ -\infty & \text{otherwise.} \end{cases}$$

Since $\left\| \sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right\|_2 \leq \gamma$ iff $-\gamma \leq -\left\| \sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right\|_2$, the dual program, maximizing $G(\lambda, \mu, \gamma)$, is equivalent to

$$\begin{aligned}
 & \text{maximize} && - \left\| \sum_{j=1}^q \mu_j v_j - \sum_{i=1}^p \lambda_i u_i \right\|_2 \\
 & \text{subject to} && \\
 & && \sum_{i=1}^p \lambda_i = 1, \quad \lambda_i \geq 0 \\
 & && \sum_{j=1}^q \mu_j = 1, \quad \mu_j \geq 0,
 \end{aligned}$$