Assignment 4 - Real Estate

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Data Cleansing

```
library(readx1)
REAL_ESTATE_SALES_DATA <- read_excel("REAL ESTATE SALES DATA.xlsx")
View(REAL_ESTATE_SALES_DATA)
real.estate<- as.data.frame(REAL_ESTATE_SALES_DATA)
str(real.estate)</pre>
```

```
## 'data.frame':
                 522 obs. of 13 variables:
         : num 1 2 3 4 5 6 7 8 9 10 ...
## $ Sales price: num 360000 340000 250000 205500 275500 ...
## $ Square feet: num 3032 2058 1780 1638 2196 ...
## $ Bedrooms : num 4 4 4 4 4 4 3 2 3 3 ...
## $ Bathrooms : num 4 2 3 2 3 3 2 1 2 3 ...
## $ AC
         : num 111111110 ...
## $ Garage : num 2 2 2 2 2 5 2 1 2 1 ...
## $ Pool
             : num 0000010000...
## $ Year
              : num 1972 1976 1980 1963 1968 ...
## $ Quality : num 2 2 2 2 2 2 2 3 3 ...
## $ Style
             : num 1111717111...
## $ lot size : num 22221 22912 21345 17342 21786 ...
## $ Highway : num 0000000000...
```

```
real.estate$Pool<- as.factor(real.estate$Pool)
real.estate$AC<- as.factor(real.estate$AC)
real.estate$Highway<- as.factor(real.estate$Highway)
real.estate$Quality<-as.factor(real.estate$Quality)
str(real.estate)</pre>
```

```
## 'data.frame':
                  522 obs. of 13 variables:
## $ Id
          : num 1 2 3 4 5 6 7 8 9 10 ...
## $ Sales price: num 360000 340000 250000 205500 275500 ...
## $ Square feet: num
                     3032 2058 1780 1638 2196 ...
## $ Bedrooms : num 4 4 4 4 4 4 3 2 3 3 ...
## $ Bathrooms : num 4 2 3 2 3 3 2 1 2 3 ...
## $ AC
             : Factor w/ 2 levels "0","1": 2 2 2 2 2 2 2 2 1 ...
## \$ Garage : num 2 2 2 2 2 5 2 1 2 1 ...
## $ Pool
              : Factor w/ 2 levels "0", "1": 1 1 1 1 1 2 1 1 1 1 ...
## $ Year
               : num 1972 1976 1980 1963 1968 ...
## $ Quality : Factor w/ 3 levels "1","2","3": 2 2 2 2 2 2 2 2 3 3 ...
              : num 1111717111...
## $ Style
## $ lot size : num 22221 22912 21345 17342 21786 ...
## $ Highway : Factor w/ 2 levels "0","1": 1 1 1 1 1 1 1 1 1 1 ...
```

```
View(real.estate)
```

