## ${\bf Part~VI}$ Preliminaries for Optimization Theory