# Data Pre-processing and kNN

COMP5318 Machine Learning and Data Mining

semester 1, 2024, week 2

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Based on slides prepared by Irena Koprinska (irena.koprinska@sydney.edu.au)

Reference: Tan ch. 2





### Outline: Data Preprocessing

- Data cleaning
  - Noise
  - Missing values
- Data preprocessing
  - Data aggregation
  - Feature extraction
  - Feature subset selection
  - Converting features from one type to another
  - Normalization of feature values
- Similarity measures
  - Euclidean, Manhattan, Minkowski
  - Hamming, SMC, Jaccard coefficient
  - Cosine similarity
  - Correlation





- Data is collection of <u>examples</u> (also called *instances*, *records*, observations, objects)
- Examples are described with <u>attributes</u> (<u>features</u>, <u>variables</u>)

**Examples** 





#### Nominal and numeric attributes

- Two types of attributes:
  - nominal (categorical) their values belong to a pre-specified, finite set of possibilities
  - numeric (continuous) their values are numbers

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

sepal	sepal	petal	petal	iris type
length	width	length	width	
5.1	3.5	1.4	0.2	iris setosa
4.9	3.0	1.4	0.2	iris setosa
4.7	3.2	1.3	0.2	iris setosa
6.4	3.2	4.5	1.5	iris versicolor
6.9	3.1	4.9	1.5	iris versicolor
5.5	2.3	4.0	1.3	iris versicolor
6.5	2.8	4.6	1.5	iris versicolor
6.3	3.3	6.0	2.5	iris virginica
5.8	2.7	5.1	1.9	iris virginica

nominal numeric





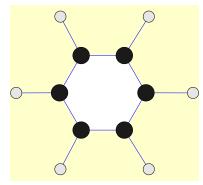
Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

#### data matrix

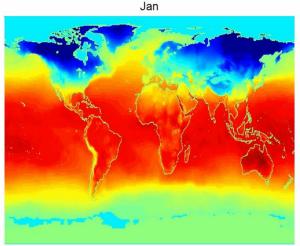
Sequential (e.g. genetic sequence)

TID	Items
1	Bread, Coke, Milk
2	Beer, Bread
3	Beer, Coke, Diaper, Milk
4	Beer, Bread, Diaper, Milk
5	Coke, Diaper, Milk

#### transaction data



graph (e.g. molecular structure)



Average monthly temperature spatio-temporal



# **Data cleaning**

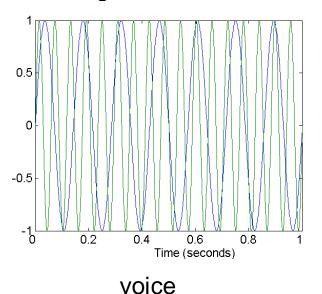


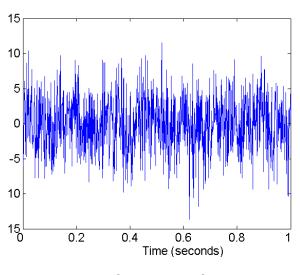


- Data is not perfect
- Noise due to
  - distortion of values
  - addition of spurious examples
  - inconsistent and duplicate data
- Missing values



- Human errors when entering data or limitations of measuring instruments, flaws in the data collection process
- 1) Noise distortion of values
  - Ex: distortion of human voice when talking on a poor phone line
    - Higher distortion => the shape of the signal may be lost

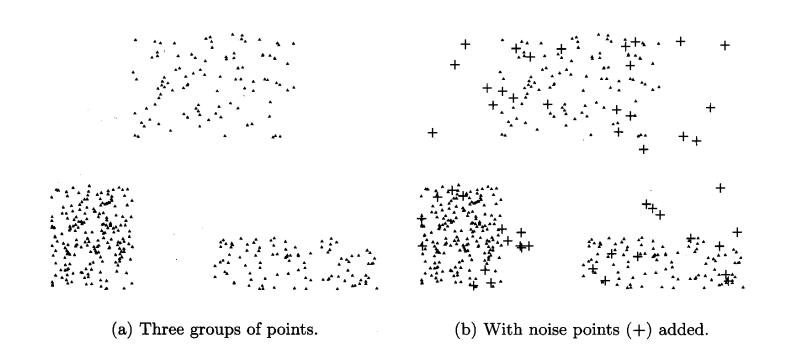




voice + noise



- 2) Noise addition of spurious examples
  - Some are far from the other examples (are outliers), some are mixed with the non-noisy data





