

Figure 54.22: Running (SVM<sub>s4</sub>) on two sets of 30 points; K = 190.

Our second run was made with K = 1/12000; see Figure 54.23. We have  $p_m = 30$  and  $q_m = 30$  and we see that the width of the slab is a bit excessive. This example demonstrates that the margin lines need not contain data points.

## 54.15 Soft Margin SVM; (SVM $_{s5}$ )

In this section we consider the version of Problem (SVM<sub>s4</sub>) in which we add the term  $(1/2)b^2$  to the objective function. We also drop the constraint  $\eta \geq 0$  which is redundant.

Soft margin SVM (SVM $_{s5}$ ):

minimize 
$$\frac{1}{2}w^{\top}w + \frac{1}{2}b^{2} + (p+q)K_{s}\left(-\nu\eta + \frac{1}{p+q}(\epsilon^{\top}\epsilon + \xi^{\top}\xi)\right)$$
subject to 
$$w^{\top}u_{i} - b \geq \eta - \epsilon_{i}, \qquad i = 1, \dots, p$$
$$-w^{\top}v_{j} + b \geq \eta - \xi_{j}, \qquad j = 1, \dots, q,$$

where  $\nu$  and  $K_s$  are two given positive constants. As we saw earlier, it is convenient to pick  $K_s = 1/(p+q)$ . When writing a computer program, it is preferable to assume that  $K_s$  is arbitrary. In this case  $\nu$  must be replaced by  $(p+q)K_s\nu$  in all the formulae.

One of the advantages of this methods is that  $\epsilon$  is determined by  $\lambda$ ,  $\xi$  is determined by  $\mu$  (as in (SVM<sub>s4</sub>)), and both  $\eta$  and b determined by  $\lambda$  and  $\mu$ . As the previous method, this