

Lecture 9.2: Prim's Algorithm

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MST-Prim( $G, w, r$ )
```

```
   $Q = V[G];$ 
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```
  for each  $u \in Q$ 
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     $\text{key}[u] = \infty;$ 
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   $\text{key}[r] = 0;$ 
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   $p[r] = \text{NULL};$ 
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  while ( $Q$  not empty)
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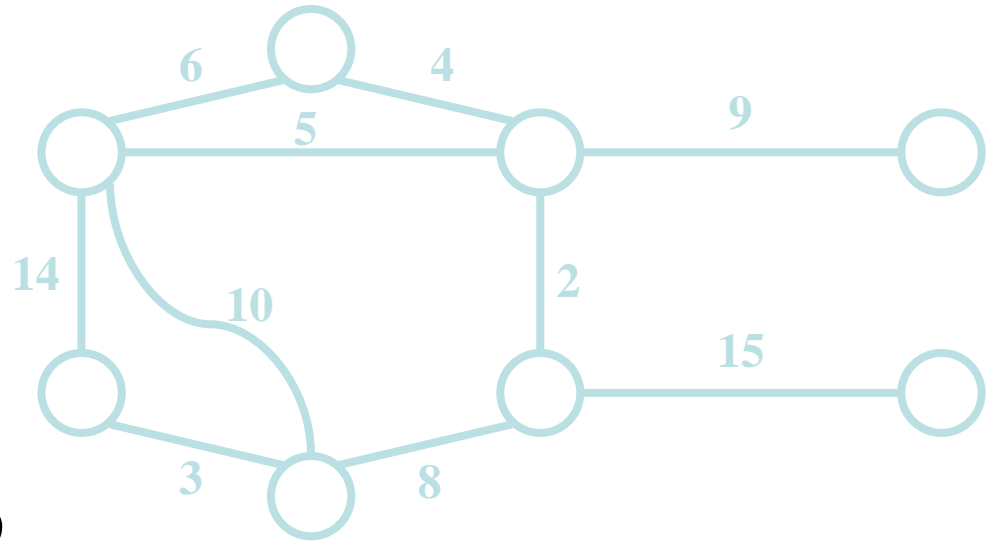
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     $u = \text{ExtractMin}(Q);$ 
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    for each  $v \in \text{Adj}[u]$ 
