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## EE1205

## EE22BTECH11014 - Barath Surya M

General form of GP

$$x(n) = x(0)r^n \quad n \ge 0 \tag{1}$$

Sum of first n terms of a geometric progression is defined as

$$y(n) = \sum_{k=0}^{n} x(k)$$
(2)

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) u(n-k)$$
(3)

$$y(n) = x(n) * u(n)$$
(4)

On Taking Z-Transform

$$Y(z) = X(z)U(z) \tag{5}$$

From Z-Transform of a term of GP

$$X(z) = \frac{x(0)}{1 - rz^{-1}} \quad |rz^{-1}| < 1 \tag{6}$$

and Z-Transform of unit step is

$$U(z) = \frac{1}{1 - z^{-1}} \quad |z^{-1}| < 1 \tag{7}$$

$$\implies Y(z) = \left(\frac{x(0)}{1 - rz^{-1}}\right) \left(\frac{1}{1 - z^{-1}}\right) \quad |rz^{-1}| < 1 \quad \text{and} \quad |z^{-1}| < 1$$
 (8)

By using Partial Fractions

$$Y(z) = x(0) \left( \frac{A}{1 - rz^{-1}} + \frac{B}{1 - z^{-1}} \right) \tag{9}$$

$$A = \frac{r}{r - 1} \tag{10}$$

$$B = \frac{-1}{r - 1} \tag{11}$$

Taking inverse Z-transform

$$y(n) = \frac{x(0)}{r-1} (r(r^n) - 1) u(n)$$
(12)

$$= x(0) \left( \frac{r^{n+1} - 1}{r - 1} \right) u(n) \tag{13}$$