



Figure 54.12: Running  $(\text{SVM}_{s2'})$  on two sets of 30 points;  $\nu = 0.51$ .

$p_f = 21, q_f = 21, p_m = 22, q_m = 23$ . Interestingly, for  $\nu = 0.7$ , we run into the singular situation where there are no support vectors.

For our next to the last run, Figure 54.14 shows the result of running the program with  $\nu = 0.95$ . We have  $p_f = 28, q_f = 28, p_m = 29, q_m = 29$ .

Figure 54.15 shows the result of running the program with  $\nu = 0.97$ . We have  $p_f = 29, q_f = 29, p_m = 30, q_m = 30$ , which shows that the largest margin has been achieved. However, after 80000 iterations the dual residual is less than  $10^{-12}$  but the primal residual is approximately  $10^{-4}$  (our tolerance for convergence is  $10^{-10}$ , which is quite high). Nevertheless the result is visually very good.

## 54.9 Soft Margin Support Vector Machines; $(\text{SVM}_{s3})$

In this section we consider a variation of Problem  $(\text{SVM}_{s2'})$  by adding the term  $(1/2)b^2$  to the objective function. The result is that in minimizing the Lagrangian to find the dual function  $G$ , not just  $w$  but also  $b$  is determined and  $\eta$  is determined under a mild condition on  $\nu$ . We also suppress the constraint  $\eta \geq 0$  which turns out to be redundant.