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      if ( $v \in Q$  and  $w(u, v) < \text{key}[v]$ )
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         $p[v] = u;$ 
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Run on example graph

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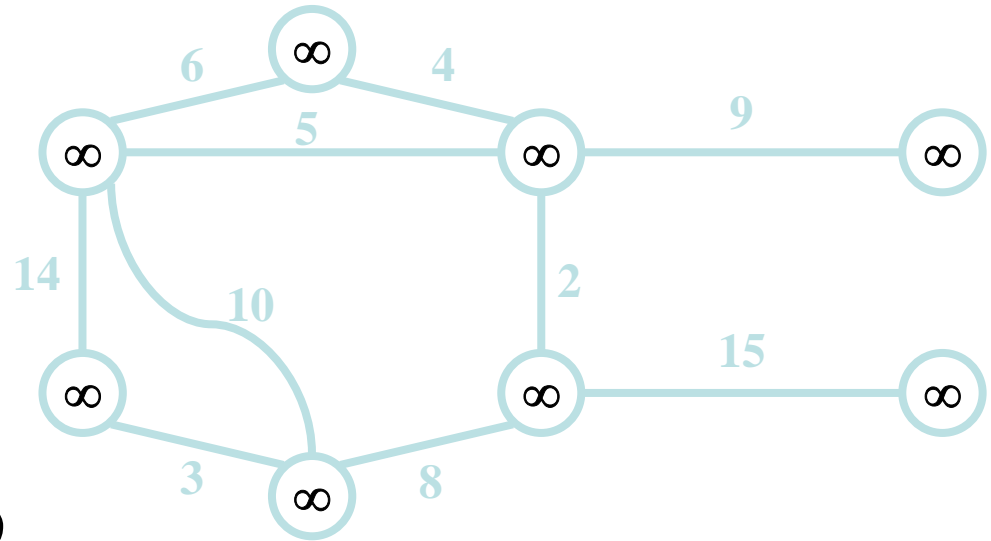
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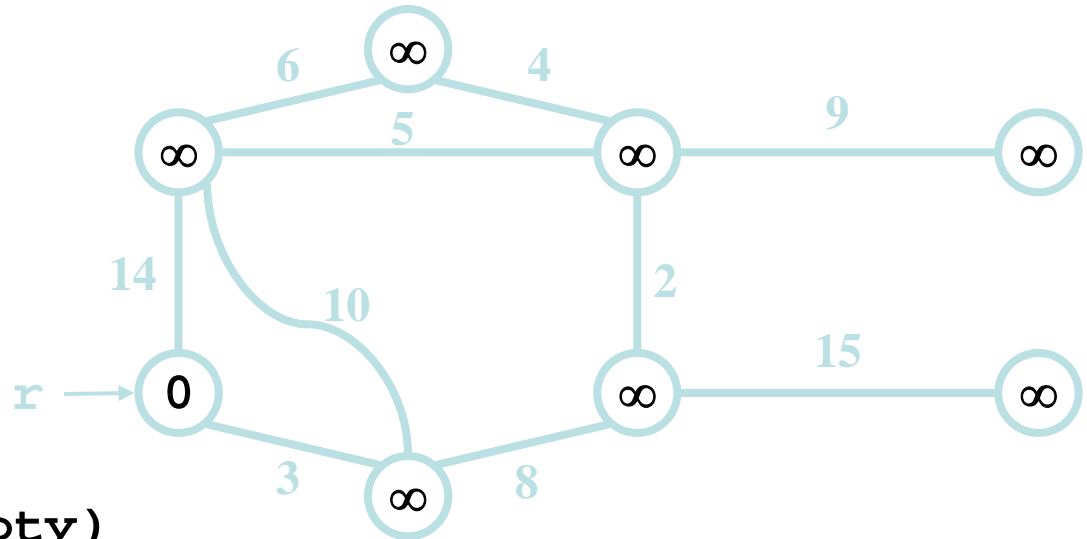