- 3) Noise inconsistent and duplicate data
  - E.g. negative weight and height values, non-existing zip codes, 2 records for the same person need to be detected and corrected
  - Typically easier to detect and correct than the other two types of noise

- Reducing noise types 1) and 2):
  - Using signal and image processing and outlier detection techniques before DM
  - Using ML algorithms that are more robust to noise give acceptable results in presence of noise



#### Dealing with missing values

- Various methods, e.g.:
- 1) Ignore all examples with missing values
- Can be done if small % missing values

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
?	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	?	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	?	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

- 2) Estimate the missing values by using the remaining values
- Nominal attributes replace the missing values for attribute A with
  - the most common value for A or
  - the most common value among the examples with the same class (if supervised learning)
- Numerical replace with the average value of the nearest neighbors (the most similar examples)



# **Data preprocessing**

## Data preprocessing



- Data aggregation
- Dimensionality reduction
- Feature extraction
- Feature subset selection
- Converting attributes from one type to another
- Normalization



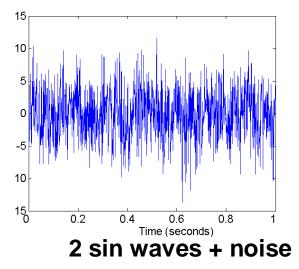


- Combining two or more attributes into one purpose:
  - Data reduction less memory and computation time; may allow the use of computationally more expensive ML algorithms
  - Change of scale provides high-level view
    - E.g. cities aggregated into states or countries
  - More stable data aggregated data is less variable than nonaggregated
    - E.g. consumed daily food (food\_day1, food\_day2, etc.) aggregated into weekly food to get a more reliable understanding of the diet (carbohydrates, fat, protein, etc.)
  - Disadvantage potential loss of interesting details

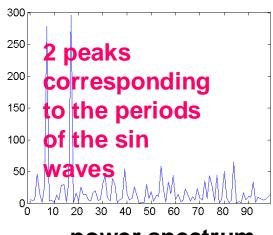
#### Feature extraction



- Feature extraction is the creation of features from raw data very important task
  - Requires domain expertise
  - Ex: classifying images into outdoors or indoors
     raw data: color value for each pixels
     extracted features: color histogram, dominant color, edge histogram, etc.
- May require mapping data to a new space, then extract features
  - The new space may reveal important characteristics



Fourier transform →



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#### Feature subset selection

- The process of removing irrelevant and redundant features and selecting a small set of features that are necessary and sufficient for good classification
- Very important for successful classification
- Good feature selection typically improves accuracy
- Using less features also means
  - Faster building of the classifiers, i.e. reduces computational cost
  - (Often) more compact and easier to interpret classification rule

#### Useful references:

Kohavi, R., John, H.: Wrappers for feature subset selection, Artificial Intelligence, vol. 97, issue 1-2 (1997), pp. 273 – 324

Hall, M.: Correlation-based Feature Selection for Discrete and Numeric Class Machine Learning. 17th Int. Conf. on Machine Learning (ICML). Morgan Kaufmann (2000) 359-366



#### Feature subset selection methods

- Brute force try all possible combinations of features as input to a ML algorithm, select the best one (impossible)
- Embedded some ML algorithms can automatically select features (e.g. decision trees)
- Filter select features before the ML algorithm is run; the feature selection is independent of the ML algorithm
  - Based on statistical measures, e.g. information gain, mutual information, odds ratio, etc.
  - Correlation-based feature selection, Relief
- Wrapper select the best subset for a given ML algorithm; use the ML algorithm as a black box to evaluate different subsets and select the best

Feature selection is well studied in ML and there are many excellent methods!