Cumulative Logit model

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
summary(model.fit1)
```

```
## formula:
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC + Garage +
Pool + Year + `lot size` + Highway
##
## link threshold nobs logLik AIC
                                     niter max.grad cond.H
## logit flexible 522 -189.55 403.09 9(0) 5.29e-08 2.8e+15
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## `Sales price` -1.966e-05 3.040e-06 -6.467 1.00e-10 ***
## Bedrooms 5.250e-01 1.672e-01 3.140 0.00169 **
## Bathrooms
                -9.014e-01 2.217e-01 -4.066 4.78e-05 ***
## AC1
              -1.179e+00 4.129e-01 -2.855 0.00431 **
## Garage
               -5.412e-01 3.114e-01 -1.738 0.08226 .
## Pool1
               3.977e-01 5.303e-01 0.750 0.45331
               -5.854e-02 1.162e-02 -5.038 4.70e-07 ***
## Year
## `lot size` -6.260e-07 1.267e-05 -0.049 0.96058
## Highway1 -4.336e-01 7.607e-01 -0.570 0.56866
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Threshold coefficients:
   Estimate Std. Error z value
## 1 2 -133.04
                   23.15 -5.747
## 2|3 -123.44
                   22.81 -5.411
```

Important Predictors:

- 1.Sales price
- 2. Square feet
- 3.Bedrooms
- 4.Bathrooms
- 5.AC
- 6.Year

Interpretation of Coefficients:

- 1. For every unit increase in Sales price the odds of quality of construction being on higher quality changes multiplicatively by a factor of 0.999980340193257 controlling for other variables.
- 2. For every unit increase in square feet the odds of quality of construction being on higher quality changes multiplicatively by a factor of 0.998570023392284 controlling for other variables.
- 3. For every unit increase in number of Bedrooms the odds of quality of construction being on higher quality changes multiplicatively by a factor of 1.69045884837909 controlling for other variables.
- 4. For every unit increase in number of Bathrooms the odds of quality of construction being on higher quality changes multiplicatively by a factor of 0.406000860469356 controlling for other variables.
- 5. For every availability of AC, the odds of quality of construction being on higher quality changes multiplicatively by a factor of 0.307586171030328 controlling for other variables.
- 6. For every unit increase in the no of cars in Garage the odds of quality of construction being on higher quality changes multiplicatively by a factor of 0.582049373882101 controlling for other variables.
- 7. For every availability of Pool, the odds of quality of construction being on higher quality changes multiplicatively by a factor of 1.48839744368959 controlling for other variables.
- 8. For every increase in Year the odds of quality of construction being on higher quality changes multiplicatively by a factor of 0.943140514024583 controlling for other variables.

```
ctable <- coef(summary(model.fit1))
p <- round(pnorm(abs(ctable[, "z value"]), lower.tail = FALSE) * 2, digits = 3)
ctable <- cbind(ctable, "p-value" = p)
ci <- confint.default(model.fit1)
ctable <- cbind(ctable, round(exp(cbind(OR = coef(model.fit1), ci)), digits = 3))
ctable</pre>
```

```
##
                                                          Pr(>|z|) p-value
                     Estimate
                                Std. Error
                                               z value
                                                                              OR
## 1 2
                -1.330367e+02 2.314907e+01 -5.74695608 9.086432e-09
                                                                     0.000 0.000
                -1.234352e+02 2.281373e+01 -5.41056594 6.282588e-08
## 2 3
                                                                     0.000 0.000
## `Sales price` -1.966124e-05 3.040232e-06 -6.46701773 9.995593e-11
                                                                     0.000 1.000
## `Square feet` -1.431018e-03 4.477076e-04 -3.19632152 1.391919e-03
                                                                     0.001 0.999
## Bedrooms
               5.249620e-01 1.671771e-01 3.14015544 1.688582e-03
                                                                     0.002 1.690
## Bathrooms
                -9.014348e-01 2.216941e-01 -4.06612062 4.780220e-05
                                                                     0.000 0.406
## AC1
               -1.178663e+00 4.128826e-01 -2.85471595 4.307534e-03
                                                                     0.004 0.308
                -5.411935e-01 3.114352e-01 -1.73774022 8.225660e-02
## Garage
                                                                     0.082 0.582
## Pool1
                3.976836e-01 5.303143e-01 0.74990169 4.533139e-01
                                                                     0.453 1.488
## Year
                -5.853971e-02 1.161903e-02 -5.03826306 4.697755e-07
                                                                     0.000 0.943
## `lot size`
                -6.260411e-07 1.266525e-05 -0.04942983 9.605768e-01
                                                                     0.961 1.000
## Highway1
                -4.336341e-01 7.607233e-01 -0.57002869 5.686582e-01
                                                                     0.569 0.648
##
                2.5 % 97.5 %
## 1 2
                0.000 0.000
## 2 3
                0.000 0.000
## `Sales price` 1.000 1.000
## `Square feet` 0.998 0.999
## Bedrooms
                1.218 2.346
## Bathrooms
                0.263 0.627
                0.137 0.691
## AC1
## Garage
                0.316 1.072
## Pool1
                0.526 4.208
## Year
                0.922 0.965
## `lot size`
                1.000 1.000
## Highway1
                0.146 2.879
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit2)
```

