

Periodic Cataclysmic Variables in the Galactic Bulge: Application of the Gregory-Loredo Algorithm

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ABSTRACT

We present the discovery of 22 X-ray periodic sources in the Limiting Window (LW), a low-extinction region in the Galactic bulge, locating 80' south of the Galactic center. Their luminosities range ($10^{31} - 10^{33} \text{ erg s}^{-1}$) and period distribution (mostly between 1 to 3 hour), indicate they are cataclysmic variables (CVs). Most of them are polars with relatively harder spectrum, suggesting an unusual sub-class of mCVs. The brighter sources (6 out of 22 with $L > 10^{32} \text{ erg s}^{-1}$) in this sample are more likely IPs, with mean M_{WD} about $0.8 M_{\odot}$. We also proved that the Gregory-Loredo (GL) method used in this work has better sensitivity and data usage compared to the Lomb-Scargle (LS) method. In combination with the simulation and the geometry of accretion in CVs, we constrain the proportion of polars to X-ray sources in LW about 14%, and the fraction of DNe is about 45%, though with more uncertainty. Still, this discovery confirms the sub-type of unusual mCVs and provides a practical way to study the population about X-ray sources based on periodic modulation.

Key words: Galaxy: bulge — X-rays: stars — X-rays: binaries

1 INTRODUCTION

Cataclysmic variables (CVs) are close binary including a white dwarf (WD) and a main-sequence or sub-giant companion, whose material could be accreted by Roche-lobe overflow or stellar wind. They can be divided into magnetic (mCVs) and nonmagnetic CVs (non-mCVs) according to their magnetic field strengths of WDs. In addition, the mCVs are split into polars ($P_{spin}/P_{orb} \simeq 1$) and IPs ($P_{spin}/P_{orb} \simeq 0.01 - 1$), depending on their level of synchronization. The evolution of CVs are driven by angular momentum losses (AML) to keep the period from expanding, which would make system detached. The existence of "period gap" is caused by the change of mechanism for angular momentum losses. The dominant AML mechanism in long-period systems ($P_{orb} \geq 3 \text{ hour}$) is "magnetic braking", whereas short-period CVs ($P_{orb} \leq 2 \text{ hour}$) are driven by gravitational radiation. Meanwhile, there is a minimum period of CVs, resulted from the mass-loss-induced loss of thermal equilibrium in companion star. The orbital period of CVs are mainly between 1 to 10 hours, making it suitable for X-ray timing analysis.

Add a paragraph here to state how CVs can be used as a probe for the parent stellar populations and the dynamical environment. Then the logical flow into the next paragraphs will highlight the relevance of the GB/LW.

It has been proved that the collective properties of CVs serve as great probe for dynamic interactions of their local environment, contributed from the high abundance of WDs in binaries. The effect

would be remarkable only with extremely high stellar density (e.g. galactic center or global clusters (Cheng et al. 2019)) for us obtaining observable evidence in Hubble time. In addition to that, the individual properties of CVs provide hints for the accretion region and magnetic field, especially from their periodic variability.

It has been suggested that the thousands of X-ray sources in galactic center are magnetic cataclysmic variables, particularly intermediate polars (IPs) (Muno et al. 2009; Zhu et al. 2018). Due to the lack of optical/infrared imaging and spectroscopy resulted from high extinction and source crowding, the direct identification of them has been really difficult. In fact, even the presence and characteristics of the He II $\lambda 4686$ and $H\beta$ line have been often used to judge if a CV is magnetic or not, the proof is far from conclusive. In Silber (1992), many IPs with weak $H\beta$ lines could not be identified from non-magnetic systems using this diagnostic. Hence the periodicity becomes a well recognized probe to study their population, because of their different features in periodic modulation (see section ??).

In Muno et al. (2003), eight periodic sources were identified as mCVs in galactic center region (GCR). Then for galactic bulge region, ten periodic sources were found by using Lomb-Scargle methods (Hong et al. 2012). They were believed as an unusual type of mCVs with harder spectra like IPs while their period distribution resembles that of polars. The research was based on the observation of low-extinction Window fields (LW), locating at $1^{\circ}4$ south of the Galactic center. Its rarity of avoiding the obscuration from molecular cloud deserved our deeper excavation of these X-ray sources. Besides, according to RK catalog (Ritter & Kolb 2003), the mCVs

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(mostly DNe) occupied 20% in CVs sample, while for GCR, this fraction was reckoned over 30-40% (Hailey et al. 2016; Hong et al. 2012). The miss of non-mCVs demands reliable explanation from analyzing the properties of these sources. It may indicate that a large number of non-mCVs still awaits discovery since faint class can be always missed in flux-limited surveys.

In this work, we have taken full usage of *Chandra* observations for LW. Meanwhile, the methods with more efficiency and the simulation with higher accuracy have been both operated. We explored the X-ray properties of 22 periodic sources (ten of them identified in Hong et al. (2012)). Section 2 describes the observation we used and the source detection process. Section 3 gives a brief overview about the main methods for period finding and focuses on the GL method we adopted in this work. Section ?? is devoted to the operation process of period finding and long timescale variability analysis. Also it addresses the detection completeness obtained from simulation. Section 5 presents the spectra analysis for these periodic sources and the estimation of mass of WDs based on the Fe line diagnostic. Section ?? deliberates over the nature of these periodic sources based on their phase-folded light curve. The comparison with previous work and the X-ray source population in the LW would be summarized in Section 6.

2 X-RAY DATA PREPARATION

2.1 *Chandra* observations

The LW towards the inner Galactic bulge has been extensively observed by *Chandra* with its Advanced CCD Imaging Spectrometer (ACIS). A total of 13 ACIS-I observations were taken, three in 2005 and ten in 2008, resulting in a total exposure of 982 ks. A log of these observations is given in Table 1. A number of previous studies have made use of all or part of these observations, which primarily focused on the identification of discrete X-ray sources and the quantification of their statistical properties (Revnivtsev et al. 2009; van den Berg et al. 2009; Hong et al. 2009; Revnivtsev et al. 2011; Hong 2012; Morihana et al. 2013; Wevers et al. 2016).

We downloaded and uniformly reprocessed the archival data with CIAO v4.10 and CALDB v4.8.1, following the standard procedure¹. The CIAO tool *reproject_aspect* was employed to align the relative astrometry among the individual observations, by matching the centroids of commonly detected point sources. ObsID 9502, which has the longest exposure (164.1 ks), served as the reference frame. The level 2 event file was created for each ObsID, with the arrival time of each event corrected to the Solar System barycenter (i.e., Temps Dynamique Barycentrique time) by using the CIAO tool *xbary*. We then constructed a merged event list, reprojecting all events to a common tangential point, [R.A., Decl.]=[267.86375, 29.58475]. The individual observations cover a similar field-of-view (FoV) due to their similar aimpoints and roll angles, as illustrated in Figure 1 which displays the merged 2–8 keV counts image. We have examined the light curve of each ObsID and found that the instrumental background was quiescent for the vast majority of time intervals. Hence we preserved all the science exposures for source detection and subsequent timing analysis, taking the advantage of uninterrupted signals within each observation.

2.2 Source detection

It is known that the LW suffers from moderate line-of-sight extinction, $N_H \approx 7 \times 10^{21} \text{ cm}^{-2}$ (Revnivtsev et al. 2011), which obscures X-ray photons with energies $\lesssim 1 \text{ keV}$. Here we focus on sources prominent in the 2–8 keV band, which are most likely CVs located in the Galactic bulge. This will also facilitate a direct comparison with the CVs found in the Nuclear Star Cluster (Zhu et al. 2018), the line-of-sight column density of which, $N_H \sim 10^{23} \text{ cm}^{-2}$, is only transparent to photons with energies $\gtrsim 2 \text{ keV}$.

Source detection was performed following the procedures detailed in Zhu et al. (2018). Briefly, we first generated for each observation an exposure map as well as point-spread function (PSF) maps with enclosed count fraction (ECF) of 50% and 90%. Both the exposure and PSF maps were weighted by a fiducial spectrum, which is an absorbed bremsstrahlung with a plasma temperature of 10 keV and a column density of $N_H = 10^{22} \text{ cm}^{-2}$, typical of the X-ray sources in the LW. We then reprojected the individual exposure maps to form a stacked exposure map in the same way as for the counts images; the PSF maps were similarly stacked, weighted by the corresponding exposure map. Next, we employed *wavdetect* to identify discrete sources in the merged 2–8 keV counts image, supplying the algorithm with the stacked exposure map and the 50%-ECF PSF map and adopting a false-positive probability threshold of 10^{-6} . This resulted in a raw list of 847 independent sources in the 2–8 keV band.

The source centroid derived from *wavdetect* was refined using a maximum likelihood method that iterates over the detected counts within the 90% enclosed counts radius (ECR). Starting from this step we consider the 1–8 keV band to maximize the signal from potential sources in the LW. Then, for each ObsID, source counts were extracted from the 90% ECR, while background counts were extracted from a concentric annulus with inner-to-outer radii of 2–4 times the 90% ECR, excluding any pixels falling within 2 times the 90% ECR of neighboring sources. Source crowding is not a general concern in the LW, but in a few cases the source extraction region was reduced to 50% ECR due to otherwise overlapping sources. The total source and background counts were obtained by summing up the individual observations. Photometry (i.e., net photon flux and its error) for individual sources were calculated using the CIAO tool *aprtates*, which takes into account the local effective exposure, background and ECF. We consider a *significant detection* for a given source in a given ObsID if the photon flux is greater than 3 times the error. We further define for each source an inter-observation *variability index*, $VI = S_{\max}/S_{\min}$, where S_{\max} and S_{\min} are the maximum and minimum photon fluxes among all the significant detections, respectively. This implicitly requires significant detections in at least two observations.

3 PERIOD SEARCHING METHOD

In this section, we first provide our motivation of employing the Gregory-Loredo (GL) algorithm, followed by a description of its basic principles (Section 3.1). We then elucidate our application of the GL algorithm to the *Chandra* data of the LW (Section 3.2). This is complemented by a set of simulations to evaluate the detection (in)completeness (Section 3.3).

¹ <http://cxc.harvard.edu/ciao>

Table 1. *Chandra* observations of the Limiting Window

ObsID	Start Time UT	Nominal R.A. ($^{\circ}$)	Nominal Decl. ($^{\circ}$)	Roll angle ($^{\circ}$)	Exposure ks	Mode
6362	2005-08-19 16:15	267.86875	-29.58800	273	37.7	FAINT
5934	2005-08-22 08:16	267.86875	-29.58800	273	40.5	FAINT
6365	2005-10-25 14:55	267.86875	-29.58800	265	20.7	FAINT
9505	2008-05-07 15:29	267.86375	-29.58475	82	10.7	VFAINT
9855	2008-05-08 05:00	267.86375	-29.58475	82	55.9	VFAINT
9502	2008-07-17 15:45	267.86375	-29.58475	281	164.1	VFAINT
9500	2008-07-20 08:11	267.86375	-29.58475	280	162.6	VFAINT
9501	2008-07-23 08:13	267.86375	-29.58475	279	131.0	VFAINT
9854	2008-07-27 05:53	267.86375	-29.58475	278	22.8	VFAINT
9503	2008-07-28 17:37	267.86375	-29.58475	275	102.3	VFAINT
9892	2008-07-31 08:07	267.86375	-29.58475	275	65.8	VFAINT
9893	2008-08-01 02:44	267.86375	-29.58475	275	42.2	VFAINT
9504	2008-08-02 21:23	267.86375	-29.58475	275	125.4	VFAINT

3.1 The Gregory-Loredo Algorithm

There exists in the literature a variety of period-searching methods, which can be broadly divided into three categories according to their working principles.

The most traditional method is based on Fourier transform and its power density spectra, which includes the classical Schuster periodogram (Schuster 1898), the Fourier analysis with unequally-spaced data (Deeming 1975), the correlation-based method (Edelson & Krolik 1988), among others.

Another widely-used method seeks to fit the data with a periodic model in the frequency space, employing statistics such as least-squares residuals to define the likelihood function and then selecting the frequency that maximizes the likelihood. The famous Lomb-Scargle periodogram (Lomb 1976; Scargle 1982, hereafter LS) belongs to this category. Note that when adopting trigonometric functions, the least-squares method falls into the Fourier method. Another variant is to replace the least-squares residuals with polynomial fits, such as that used in Schwarzenberg-Czerny (1996).

The last category is the phase-folding method. For each trial period the time-tagged data is folded as a function of phase, and the best-fit period is found by optimizing the cost function through the frequency space. Cost function are designed to evaluate how much the phase-folded light curve deviate from constant. Methods belonging this category use diverse cost functions. Several widely known examples are the Epoch Folding (EF) algorithm (Leahy et al. 1983), the Phase Dispersion Minimization (Stellingwerf 1978), the GL algorithm (Gregory & Loredo 1992).