### Feature weighting



- Can be used instead of feature reduction or in conjunction with it
- The more important features are assigned a higher weight, the less important – lower weight
  - manually based on domain knowledge
  - automatically some classification algorithms do it (e.g. boosting) or may do it if this option is selected (k-nearest neighbor)
- Key idea: features with higher weights play more important role in the construction of the ML model



#### Converting attributes from one type to another

- Converting numeric attributes to nominal (discretization)
- Converting numeric and nominal attributes to binary attributes (binarization)
- Needed as some ML algorithms work only with numeric, nominal or binary attributes



- Converting categorical and numeric attributes into binary
  - There is no best method; the best one is the one that works best for a given ML algorithm but all possibilities cannot be evaluated
- Simple technique
  - categorical attribute -> integer -> binary
  - numeric attribute -> categorical -> integer -> binary

Table 2.5. Conversion of a categorical attribute to three binary attributes.

Categorical Value	Integer Value	$x_1$	$x_2$	$x_3$
awful	0,	0	0	0
$poor \ OK$	. 1	0	0	1
OK	2	0	1	0
good	3	0	1	1
$\_\_\_great$	4	1	0	0

categorical -> binary

Table 2.6. Conversion of a categorical attribute to five asymmetric binary attributes.

Categorical Value	Integer Value	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$
awful	0	1	0	0	0	0
poor	1	0	1	0	0	0
OK	<b>2</b>	0	0	1	0	0
$egin{aligned} good \ great \end{aligned}$	3	0	0	0	1	0
great	4	0	0	0	0	1

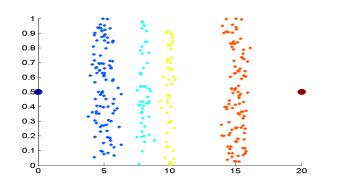




- Converting numeric attributes into nominal
- 2 types: unsupervised and supervised
  - Unsupervised class information is not used
  - Supervised class information is used
- Decisions to be taken

numeric -> nominal

- How many categories (intervals)?
- Where should the splits be?



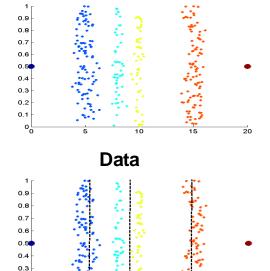
2-dim data; x and y are numeric attributes

Goal: convert x from numeric to nominal



## Unsupervised discretization

- How many intervals?
  - The user specifies them, e.g. 4
- Where should the splits be?
  - 3 methods



**Equal frequency** 

Equal width

K-means

- equal width 4 intervals with the same width [0,5), [5, 10) etc.
- equal frequency 4
   intervals with the same
   number of points in each
   of them
- clustering (e.g. k-means)
   4 intervals determined
   by a clustering method



#### Normalization and standardization

- Attribute transformation to a new range, e.g. [0,1]
- Used to avoid the dominance of attributes with large values over attributes with small values
- Required for distance based ML algorithms; some other algorithms also work better with normalized data
  - E.g. age (in years) and annual *income* (in dollars) have different scales A=[20, 40 000]
     B=[40, 60 000]
     D(A,B)=|20-40| + |40 000-60 000|=20 020
     Difference in *income* dominates, age doesn't contribute
- Solution: first normalize or standardize then calculate distance



#### Normalization and standardization (2)

#### Performed for <u>each</u> attribute

#### **Normalization**

(also called min-max scaling):

$$x' = \frac{x - \min(x)}{\max(x) - \min(x)}$$

x – original value

x' – new value

x – all values of the attribute; a vector

min(x) and max(x) – min and max values of the attribute (of the vector x)

 $\mu(x)$  - mean value of the attribute

 $\sigma(x)$  - standard deviation of the attribute

#### Standardization:

$$x' = \frac{x - \mu(x)}{\sigma(x)}$$

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### Normalization - example

Examples with 2 attributes: age and income:

A=[20, 40 000]

B=[40, 60 000]

 $C=[25, 30\ 000]$ 

. .

Suppose that:

for age: min = 0, max=100

for *income*: min=0, max=100 000

#### After normalization:

A=[0.2, 0.4]

B=[0.4, 0.6]

C=[0.25, 0.3]

. . .