```
## Likelihood ratio tests of cumulative link models:
##
           formula:
## model.fit2 as.factor(Quality) ~ `Square feet` + Bedrooms + Bathrooms + AC + Garage + Pool
+ Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
           link: threshold:
## model.fit2 logit flexible
## model.fit1 logit flexible
##
##
                   AIC logLik LR.stat df Pr(>Chisq)
          no.par
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Ho: Sales Price is not a significant variable Ha: Sales Price is a significant variable

Since p-value is less than α = 0.01, we reject Ho. Therefore, Sales Price is a significant variable.

2.Square feet

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit3)
```

```
## Likelihood ratio tests of cumulative link models:
##
             formula:
##
## model.fit3 as.factor(Quality) ~ `Sales price` + Bedrooms + Bathrooms + AC + Garage + Pool
+ Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit3 logit flexible
## model.fit1 logit flexible
##
##
                      AIC logLik LR.stat df Pr(>Chisq)
             no.par
## model.fit1
                12 403.09 -189.55 11.327 1
                                              0.000764 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Ho: Square feet is not a significant variable

Ha: Square feet is a significant variable

Since p-value is less than $\alpha = 0.01$, we reject Ho.

Therefore, Square feet is a significant variable.

3.Bedrooms

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit4)
```

```
## Likelihood ratio tests of cumulative link models:
##
             formula:
##
## model.fit4 as.factor(Quality) ~ `Sales price` + `Square feet` + Bathrooms + AC + Garage +
Pool + Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit4 logit flexible
## model.fit1 logit flexible
##
##
                      AIC logLik LR.stat df Pr(>Chisq)
             no.par
## model.fit1
                12 403.09 -189.55 10.135 1
                                              0.001455 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Ho: Bedrooms is not a significant variable

Ha: Bedrooms is a significant variable

Since p-value is less than $\alpha = 0.01$, we reject Ho.

Therefore, Bedrooms is a significant variable.

4.Bathrooms

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit5)
```

```
## Likelihood ratio tests of cumulative link models:
##
             formula:
##
## model.fit5 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + AC + Garage + P
ool + Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit5 logit flexible
## model.fit1 logit flexible
##
##
                      AIC logLik LR.stat df Pr(>Chisq)
             no.par
## model.fit1
                12 403.09 -189.55 18.038 1 2.165e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Ho: Bathrooms is not a significant variable

Ha: Bathrooms is a significant variable

Since p-value is less than $\alpha = 0.01$, we reject Ho.

Therefore, Bathrooms is a significant variable.

5.AC

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit6)
```

```
## Likelihood ratio tests of cumulative link models:
##
             formula:
##
## model.fit6 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + Gar
age + Pool + Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit6 logit flexible
## model.fit1 logit flexible
##
##
                      AIC logLik LR.stat df Pr(>Chisq)
             no.par
## model.fit1
                12 403.09 -189.55
                                   8.928 1
                                              0.002808 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Ho: AC is not a significant variable Ha: AC is a significant variable

Since p-value is less than α = 0.01, we reject Ho. Therefore, Bathrooms is a significant variable.

6.Garage

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit7)
```

```
## Likelihood ratio tests of cumulative link models:
##
##
             formula:
## model.fit7 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Pool + Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit7 logit flexible
## model.fit1 logit flexible
##
##
                      AIC logLik LR.stat df Pr(>Chisq)
             no.par
## model.fit1
                12 403.09 -189.55 3.2482 1
                                                0.0715 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Ho: Garage is not a significant variable

Ha: Garage is a significant variable

Since p-value is greater than $\alpha = 0.01$, we fail to reject Ho.

Therefore, Garage is a not significant variable.