In X-ray observations, the detection of periodic signals is often involved with irregularly and sparsely sampled data. The small number of photons often makes lower signal-to-noise ratio when using time bins to get photometric data. The relatively few detected photons makes it more appropriate for the last group of methods since they handle event data without binning. Another characteristic for astronomical observation is the interrupted time series. In frequency space, this kind of window function leads to the heavy contamination for intrinsic data. Still, the phase-folding methods can avoid the effect of non-uniformed data since the process does not contain information in non-observed time.

Considering the above, here we use GL method to find periodic signals. GL method applies the Bayesian probability theory to the cost function. We would make a brief overview about Bayes's theorem and the identification of periodic signals in GL method

in appendix A. The key of this algorithm is the multiplicity of the binned distribution of events.

$$W_m(\omega, \phi) = \frac{N!}{n_1! n_2! n_3! \cdots n_m!} \quad (1)$$

N represents the total number of counts in data, m signifies the number of bins. $n_i(\omega, \phi)$ is the number of events falling into the i th of m phase bins by given the frequency ω and the phase ϕ , where $\sum_{i=1}^m n_i(\omega, \phi) = N$. For the data of N counts, the model defined by ω and ϕ , the multiplicity is the number of ways that the distribution could have arisen by chance. The probability of periodic is inversely proportional to the multiplicity. It could be easily proved that when the value of n_i are far apart, the multiplicity is reduced to a lower value. In simpler terms, the more the stepwise model deviate from constant, the higher the signal is periodic.

In general, the GL method follows these steps: (1) Compute the multiplicity for all the set of (m, ω, ϕ) . (Eqn. 1)

(2) Apply the integration in (ω, ϕ) space, and produce the so-called "odds ratio" using Bayesian theorem when m took a certain value. (Eqn. A16)

(3) Add up the normalized odds ratio and the probability of whether the dataset is periodic would be obtained. (Eqn. A20)

(4) Compare all the odds ratio integrated at only ϕ space, the ω with the highest odds ratio corresponds the period of signal. (Eqn. A21)

3.2 Application to the LW

Though we did source detection in 2-8 keV band to reduce the contamination from non-CV sources, here we still extracted photons from sources in 1-8 keV band to keep as more as possible source information. Besides, in order to compensate for uneven distribution over the bins, we provide "epoch" for each source. The "epoch" offered the start time and end time of each observations covered the source with at least one counts in source region. See Eqn. A17 in appendix for detailed illustration about the use of epoch. For the sake of changing aimpoint, we used individual source extract region for different observations. Explicitly, the 90% ECR aperture whose radius defined by specific PSF map was applied for counts in that observation. Since the phase-folding method directly manipulated each photons and we could not distinguish background photon from source photon, the local background information were not provided

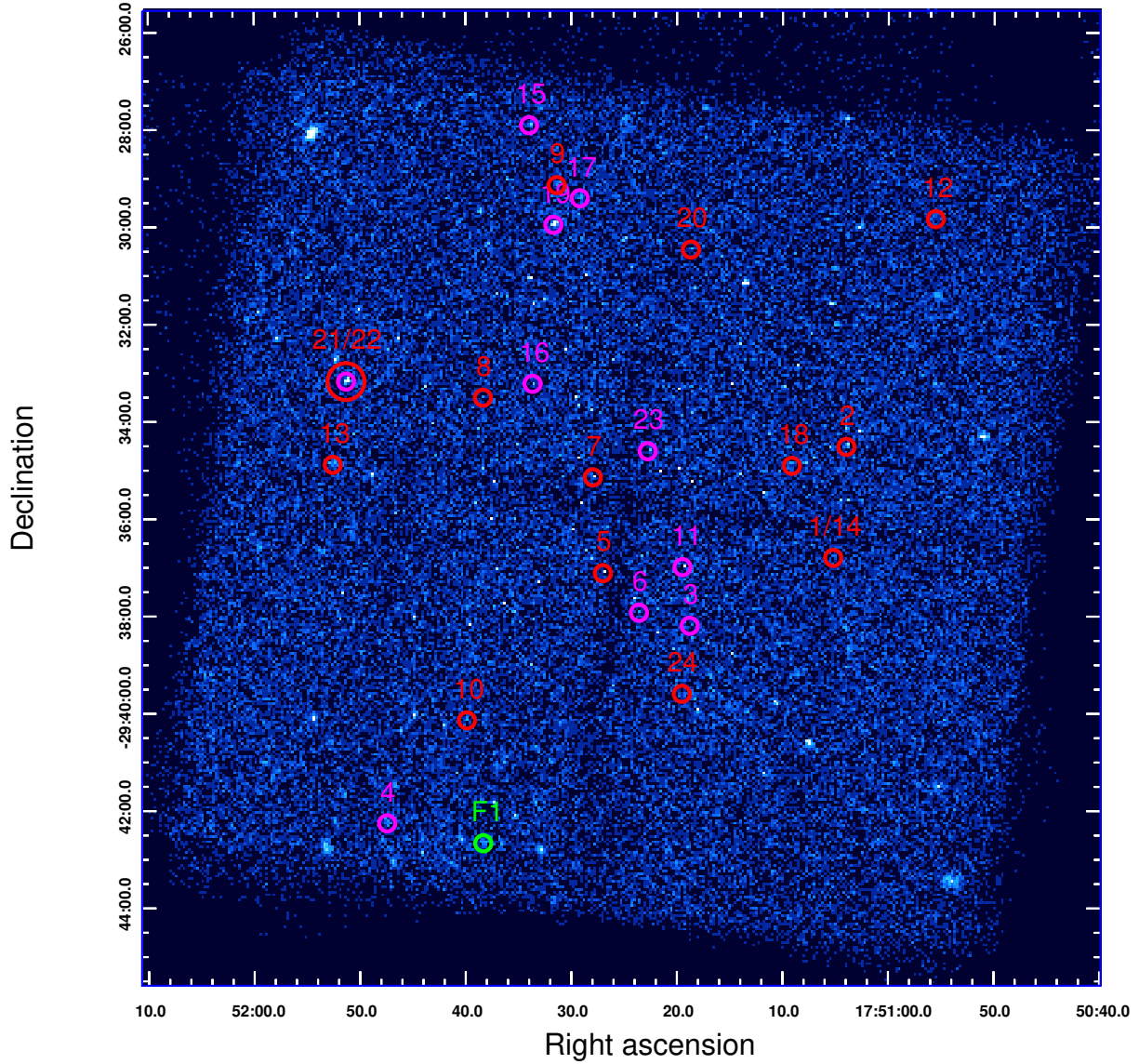


Figure 1. 2–8 keV counts image of the Limiting Window, combining 13 *Chandra*/ACIS-I observations. Locations of the 23 periodic sources are marked with colored circles (*magenta*: ten sources previously reported by (Hong et al. 2012); *red*: twelve newly discovered in this work and belonging to the Galactic bulge; *green*: one newly discovered and located in the foreground). Source numbering is the same as in Table 2. In particular, 1/14 and 21/22 are the two sources each showing two periodic signals.

for timing analysis. The combination of each source event list and the corresponding epoch were then employed as the input of GL method.

As mentioned in section 3.1, the GL method folds the dataset at trial period or frequency. Then the resolution of frequency must be balanced between computational power and accuracy. Here we generate the frequency resolution depended on the data timescale.

For the data span in timescale T , the arrival time of photon t_i , the changing angular frequency influence the phase of photon more

as i grows. The most vulnerable photon is the last photon arrived, whose arrival time is T , and the change of phase is

$$d\phi_N = \phi'_N - \phi_N \quad (2a)$$

$$\phi'_N = (\omega + d\omega) \cdot T - \lfloor (\omega + d\omega) \cdot T \rfloor \quad (2b)$$

$$\phi_N = \omega \cdot T - \lfloor \omega \cdot T \rfloor \quad (2c)$$

Assuming $\lfloor (\omega + d\omega) \cdot T \rfloor = \lfloor \omega \cdot T \rfloor$, ($\lfloor a \rfloor$ means the integral part of a), then

$$d\phi_N = d\omega \cdot T \quad (3)$$

In this work, we take 12 as the largest number of phase bins, that demands the change of photon phase should be smaller than $\frac{1}{12} \cdot 2\pi$ to guarantee the nearly non-change of phase-folded light curve. Although we can not ensure every photon to meet the requirement since its location in the same phase bin could be arbitrary. It would satisfy the situation at nearly perfect level if we keep the deviation of phase of last photon smaller than $\frac{1}{12} \cdot 2\pi$. As shown in Eqn. 4

$$d\phi_N = d\omega \cdot T < \frac{1}{12} \cdot 2\pi \quad (4a)$$

$$d\omega < \frac{\pi}{6T} \quad (4b)$$

The total span of 13 observation is about three years, i.e., 10^8 s, so the resolution of angular frequency is 5×10^{-9} . When the ω increases, corresponding the period decreases, the same resolution brings numerous discrete frequencies and raises running time greatly. Thus we used three different resolutions $10^{-7}, 10^{-8}, 10^{-9}$ in three period ranges (300s, 3000s), (3000s, 10000s), (10000s, 50000s). The ranges was chosen for the orbital period distribution of CVs, as shown in Figure 8. There is a period gap in distribution at 2-3 hours, and a period minimum at about 70 minutes. Then the first range covers roughly the spin period of IPs, the other two ranges overlay the orbital period below and beyond the period gap respectively.

Generally, for each source, we provide the dataset for GL method. Then we got the most periodic signal with its probability in three period ranges. Taking 90% as threshold to determine the periodicity, finally we choose all the candidate sources with at least one periodic signal.

3.3 Detection completeness

For a given period searching algorithm, the detection rate depends on both the number of observed counts, the intrinsic shape of light curve, as well as the observing cadence. To quantify the detection rate and hence gain insight on the nature of the periodic sources, we perform simulations following the merit of [Cicuttin et al. \(1998\)](#). Two functional forms of light curve are considered: a sinusoidal function and a piecewise function. While these are admittedly idealized shapes, they can represent realistic light curves, e.g., resulted from rotational modulation or eclipsing.

A sinusoidal light curve follows,

$$\lambda(t) = \lambda_0 [1 + A_0 \sin(\omega t + \phi)], \quad (5)$$

where $\omega = 2\pi/P$, A_0 is the relative amplitude of variation, and λ_0 is the mean count rate which may include contribution from a constant background. The phase ϕ is arbitrarily set at zero. For a direct comparison with the observation, we relate λ_0 with the total number of counts, $C = \lambda_0 T$, where T is the exposure time of a given observation. This holds since T is typically much longer than the modulation period (P). The simulations are run with a selected number of pa-

rameters due to constraints in computational power. Specifically, we adopt total counts $C=50, 100, 200, 300, 400$ and 500 , amplitudes $A_0=0.5, 0.6, 0.7, 0.8$ and 0.9 , and periods $P=554, 5540$ and 45540 sec, resulting in $6 \times 5 \times 3 = 90$ combinations. The chosen periods are representative of the actually searched ranges (Section 3.2), whereas the adopted total counts well sample the range of observed counts from the LW sources.

We thus simulate 100 light curves for each combination of parameters, taking into account Poisson errors and the exact start and end times of the 13 ACIS-I observations. The arrival time of each simulated count is further randomly modified by an amount of 3.2 sec to mimic the effect of ACIS frame time. The simulated light curve is then searched for a periodic signal using the GL algorithm in the same manner as in Section 3.2. We claim a valid detection if the found period has a detection probability greater than 90% and its value is consistent with the input period to within 0.1%. The detection rate for a given combination of parameters is taken to be the fraction of the 100 light curves with a valid detection.

The top, middle, bottom panel of Figure 2 show the results of three period respectively. We could think of 0.1 as extremely low. Then it is obviously illustrated that when counts equals 50, the detection rate are almost always extremely low despite the period and amplitude, except for the longest period and high amplitude. While for counts of 100, the detection rate could invariably exceed 50%, which is sufficient enough for period finding procedure. Thus we could roughly say that when counts lower than 100, the detection rate is extremely low. The periodic signal in this circumstance are not reliable. Besides, it can be seen that the algorithm is nearly no bias of period, except a slight improvement of detection rate with increasing period.

The piecewise function, which mimics an eclipse against an otherwise constant flux, takes the form of

$$\lambda(t) = \begin{cases} \lambda_0 & \phi(t) \in [0, (1-w)\pi) \cup ((1+w)\pi, 2\pi], \\ f\lambda_0 & \phi(t) \in [(1-w)\pi, (1+w)\pi], \end{cases} \quad (6)$$

where w accounts for the eclipsing width (duration) in phase space, and f characterizes the relative depth of the eclipse ($0 \leq f \leq 1$; $f = 0$ corresponds to total eclipse). Here the eclipse is assumed to occur around $\phi = \pi$. Again, λ_0 can be related to the total counts as $C = (1-fw)\lambda_0 T$. We set $f = 0.1$ and $w = 0.1$ in our simulations, which are typical of eclipsing CVs, since the radius ratio of WD, companion star and orbit are about 1:10:50. **[try $f=0.2, 0.5$? f might be too small. better try more values]** We test three values for the period, $P=5258, 15258$ and 45258 sec. Then the simulation were run 100 times at each set of parameter. Results of detection rate (also taking 90% as threshold) is shown is Figure 3. It is noteworthy that the efficiency soars to 1 when the number of counts goes up. And a marked rise appears with the growth of period.

