

$$\text{If } \theta \sim \text{Gamma}(\nu_0, \lambda_0)$$

$$E(\theta) = \frac{\nu_0}{\lambda_0}$$

$$V(\theta) = \frac{\nu_0}{\lambda_0^2}$$

How we could get $\nu_0 = 80$

$$\lambda_0 = 20 ?$$

Ask say 10 experts about $\theta = \frac{1}{2}$

$$\theta_1 \dots \theta_{10} \quad \text{Mean}(\theta_1 \dots \theta_{10})$$

$$V(\theta_1 \dots \theta_{10})$$

$$\text{match with } \frac{\nu_0}{\lambda_0} \quad \frac{\nu_0}{\lambda_0^2}$$

Predictive distribution

$$P(X_{\text{new}} > 4.8) = E \left[P(X_{\text{new}} > 4.8 \mid \theta) \right] \quad 1 - \text{pnorm}(4.8, 5, \frac{1}{\sqrt{\theta}})$$

$$\theta \sim \text{Gamma}(\nu_1, \lambda_1)$$

$$X_{\text{new}} \sim N(\mu=5, \sigma^2_{1/\theta})$$