7.Pool

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit8)
```

```
## Likelihood ratio tests of cumulative link models:
##
## model.fit8 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Year + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
              link: threshold:
## model.fit8 logit flexible
## model.fit1 logit flexible
##
##
                        AIC logLik LR.stat df Pr(>Chisq)
              no.par
## model.fit8
                11 401.65 -189.82
## model.fit1
                  12 403.09 -189.55 0.5584 1
                                                   0.4549
```

Ho: Pool is not a significant variable

Ha: Pool is a significant variable

Since p-value is greater than $\alpha = 0.01$, we fail to reject Ho.

Therefore, Pool is a not significant variable.

8.Year

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit9)
```

```
## Likelihood ratio tests of cumulative link models:
##
##
             formula:
## model.fit9 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + `lot size` + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit9 logit flexible
## model.fit1 logit flexible
##
##
                       AIC logLik LR.stat df Pr(>Chisq)
             no.par
                11 429.59 -203.80
## model.fit9
## model.fit1
                 12 403.09 -189.55 28.499 1 9.373e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Ho: Year is not a significant variable

Ha: Year is a significant variable

Since p-value is less than α = 0.01, we reject Ho.

Therefore, Year is a significant variable.

9.lot size

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1,model.fit10)
```

```
## Likelihood ratio tests of cumulative link models:
##
               formula:
##
## model.fit10 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + Highway
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
              link: threshold:
## model.fit10 logit flexible
## model.fit1 logit flexible
##
##
              no.par
                         AIC logLik LR.stat df Pr(>Chisq)
## model.fit10
                  11 401.09 -189.55
## model.fit1
                   12 403.09 -189.55 0.0024 1
                                                    0.9606
```

Ho: lot size is not a significant variable Ha: lot size is a significant variable

Since p-value is greater than $\alpha = 0.01$, we fail to reject Ho.

Therefore, lot size is a not significant variable.

10.Highway

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
anova(model.fit1, model.fit11)
```

```
## Likelihood ratio tests of cumulative link models:
##
              formula:
##
## model.fit11 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size`
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
##
             link: threshold:
## model.fit11 logit flexible
## model.fit1 logit flexible
##
##
             no.par
                       AIC logLik LR.stat df Pr(>Chisq)
## model.fit1
                 12 403.09 -189.55 0.3274 1
                                                0.5672
```

Ho: Highway is not a significant variable Ha: Highway is a significant variable

Since p-value is greater than α = 0.01, we fail to reject Ho.

Therefore, Highway is a not significant variable.

Predictors to be retained are:

Important Predictors:

- 1.Sales price
- 2.Square feet
- 3.Bedrooms
- 4.Bathrooms
- 5.AC
- 6.Year

Backward elimination method:

```
library(bootStepAIC)
```

```
## Loading required package: MASS
```

```
stepAIC(model.fit1,direction = "backward")
```

```
## Start: AIC=403.09
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms +
## Bathrooms + AC + Garage + Pool + Year + `lot size` + Highway
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
                  Df
##
                        ATC
                 1 401.09
## - `lot size`
## - Highway
                  1 401.42
                  1 401.65
## - Pool
## <none>
                   403.09
                 1 404.34
1 410.02
## - Garage
## - AC
## - Bedrooms 1 411.23
## - `Square feet` 1 412.42
## - Bathrooms 1 419.13
## - Year
                   1 429.59
## - `Sales price` 1 464.59
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
##
## Step: AIC=401.09
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms +
       Bathrooms + AC + Garage + Pool + Year + Highway
##
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
##
                  Df
                        AIC
## - Highway
                  1 399.43
## - Pool
                  1 399.66
## <none>
                     401.09
                 1 402.34
## - Garage
## - AC
                  1 408.19
                 1 409.23
## - Bedrooms
## - `Square feet` 1 410.56
## - Bathrooms
                 1 417.14
## - Year
                   1 429.15
## - `Sales price` 1 466.77
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
##
## Step: AIC=399.43
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms +
##
       Bathrooms + AC + Garage + Pool + Year
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
##
                  Df
                        AIC
## - Pool
                  1 398.03
## <none>
                    399.43
                1 400.78
## - Garage
## - AC
                  1 406.29
## - Bedrooms
                  1 407.53
## - `Square feet` 1 408.78
## - Bathrooms
                 1 415.42
## - Year
                   1 428.09
## - `Sales price` 1 464.91
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
##
## Step: AIC=398.03
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms +
       Bathrooms + AC + Garage + Year
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
  Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
    Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
   Consider formula(paste(x, collapse = " ")) instead.
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
##
                 Df
                        AIC
## <none>
                     398.03
                 1 399.28
## - Garage
                  1 404.62
## - AC
## - Bedrooms
                1 406.08
## - `Square feet` 1 407.22
                 1 413.67
## - Bathrooms
## - Year
                   1 427.37
## - `Sales price` 1 462.98
## formula:
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC + Garage +
Year
##
## link threshold nobs logLik AIC niter max.grad cond.H
  logit flexible 522 -190.01 398.03 9(0) 5.76e-08 4.1e+15
##
##
## Coefficients:
## `Sales price` `Square feet`
                                   Bedrooms
                                                Bathrooms
                                                                    AC1
     -1.957e-05 -1.409e-03
                                  5.222e-01 -8.872e-01 -1.135e+00
##
##
         Garage
                         Year
##
     -5.429e-01
                   -5.934e-02
##
## Threshold coefficients:
## 1 2
            2 | 3
## -134.5 -124.9
mod.reduced<-clm(as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms +</pre>
AC + Garage + Year, data=real.estate)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
summary(mod.reduced)
```

