

Figure 38.2: The Sierpinski gasket, version 2

The result of 7 iterations starting from the line segment (-1,0), (1,0)), is shown in Figure 38.3. This curve converges to the boundary of the Sierpinski gasket.

A different kind of fractal is the *Heighway dragon*.

Example 38.3. The Heighway dragon is specified by the following two contractions:

$$x' = \frac{1}{2}x - \frac{1}{2}y,$$

$$y' = \frac{1}{2}x + \frac{1}{2}y,$$

$$x' = -\frac{1}{2}x - \frac{1}{2}y,$$

$$y' = \frac{1}{2}x - \frac{1}{2}y + 1.$$

It can be shown that for any number of iterations, the polygon does not cross itself. This means that no edge is traversed twice and that if a point is traversed twice, then this point is the endpoint of some edge. The result of 13 iterations, starting with the line segment ((0,0),(0,1)), is shown in Figure 38.4.

The Heighway dragon turns out to fill a closed and bounded set. It can also be shown that the plane can be tiled with copies of the Heighway dragon.

Another well known example is the *Koch curve*.