D(A,B)=|0.2-0.4| + |0.4-0.6|=0.4, i.e. *income* and *age* contribute equally



# **Similarity measures**

## Measuring similarity



- Many ML algorithms require to measure the similarity between 2 examples
- 2 measures
  - Distance
  - Correlation



#### Euclidean and Manhattan distance

- Distance measures for numeric attributes
  - A, B examples with attribute values  $a_1$ ,  $a_2$ ,...,  $a_n$  &  $b_1$ ,  $b_2$ ,...,  $b_n$
  - E.g. A= [1, 3, 5], B=[1, 6, 9]
- Euclidean distance (L2 norm) most frequently used

$$D(A,B) = \sqrt{(a_1 - b_1)^2 + (a_2 - b_2)^2 + \dots + (a_n - b_n)^2}$$

$$D(A,B) = sqrt ((1-1)^2+(3-6)^2+(5-9)^2)=5$$

Manhattan distance (L1 norm)

$$D(A,B) = |a_1 - b_1| + |a_2 - b_2| + \dots + |a_n - b_n|$$

$$D(A,B)=|1-1|+|3-6|+|5-9|=7$$





Minkowski distance – generalization of Euclidean & Manhattan

$$D(A,B) = (|a_1 - b_1|^q + |a_2 - b_2|^q + \dots + |a_n - b_n|^q)^{1/q}$$

*q* – positive integer

- Weighted distance each attribute is assigned a weight according to its importance (requires domain knowledge)
  - Weighted Euclidean:

$$D(A,B) = \sqrt{w_1|a_1 - b_1|^2 + w_2|a_2 - b_2|^2 + \dots + w_n|a_n - b_n|^2}$$



## Similarity between binary vectors

- Hamming distance = Manhattan for binary vectors
  - Counts the number of different bits

$$D(A,B) = |a_1 - b_1| + |a_2 - b_2| + \dots + |a_n - b_n|$$

```
A = [1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]
B = [0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1]
D(A,B) = 3
```

Similarity coefficients

f00: number of matching 0-0 bits

f01: number of matching 0-1 bits

f10: number of matching 1-0 bits

f11: number of matching 1-1 bits

Calculate these coefficients for the example above!

Answer: 
$$f01 = 2$$
,  $f10 = 1$ ,  $f00 = 7$ ,  $f11 = 0$ 



#### Similarity between binary vectors (2)

Simple Matching Coefficient (SMC) - matching 1-1 and 0-0 / num. attributes
 SMC = (f11+f00)/(f01+f10+f11+f00)

```
Ex.: A = [1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]

B = [0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1]

f01 = 2, f10 = 1, f00 = 7, f11 = 0

SMC = (0+7) / (2+1+0+7) = 0.7
```

- Task: Suppose that A and B are the supermarket bills of 2 customers. Each product in the supermarket corresponds to a different attribute.
  - attribute value = 1 product was purchased
  - attribute value = 0 product was not purchased
- SMC is used to calculate the similarity between A and B. Is there any problem using SMC?



#### Similarity between binary vectors (2)

- Yes, SMC will find all customer transactions (bills) to be similar
- Reason: The number of products that are <u>not</u> purchased in a transaction is much bigger than the number of products that are purchased
- => f00 will be very high (not purchased products)
  - f11 will be low (purchased products)
  - f00 will be much higher than f11 and its effect will be lost

$$SMC = (f11+f00)/(f01+f10+f11+f00)$$

 => More generally, the problem is that the 2 vectors A and B contain many 0s, i.e. are very sparse => SMC is not suitable for sparse data

$$A = [1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$
$$B = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1]$$



- An alternative: Jaccard coefficient
  - counts matching 1-1 and ignores matching 0-0
     J=f11/(f01+f10+f11)

A = 
$$[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$
  
B =  $[0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1]$   
 $f01 = 2$ ,  $f10 = 1$ ,  $f00 = 7$ ,  $f11 = 0$   
J =  $0 / (2 + 1 + 0) = 0$  (A and B are dissimilar)

Compare with SMC:

SMC= (0+7) / (2+1+0+7) = 0.7 (A and B are highly similar - incorrect)