4 PERIOD SEARCHING RESULTS

According to the simulations in Section 3.3, a periodic signal is hard to detect in sources with total counts $C \lesssim 100$, even in the case of high variation amplitudes. Therefore, we restrict our period searching to sources with $C \geq 100$, which include 667 of the 847 sources in the raw list.

Adopting a probability threshold of 90%, we obtain 48 tentative periodic signals from the three period ranges. However, it is necessary to filter spurious detections, which may be caused by several effects:

- (i) By design, the ACIS is dithered to distribute photons over

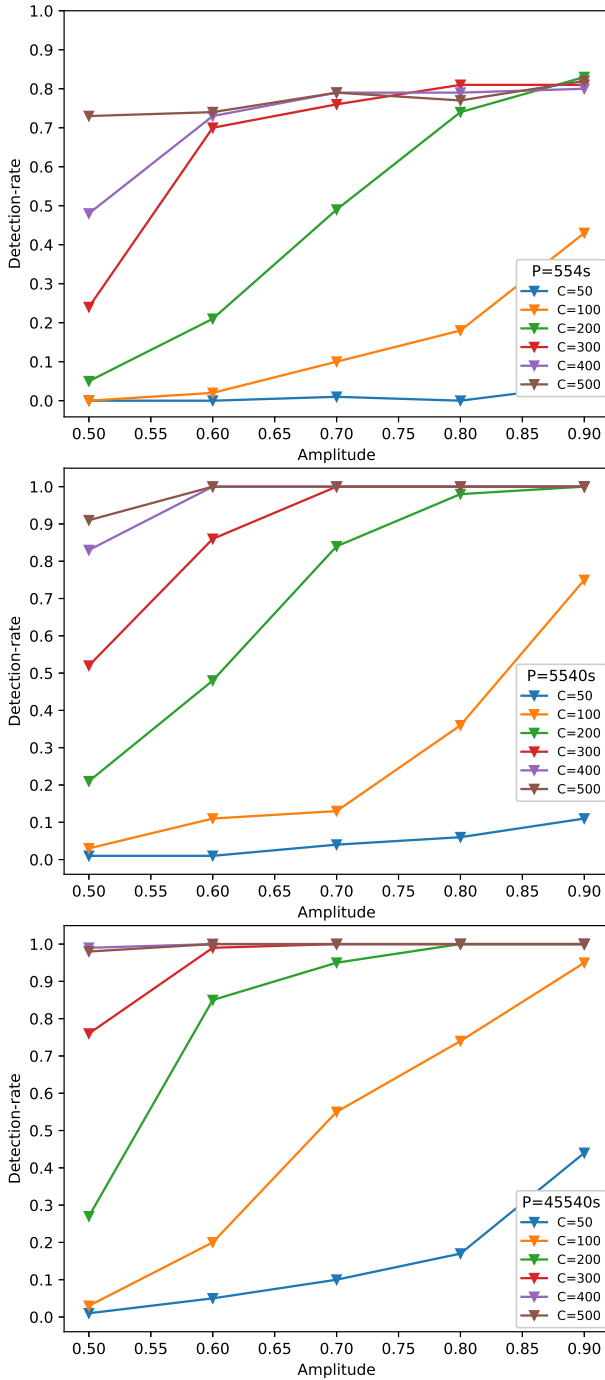


Figure 2. Detection rate obtained from simulation results for sinusoidal variation. The results of top, middle, bottom are respectively from modulation period as 554s, 5540s, 45540s. The other two parameters, A_0 and number of counts, are labeled by x-axis and colors.

more CCD pixels to avoid pile-up and to fill CCD gaps. The dither period is 706.96 s in pitch and 999.96 s in yaw. Any signals detected at these two periods and their harmonics are thus excluded. These are mostly found in sources located close to CCD gaps.

(ii) In certain sources, multiple detections can be caused by second and third harmonics of the same intrinsic signal (i.e., 2 and 3 times the true period). These can be easily identified by the sign of double-peak or triple-peak in the phase-folded light curves, provided that the intrinsic signal has a single-peak structure.

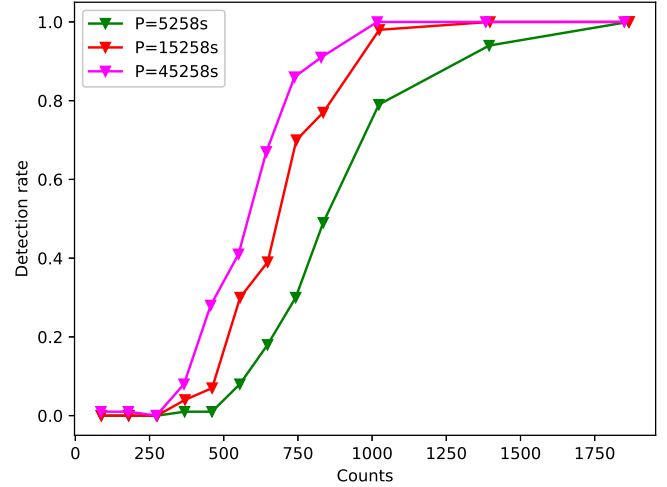


Figure 3. Detection rate obtained from simulation results for eclipsing models. Magenta, red and green denotes for $P=45258s$, $15258s$ and $5258s$ respectively.

However, if a single-peak structure were not the case, it is more difficult to distinguish the true period and the half harmonics. Hence we assume that there is no half harmonics and always take the lowest period among the multiple detections as the true period. Appendix B provides more discussions about harmonics.

(iii) In certain sources, strong flux variations or outbursts occupying one particular observation can also cause a false periodic signature. This is because the GL algorithm, which directly analyzes the phase-folded light curve, can be fooled if there were too many photons found in a single observation, producing excess in certain phase bins. In this case the algorithm may "think" there exists a period especially in the third period range. Among the sources with tentative periods, four exhibit a variability index $VI > 10$, indicating strong variations. We reanalyze their light curves on subsets covering only the outbursting or quiescent epochs. For three of them, the tentative period cannot be recovered in either subset. Therefore, these three signals are probably false detections. The remaining source is kept since its period can be recovered in both the outbursting and quiescent epochs. [Table 2 shows no source with $VI > 10$.]

The above filtering thus results in 25 valid periodic signals in 23 sources. Among them, 10 periodic signals were reported by Hong et al. (2012) and are confirmed here with the GL algorithm, while the remaining 15 periods are new discoveries (a comparison between our work and Hong et al. 2012 is addressed in Section 6.1). The basic information of these periodic sources are listed in Table 2, sorted by the order of increasing period. Locations of these sources are marked in Figure 1.

In two cases, two different periods are found for the same source, hence each of them is assigned two IDs: #1/#14 and #21/#22. The phase-folded light curve at the two modulation periods, the long-term, inter-observation light curve and the spectra (Section 5) of these two sources are shown in Figure 4 and Figure 5. For left panel, though the GL method could not distinguish background photons, we still define the local background from photometric results, shown as the yellow strip in the left panel of Figure C1. The width of strip represents the Poisson error range. Additionally, since the bin size in phase-folded light curve has no effect on the shape, we chose the bin size between 20 to 50, to get the most distinct display. For middle panel, the valid detection (defined in 2.2) are

plotted with dots plus error range. While the non-valid detection are shown in arrows, providing only the upper limits. Meanwhile, the x-axis in right panel were plotted in discontinuous style for better demonstration effect, since the short interval over the last eight observations. For right panel, the spectra illustrated here were fitted in the range of 1–8 keV, consistent with the timing analysis. Similar figures of the remaining 21 sources are presented in Appendix C.

5 X-RAY SPECTRAL ANALYSIS

We perform spectral analysis for all 23 confirmed periodic sources to gain insight on their nature. Source and background spectra are extracted from the same regions as described in Section 2.2, along with the ancillary response files (ARFs) and redistribution matrix files (RMFs), by using the CIAO tool *specextract*. The spectra from individual observations are then coadded to form a combined spectrum of a given source, with the corresponding ARFs and RMFs weighted by the effective exposure. **Further, the spectrum is adaptively binned to achieve a minimum of 20 counts and a signal-to-noise ratio greater than 2 per bin.**

The resultant spectra are analyzed using XSPEC v12.9.1. Since these sources are expected to be CVs, we adopt a fiducial spectral model (Zhu et al. 2018; Xu et al. 2019), which consists of a bremsstrahlung continuum and three Gaussian lines centered at 6.40, 6.68 and 6.97 keV, all these components subject to an unknown line-of-sight absorption (*phabs* in XSPEC). The three lines (hereafter referred to as the 6.4, 6.7 and 7.0 keV lines) correspond to neutral Fe $K\alpha$, Fe XXV $K\alpha$ and Fe XXVI $Ly\alpha$, respectively, which are among the most commonly detected emission lines in CV spectra. The latter two lines, in particular, arise from the post-shock plasma near the WD surface, and their flux ratio ($I_{7.0}/I_{6.7}$) has proven to be a robust tracer of the plasma temperature, hence also a good indicator of the WD mass (Xu et al. 2016).

It turns out that the plasma temperature (T_b) is not well constrained in most sources, due to a moderate number of counts and the insufficient sensitivity of *Chandra* at energies above 8 keV. Hence for such cases we fix T_b at 40 keV, which is typical of IPs when their hard X-ray (up to tens of keV) spectra are available (Xu et al. 2016; Hailey et al. 2016). Setting a lower value of T_b , for instance, at 20 keV, does not affect our following conclusions.

Again due to the limited number of counts, most of the periodic sources show weak or non-detected Fe lines. We have applied a bootstrapping method using the *multifake* tool in XSPEC to derive the 90% confidence range for the fluxes of the three Fe lines. It turns out that only one sources, LW21 (same as LW22), shows a significant line at both 6.7 keV and 7.0 keV. The flux ratio and its 90% error are similarly determined for this sources, resulting in $I_{7.0}/I_{6.7} = 0.91^{+1.22}_{-0.56}$ for LW21. According to the empirical line ratio–WD mass ($I_{7.0}/I_{6.7}$ – M_{WD}) relation of Xu et al. (2019), which is calibrated with CVs in the solar neighborhood, we can infer $M_{WD} \approx 0.8$ (1.2) M_\odot for LW21, provided that both sources are IPs (DNe). It is noteworthy that there exists no empirical $I_{7.0}/I_{6.7}$ – M_{WD} relation for polars, mainly due to the small number of known polars in the solar neighborhood (Xu et al. 2019).

We further divide the 22 periodic sources into two groups based on their luminosities. Here source F1 is excluded since we are only interested in sources located in the bulge. The H (L) group consists of 6 (16) sources having an unabsorbed 1–8 keV luminosity above (below) 1.0×10^{32} erg s $^{-1}$, which is derived from the individual best-fit spectral model. The cumulative spectrum of each group is fitted with the same fiducial model, i.e., bremsstrahlung plus

three Gaussian lines. The improved S/N in the cumulative spectrum allows us to detect all three Fe lines and constrain their flux ratios. The group has $I_{7.0}/I_{6.7} = 0.78^{+0.10}_{-0.09}$, thus inferring a mean WD mass of $M_{WD} \approx 0.8$ (1.2) M_\odot if they are IPs (DNe). On the other hand, the L group shows no constrain of line ratio, we can only provide its upper limit, i.e., 0.39, corresponding $M_{WD} < 0.45$ (0.80) M_\odot if they are IPs (DNe).

Results of the above spectral analysis are summarized in Table 3.

6 DISCUSSION

6.1 Comparison with previous work

We have found 25 periodic signals from 23 sources in the LW. This is to be contrasted with the 10 periodic signals from 10 sources found by Hong et al. (2012), which are all recovered in this work (Table 2), while the remaining 15 periods are new detections. Since Hong et al. (2012) and this work have used the same set of *Chandra* observations, this difference must be owing to the different period searching methods employed.

Hong et al. (2012) employed the LS periodogram, which, as described in Section 3.1, handles the light curve in time space, while the GL algorithm processes the light curve in phase space with tolerance for observing gaps. **We have applied the LS periodogram to our data in essentially the same way as Hong et al. (2012) and confirmed that only those 10 periods can be detected by this method.**

Besides, we also did 100 times of simulations for each signal. We had to use sinusoidal variations for simulating process though many of them may deviate much from real shape. The counts rate and period can be directly attained from data, while the amplitude is hard to determine since the deviation. In Hong et al. (2012), they got A_0 from A_{rms} depended on Rayleigh statistics. The definition of A_{rms} and the relation between A_{rms} and A_0 , which were taken by Hong et al. (2012), are described below.

$$A_{rms} = \left(\frac{Z_1^2}{N} \right)^{1/2} \frac{N}{N - B} \quad (7a)$$

$$Z_1^2 = \frac{2}{N} \left\{ \left[\sum_j \cos \phi(t_j) \right]^2 + \left[\sum_j \sin^2 \phi(t_j) \right]^2 \right\} \quad (7b)$$

$$A_0 = \sqrt{2} A_{rms} \quad (7c)$$

where equation 7c only works for sinusoidal modulations. N and B represent the total counts in source region and local background respectively. t_j and $\phi(t_j)$ refer to the arrival time and phase of each photon. Z_1^2 is the classical Rayleigh statistic method (Buccheri et al. 1983; Muno et al. 2003). Meanwhile, they provided another way to obtain A_0 . From phase-folded light curve, they defined $A_M = 1 - R_{min}/R_{max}$, and $A_M = 2A_0/(1 + A_0)$, where R_{min} (R_{max}) is the minimum (maximum) count rate of the folded light curve.

