

# Finance

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26/11/2021

## Stocks: Airlines:

Lufthansa (German); DLAKY

Southwest Airlines; LUV

Easy Jet (British); EZJ

RyanAir Holdings plc (British); RYAAY

United Airlines Holdings Inc (American); UAL

American Airlines Group Inc (American); AAL

Spirit Airlines Inc (American); SAVE

## Beer Industry:

Carlsberg (Danish); CABGY Heineken (Netherlands); HEINY

Anheuser-Busch InBev (Belgium); BUD

Harboe (Danish); CPH: HARB-B

Guinness from Diageo; DEO

Molson Coors Brewing; TAP Tsingtao Brewery Group; OTCMKTS: TSGTF Asahi Group Holding Ltd;  
OTCMKTS: ASBRF

```
returns <- tq_get(tickers, get="stock.prices") %>%
  group_by(symbol) %>%
  tq_transmute(select=adjusted,
               mutate_fun=periodReturn,
               period="monthly",
               col_rename = "monthly_return")

returns <- returns %>%
  pivot_wider(names_from = symbol, values_from = monthly_return)

#monthly returns
returns <- returns[1:131,]
```

**Part 1** 1. Table of mean, sd, skewness, kurtosis and beta.

```
returns <- as.data.frame(returns)
returnsNA <- as.data.frame(na.omit(returns))
returnsIVV <- returns[1:16]

# columns of table
Stocks <- stock_names[1:15]
Means <- rep(NA, 15)
Sd <- rep(NA, 15)
Skewness <- rep(NA, 15)
Kurtosis <- rep(NA, 15)
```

```

table <- data.frame(Stocks,Means,Sd,Skewness,Kurtosis)

# means
for(i in 1:15)
{
  table$Means[i] <- mean(returnsNA[,i+1])
}

# sd
for(i in 1:15)
{
  table$Sd[i] <- sd(returnsNA[,i+1])
}

# skewness should be around 0 to be normally distributed
for(i in 1:15)
{
  table$Skewness[i] <- Skew(returnsNA[,i+1])
}

# kurtosis should be around 3 to be normally distributed
for(i in 1:15)
{
  table$Kurtosis[i] <- Kurt(returnsNA[,i+1])
}

# betas
#CAPM model, risk free and market portfolio IVV
table

```

| ##    | Stocks    | Means         | Sd         | Skewness    | Kurtosis  |
|-------|-----------|---------------|------------|-------------|-----------|
| ## 1  | Lufthansa | -0.0005930083 | 0.11241027 | 0.08667032  | 0.1488168 |
| ## 2  | Southwest | 0.0171885468  | 0.09277315 | 0.21544579  | 0.5677506 |
| ## 3  | EasyJet   | 0.0079285412  | 0.07815002 | -0.05386680 | 0.3734066 |
| ## 4  | RyanAir   | 0.0134598915  | 0.08810162 | 0.03841435  | 0.7835927 |
| ## 5  | United    | 0.0117156991  | 0.11468114 | -0.40046581 | 2.6059592 |
| ## 6  | American  | 0.0128577554  | 0.14004608 | 0.92824441  | 3.3713287 |
| ## 7  | Spirit    | 0.0129167067  | 0.12816431 | -0.27125023 | 3.0894567 |
| ## 8  | Carlsberg | 0.0048833354  | 0.07151443 | -0.38252473 | 0.9578615 |
| ## 9  | Heineken  | 0.0068923311  | 0.06196124 | -0.11333085 | 0.3347802 |
| ## 10 | AB        | 0.0025169668  | 0.07827691 | -0.03417490 | 1.4085001 |
| ## 11 | Harboe    | -0.0004547538 | 0.06049694 | 0.65593756  | 0.6983457 |
| ## 12 | Guinness  | 0.0101843141  | 0.04608098 | 0.24639304  | 1.2094121 |
| ## 13 | Molson    | 0.0015157556  | 0.07310860 | 0.77435046  | 2.3018081 |
| ## 14 | Tsingtao  | 0.0073310755  | 0.09659968 | 0.29240859  | 1.0474625 |
| ## 15 | Asahi     | 0.0083592940  | 0.07193289 | -0.41777156 | 4.1653067 |

