

If only R is desired, then `houseqr` does the job. In order to obtain R , we need to compose the Householder transformations. We present a simple method which is not the most efficient (there is a way to avoid multiplying explicitly the Householder matrices).

The function `buildhouse` creates a Householder reflection from a vector v .

```
function P = buildhouse(v,i)
% This function builds a Householder reflection
%   [I 0 ]
%   [0 PP]
%   from a Householder reflection
%   PP = I - 2uu*uu'
%   where uu = v(i:n)
%   If uu = 0 then P = I
%
n = size(v,1);
if v(i:n) == zeros(n - i + 1,1)
    P = eye(n);
else
    PP = eye(n - i + 1) - 2*v(i:n)*v(i:n)';
    P = [eye(i-1) zeros(i-1, n - i + 1); zeros(n - i + 1, i - 1) PP];
end
end
```

The function `buildQ` builds the matrix Q in the QR -decomposition of A .

```
function Q = buildQ(u)
% Builds the matrix Q in the QR decomposition
% of an nxn matrix A using Householder matrices,
% where u is a representation of the n - 1
% Householder reflection by a list u of vectors produced by
% houseqr
n = size(u,1);
Q = buildhouse(u(:,1),1);
for i = 2:n-1
    Q = Q*buildhouse(u(:,i),i);
end
end
```

The function `buildhouseQR` computes a QR -factorization of A . At the end, if some entries on the diagonal of R are negative, it creates a diagonal orthogonal matrix P such that PR has nonnegative diagonal entries, so that $A = (QP)(PR)$ is the desired QR -factorization of A .