Though A_M depends on the bin size of phase-folded light curve, we still prefer it rather than A_{rms} to get the amplitude, i.e., A_0 , since the deviation between sinusoidal variation and real shape sometimes made A_0 exceeds one when it was calculated from A_{rms} .

Still, we took 90% as threshold to get valid detection at 0.1% accuracy. The percentage of valid detection would be represented by P_{det} . And A_M was obtained with bin size fixed at 20. For directly comparison, we also ran the simulation based on the same

Table 2. Information on the periodic X-ray sources in the Limiting Window

ID	R.A.	Decl.	Period	P_{GL}	H-ID	C	A_0	P_{det}	P'_{det}	VI	Harmonics
LW	°	°	(s)					%	%		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
1 [†]	267.77173	-29.61332	853.83	0.90277	-	202	0.76	86	-	1.92	-
2	267.76657	-29.57529	3820.83	0.99222	-	902	0.54	99	-	1.94	-
3	267.82829	-29.63660	4728.90	1.00000	H6	394	0.75	98	99	2.13	Third
4	267.94766	-29.70427	4886.79	0.99994	H8	784	0.56	100	98	1.90	-
5	267.86255	-29.61859	5072.97	0.99933	-	293	0.76	100	-	2.34	Second
6	267.84831	-29.63212	5130.57	1.00000	H2	437	0.76	100	100	2.51	Second
7	267.86651	-29.58575	5144.97	0.99880	-	335	0.77	100	-	2.48	Second
8	267.90982	-29.55845	5158.75	1.00000	-	121	1.00	100	-	2.30	Second
9	267.88075	-29.48562	5231.49	0.94949	-	347	0.67	100	-	1.65	-
10	267.91616	-29.66900	5252.93	0.91425	-	211	0.83	100	-	-	-
11	267.83116	-29.61651	5261.93	1.00000	H10	438	0.88	100	31	1.46	Second
12	267.73141	-29.49721	5334.76	0.99952	-	760	0.51	100	-	1.25	Second
13	267.96901	-29.58142	5501.16	0.99094	-	512	0.61	100	-	2.89	-
14 [†]	267.77173	-29.61332	5608.21	0.96821	-	202	0.81	100	-	1.92	Third
15	267.89161	-29.46508	6335.85	1.00000	H5	823	0.62	100	100	2.09	Second
16	267.89024	-29.55369	6597.55	1.00000	H9	487	0.72	100	99	4.30	Second
17	267.87162	-29.49011	7448.98	0.99999	H3	535	0.73	100	100	1.76	Second
18	267.78806	-29.58177	7756.19	0.99941	-	214	0.91	98	-	4.76	Second
19	267.88203	-29.49922	8546.28	1.00000	H4	3402	0.30	99	93	3.27	Second
20	267.82785	-29.50770	8844.82	0.90987	-	263	0.69	93	-	1.82	Second
21 [‡]	267.96375	-29.55290	9877.52	0.99992	-	1963	0.40	100	-	1.44	-
22 [‡]	267.96375	-29.55290	10342.30	1.00000	H1	1963	0.76	100	99	1.44	-
23	267.84487	-29.57680	12002.70	1.00000	H7	307	1.00	100	100	1.86	Second
24	267.83142	-29.65992	47317.12	0.98850	-	138	0.88	87	-	-	-
F1	267.90974	-29.71112	42219.03	1.00000	-	1039	-	-	-	23.6	-

Notes: (1) Source sequence number assigned in the order of increasing period. The same source with multiple period signal was denoted as [†] and [‡]. F1 represents the periodic foreground source. (2) R.A.(J2000) of the centroid of source. (3) Decl.(J2000) of the centroid of source. (4) The modulation period determined by GL method. (5) The probability of periodic signal defined by Eqn. A20. (6) The cross-match results with previous work. H_i represents the i th source in Table 2 of [Hong et al. \(2012\)](#). (7) The number of counts in the 1-8 keV band. (8) The amplitude of variation obtained in this work. (9) The detection probability of periodicity based on simulations of 100 sinusoidal light curves for each source. (10) The detection probability of periodicity simulated as the same process described in column(9), while the amplitude are taken from [Hong et al. \(2012\)](#). (11) $VI = S_{max}/S_{min}$, where S_{max} and S_{min} are the maximum and minimum photon fluxes among all the valid detections. For source #10 and #24, no VI are provided since the lack of valid detections. (12) The note gives the significant harmonic detected by the algorithm.

A_0 defined in [Hong et al. \(2012\)](#) for the ten collective sources. A flagrant contrast was illustrated in Figure 6 based on that two columns. Apparently, GL method has better performance compared with LS method.

The improvement on detecting efficiency and data usage brought more periodic signals than [Hong et al. \(2012\)](#). Additionally, we operated the simulation not only for sinusoidal variation, but also for eclipsing models to describe the dip in orbital modulation. Combining the simulation results and more than twice the sample, we were allowed to discuss the source properties and the distribution of CVs in galactic bulge region on a better level.

6.2 Classifying the periodic X-ray sources

These periodic sources are with luminosities ranged from 10^{31} to 10^{33} erg s⁻¹, combined with the period distribution, mostly about 1-3 hours. All of these properties suggest that they belong to cataclysmic variables. Before we start to discuss the nature of these periodic sources, we should take a look at CVs in the field. Their period distribution, including polars, IPs and DNe, are shown in Figure 8. It can be easily seen that the period distribution of these LW sources resembles those of polars more than others, since most

of these are below the period gap. While DNe and IPs both have a considerable number of systems with period beyond the gap. According to the our simulation results in section 3.3, this can not be resulted from selection bias of algorithm.

For non-magnetic CVs like DNe, the common phase-folded light curve exhibits narrow dip, due to the eclipse of the white dwarf, as modeled in section 3.3. The typical light curve is like #22 in Figure C1. While the simultaneous existence of #21 and #22 and the 2% period difference suggest it might be an asynchronous intermediate polar. Besides, the central dip of #3, #18 and #20 are also similar to this circumstance. Since the eclipse happens in nearly all types of CVs, we could only set three as an upper limit of number of DNe in our sample.

For magnetic CVs, including IPs and polars, their orbit modulation could give rise to more complicated shape of light curve. For polars, consider the simplistic situation, whose accretion is nearly onto one pole, then the shape of light curve would be divided into two groups. Suppose an inclination i , the angle between rotation axis and magnetic axis is β , the magnetic colatitude of accretion is ϵ . Then if $i + \beta + \epsilon > 90^\circ$, we would see alternately two poles, the shape would be like #6, with half of orbit cycle showing no emission. This so-called "two-pole" behavior are more complicated

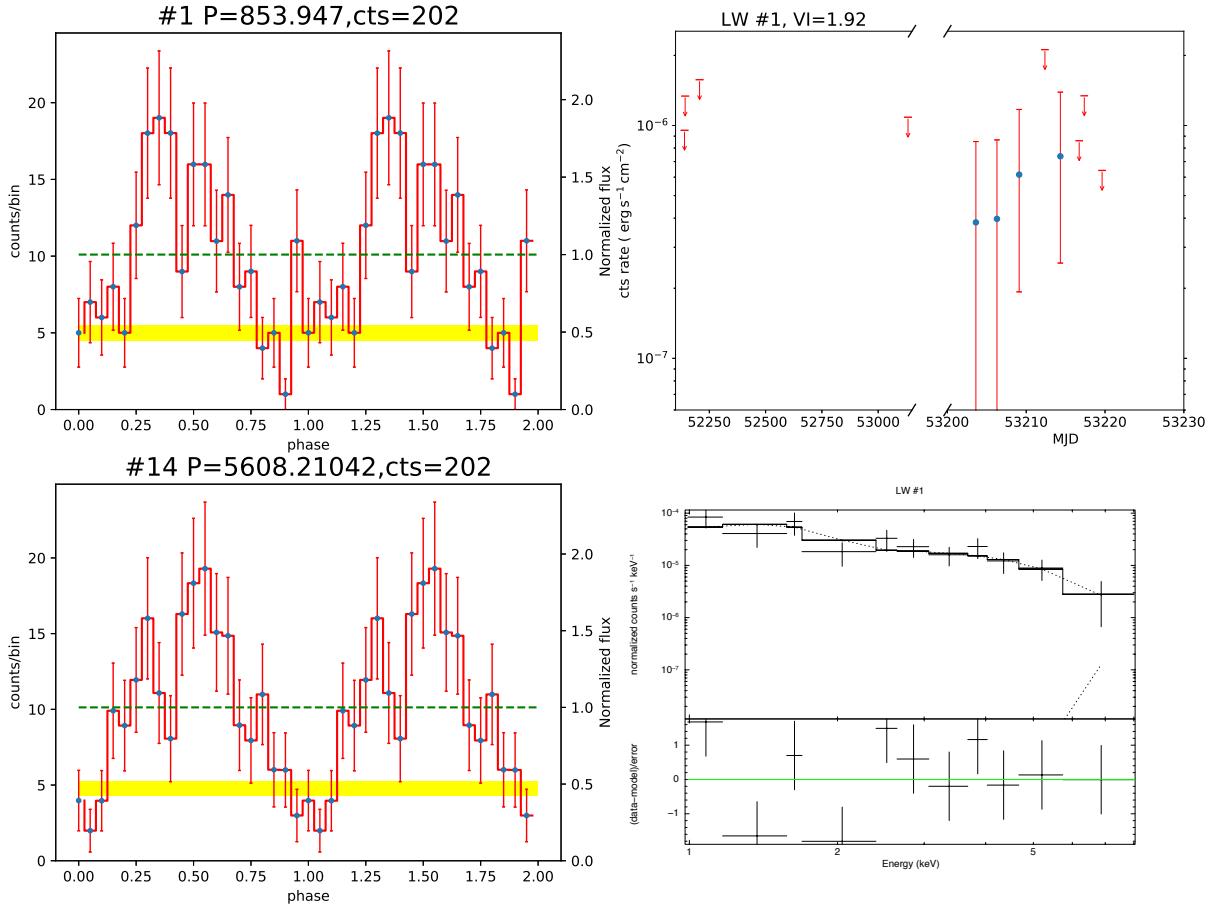


Figure 4. The phase-folded light curve at the two modulation periods, the long-term, inter-observation light curve and the spectra for #1(#14) source.

if the accretion goes to both two poles, the gap with half orbit cycle would be partially filled (like #16) by second pole's emission. Sometimes it may completely reverse in hard X-ray band cause the accretion shock in second pole producing most of hard X-rays (Heise et al. 1985). On the other hand, if $i + \beta + \epsilon < 90^\circ$ and $\beta < i$, in which the accreting pole is always visible, the modulation would caused by the obscuring of accretion stream. The width and depth of the dip in phase space are determined by many reasons and totally unpredictable.

For IPs, the orbital modulation could be resulted by eclipse of WD, the absorption of X-rays emitted near the white dwarf surface (Hellier et al. 1993), or the "disc-overflow" model in (Norton et al. 1996). The shape of light curve in IPs could be any kinds of dips or sinusoidal variation. The only robust identification is to determine both their spin and orbital period, like the #1(#14) and #21(#22) in our sample.

Based on our current understanding of the shape and distribution of orbital modulation, we conclude that the periodic sources discovered are mostly polars, with several IPs(two determined) and DNe(three as upper limit).

6.3 CV populations in the Galactic bulge

Firstly, we assumed that the fraction of polars in the total sample of 667 sources is α . The sinusoidal variation happens in "two-pole" situation, which takes 90° in total 360° . Then we can set 25% as the upper limit for polars with sinusoidal variation intrinsically.

We assumed the even distribution for amplitude from 0.5 to 0.9 and took the simulation results for $P=5540$ s and $P=45540$ s as the detection rate for period under(60% of the total number) and beyond the period gap(40% of the total number). The value of 60% and 40% are estimated from Figure 8. Then we set width=100 for our binning of counts, from 75 to 3575, which consist nearly all detected sources. The choice of value balance the number of counts taken from observation and simulation. The predicted number of periodic sources which "should" be detected in each bin is calculated by:

$$Np_i = N_i \times DR \times 25\% \times 667 \times \alpha \quad (8)$$

N_i is the product of number of sources detected in the bin. DR denotes the detection rate weighted from simulation. Then we sum all Np_i together and force it equals to 20, getting α about 14%. The comparison between Np_i and the real detected 20 periodic sources(two determined IPs excluded) are plotted in Figure 7. The perfect agreement between their population proves the validity of estimation.