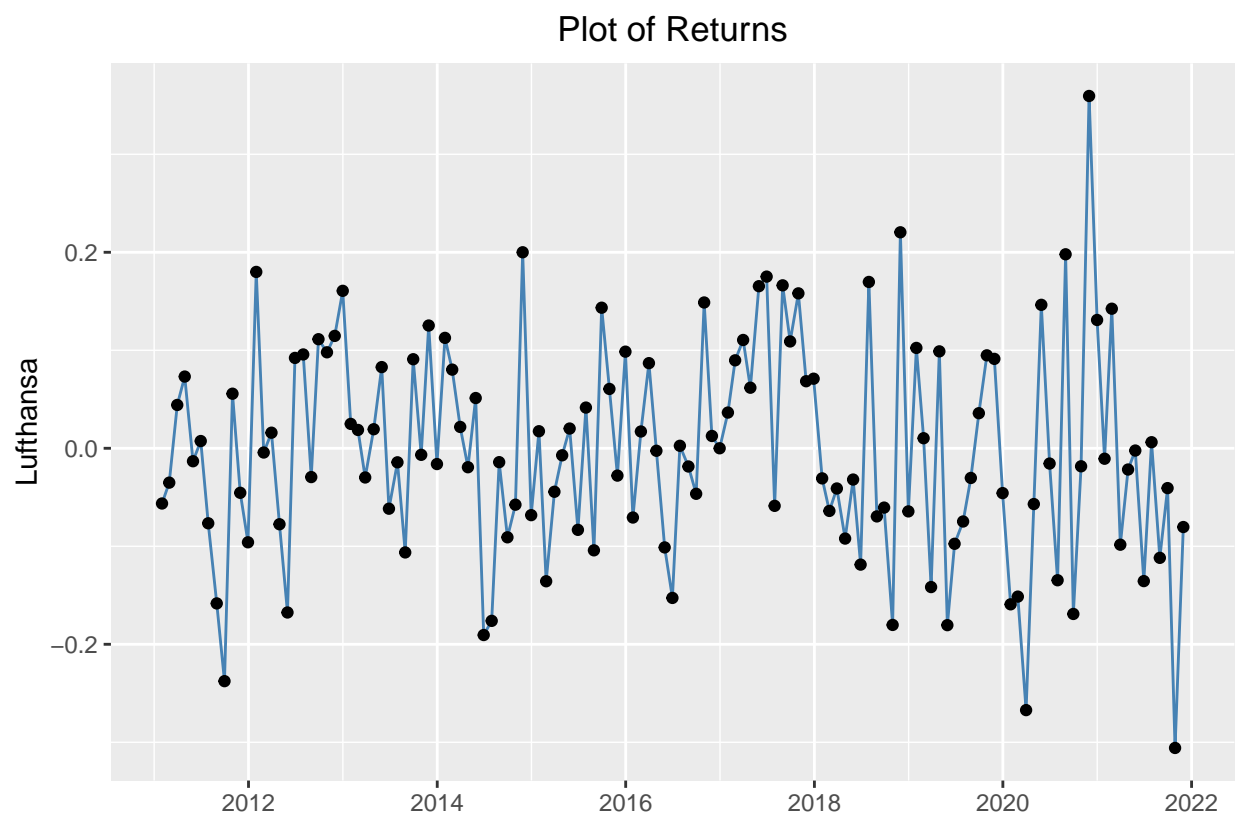
2. Plot each set of returns

```

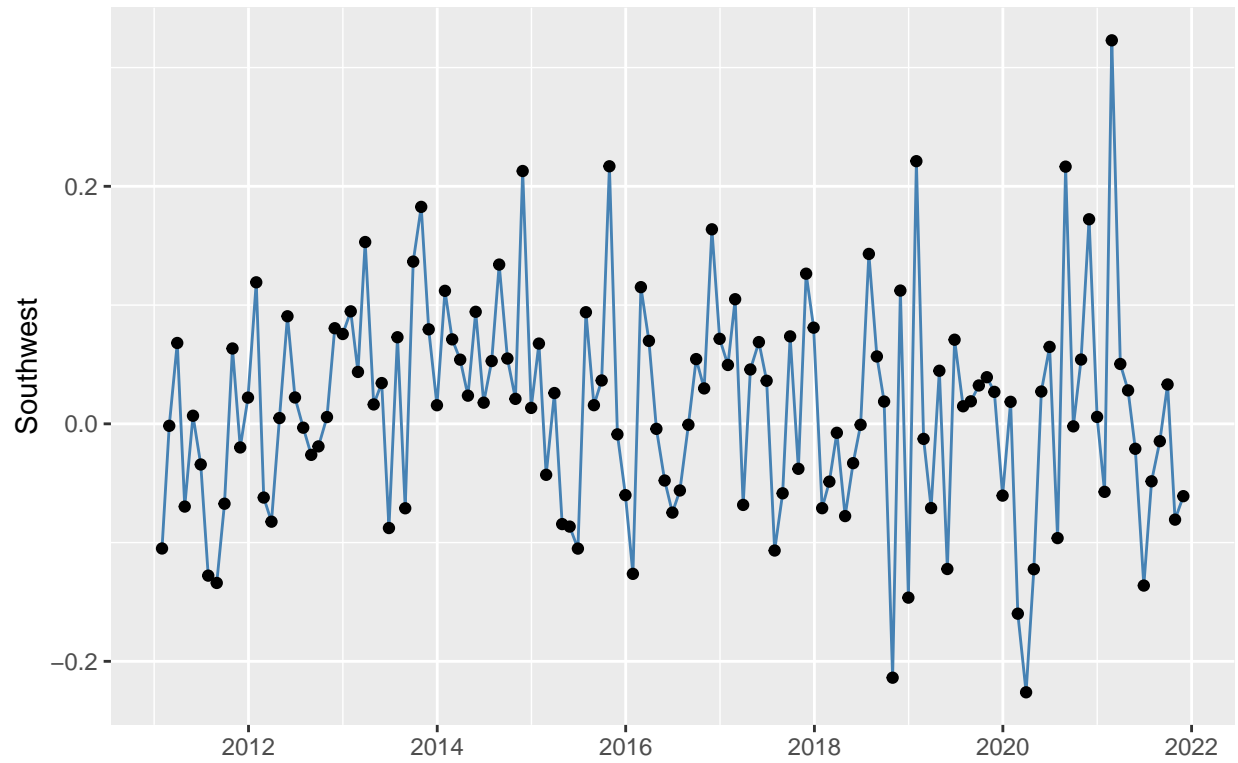
returns <- as.data.frame(returns)

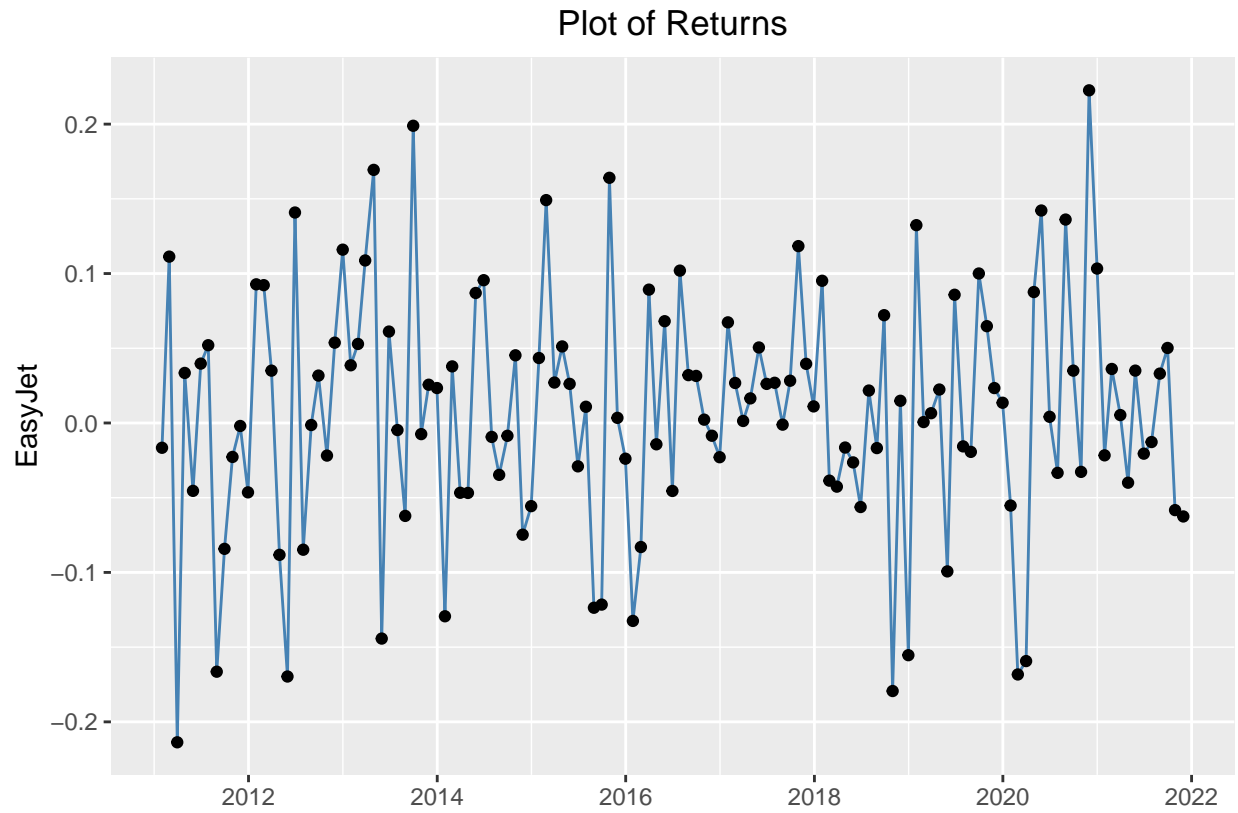
for (i in 1:15)
{
  names <- list(stock_names)