- Useful for sparse data (both binary and non-binary)
- Widely used for classification of text documents

$$\cos(A, B) = \frac{A \bullet B}{\|A\| \|B\|}$$

- - vector dot product, ||A|| length of vector A
- Geometric representation: measures the angle between A and B
  - Cosine similarity=1 => angle(A,B)=0°
  - Cosine similarity =0 => angle (A,B)=90°



### Cosine similarity - example

Two document vectors:

$$d_1 = 3205000200$$
  
 $d_2 = 1000000102$ 

$$\cos(A, B) = \frac{A \bullet B}{\|A\| \|B\|}$$

$$d_1 \bullet d_2 = 3*1 + 2*0 + 0*0 + 5*0 + 0*0 + 0*0 + 0*0 + 2*1 + 0*0 + 0*2 = 5$$

$$||d_1|| = (3*3 + 2*2 + 0*0 + 5*5 + 0*0 + 0*0 + 0*0 + 2*2 + 0*0 + 0*0)^{1/2} = (42)^{-1/2} = 6.481$$

$$||d_2|| = (1*1 + 0*0 + 0*0 + 0*0 + 0*0 + 0*0 + 0*0 + 1*1 + 0*0 + 2*2)^{-1/2} = (6)^{-1/2} = 2.245$$

$$= \cos(d_1, d_2) = 0.3150$$





- Measures *linear* relationship between numeric attributes
- Pearson correlation coefficient between data objects (instances) x and y with dimensionality n

$$corr(\mathbf{x}, \mathbf{y}) = \frac{covar(\mathbf{x}, \mathbf{y})}{std(\mathbf{x}) std(\mathbf{y})}$$

where:

$$mean(\mathbf{x}) = \frac{\sum_{k=1}^{n} x_k}{n} \quad std(\mathbf{x}) = \sqrt{\frac{\sum_{k=1}^{n} (x_k - mean(\mathbf{x}))^2}{n-1}}$$

$$\operatorname{covar}(\mathbf{x}, \mathbf{y}) = \frac{1}{n-1} \sum_{k=1}^{n} (x_k - mean(x))(y_k - mean(y))$$

- Range: [-1, 1]
  - -1: perfect negative correlation
  - +1: perfect positive correlation
  - 0: no correlation



### Correlation - examples

- Ex1: corr(x,y)=? x=(-3, 6, 0, 3, -6) y=(1,-2, 0,-1, 2)
- Ex2: corr(x,y)=? x=(3, 6, 0, 3, 6) y=(1, 2, 0, 1, 2)
- Ex3: corr(x,y)=?
  x=(-3, -2, -1, 0, 1, 2, 3)
  y=(9, 4, 1, 0, 1, 4, 9)





$$x=(-3, 6, 0, 3, -6)$$

$$y=(1,-2,0,-1,2)$$

$$corr(x,y) = -1$$

perfect negative linear correlation

$$x=(3, 6, 0, 3, 6)$$

$$y=(1, 2, 0, 1, 2)$$

$$corr(x,y) = +1$$

perfect positive linear correlation

$$x=(-3, -2, -1, 0, 1, 2, 3)$$

$$y=(9, 4, 1, 0, 1, 4, 9)$$

$$corr(x,y) = 0$$

no linear correlation

However, there is a non-linear

relationship: y=x<sup>2</sup>



### Correlation – visual evaluation

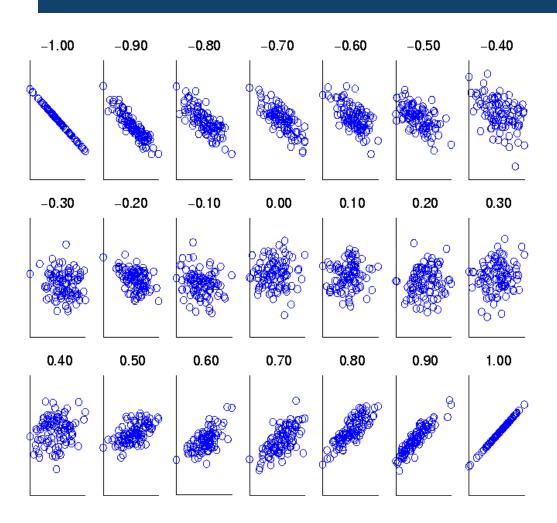


Figure 5.11. Scatter plots illustrating correlations from -1 to 1.