Since the real luminosity function should be gentle than that of total sample, which means there could be more polars at the bright band, then it demanding lower numbers of polar to balance the high detection rate for bright sources. In general, the 14% should be treated as the upper limit for polars, especially when we considered all the 20 sources(already excluding the two IPs) are polars.

While for DNe, we are constrained by lack of reliable X-ray luminosity function(XLF). We have already set the three as the upper limit of DNe. The steeper XLF for DNe than the XLF for total sample

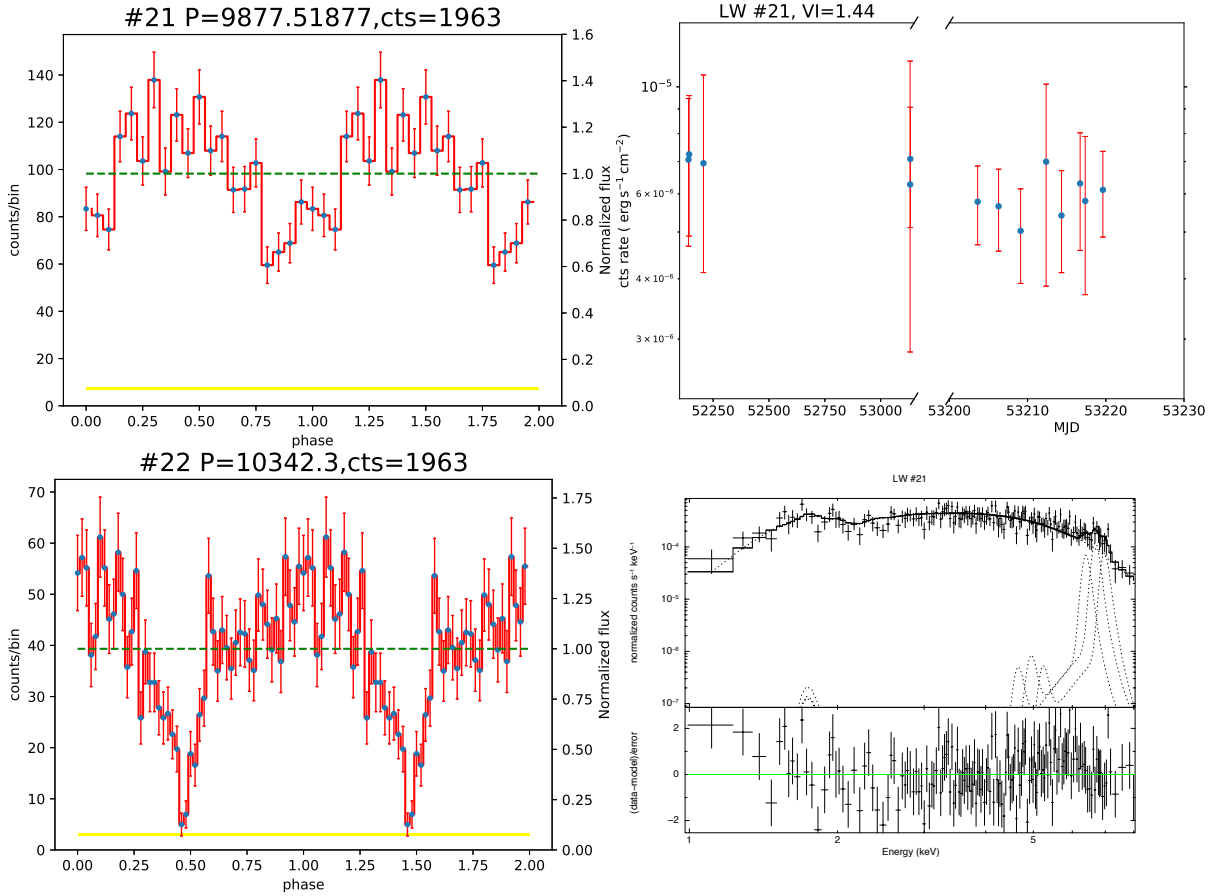


Figure 5. The phase-folded light curve at the two modulation periods, the long-term, inter-observation light curve and the spectra for #21(#22) source.

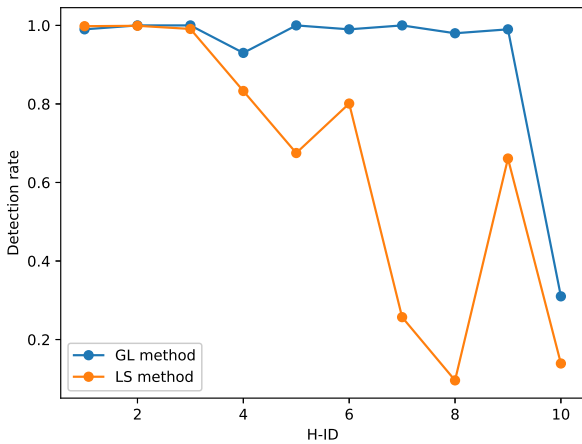


Figure 6. The comparison of efficiency between two methods. H-ID is the sequence number given by (Hong et al. 2012), same as column(6) in Table 2. The detection rate of LS method are taken from Table 2 in (Hong et al. 2012)

would only contribute the lower limit for their proportion. This conflict increases the uncertainty of estimation. Here we still present the estimation for fraction of DNe. Intrinsically, the eclipse of white dwarf depends on the inclination angle, radius of companion star

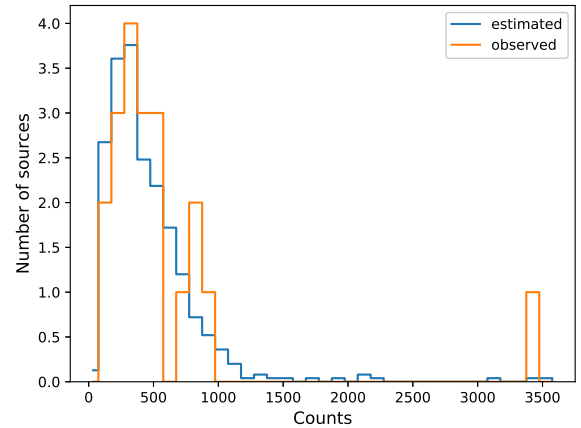


Figure 7. The comparison between estimated and the real detected number of sources.

and orbit. If we set β as probability of eclipsing, i as inclination, R_1, R_2, R_{orb} as radius of WD, companion star and orbit respectively. Then the β need to fulfill:

$$R_{orb} \times \cos(90 - \beta) \leq R_1 + R_2 \quad (9)$$

We took parameters from simulation operated by (Knigge et al. 2011), in which R_1 is fixed at when M_{WD} equals 0.75 solar mass.

Table 3. X-ray spectral properties of the periodic sources

ID	N_H	T_b	$I_{6.4}/I_{6.7}$	$I_{7.0}/I_{6.7}$	$I_{6.7}$	χ^2/dof	L_{1-8}
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
1 [†]	$0.51^{+0.75}_{-0.34}$	40 (fixed)	-	-	-	1.14/5	$1.82^{+0.64}_{-0.51}$
2	$2.17^{+0.54}_{-0.46}$	$20.7^{+56.9}_{-9.92}$	-	-	-	0.86/78	$23.1^{+2.70}_{-2.01}$
3	$1.34^{+0.70}_{-0.40}$	$46.4^{+46.1}_{-38.5}$	-	-	-	0.98/33	$6.61^{+1.05}_{-0.77}$
4	$1.15^{+0.69}_{-0.50}$	$11.3^{+53.3}_{-4.71}$	-	-	-	0.91/27	$22.5^{+2.94}_{-4.42}$
5	$1.02^{+0.27}_{-0.23}$	40 (fixed)	-	-	-	1.00/33	$5.59^{+0.77}_{-0.70}$
6	$1.82^{+0.57}_{-0.50}$	$6.90^{+12.4}_{-2.90}$	-	-	-	1.12/42	$9.23^{+1.24}_{-1.11}$
7	$1.62^{+0.62}_{-0.49}$	$41.6^{+43.0}_{-32.3}$	-	-	-	0.86/39	$6.70^{+0.89}_{-0.81}$
8	$2.06^{+1.51}_{-0.94}$	40 (fixed)	-	-	-	0.93/7	$1.76^{+0.54}_{-0.42}$
9	$1.29^{+1.34}_{-0.67}$	$20.8^{+95.8}_{-20.8}$	-	-	-	1.10/7	$3.50^{+1.22}_{-0.86}$
10	$2.50^{+7.25}_{-1.56}$	40 (fixed)	-	-	-	0.85/5	$2.14^{+1.76}_{-0.75}$
11	$1.85^{+0.39}_{-0.33}$	40 (fixed)	-	-	-	1.22/47	$9.49^{+1.11}_{-1.02}$
12	$6.23^{+9.67}_{-3.66}$	40 (fixed)	-	-	-	0.78/6	$7.58^{+5.76}_{-2.93}$
13	$0.90^{+0.30}_{-0.24}$	40 (fixed)	-	-	-	1.15/38	$8.48^{+1.12}_{-1.04}$
14 [†]	$0.51^{+0.75}_{-0.34}$	40 (fixed)	-	-	-	1.14/5	$1.82^{+0.64}_{-0.51}$
15	$1.46^{+0.48}_{-0.38}$	40 (fixed)	-	-	-	1.16/42	$12.8^{+1.77}_{-1.61}$
16	$0.89^{+0.18}_{-0.16}$	40 (fixed)	-	-	-	1.43/51	$8.47^{+0.88}_{-0.83}$
17	$2.68^{+0.63}_{-0.52}$	40 (fixed)	-	-	-	0.75/36	$11.3^{+1.61}_{-1.45}$
18	$2.01^{+0.92}_{-0.66}$	40 (fixed)	-	-	-	0.53/14	$4.21^{+0.89}_{-0.77}$
19	$1.82^{+0.10}_{-0.10}$	40 (fixed)	-	-	-	0.95/185	$83.9^{+3.25}_{-3.16}$
20	$2.09^{+2.45}_{-1.16}$	$4.04^{+28.2}_{-2.54}$	-	-	-	1.04/12	$5.39^{+1.81}_{-1.47}$
21 [‡]	$2.83^{+0.25}_{-0.23}$	40 (fixed)	$0.47^{+0.72}_{-0.35}$	$0.91^{+1.22}_{-0.56}$	31.7	1.10/147	$60.0^{+3.25}_{-3.12}$
22 [‡]	$2.83^{+0.25}_{-0.23}$	40 (fixed)	$0.47^{+0.72}_{-0.35}$	$0.91^{+1.22}_{-0.56}$	31.7	1.10/147	$60.0^{+3.25}_{-3.12}$
23	$1.83^{+0.44}_{-0.37}$	40 (fixed)	-	-	-	1.47/35	$9.23^{+1.22}_{-1.13}$
24	$0.83^{+3.31}_{-0.83}$	$2.30^{+1.59}_{-0.85}$	-	-	-	0.80/2	$0.77^{+7.82}_{-0.36}$
F1	$0.35^{+0.16}_{-0.13}$	$4.78^{+3.55}_{-1.58}$	-	-	-	1.19/55	$8.73^{+1.09}_{-0.98}$
H	$1.99^{+0.10}_{-0.97}$	40 (fixed)	$0.28^{+0.10}_{-0.09}$	$0.78^{+0.18}_{-0.16}$	$8.76^{+3.57}_{-3.57}$	1.19/205	$31.8^{+0.95}_{-0.95}$
L	$1.33^{+0.12}_{-0.11}$	40 (fixed)	< 0.18	< 0.39	$2.53^{+1.10}_{-1.10}$	1.09/168	$5.36^{+0.24}_{-0.24}$

Notes: (1) Source sequence number as in Table 2, except “H” and “L”, which refer to the bright and faint group of sources (excluding source F1), i.e., having 1–8 keV luminosity above (below) 10^{32} erg s⁻¹. †Sources 1 and 14 are the same source with two different periods; ‡Sources 21 and 22 are the same source with two different periods. (2) Line-of-sight absorption column density, in units of 10^{22} cm⁻². (3) The bremsstrahlung temperature, in units of keV. Fixed at a value of 40 keV when the spectrum provides no significant constraint to this parameter. (4)–(5) Flux ratio of the 6.4 or 7.0 keV line to the 6.7 keV line. (6) Integrated flux of the 6.7 keV line, in units of 10^{-8} ph cm⁻² s⁻¹. (7) χ^2 and degree of freedom of the best-fit model. (8) 1–8 keV unabsorbed luminosity, in units of 10^{31} erg s⁻¹. Quoted errors are at the 90% confidence level.

Assuming that inclination is even distributed in $(0, 90^\circ)$, the probability of eclipsing (hereafter EP) are plotted in Figure 9.