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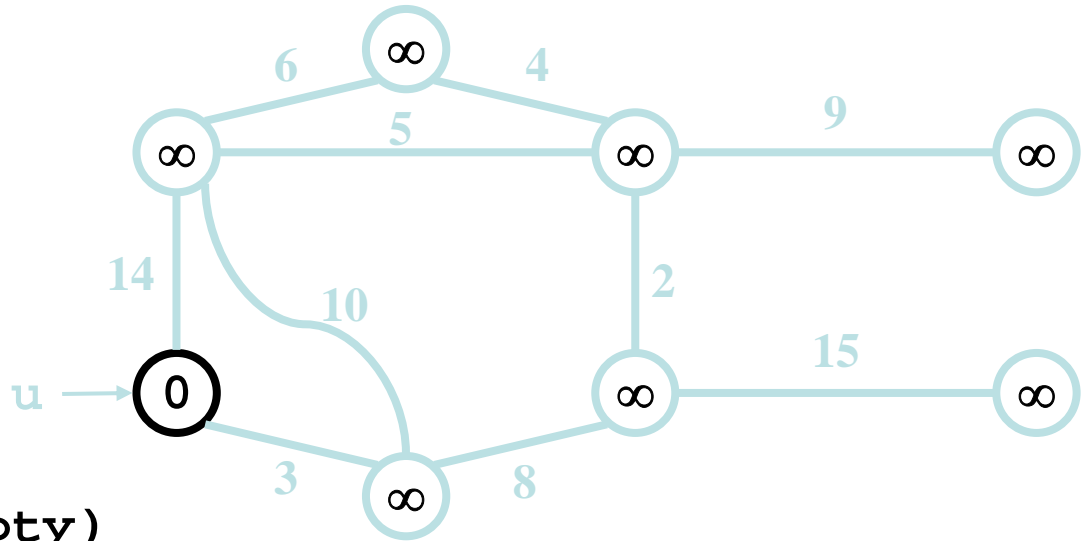
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     $u = \text{ExtractMin}(Q);$  Black vertices have been removed from  $Q$ 
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    for each  $v \in \text{Adj}[u]$ 
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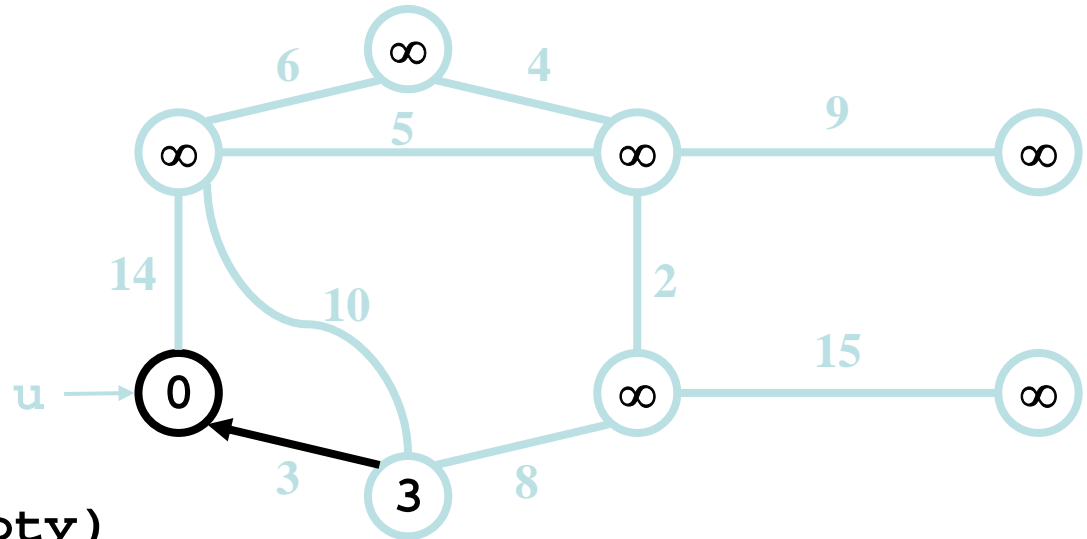