### Distance measures for nominal attributes

- Various options depending on the task and type of data type; requires domain expertise
- E.g.:
  - difference =0 if attribute values are the same
  - difference =1 if they are not
  - Example: 2 attributes = temperature and windy
    - temperature values: low and high
    - windy values: yes and no

```
A={high, no}
B={high, yes}
d(A,B) =(0+1)<sup>1/2</sup>=1 (Euclidean distance)
```

# Nearest Neighbor algorithm

COMP5318 Machine Learning and Data Mining semester 2, 2021, week 2

#### **Nguyen Hoang Tran**

Based on slides prepared by Irena Koprinska (irena.koprinska@sydney.edu.au)

Reference: Witten ch.4: 91-96, 135-141, 115-119; Tan ch.4: 208-212





### Classification task – setup and an example

- Given: a set of *labelled* examples (labelled with the class values)
  - 14 examples
  - 4 attributes (features): outlook, temperature, humidity and windy
  - class: play
- Task: Build a model (classifier) that can be used to predict the class of new (unseen) examples

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

- e.g. predict the class (yes or no) of this new example: outlook=sunny, temp=hot, humidity=low, windy=true
- Examples used to build the model are called training set
- To evaluate performance, we measure the accuracy on test data
  - Test data hasn't been used to build the classifier; it is also labelled
  - accuracy proportion of correctly classified test examples



### Two types of attributes: categorical and numeric

- categorical (nominal) their values belong to a pre-specified, finite set of possibilities
- numeric (continuous) their values are numbers

outlook	temp.	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

sepal	sepal	petal	petal	iris type
length	width	length	width	
5.1	3.5	1.4	0.2	iris setosa
4.9	3.0	1.4	0.2	iris setosa
4.7	3.2	1.3	0.2	iris setosa
6.4	3.2	4.5	1.5	iris versicolor
6.9	3.1	4.9	1.5	iris versicolor
5.5	2.3	4.0	1.3	iris versicolor
6.5	2.8	4.6	1.5	iris versicolor
6.3	3.3	6.0	2.5	iris virginica
5.8	2.7	5.1	1.9	iris virginica
• • •				

categorical

numeric

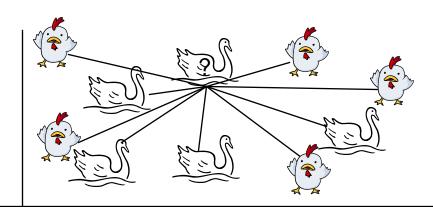


# **Nearest Neighbor Algorithm**



### Nearest neighbour algorithm

- Remember all training examples
- To make a prediction for a new unlabelled example:
  - Find the nearest training example to it using a distance measure
  - The class label of the nearest neighbor will be the predicted label for the new example





### Nearest neighbor - example

#### Ex.1

The dataset below consists of 4 examples described with 3 numeric features (a1, a2 and a3); the class has 2 values: yes and no.

What will be the prediction of the Nearest Neighbor algorithm using the Euclidean distance for the following new example: a1=2, a2=4, a3=2?

	a1	a2	a3	class
1	1	3	1	yes
2	3	5	2	yes
3	3	2	2	no
4	5	2	3	no

Exercise adapted from M. Kubat, Introduction to Machine Learning, Springer, 2017



The dataset below consists of 4 examples described with 3 numeric features (a1, a2 and a3); the class has 2 values: yes and no.

What will be the prediction of the Nearest Neighbor algorithm using the Euclidean distance for the following new example: a1=2, a2=4, a3=2?

	a1	a2	a3	class
1	1	3	1	yes
2	3	5	2	yes
3	3	2	2	no
4	5	2	3	no

D(new, ex1) = 
$$sqrt[(2-1)^2+(4-3)^2+(2-1)^2]=sqrt(3)$$
 yes D(new, ex2) =  $sqrt[(2-3)^2+(4-5)^2+(2-2)^2]=sqrt(2)$  yes D(new, ex3) =  $sqrt[(2-3)^2+(4-2)^2+(2-2)^2]=sqrt(5)$  no D(new, ex4) =  $sqrt[(2-5)^2+(4-2)^2+(2-3)^2]=sqrt(14)$  no