We utilized the simulation results of 5258s and 15258s as the detection rate for period under (75% of the total number) and beyond the period gap (25% of the total number). The fraction was taken from the DNe distribution in solar neighborhood. Besides, EP was chosen as 0.18 and 0.20 for this two types. Similarly, the predicted number of periodic non-mCVs which “should” be detected in each counts bin is:

$$Np_i = N_i \times DR \times EP \times 667 \times \alpha \quad (10)$$

Since the sum of Np_i was assigned as three, the α would be around 0.67 if we set 10^{32} erg s⁻¹ (roughly corresponding 675 counts) as the upper limit of luminosity for DNe. The rationality of the limit has been proved by the DNe sample from solar neighborhood in

(Xu et al. 2016), based on Suzaku observation. The uncertainty of this fraction comes from our limited acquaintance about XLF for DNe, and the subjective diagnostic for the phase-folded light curve.

7 SUMMARY

1. We have discovered 22 periodic sources with 24 signal in the LW by using GL method, including 10 of them already found by LS method in Hong et al. (2012). Their luminosity range locates at $10^{31} - 10^{33}$ erg s⁻¹. The general feature of these 22 sources resembles that of polars. Three of them with narrow dip are likely DNe. Two of them are determined as IP.

2. We estimate the mass of WD from two sources with great



Figure 8. The period distribution of the LW sources (dark-blue line), the spin (purple) and orbital (green) periods of IPs, the periods (sky-blue) of polars and the orbital (red) periods of DNe from the RK catalog (Ritter & Kolb 2003), version 7.20). The famous period gap (yellow line) and period minimum (orange dashed line) are also plotted, whose value are taken from (Knigge et al. 2011).



Figure 9. Probability of eclipsing in CVs. The break around 3.2 hours resulted by different model for CVs beyond and below the period gap.

identification for Fe XXVI and Fe XXV emission lines, i.e. $0.8 M_{\odot}$ for #21(#22), and $0.5(1.0) M_{\odot}$ for #23 if being an IP(DN).

3. We provide well-constrained fraction of polars in the whole sample, i.e., 14% as the upper limit. The estimation on fraction of non-mCVs is about 45% while the certainty is restricted by limited appreciation about their XLF. Combined with the period

distribution, we conclude that the periodic sources are mainly polars with relatively harder spectra, especially in the luminosity range that lower than $10^{32} \text{ erg s}^{-1}$. Besides, the H sources ($L > 10^{32} \text{ erg s}^{-1}$), whose emission is mostly contributed by IPs, indicate $M_{WD} \sim 0.8 M_{\odot}$, consistent with the previous result $0.8 \pm 0.07 M_{\odot}$ in (Yu et al. 2018).

4. The lower luminosity and narrow eclipsing model for orbital modulation reduced the detection rate simultaneously for periodicity. That may explain why we had no trace on non-mCVs in GCR in earlier period searching work.

5. We proved the higher detection rate, more usage of data and ignorance of observation gap for GL method compared with LS method. It is noteworthy that the shape of light curve in GL method could be modified according to different scenarios. It was applied on detection of planetary transits by using customized eclipsing model (Aigrain & Favata 2002). For the utility of GL method, there is still room for improvement in the future.

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APPENDIX A: A BRIEF INTRODUCTION TO THE GREGORY-LOREDO ALGORITHM

The basic rules for Bayesian probabilities are the sum rule:

$$p(H_i|I) + p(\bar{H}_i|I) = 1 \quad (\text{A1})$$

And the product rule:

$$p(H_i, D|I) = p(H_i|I) \cdot p(D|H_i, I) = p(D|I) \cdot p(H_i|D, I) \quad (\text{A2})$$

From equation A2 we could easily derive Bayes's theorem.

$$p(H_i|D, I) = p(H_i|I) \cdot \frac{p(D|H_i, I)}{p(D|I)} \quad (\text{A3})$$

The symbols in this work follow the same expression used in (Gregory & Loredo 1992). Throughout this work, these symbols could be briefly practically understood. H_i signifies model, D signifies dataset, I represents the ensemble of all the hypotheses considered i.e. all the model used. GL method employs stepwise function for periodic signal. Each model has $(m + 2)$ parameters: angular frequency $\omega = 2\pi/P$, P represents period; phase parameter ϕ ; and m values r_j , signifies the counts rate in each phase bin where $j=1$ to m . The following we replace H_i with M_i to denote the model where i represents the number of bins in stepwise model. Then the Bayes's theorem can be written as:

$$p(M_i|D, I) = p(M_i|I) \cdot \frac{p(D|M_i, I)}{p(D|I)} \quad (\text{A4})$$

We could write $I = M_1 + M_2 + M_3 + \dots$, where “+” stands for “or”. Thus the proposition (M_i, I) is true if and only if model M_i is true i.e. $(M_i, I) = M_i$. GL method defines odds ratio to make the model comparison.

$$O_{ij} = \frac{p(M_i|D, I)}{p(M_j|D, I)} = \frac{p(M_i|I)}{p(M_j|I)} \cdot \frac{p(D|M_i, I)}{p(D|M_j, I)} \quad (\text{A5})$$

Note that M_1 means constant model, $M_i (i=2, 3, 4 \dots N_{mod})$, where N_{mod} is the total number of models considered.) represents periodic model. The probabilities for each model can be deduced by A5

$$p(M_i|D, I) = O_{i1} \cdot p(M_1|D, I) \quad (\text{A6})$$

$$p(M_1|D, I) = \frac{\sum_{j=1}^{N_{mod}} p(M_j|D, I)}{\sum_{j=1}^{N_{mod}} O_{j1}} = \frac{1}{\sum_{j=1}^{N_{mod}} O_{j1}} \quad (\text{A7})$$

Substitute A7 into A6, we got

$$p(M_i|D, I) = \frac{O_{i1}}{\sum_{j=1}^{N_{mod}} O_{j1}} \quad (\text{A8})$$

Then the probability that the signal is periodic is :

$$p(M_m(m > 1)|D, I) = \frac{\sum_{m=2}^{m_{max}} O_{m1}}{1 + \sum_{m=2}^{m_{max}} O_{m1}} \quad (\text{A9})$$

The odds ratio can be calculated by the probability for model:

$$O_{m1} = \frac{p(M_m|D, I)}{p(M_1|D, I)} \quad (\text{A10})$$

Using Bayes's theorem shown as A4,

$$O_{m1} = \frac{p(M_m|I) \cdot p(D|M_m)}{p(M_1|I) \cdot p(D|M_1)} \quad (\text{A11})$$

Following the same assignment by (Gregory & Loredo 1992), we also consider the probability of periodic and aperiodic signals are the same. Then the priors for model can be written explicitly as :

$$p(M_1|I) = \frac{1}{2} \quad (\text{A12})$$

$$p(M_m|I) = \frac{1}{2^v}, \quad v = m_{max} - 1 \quad (\text{A13})$$

Since the essence of the algorithm is not our subject, we directly introduce the Eqn. 5.27 in (Gregory & Loredo 1992) as follows. It must be emphasized that this equation worked for the situation when the period and phase are both unknown.

$$p(D|M_m) = \frac{\Delta t^N (m-1)! N! \gamma(N+1, A_{max}) T}{2\pi A_{max} (N+m-1)! T^{N+1} \ln(\omega_{hi}/\omega_{lo})} \times \int_{\omega_{lo}}^{\omega_{hi}} \frac{d\omega}{\omega} \times \int_0^{2\pi} d\phi \frac{m^N}{W_m(\omega, \phi)} \quad (A14)$$

Substituting $m = 1$ into A14, we got:

$$p(D|M_1) = \frac{\Delta t^N N! \gamma(N+1, A_{max}) T}{A_{max} N! T^{N+1}} \quad (A15)$$

Substituting A12, A13, A14, A15 into A11, the odds ratio could be written as follows, which is the same as equation 5.28 in GL method:

$$O_{m1} = \frac{1}{2\pi \nu \ln(\omega_{hi}/\omega_{lo})} \binom{N+m-1}{N}^{-1} \times \int_{\omega_{lo}}^{\omega_{hi}} \frac{d\omega}{\omega} \times \int_0^{2\pi} d\phi \frac{m^N}{W_m(\omega, \phi)} \quad (A16)$$

In astronomical dataset, the observation always brings data gaps. For example, when the period is long and the exposure time for single observation is low, different bins may not be covered fairly. Then the initial assumptions above mentioned may fail, leading to some fake detections especially at low frequencies. In appendix B to (Gregory & Loredo 1992), a solution to this problem has been proposed. They defined a weighting factor $S(\omega, \phi)$, where $\tau_j(\omega, \phi)$ signifies the exposure time in each bin:

$$S(\omega, \phi) = \prod_{j=1}^m s_j^{-n_j} \quad (A17)$$

$$s_j(\omega, \phi) = \frac{\tau_j(\omega, \phi)}{T/m} \quad (A18)$$

Then the odds ratio should be modified as:

$$O_{m1} = \frac{1}{2\pi \nu \ln(\omega_{hi}/\omega_{lo})} \binom{N+m-1}{N}^{-1} \times \int_{\omega_{lo}}^{\omega_{hi}} \frac{d\omega}{\omega} \times \int_0^{2\pi} d\phi \frac{S(\omega, \phi) m^N}{W_m(\omega, \phi)} \quad (A19)$$

Ultimately, the probability of whether the dataset is periodic is:

$$p(\text{periodic}) = \frac{\sum_{m=2}^{m_{max}} O_{m1}}{1 + \sum_{m=2}^{m_{max}} O_{m1}} \quad (A20)$$

The posterior probability of the frequency indicates the period of the signal:

$$O_{m1}(\omega) = \frac{1}{2\pi \nu} \binom{N+m-1}{N}^{-1} \times \int_0^{2\pi} d\phi \frac{S(\omega, \phi) m^N}{W_m(\omega, \phi)} \quad (A21)$$

The period locates at $P = 2\pi/\omega$ when $O_{m1}(\omega)$ takes the highest value.

APPENDIX B: TREATMENT OF HARMONICS

To determine the intrinsic period, whether it's rotation period or orbital period, from primary period and harmonics, we should not focus on data and the significance of signals. In that the intensities of signals could not reflect the authenticity of the signal precisely. For the sake of identification, the physical mechanism of period in CVs must be introduced.

Here we take the 6th signal as an illustration, the phase-folded light curve of primary period and second harmonic show classic single-peak shape and double-peak shape, see the left two panels in Figure B1. For comparison, we also present the phase-folded light curve of J1817-2508 based on XMM-Newton observations (obsID=0601270301). We processed the EPIC PN and MOS data with the standard tool *emchain* and *epchain* in SAS v18.0.0. Similarly, the arrival time of photons were corrected at the Solar barycenter by applying the task *barycen*. Then we extract the 0.2-10 keV light curve and folded it from PN data for it has the largest effective area.

The J1817-2508, which was also called IGR J18173-2509, has been determined with pulsation at 830.70s from Swift-XRT detection. Then the signal of 1660s has also been detected from Chandra observation (Nichelli et al. 2009) and the optical period of 1690s (Bernardini et al. 2012). All the above strongly suggests that the true spin period is about 1660s, twice the first detected X-ray period, even though the two peaks in modulation are quite similar, as shown in the lower right panel in Figure B1.