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     $u = \text{ExtractMin}(Q);$  Black arrows indicate parent pointers
```

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    for each  $v \in \text{Adj}[u]$ 
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`while (Q not empty)`

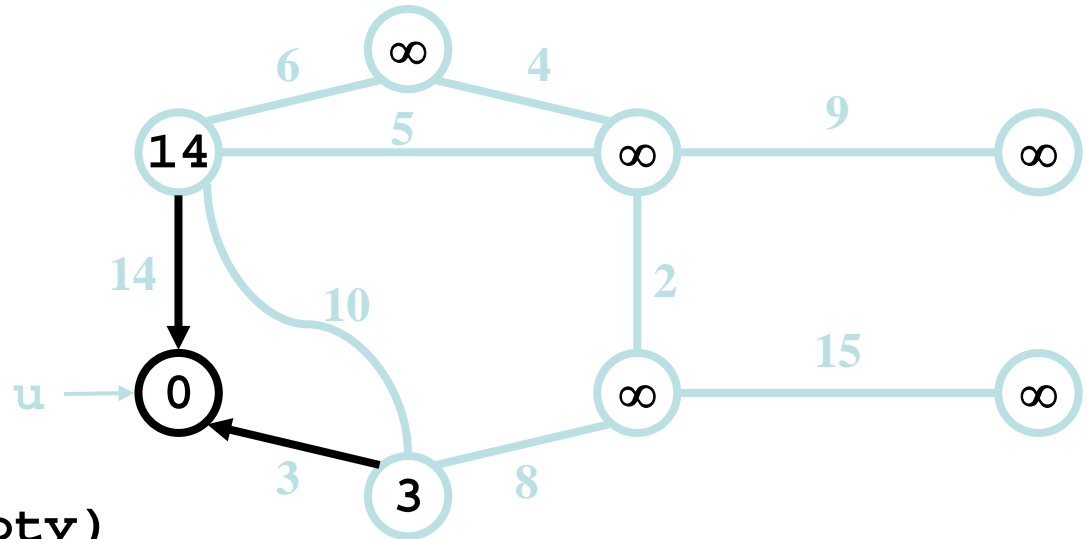
`$u = \text{ExtractMin}(Q);$`

`for each $v \in \text{Adj}[u]$`