  print(ggplot(returns, aes(x=date, y=returns[,i+1])) +
    geom_line(color="steelblue") +
    geom_point() +
    xlab("") +
    ylab(names[[1]][i])+
    ggtitle("Plot of Returns") +
    theme(plot.title = element_text(hjust = 0.5)))
}

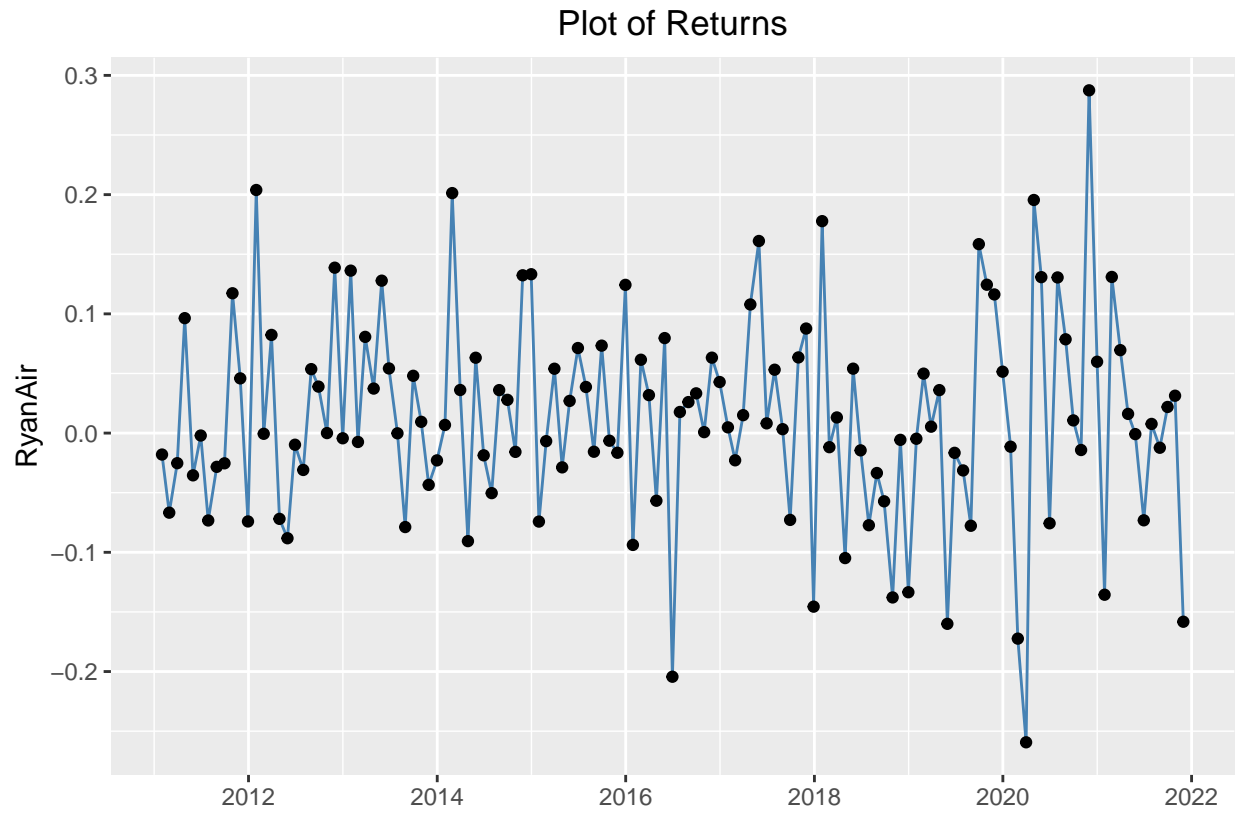
```