The closest nearest neighbor is ex. 2, hence the nearest neighbor algorithm predicts class=yes for the new example



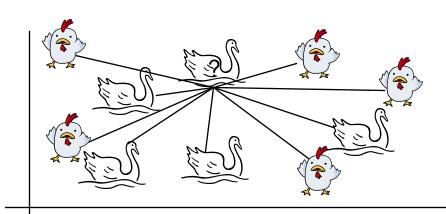
### Computational complexity

- No model is built; just storing training examples
- Classification (prediction for a new example)
  - Compare each unseen example with each training example
  - If m training examples with dimensionality n => lookup for 1 unseen example takes m\*n computations, i.e. O(mn)
- Memory requirements you need to remember each training example,
   O(mn)
- Impractical for large data due to time and memory requirements
- However, there are variations allowing to find the nearest neighbours more efficiently
  - e.g. by using more efficient data structures such as KD-trees and ball trees, see Witten p.136-141



### From 1-nearest neighbor to k-nearest neighbor

- Using the closest 1 example (to predict the class of the new example) is called 1-Nearest Neighbor
- Using the k closest examples is called k-Nearest Neighbor
  - majority voting is used to take the decision
- What will be the prediction of 3-Nearest Neighbor?





### k-nearest neighbor

- K-Nearest Neighbor is very sensitive to to the value of k
  - rule of thumb: k ≤ sqrt(#training\_examples)
  - commercial packages typically use k=10
- Using more nearest neighbors increases the robustness to noisy examples
- K-Nearest Neighbor can be used not only for classification, but also for regression
  - The prediction will be the average value of the class values (numerical) of the k nearest neighbors



### k-nearest neighbor - example

The dataset below consists of 4 examples described with 3 numeric features (a1, a2 and a3); the class has 2 values: yes and no.

What will be the prediction of the 3-Nearest Neighbor algorithm using the Euclidean distance for the following new example: a1=2, a2=4, a3=2?

	a1	a2	a3	class
1	1	3	1	yes
2	3	5	2	yes
3	3	2	2	no
4	5	2	3	no

D(new, ex1) = 
$$sqrt[(2-1)^2+(4-3)^2+(2-1)^2]=sqrt(3)$$
 yes D(new, ex2) =  $sqrt[(2-3)^2+(4-5)^2+(2-2)^2]=sqrt(2)$  yes D(new, ex3) =  $sqrt[(2-3)^2+(4-2)^2+(2-2)^2]=sqrt(5)$  no D(new, ex4) =  $sqrt[(2-5)^2+(4-2)^2+(2-3)^2]=sqrt(14)$  no

The closest 3 nearest neighbors are ex.2 (yes), ex.1 (yes) and ex.3 (no); the majority class is yes. Hence, 3-Nearest Neighbor predicts class =yes



### Weighted nearest neighbor

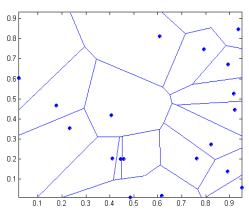
- Idea: Closer neighbors should count more than distant neighbors
- Distance-weighted nearest-neighbor algorithm
  - Find the k nearest neighbors
  - Weight their contribution based on their distance to the new example
    - bigger weight if they are closer
    - smaller weight if they are further
    - e.g. the vote can be weighted according to the distance weight  $w = 1/d^2$



### Decision boundary of 1-nearest neighbor

- Nearest neighbor classifiers produced decision boundaries with an arbitrary shape
- The 1-nearest neighbor boundary is formed by the edges of the Voronoi diagram that separate the points of the two classes
- Voronoi region:
  - Each training example has an associated Voronoi region; it contains the data points for which this is the closest example







### K-nearest neighbor - discussion

- Often very accurate
- Has been used in statistics since 1950s
- Slow for big datasets
- Distance-based requires normalization
- Produces arbitrarily shaped decision boundary defined by a subset of the Voronoi edges
- Not effective for high-dimensional data (data with many features)
  - The notion of "nearness" is not effective in high dimensional data
  - Solution dimensionality reduction and feature selection
- Sensitive to the value of k

## Q&A