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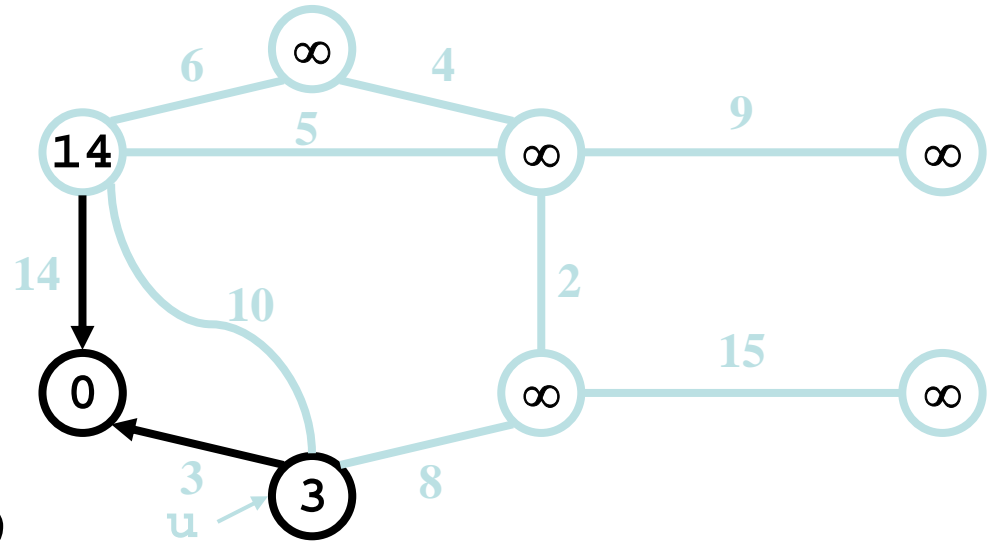
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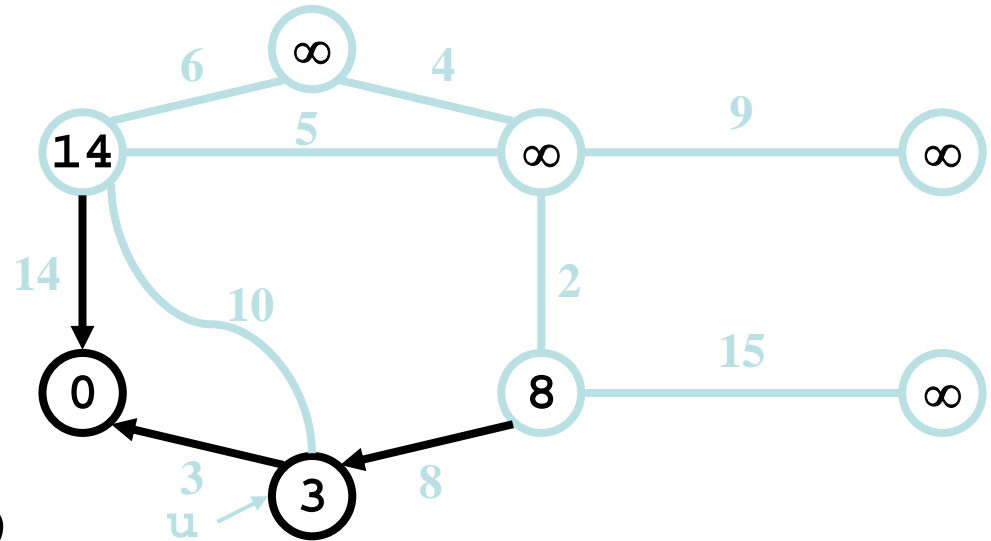
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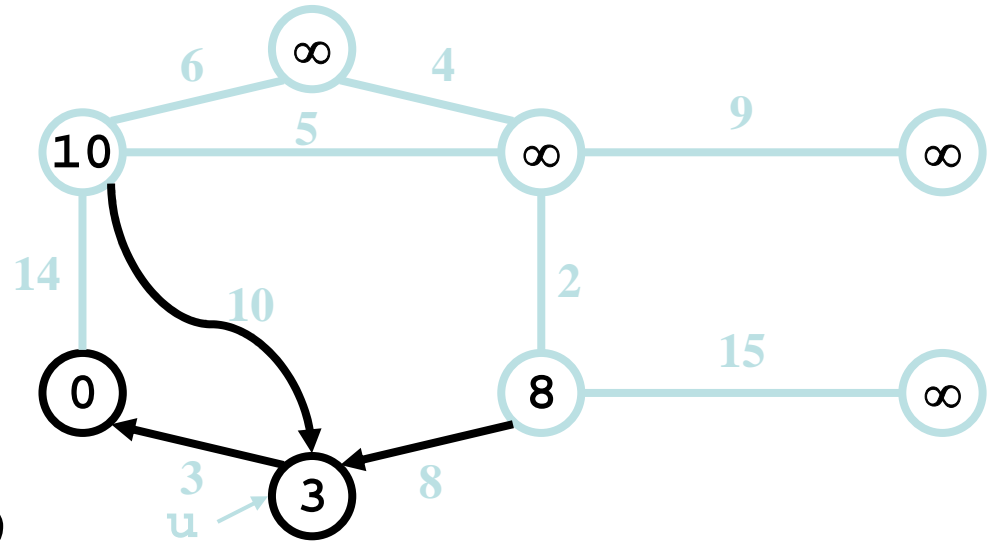
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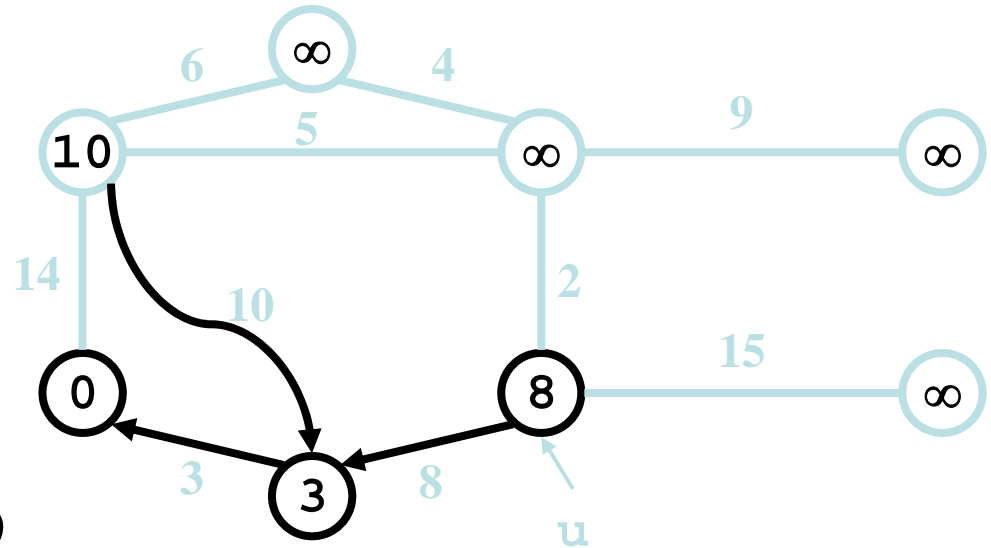
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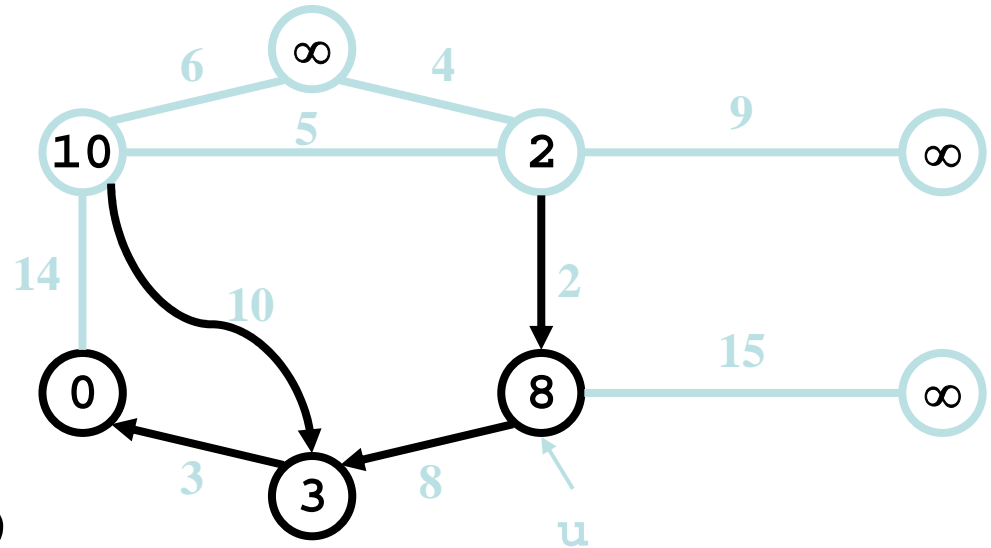