```
## formula:
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC + Garage +
Year
## data:
           real.estate
##
## link threshold nobs logLik AIC niter max.grad cond.H
## logit flexible 522 -190.01 398.03 9(0) 5.76e-08 4.1e+15
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## `Sales price` -1.957e-05 2.951e-06 -6.632 3.32e-11 ***
## `Square feet` -1.409e-03 4.453e-04 -3.163 0.00156 **
## Bedrooms
               5.222e-01 1.670e-01 3.127 0.00176 **
## Bathrooms
               -8.872e-01 2.201e-01 -4.031 5.56e-05 ***
               -1.135e+00 4.037e-01 -2.811 0.00493 **
## AC1
              -5.429e-01 3.117e-01 -1.741 0.08161 .
## Garage
## Year
               -5.934e-02 1.147e-02 -5.174 2.29e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Threshold coefficients:
      Estimate Std. Error z value
## 1 2 -134.46 22.84 -5.886
## 2 3 -124.88
                   22.49 -5.552
```

```
anova(model.fit1 , mod.reduced , type = 1)
```

```
## Likelihood ratio tests of cumulative link models:
##
               formula:
##
## mod.reduced as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Year
## model.fit1 as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC
+ Garage + Pool + Year + `lot size` + Highway
              link: threshold:
##
## mod.reduced logit flexible
## model.fit1 logit flexible
##
##
              no.par
                        AIC logLik LR.stat df Pr(>Chisq)
## mod.reduced 9 398.03 -190.01
## model.fit1
                  12 403.09 -189.55 0.9376 3
                                                   0.8164
```

Variables to be retained: Sales price Square feet Bedrooms Bathrooms AC

Year

Binary Logistic Regression Model

Loading required package: carData

```
estate.data<- as.data.frame(REAL_ESTATE_SALES_DATA)
estate.data$Pool<- as.factor(estate.data$Pool)
estate.data$AC<- as.factor(estate.data$AC)
estate.data$Highway<- as.factor(estate.data$Highway)
library(car)</pre>
```

```
estate.data$Quality_High <- recode(estate.data$Quality,"1=1;c(2,3)=0")
estate.data$Quality_Medium <- recode(estate.data$Quality,"2=1;c(1,3)=0")
estate.data$Quality_Low <- recode(estate.data$Quality,"3=1;c(1,2)=0")
str(estate.data)</pre>
```