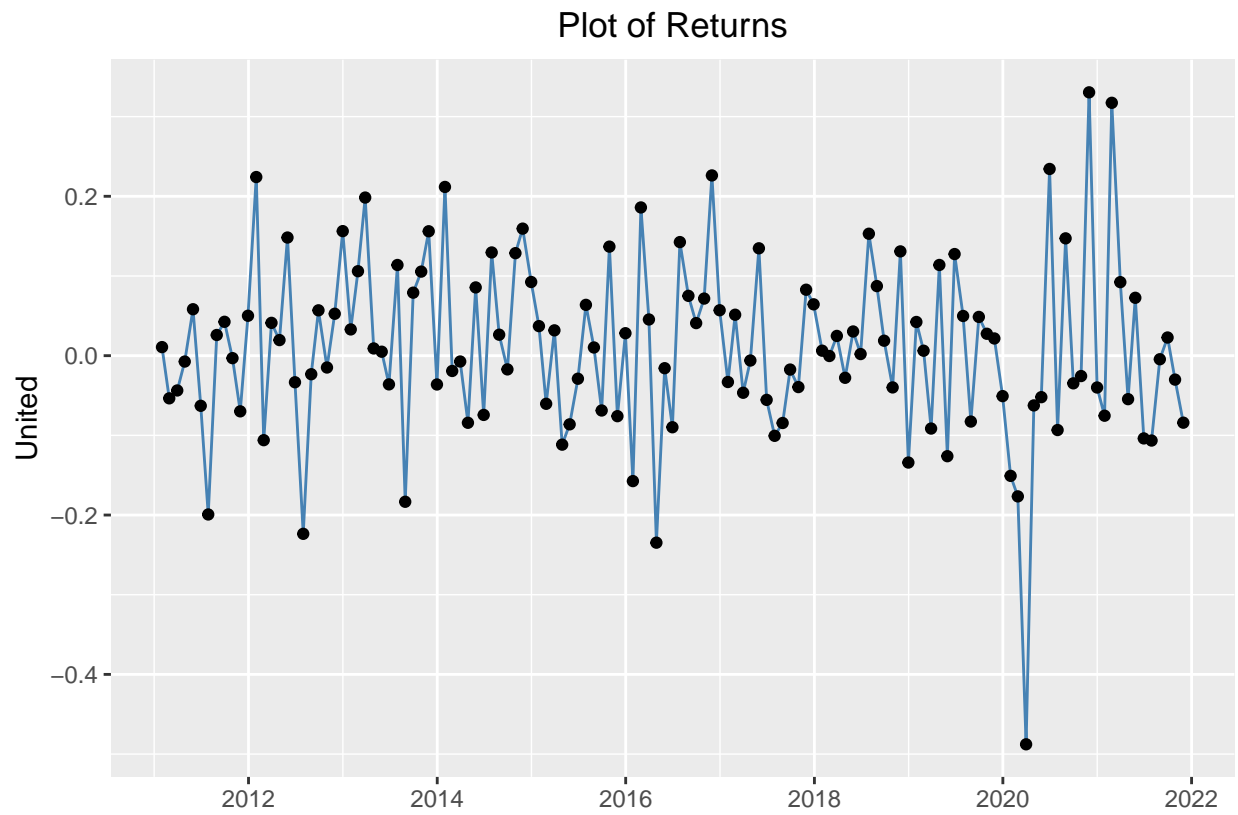


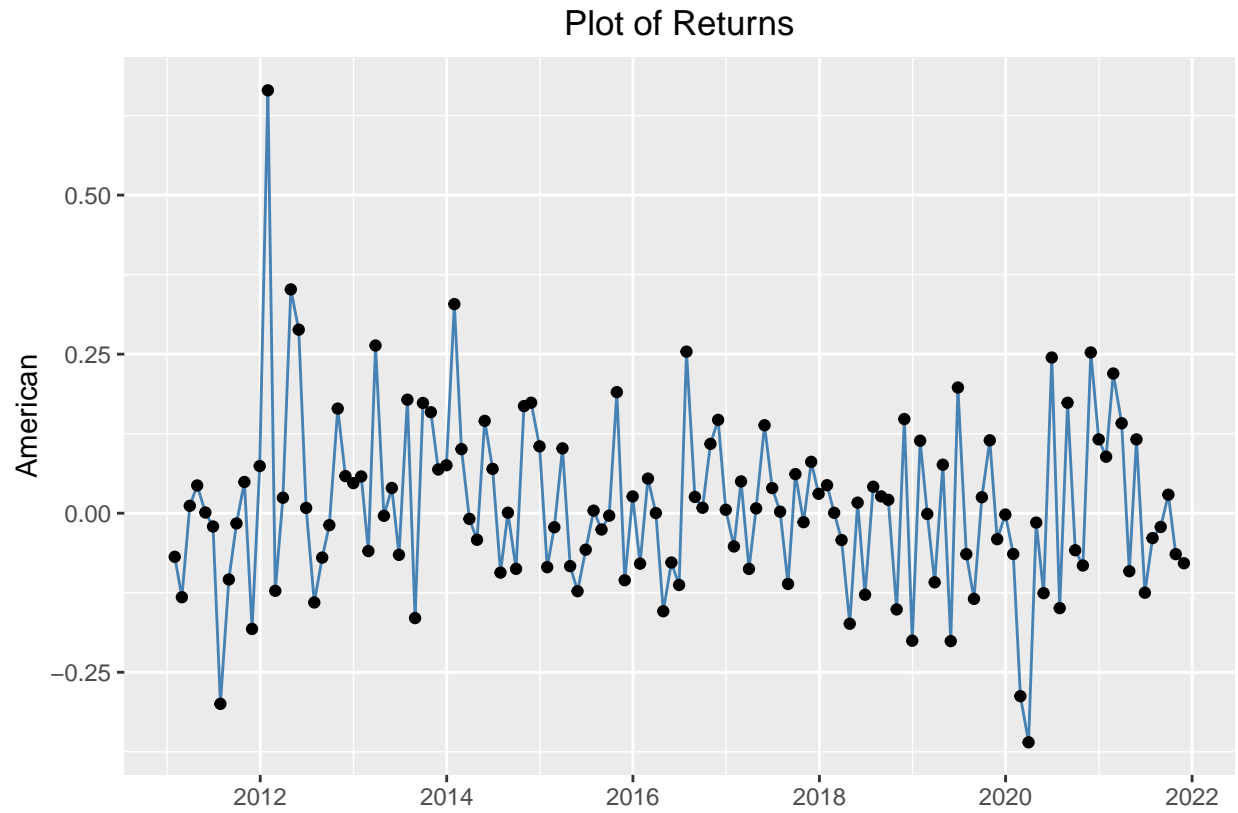
Plot of Returns







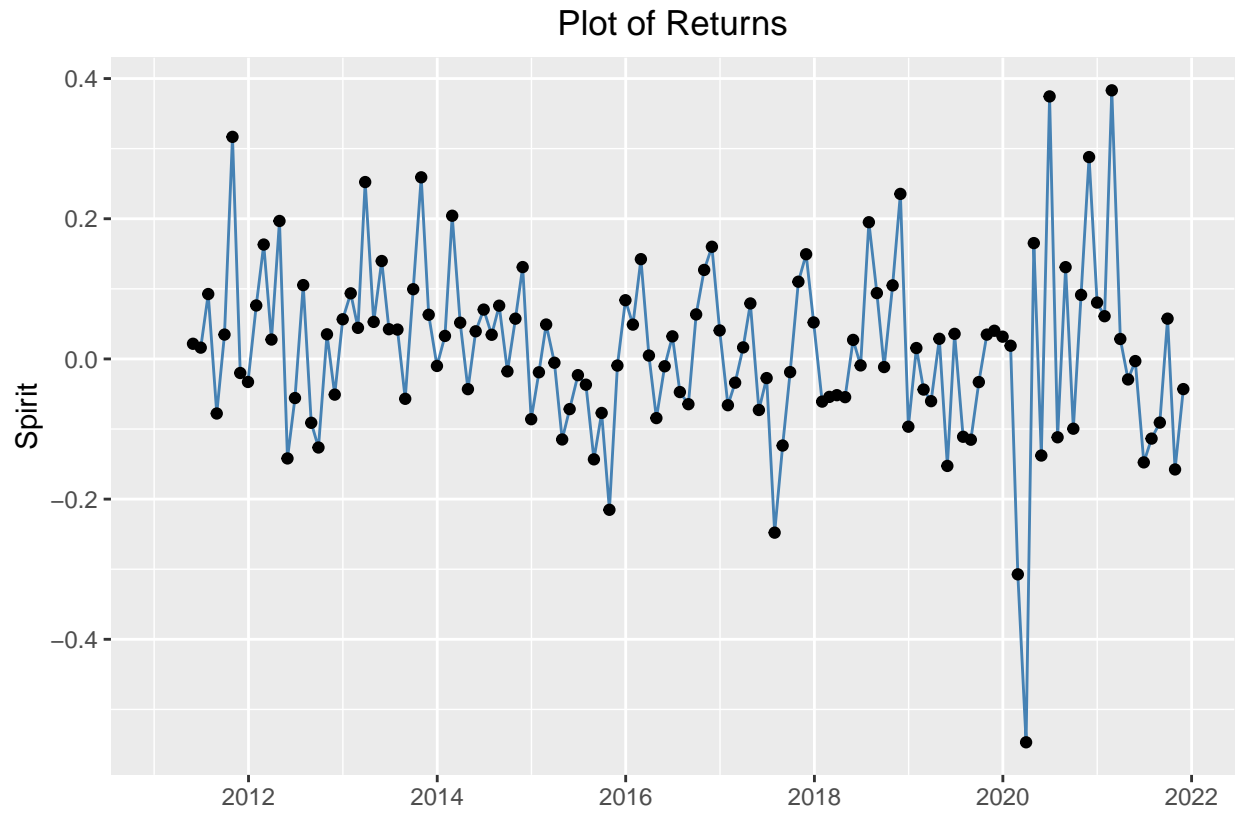


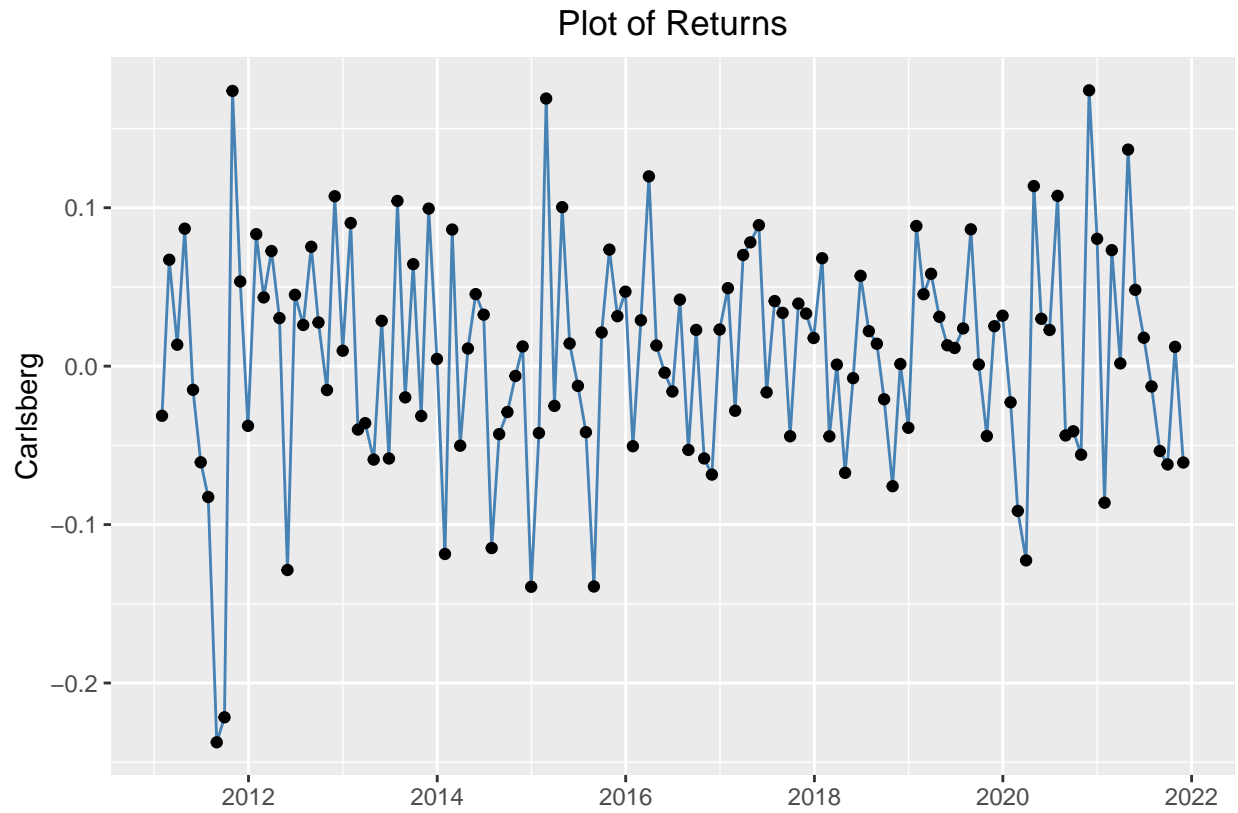


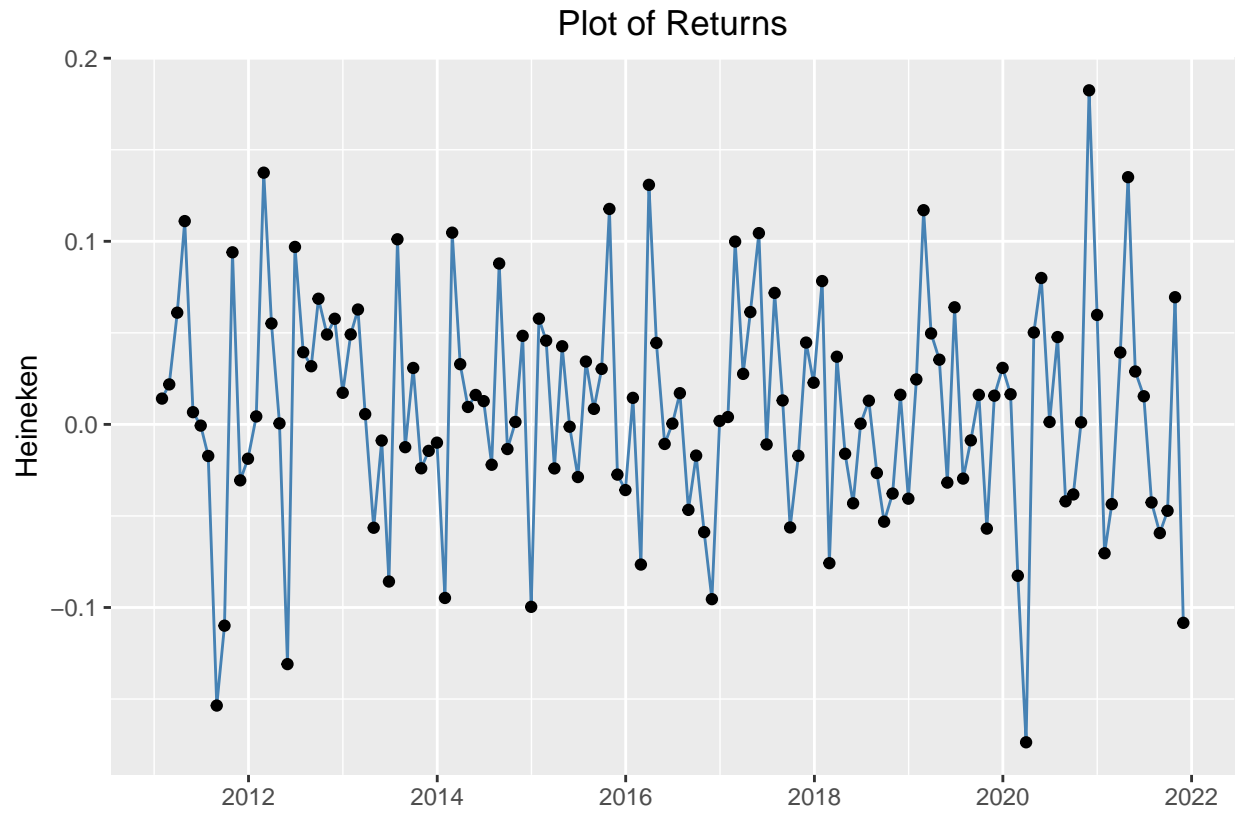