The properties of J1817-2508 indicates that phase-folded light curve could be extremely deceptive under the circumstances that sources with symmetric dipole structure. We could not precisely determine the true rotation period without optical observations. However, the physical origins of periodic signals may provide additional constrains on the judgement. The double-peak shape only happens in IP with accretion column model. The two poles where accretion region lied on, would be the brightest. When we look at them at a specific angle, the two poles alternatively flitting across the face of WDs, and then produce the double-peaked pulsation. In this kind of situation, the modulation period must be the rotation period of WDs, mostly under one hour. While the second harmonics of our sources, are mostly beyond 3 hours. It would be a risky assumption if these harmonics served as spin period. On the other hand, despite the WDs in polars may have such long rotation

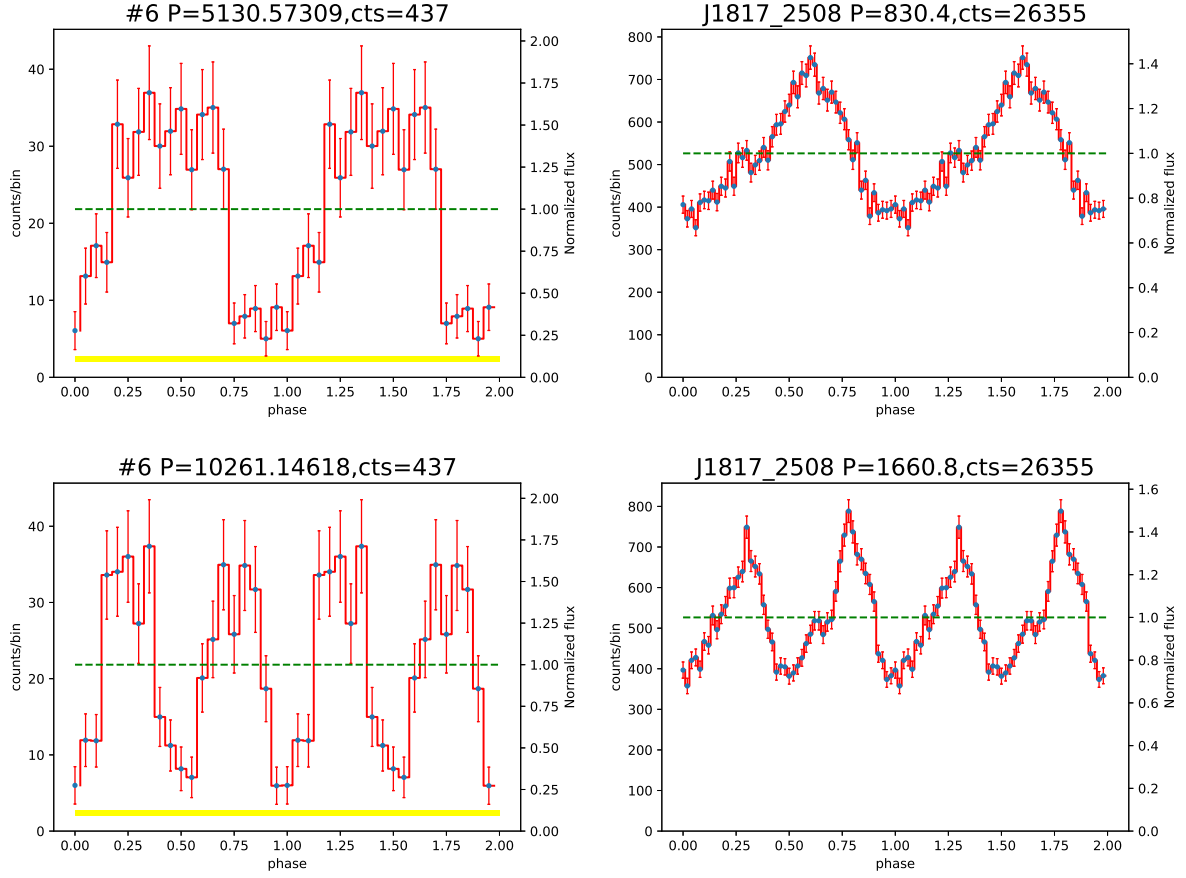


Figure B1. The top left and bottom left panel show the folded light curve of LW 6, at true period and second harmonics, respectively. The top right and bottom right panel display the folded light curve of J1817-2508. While for this source, the double-peaked shape (bottom right) at 1660s are the real signal of rotation.

period from synchronization effect, their accretion stream always falls on the single pole, emitting most of the soft X-ray radiation. Then the double-peaked pulsation are almost impossible.

In conclusion, according to the length of period in our sources, we took the single-peaked signal, normally the shortest period, as the real orbital period. The double-peaked shape in harmonics are treated as spurious signal.

APPENDIX C: FIGURES FOR PERIODIC X-RAY SOURCES**REFERENCES**

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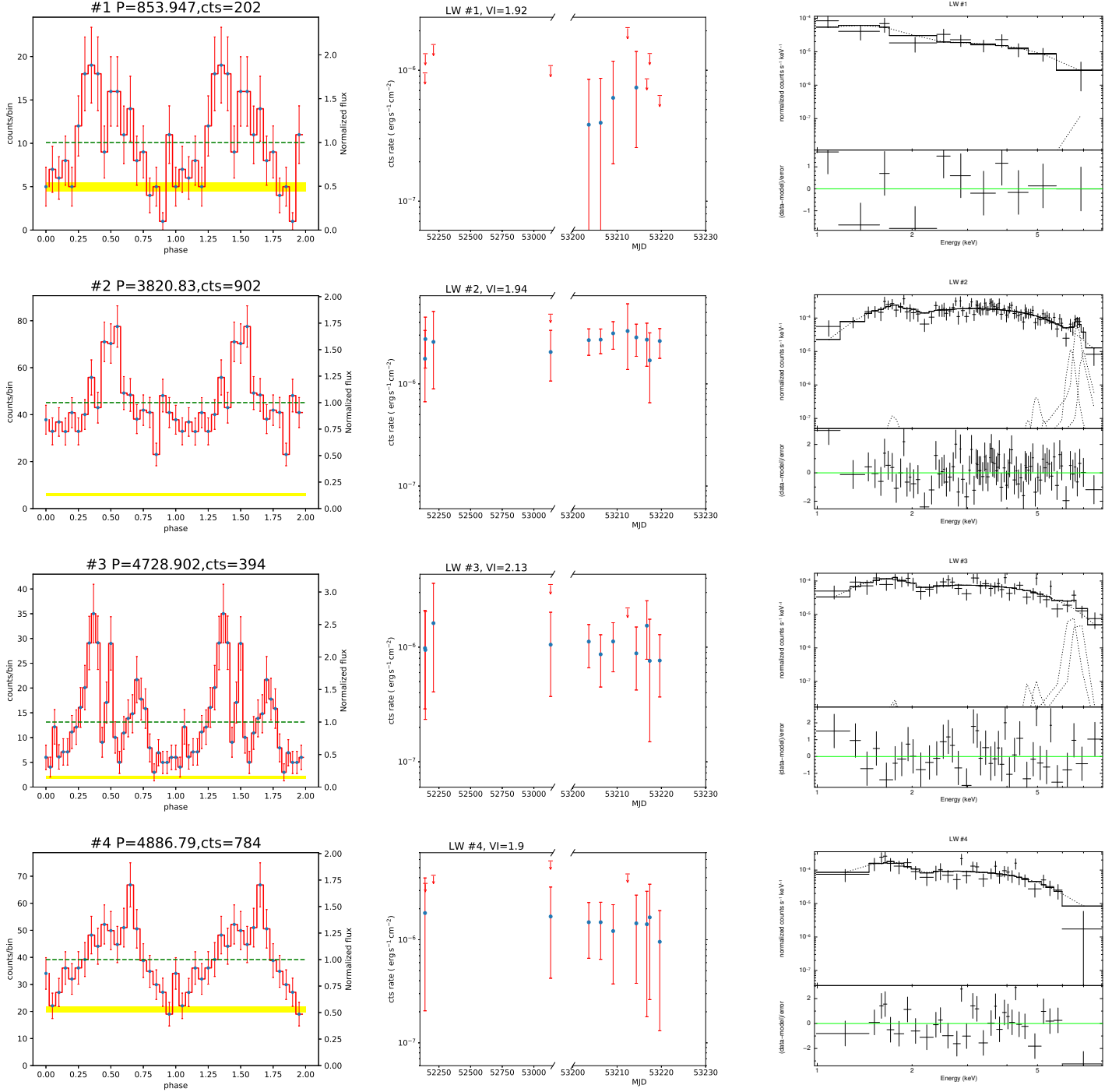