```
## 'data.frame': 522 obs. of 16 variables:
## $ Id
                 : num 1 2 3 4 5 6 7 8 9 10 ...
## $ Sales price : num 360000 340000 250000 205500 275500 ...
## $ Square feet : num 3032 2058 1780 1638 2196 ...
## $ Bedrooms
                 : num 4444443233...
## $ Bathrooms
                : num 4 2 3 2 3 3 2 1 2 3 ...
## $ AC
                : Factor w/ 2 levels "0", "1": 2 2 2 2 2 2 2 2 1 ...
## $ Garage
                : num 2 2 2 2 2 5 2 1 2 1 ...
## $ Pool
                : Factor w/ 2 levels "0", "1": 1 1 1 1 1 2 1 1 1 1 ...
## $ Year
                : num 1972 1976 1980 1963 1968 ...
## $ Quality
                : num 2 2 2 2 2 2 2 3 3 ...
## $ Style
                 : num 1111717111...
## $ lot size
                : num 22221 22912 21345 17342 21786 ...
                 : Factor w/ 2 levels "0", "1": 1 1 1 1 1 1 1 1 1 1 ...
## $ Highway
## $ Quality_High : num 0000000000...
## $ Quality_Medium: num 1 1 1 1 1 1 1 1 0 0 ...
## $ Quality_Low
                 : num 000000011...
```

```
View(estate.data)
```

```
attach(estate.data)
```

```
## The following objects are masked from real.estate:
##
## AC, Bathrooms, Bedrooms, Garage, Highway, Id, lot size, Pool,
## Quality, Sales price, Square feet, Style, Year
```

```
##
## Call:
## glm(formula = Quality_High ~ `Sales price` + `Square feet` +
       Bedrooms + Bathrooms + AC + Garage + Pool + Year + `lot size` +
       Highway, family = binomial(link = "logit"))
##
##
## Deviance Residuals:
      Min
           1Q Median
                               30
                                          Max
## -3.3751 -0.1051 -0.0403 0.0000
                                        2.6958
##
## Coefficients:
##
          Estimate Std. Error z value Pr(>|z|)
## (Intercept) -4.519e+01 1.439e+03 -0.031 0.9750
## `Sales price` 2.034e-05 3.516e-06 5.787 7.18e-09 ***
## `Square feet` 9.282e-04 6.107e-04 1.520 0.1285
## Bedrooms -5.666e-01 2.934e-01 -1.931 0.0535 .
## Bathrooms
## AC1
                4.025e-01 3.330e-01 1.209 0.2267
                1.674e+01 1.439e+03 0.012 0.9907
## Garage 8.570e-01 4.970e-01 1.725 0.0846 .
## Pool1 -3.868e-01 7.882e-01 -0.491 0.6236
## Pool1
## Year
                7.897e-03 2.213e-02 0.357 0.7212
## `lot size` -2.354e-05 2.265e-05 -1.039 0.2986
## Highway1 1.454e+00 1.705e+00 0.853 0.3939
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 403.92 on 521 degrees of freedom
## Residual deviance: 110.24 on 511 degrees of freedom
## AIC: 132.24
##
## Number of Fisher Scoring iterations: 19
```

```
##
## Call:
## glm(formula = Quality_Medium ~ `Sales price` + `Square feet` +
      Bedrooms + Bathrooms + AC + Garage + Pool + Year + `lot size` +
##
      Highway, family = binomial(link = "logit"))
##
## Deviance Residuals:
      Min 1Q Median 3Q
##
                                        Max
## -3.2048 -0.8443 0.4748 0.8148
                                     2.3498
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -7.616e+01 1.691e+01 -4.504 6.68e-06 ***
## `Sales price` -1.356e-05 1.917e-06 -7.074 1.50e-12 ***
## `Square feet` 5.231e-04 3.251e-04 1.609 0.107601
               8.308e-02 1.345e-01 0.618 0.536746
## Bedrooms
## Bathrooms
               1.082e+00 1.909e-01 5.669 1.43e-08 ***
## AC1
               1.551e+00 3.327e-01 4.662 3.13e-06 ***
             -7.346e-02 2.044e-01 -0.359 0.719253
## Garage
## Pool1
               6.034e-02 4.125e-01 0.146 0.883718
               3.748e-02 8.680e-03 4.318 1.57e-05 ***
## Year
## `lot size`
              4.095e-05 1.079e-05 3.794 0.000148 ***
## Highway1 -3.463e-01 6.844e-01 -0.506 0.612876
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 717.19 on 521 degrees of freedom
##
## Residual deviance: 549.18 on 511 degrees of freedom
## AIC: 571.18
##
## Number of Fisher Scoring iterations: 4
```

