

Figure 54.5: Figure (1) illustrates the case of  $u_i$  contained in the margin and occurs when  $\epsilon_i = 0$ . Figure (1) also illustrates the case of  $v_j$  contained in the margin when  $\xi_j = 0$ . The left illustration of Figure (2) is when  $u_i$  is inside the margin yet still on the correct side of the separating hyperplane  $w^{\top}x - b = 0$ . Similarly,  $v_j$  is inside the margin on the correct side of the separating hyperplane. The right illustration depicts  $u_i$  and  $v_j$  on the separating hyperplane. Figure (3) illustrations a misclassification of  $u_i$  and  $v_j$ .

separating hyperplane  $H_{w,b}$ ; if  $\xi_j \leq \delta$ , then  $v_j$  is classified correctly, and if  $\xi_j > \delta$ , then  $v_j$  is misclassified ( $v_j$  lies on the wrong side of the separating hyperplane, the blue side). See Figure 54.5.

(3) If  $\lambda_i = 0$ , then  $\epsilon_i = 0$  and the *i*-th inequality may or may not be active, so

$$w^{\top}u_i - b - \delta > 0.$$

Thus  $u_i$  is in the closed half space on the blue side bounded by the blue margin hyperplane  $H_{w,b+\delta}$  (of course, classified correctly).

Similarly, if  $\mu_j = 0$ , then

$$w^{\mathsf{T}}v_i - b + \delta \leq 0$$

and  $v_j$  is in the closed half space on the red side bounded by the red margin hyperplane  $H_{w,b-\delta}$  (of course, classified correctly). See Figure 54.6.