Figure C1. First figure

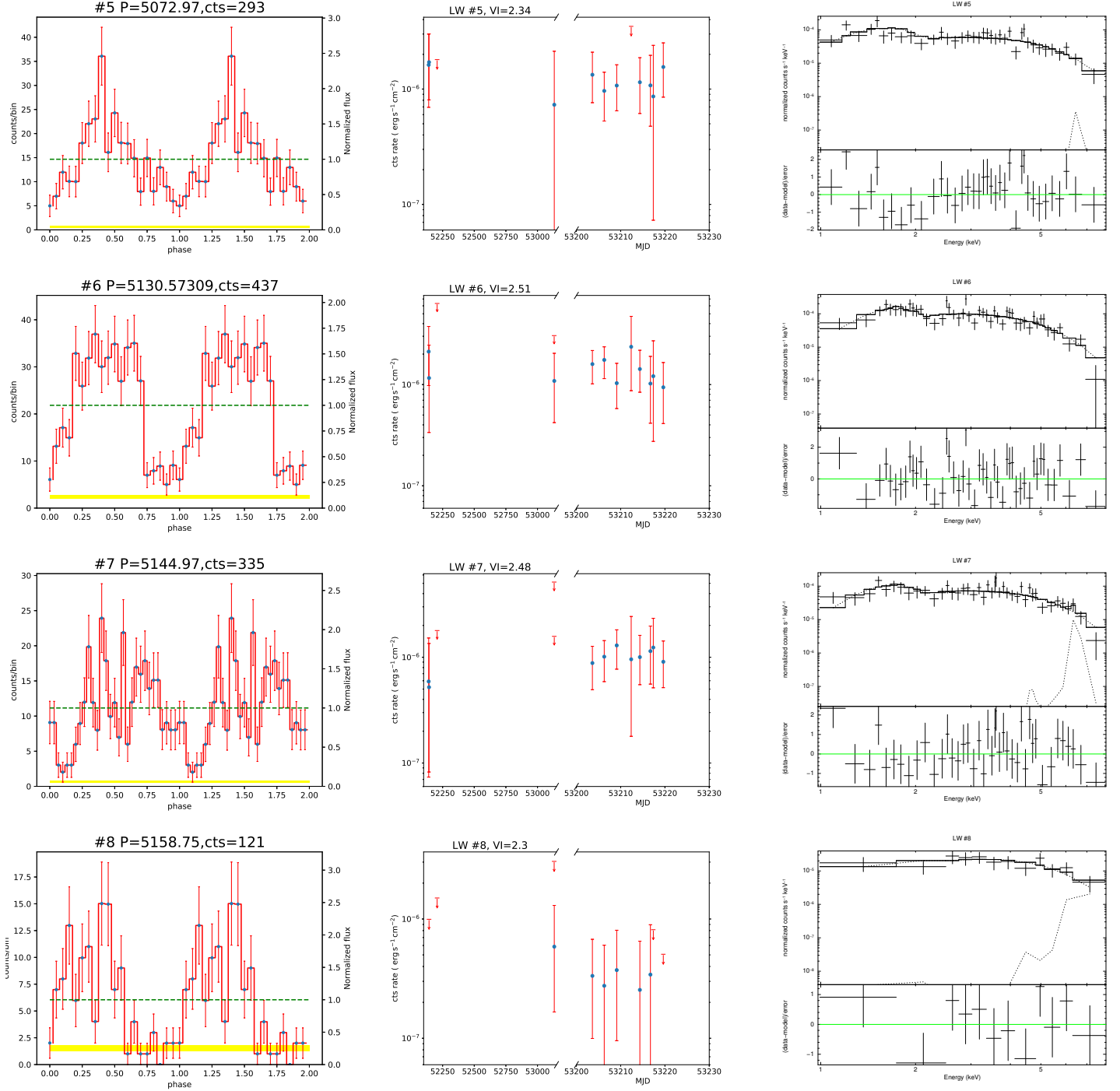


Figure C2. First figure continued

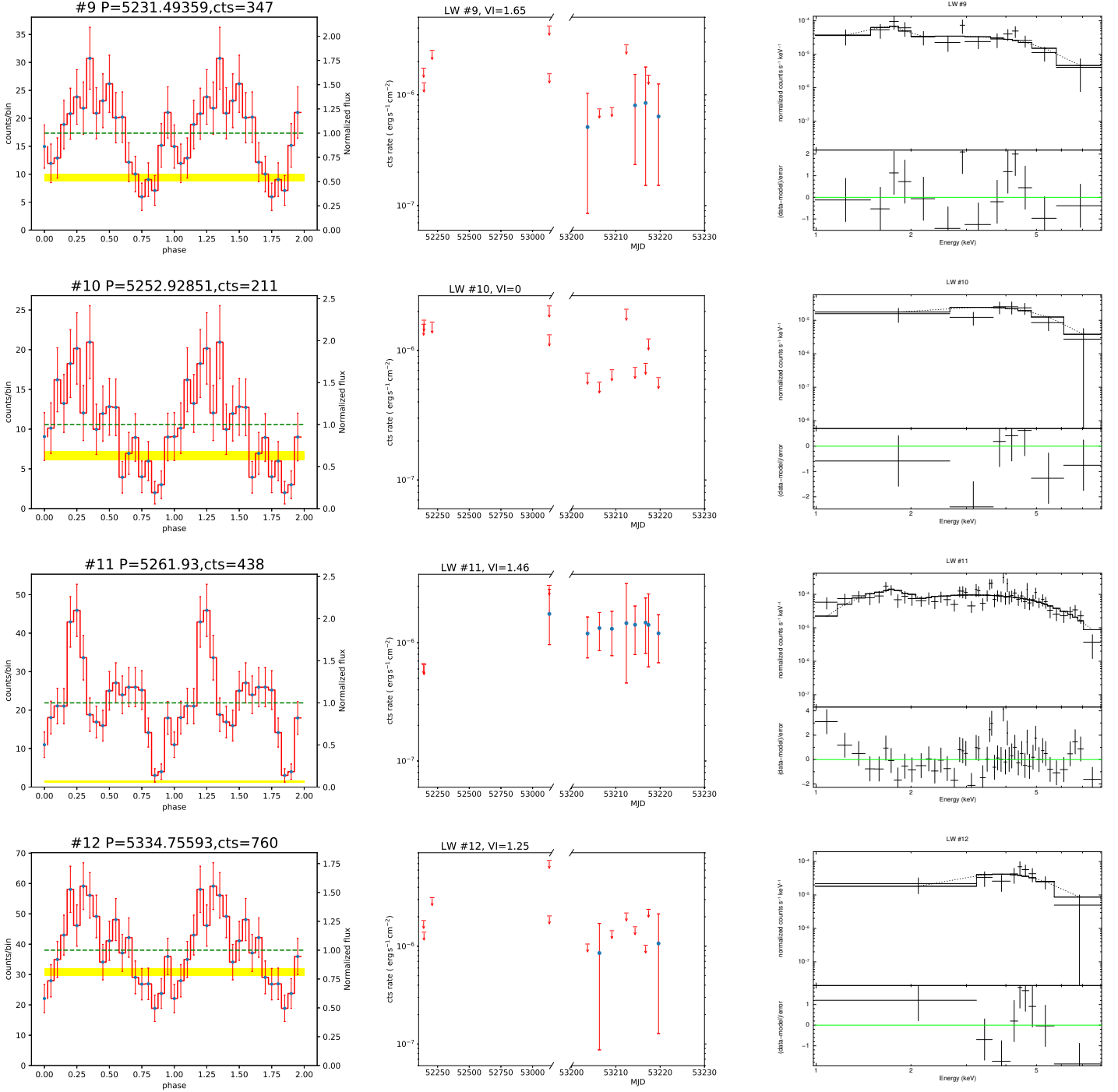


Figure C3. First figure continued

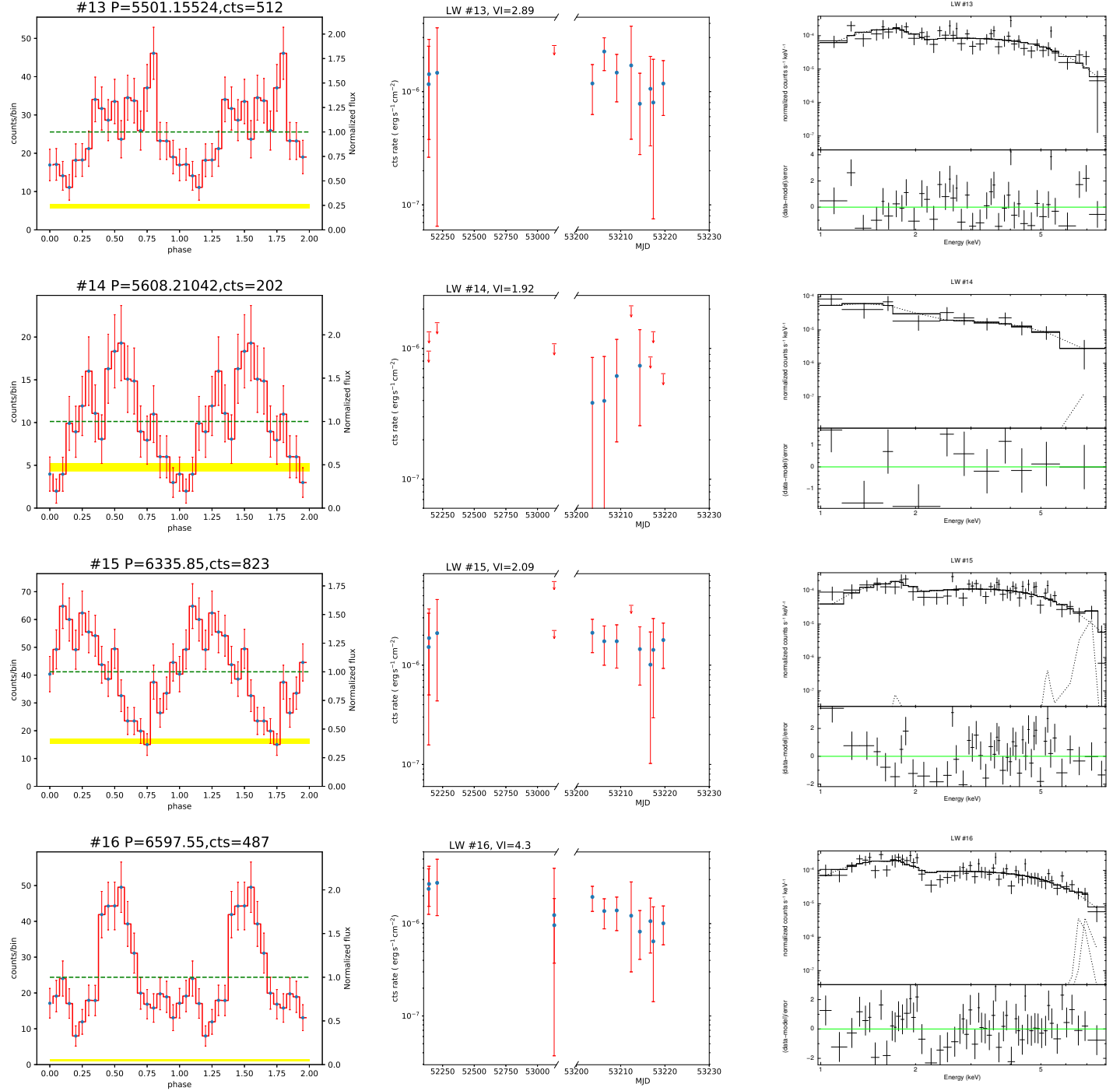


Figure C4. First figure continued

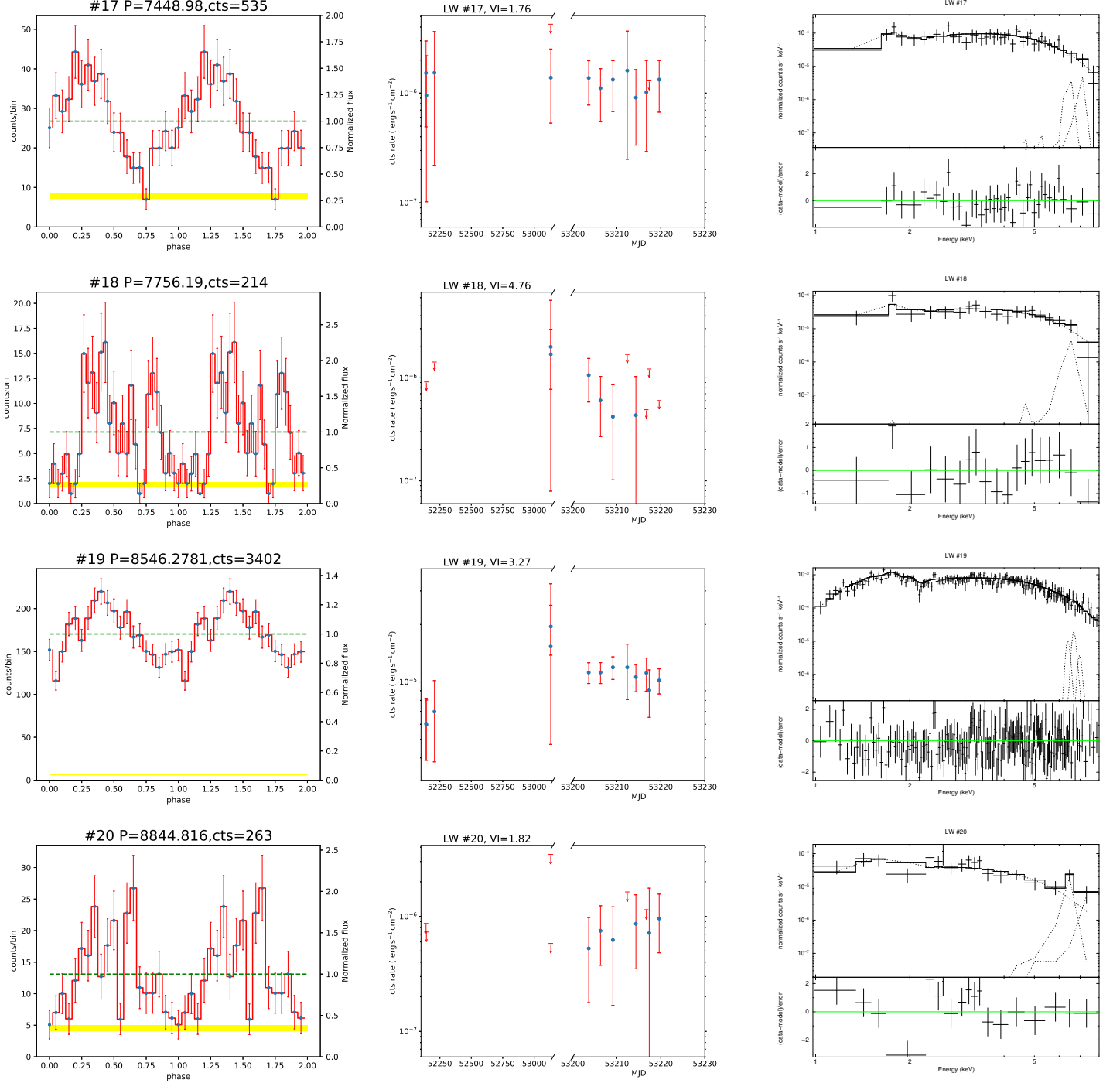


Figure C5. First figure continued

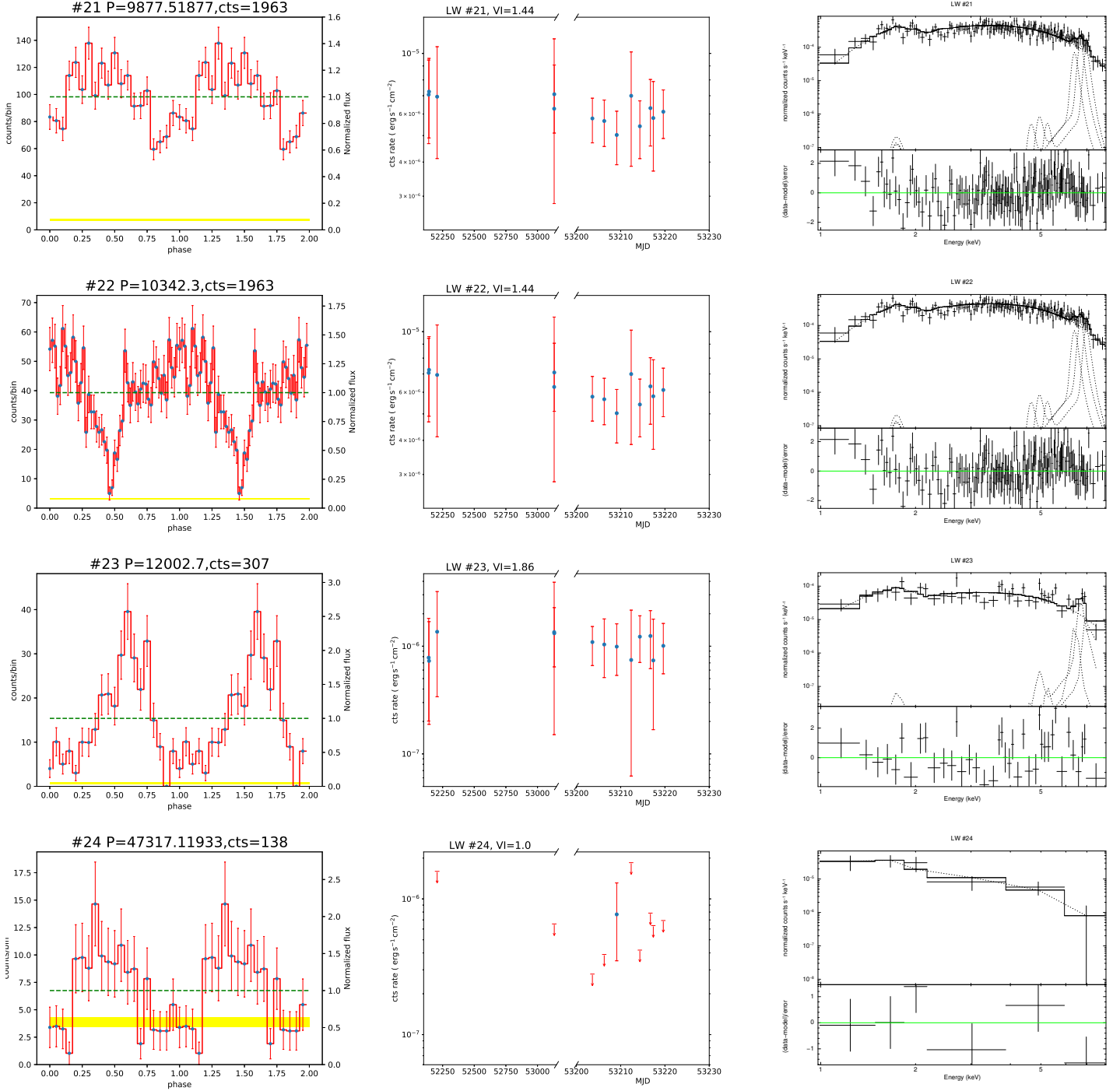


Figure C6. First figure continued