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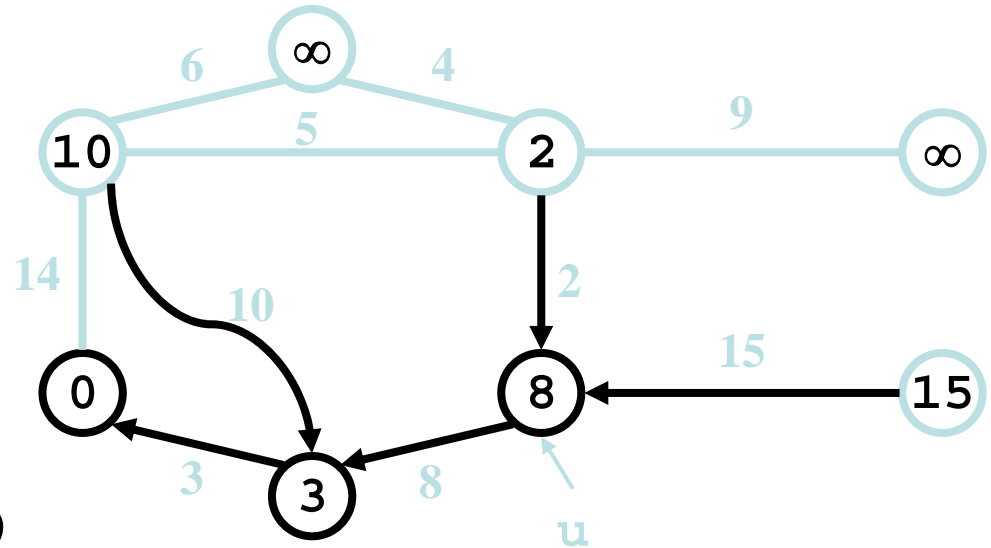
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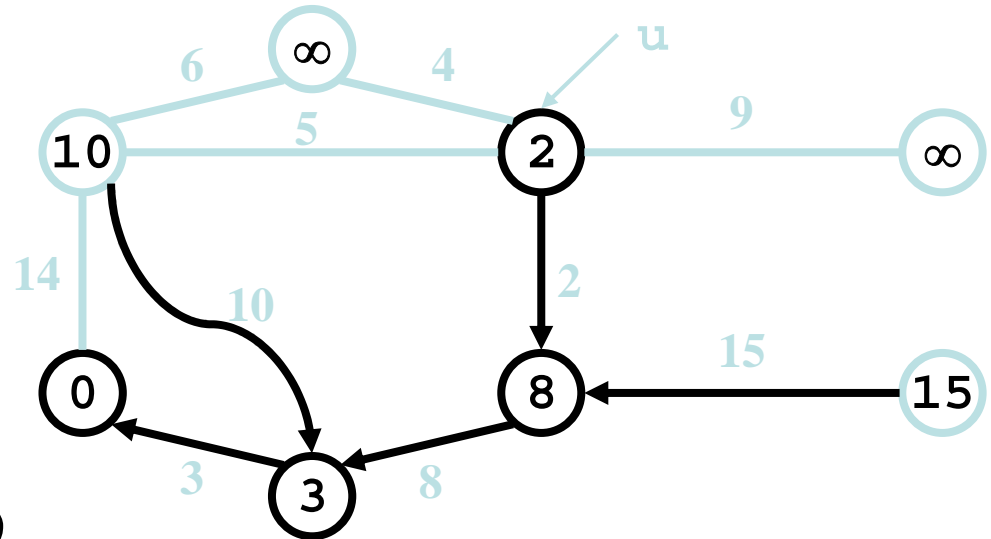
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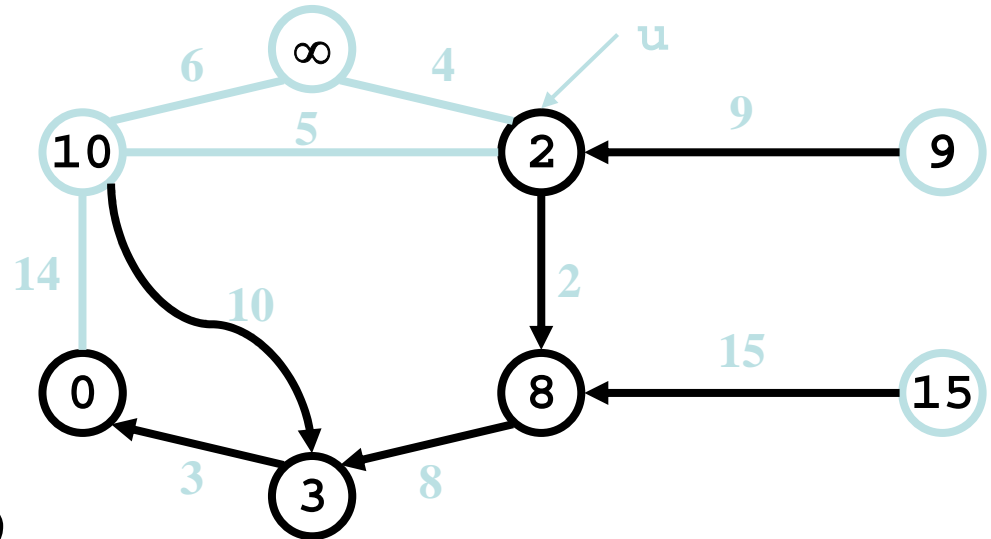
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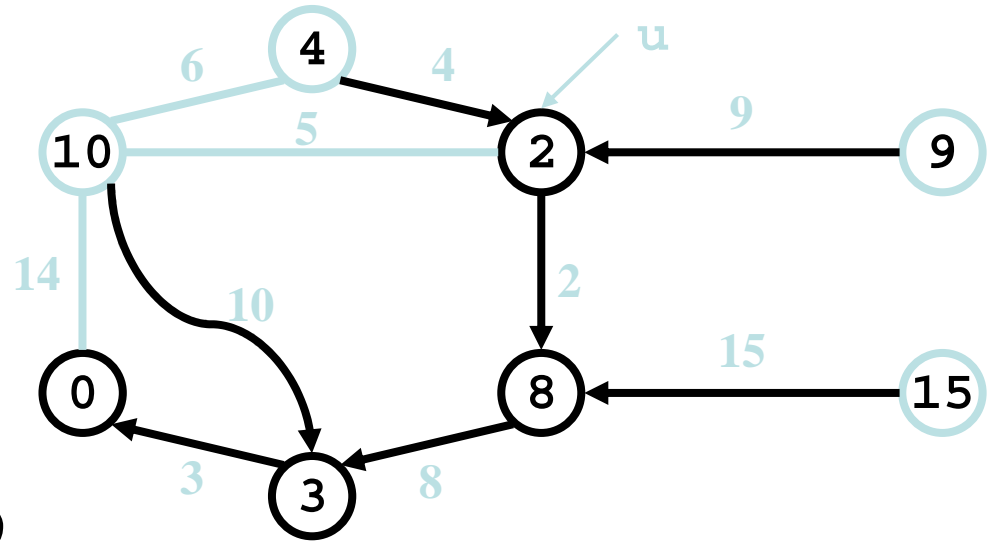