```
## Warning: Removed 4 row(s) containing missing values (geom_path).
```

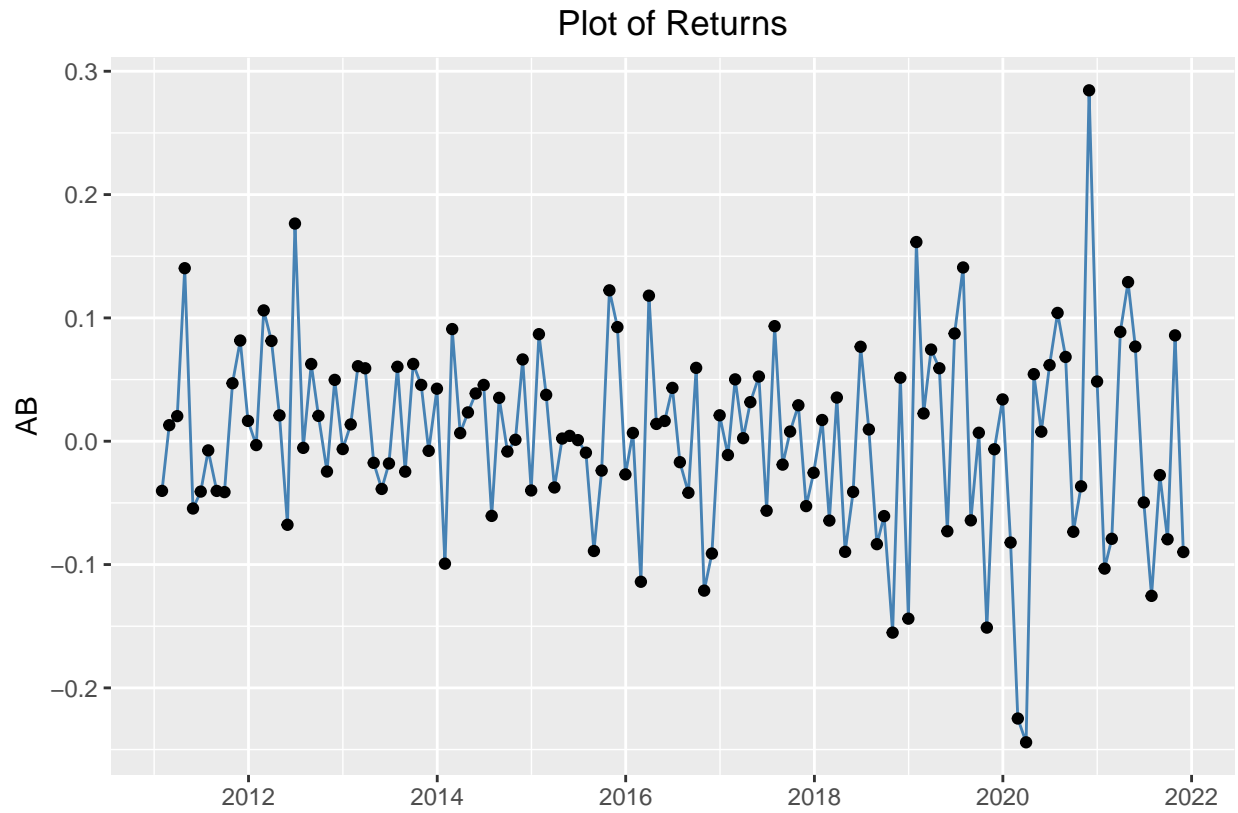
```
## Warning: Removed 4 rows containing missing values (geom_point).
```



