

which is never null, and thus,  $\mu = 0$ , but since  $(\overrightarrow{a_0a_1}, \dots, \overrightarrow{a_0a_m})$  is a basis of  $\overrightarrow{E}$ , we must also have  $\lambda_i = 0$  for all  $i, 1 \leq i \leq m$ .

Given any element  $\langle x, \lambda \rangle \in \widehat{E}$ , if

$$x = a_0 + x_1 \overrightarrow{a_0a_1} + \dots + x_m \overrightarrow{a_0a_m}$$

over the affine frame  $(a_0, (\overrightarrow{a_0a_1}, \dots, \overrightarrow{a_0a_m}))$  in  $E$ , in view of the definition of  $\widehat{+}$ , we have

$$\begin{aligned} \langle x, \lambda \rangle &= \langle a_0 + x_1 \overrightarrow{a_0a_1} + \dots + x_m \overrightarrow{a_0a_m}, \lambda \rangle \\ &= \langle a_0, \lambda \rangle \widehat{+} \lambda x_1 \overrightarrow{a_0a_1} \widehat{+} \dots \widehat{+} \lambda x_m \overrightarrow{a_0a_m}, \end{aligned}$$

which shows that over the basis  $(\overrightarrow{a_0a_1}, \dots, \overrightarrow{a_0a_m}, a_0)$  in  $\widehat{E}$ , the coordinates of  $\langle x, \lambda \rangle$  are

$$(\lambda x_1, \dots, \lambda x_m, \lambda).$$

□

If  $(x_1, \dots, x_m)$  are the coordinates of  $x$  w.r.t. the affine frame  $(a_0, (\overrightarrow{a_0a_1}, \dots, \overrightarrow{a_0a_m}))$  in  $E$ , then  $(x_1, \dots, x_m, 1)$  are the coordinates of  $x$  in  $\widehat{E}$ , i.e., the last coordinate is 1, and if  $u$  has coordinates  $(u_1, \dots, u_m)$  with respect to the basis  $(\overrightarrow{a_0a_1}, \dots, \overrightarrow{a_0a_m})$  in  $\overrightarrow{E}$ , then  $u$  has coordinates  $(u_1, \dots, u_m, 0)$  in  $\widehat{E}$ , i.e., the last coordinate is 0. Figure 25.3 shows the affine frame  $(a_0, a_1, a_2)$  in  $E$  viewed as a basis in  $\widehat{E}$ .

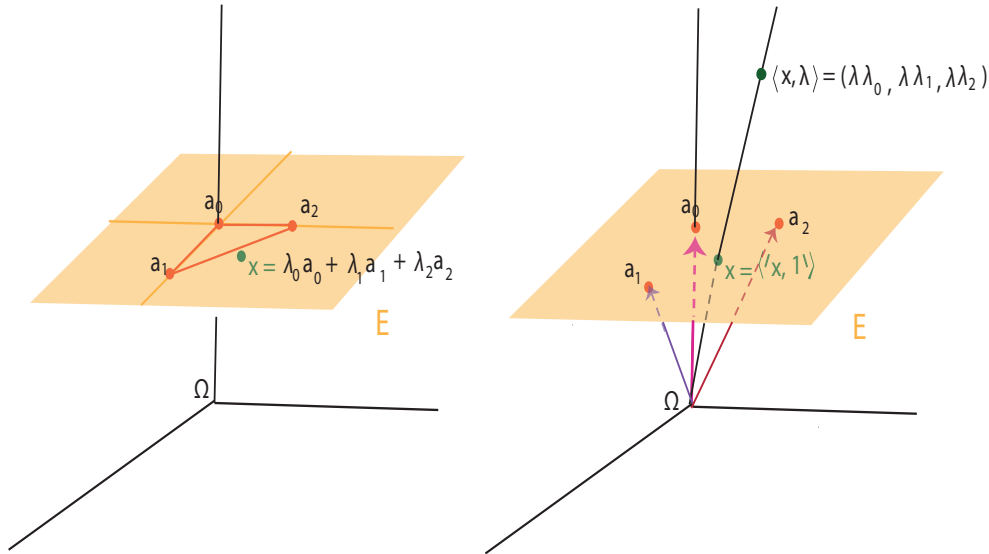


Figure 25.3: The basis  $(a_0, a_1, a_2)$  in  $\widehat{E}$ .