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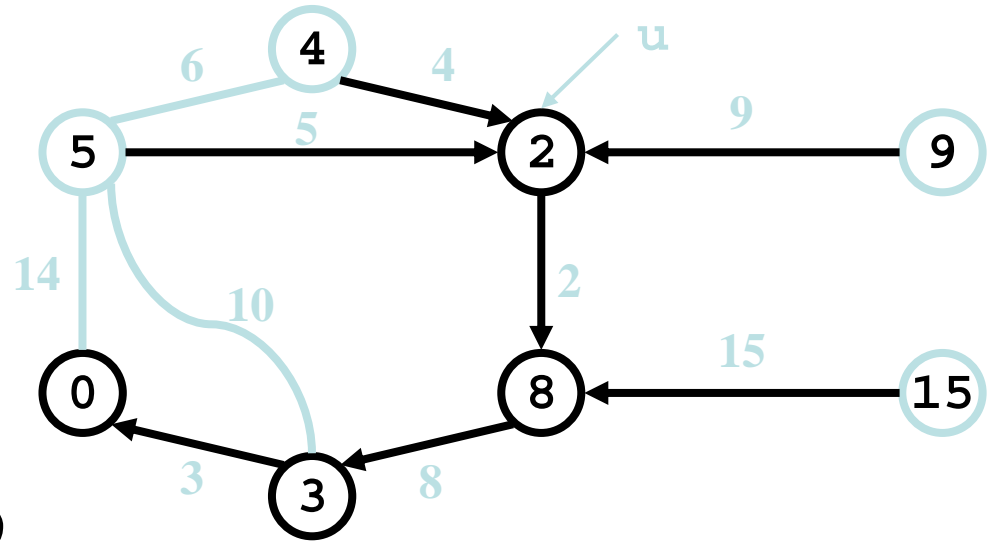
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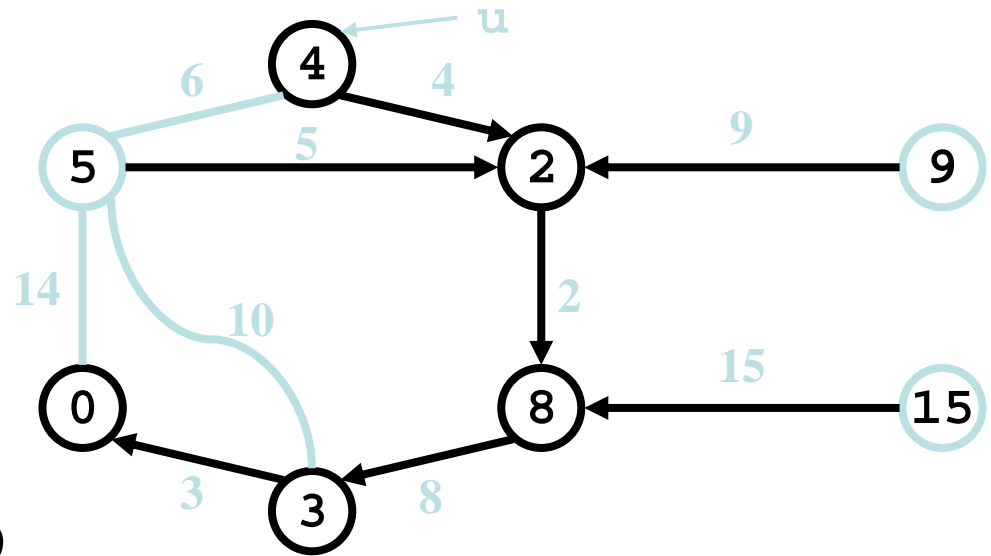
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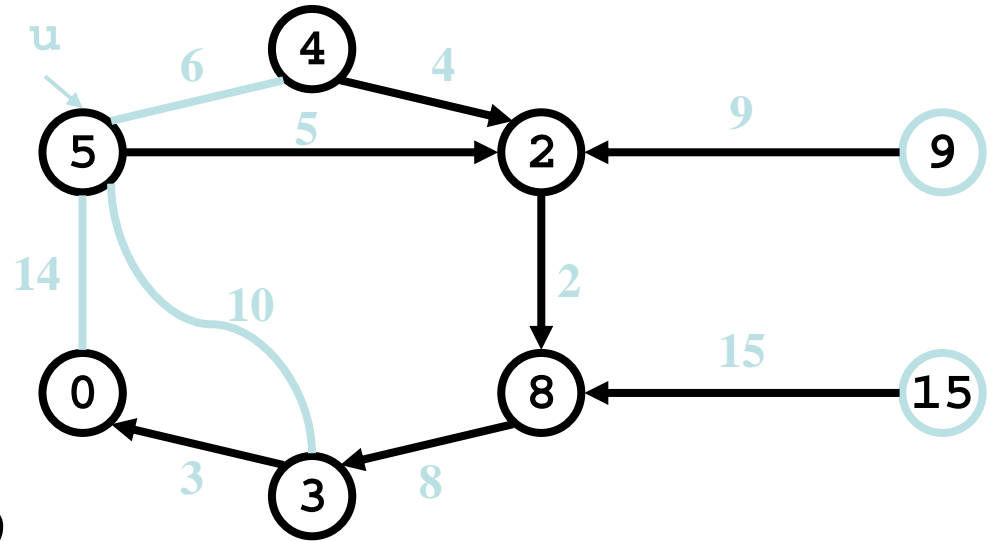
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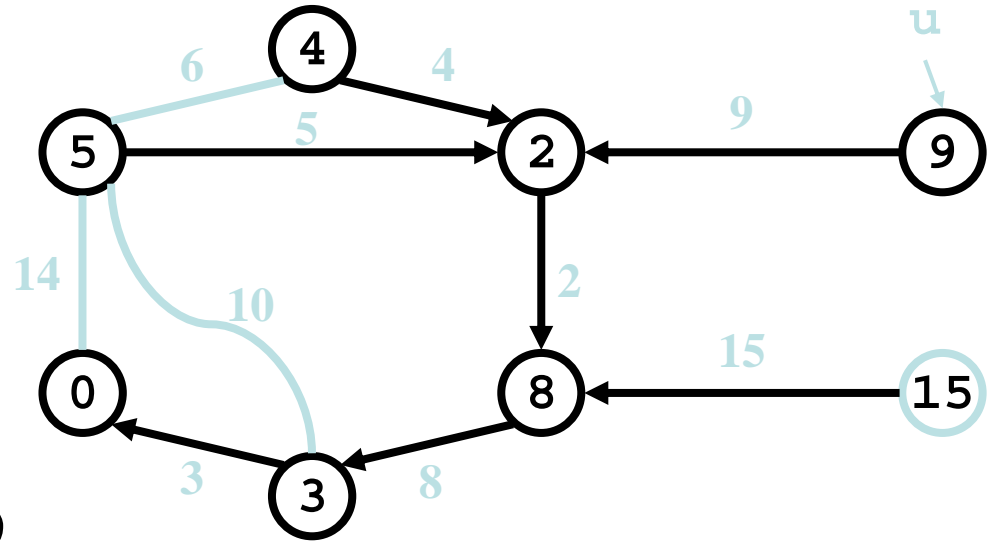
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