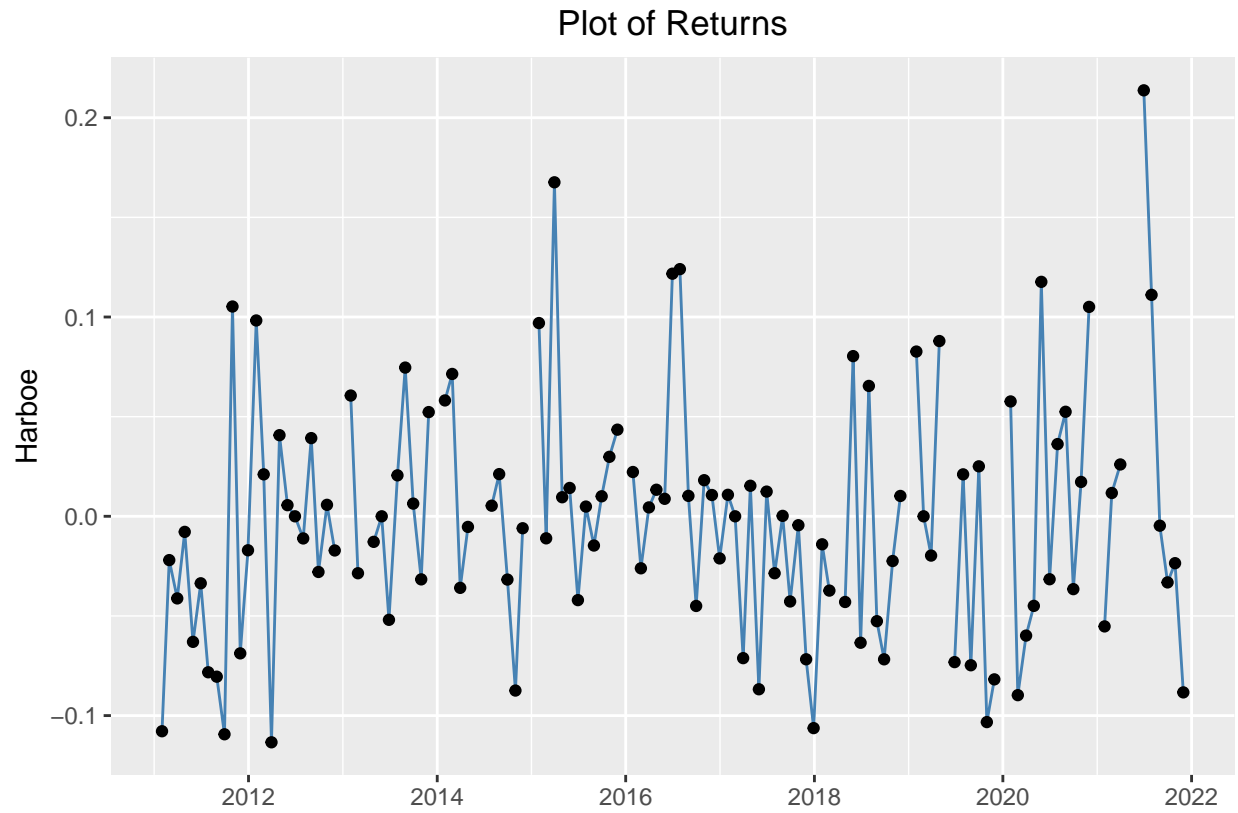


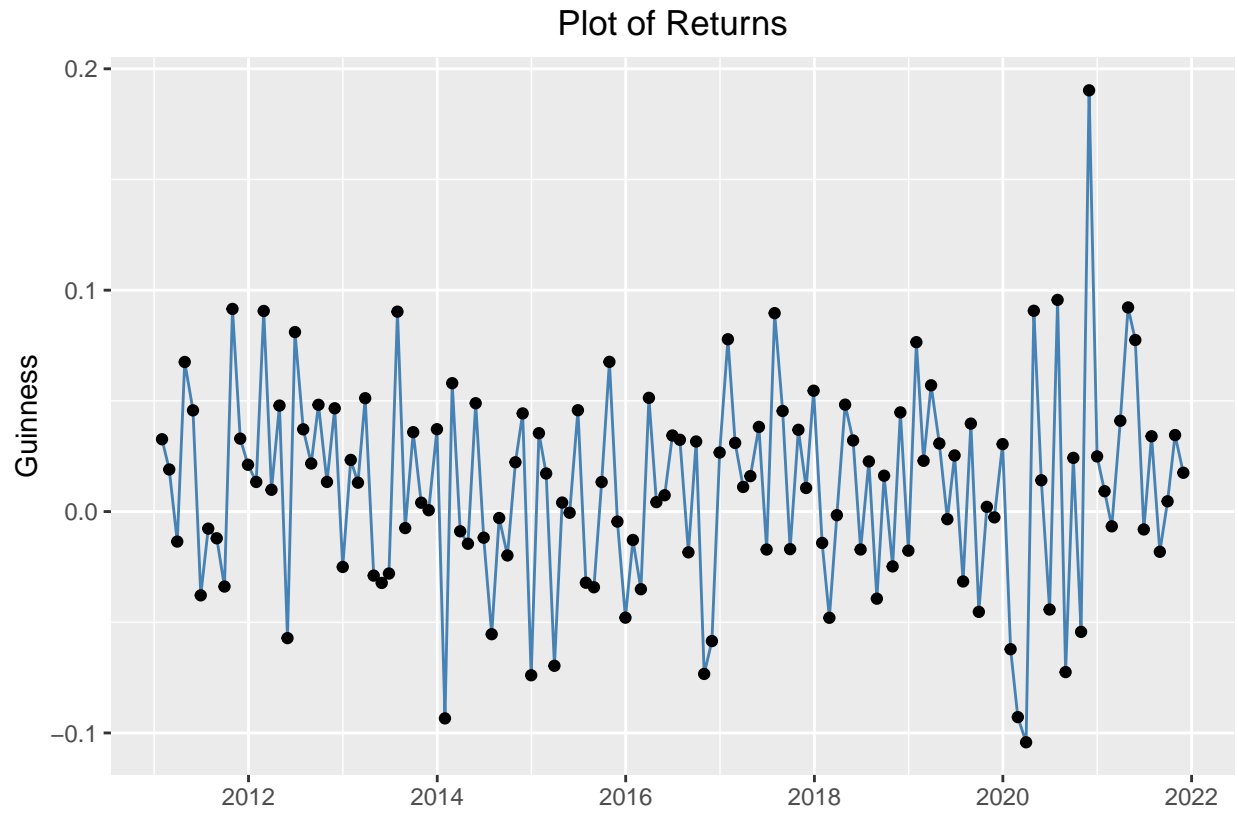


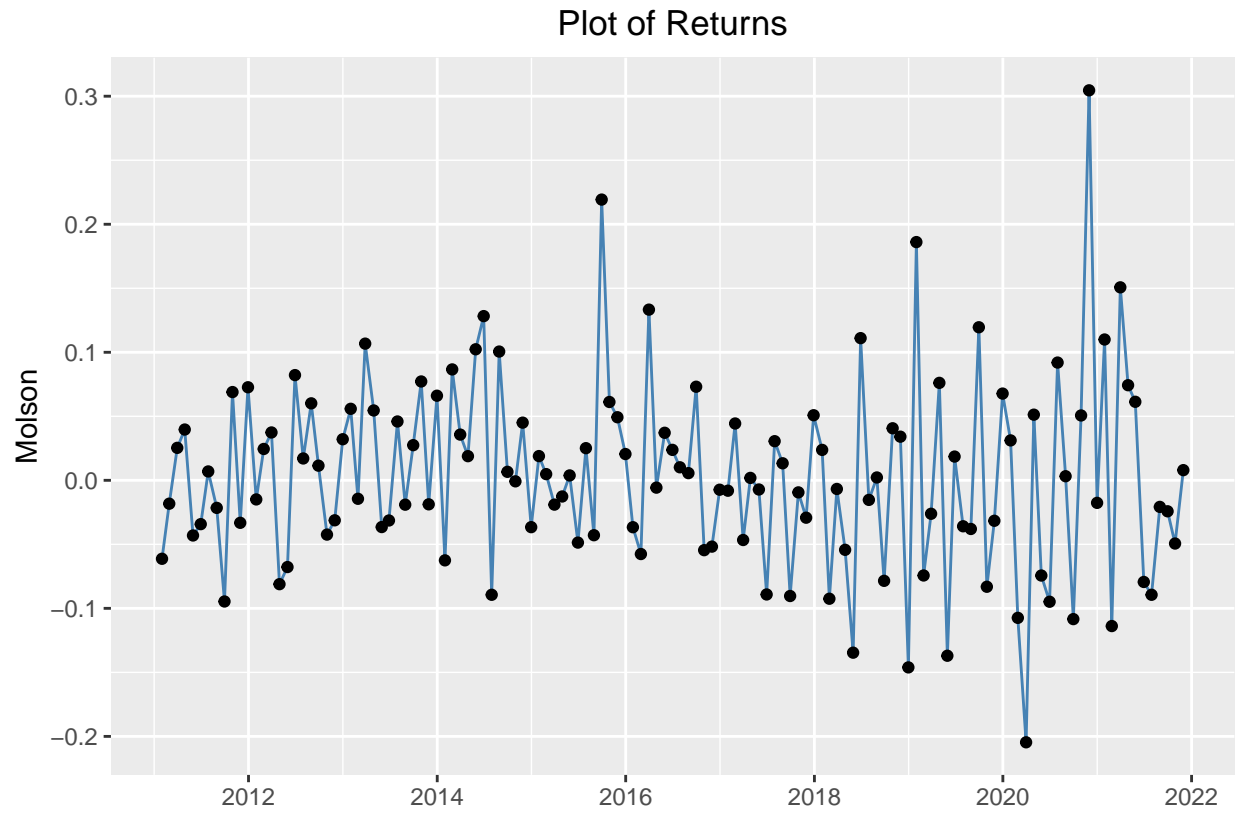




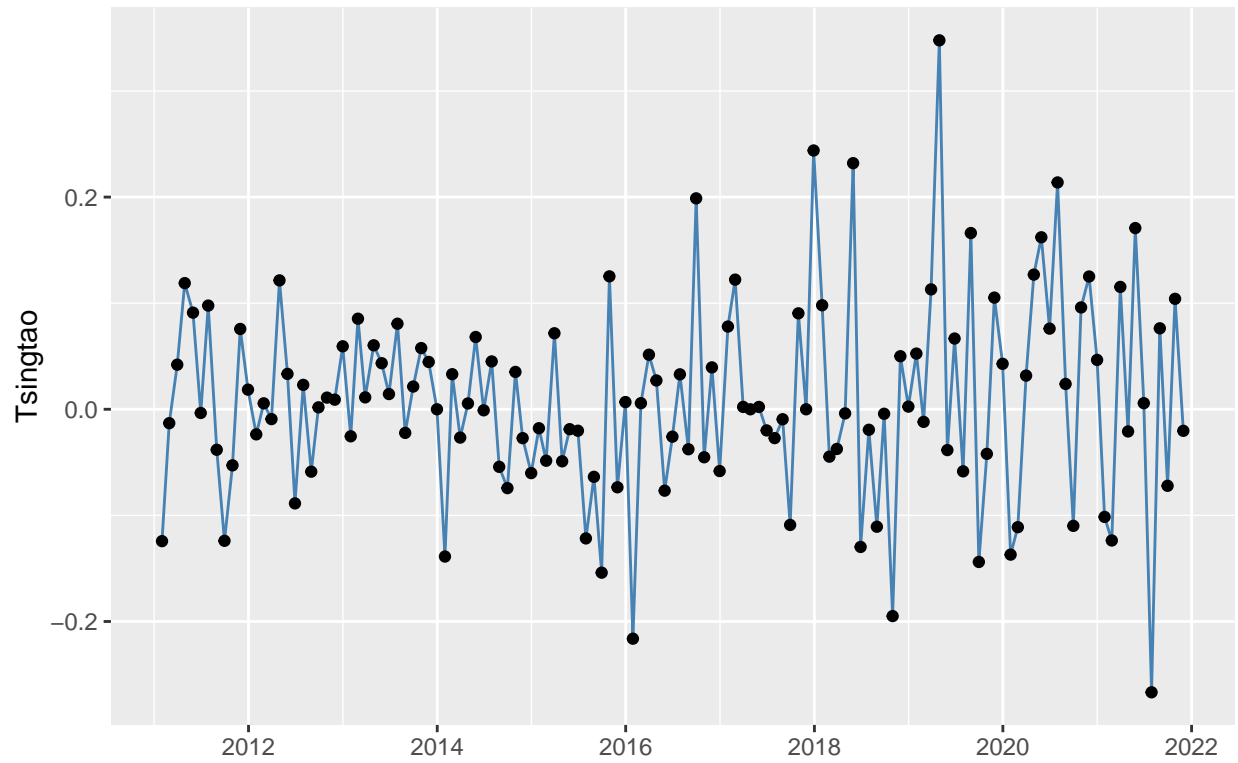
## Warning: Removed 14 rows containing missing values (geom\_point).