```
##
## Call:
## glm(formula = Quality_Low ~ `Sales price` + `Square feet` + Bedrooms +
      Bathrooms + AC + Garage + Pool + Year + `lot size` + Highway,
##
      family = binomial(link = "logit"))
##
## Deviance Residuals:
##
      Min 1Q Median
                                 3Q
                                         Max
## -2.9434 -0.2669 -0.0159 0.1997
                                      3.5518
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 1.701e+02 3.034e+01 5.606 2.07e-08 ***
## `Sales price` -1.318e-05 5.882e-06 -2.240 0.025110 *
## `Square feet` -2.710e-03 7.777e-04 -3.485 0.000493 ***
                5.834e-01 2.298e-01 2.539 0.011115 *
## Bedrooms
              -1.423e+00 3.297e-01 -4.316 1.59e-05 ***
## Bathrooms
               -1.013e+00 4.649e-01 -2.179 0.029368 *
## AC1
              -4.229e-01 4.468e-01 -0.946 0.343926
## Garage
## Pool1
               9.414e-01 7.739e-01 1.216 0.223829
               -8.150e-02 1.533e-02 -5.315 1.07e-07 ***
## Year
## `lot size`
              -2.802e-06 1.636e-05 -0.171 0.864028
              1.133e-01 9.014e-01 0.126 0.899990
## Highway1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 649.79 on 521 degrees of freedom
## Residual deviance: 246.09 on 511 degrees of freedom
## AIC: 268.09
##
## Number of Fisher Scoring iterations: 8
```

Comparison of slope

Variable Cumulative Binary: High Quality Binary: Medium Quality Binary: Low Quality

Sales price -0.000020 0.00002 -0.00001 -0.000013

Square feet -0.001431 0.00093 0.00052 -0.002710

Bedrooms 0.525000 -0.56660 0.08308 0.583400

Bathrooms -0.901400 0.40250 1.08200 -1.423000

AC1 -1.179000 16.74000 1.55100 -1.013000

Garage -0.541200 0.85700 -0.07346 -0.422900

Pool1 0.397700 -0.38680 0.06034 0.941400

Year -0.058540 0.00790 0.03748 -0.081500

lot size -0.000001 -0.00002 0.00004 -0.000003

Highway1 -0.433600 1.45400 -0.34630 0.113300

Final Model

```
mod.final<-clm(as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC</pre>
+ Year + Year, data=real.estate)
```

Warning: Using formula(x) is deprecated when x is a character vector of length > 1.
Consider formula(paste(x, collapse = " ")) instead.

```
## Warning: (2) Model is nearly unidentifiable: very large eigenvalue
## - Rescale variables?
## In addition: Absolute and relative convergence criteria were met
```

```
summary(mod.final)
```

```
## formula:
## as.factor(Quality) ~ `Sales price` + `Square feet` + Bedrooms + Bathrooms + AC + Year + Ye
## data:
          real.estate
##
## link threshold nobs logLik AIC niter max.grad cond.H
## logit flexible 522 -191.64 399.28 9(0) 9.28e-08 1.6e+16
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## `Sales price` -2.036e-05 2.909e-06 -7.000 2.56e-12 ***
## Bedrooms 5.242e-01 1.671e-01 3.137 0.001707 **
## Bathrooms -8.833e-01 2.180e-01 -4.051 5.09e-05 ***
## AC1
             -1.220e+00 3.989e-01 -3.059 0.002219 **
## Year
          -6.309e-02 1.121e-02 -5.629 1.82e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Threshold coefficients:
##
     Estimate Std. Error z value
## 1 2 -141.19 22.42 -6.297
## 2 3 -131.54
                22.06 -5.964
```