Lecture 10.2: Kruskal's Algorithm

```
Kruskal()
   T = \emptyset;
   for each v \in V
      MakeSet(v);
   sort E by increasing edge weight w
   for each (u,v) \in E (in sorted order)
      if FindSet(u) # FindSet(v)
          T = T | \{\{u,v\}\}\};
          Union(FindSet(u), FindSet(v));
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