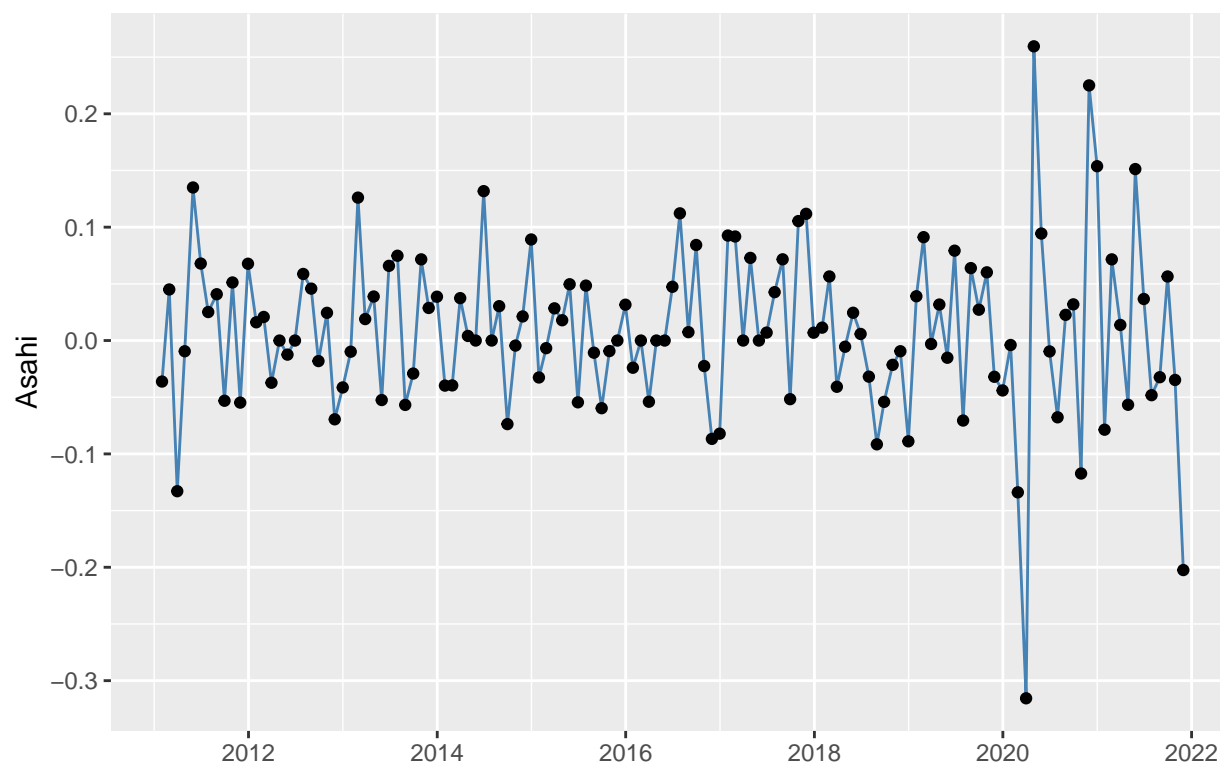


Plot of Returns





Plot of Returns

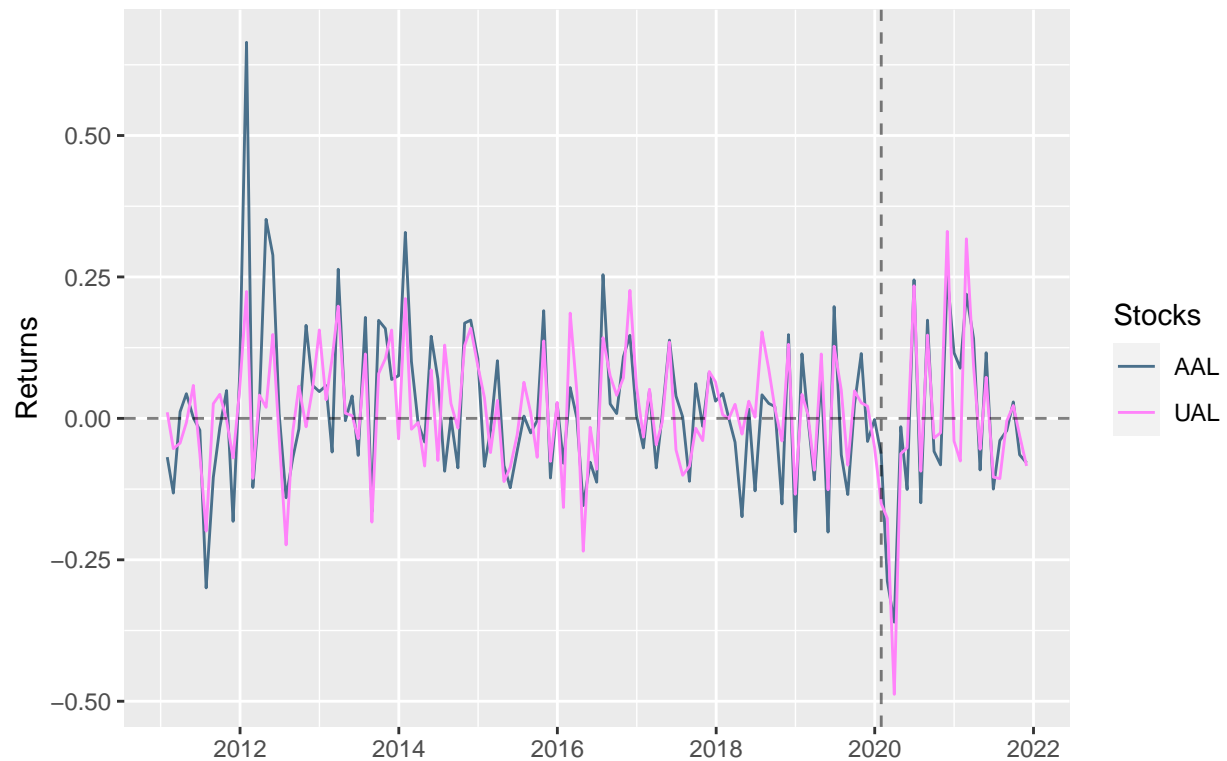


```
#united airlines and american airlines
```

```
airlines <- returns %>%
  select(date, UAL, AAL) %>%
  gather(key="Stocks", value = "Returns", -date)
```

```
ggplot(airlines, aes(x = date, y = Returns)) +
  geom_line(aes(color = Stocks)) +
  scale_color_manual(values = c("skyblue4", "orchid1")) +
  geom_hline(yintercept=0, linetype="dashed", alpha=0.5)+
  geom_vline(xintercept = as.Date("2020-01-31"), linetype="dashed", alpha=0.5) +
  ggtitle("Returns of United and American Airlines") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("")
```

## Returns of United and American Airlines



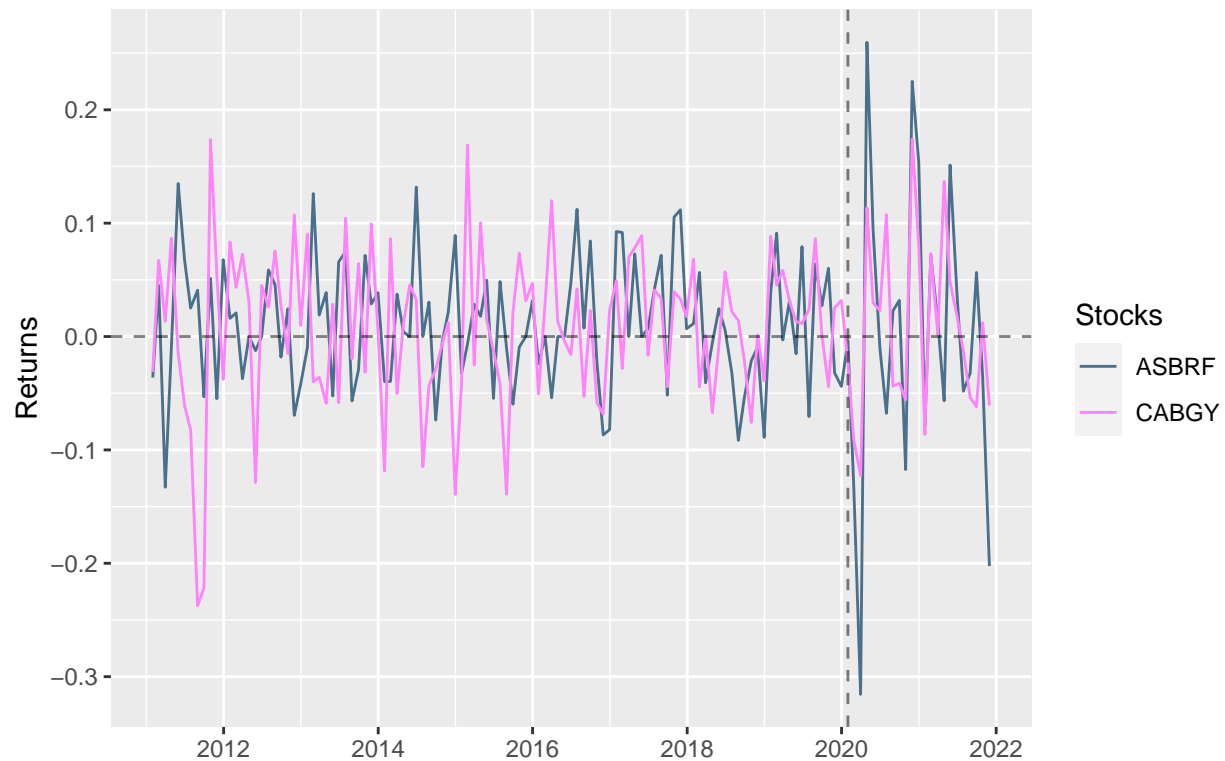
```
rm(airlines)

#carslberg and asahi

beers <- returns %>%
  select(date, CABGY, ASBRF ) %>%
  gather(key="Stocks", value = "Returns", -date)

ggplot(beers, aes(x = date, y = Returns)) +
  geom_line(aes(color = Stocks)) +
  scale_color_manual(values = c("skyblue4", "orchid1")) +
  geom_hline(yintercept=0, linetype="dashed", alpha=0.5)+
  geom_vline(xintercept = as.Date("2020-01-31"), linetype="dashed", alpha=0.5) +
  ggtitle("Returns of Carlsberg and Asahi") +
  theme(plot.title = element_text(hjust = 0.5)) +
  xlab("")
```

## Returns of Carlsberg and Asahi



```
rm(beers)
```

### 3. Plot equity curve

<https://bookdown.org/compfinezbook/introcompfinr/ReturnCalculationsR.html#>

```
returnsNA <- as.data.frame(na.omit(returns)) #doesn't work with NA values

equityCurve <- as.data.frame(matrix(c(rep(NA,113*15)), nrow= 113))
for (i in 1:15)
{
  equityCurve[,i] <- cumprod(1 + returnsNA[,i+1])
}

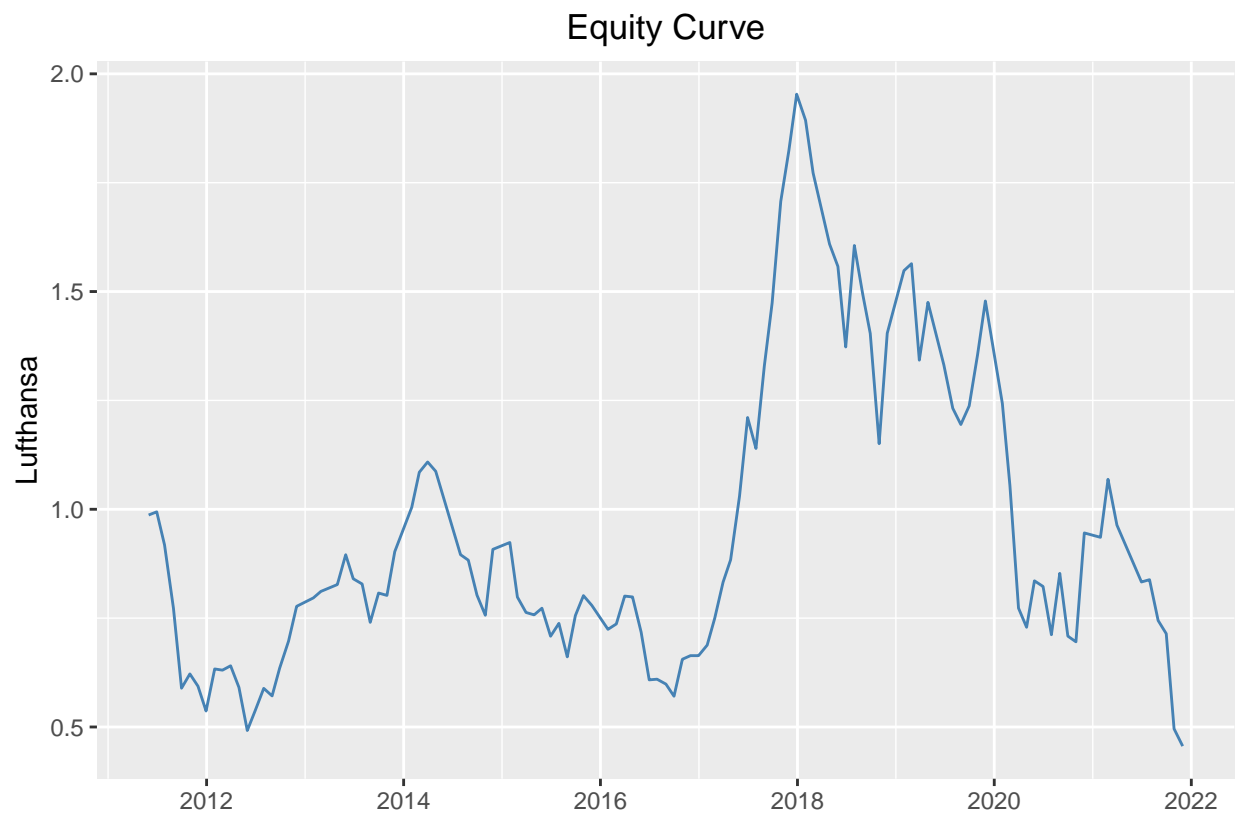
equityCurve <- cbind(returnsNA[,1], equityCurve)
colnames(equityCurve)[1] <- "date"

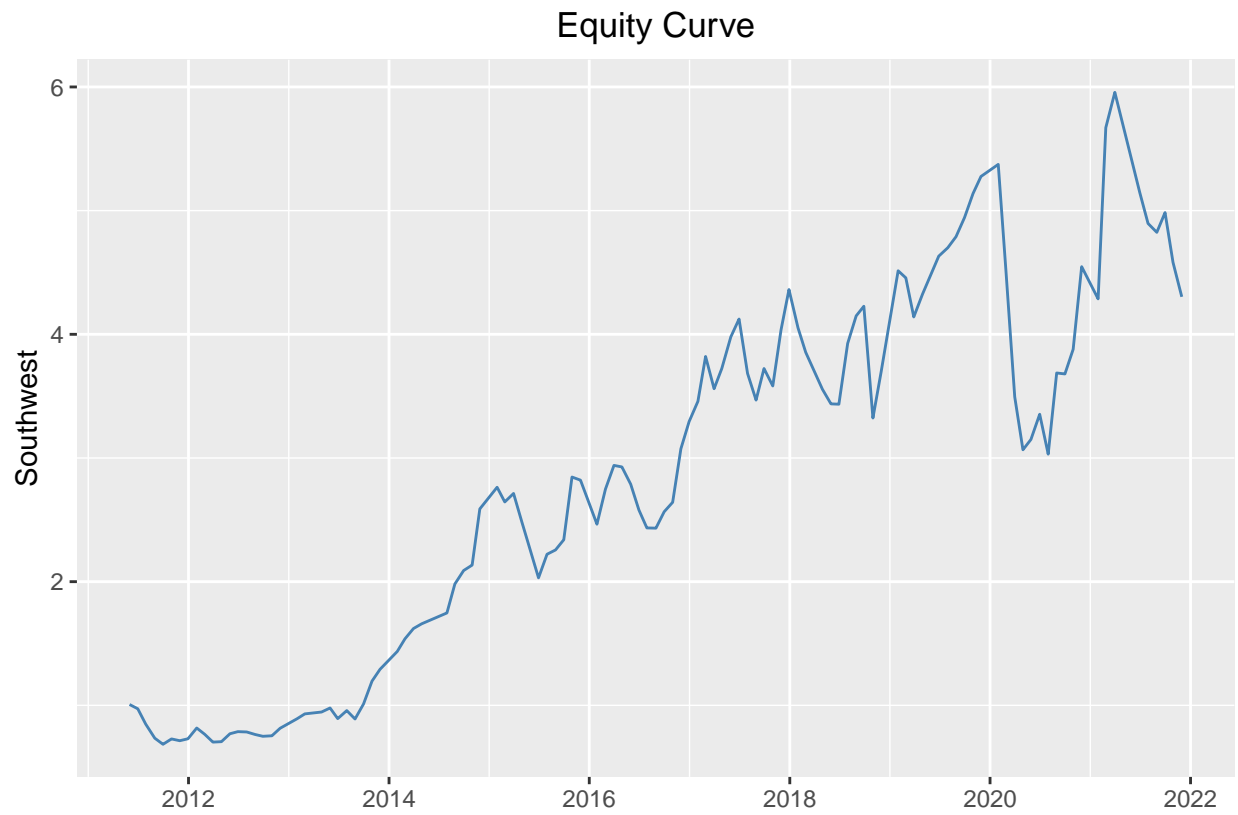
#airlines 7
for (i in 1:7)
{
  names <- list(stock_names)
  print(ggplot(equityCurve, aes(x=date, y=equityCurve[,i+1])) +
    ggtitle("Equity Curve") +
    theme(plot.title = element_text(hjust = 0.5))+
    geom_line(color="steelblue") +
```

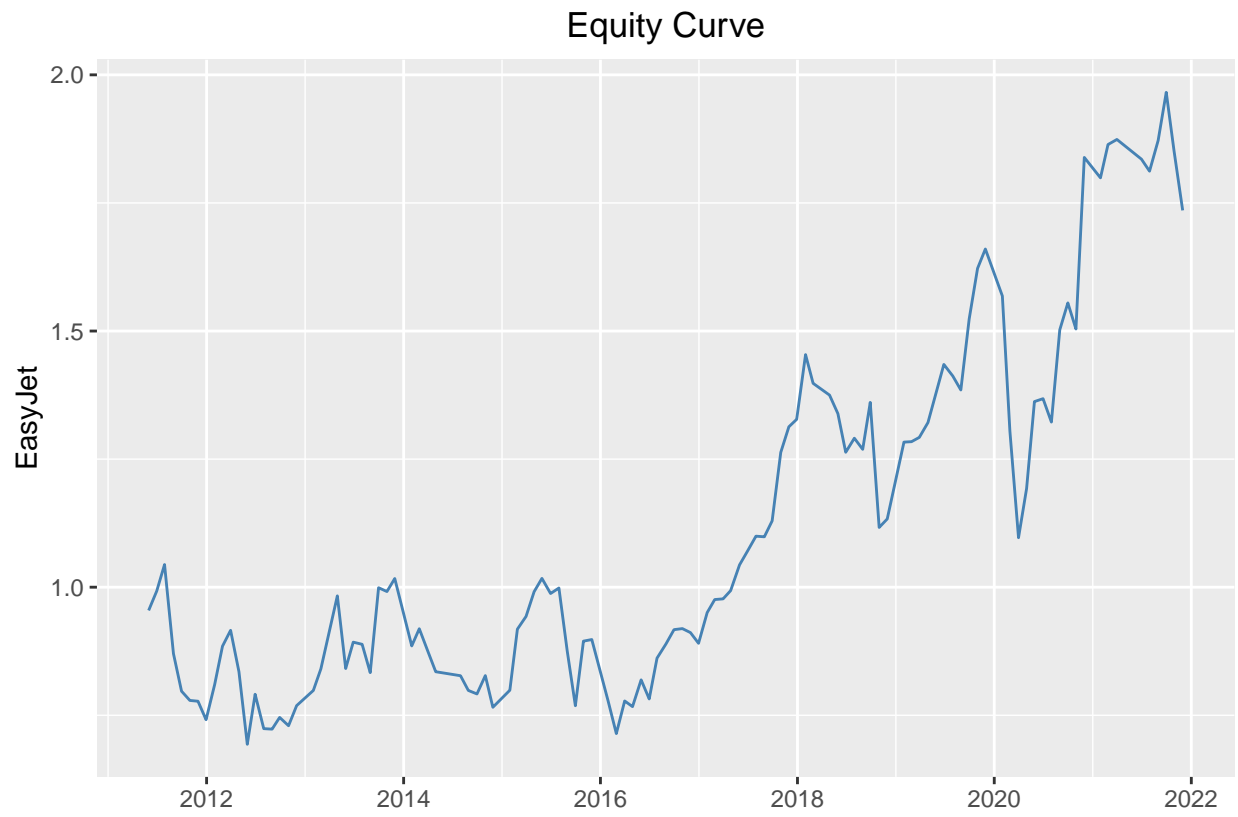
```

xlab("") +
ylab(names[[1]][i]))
}

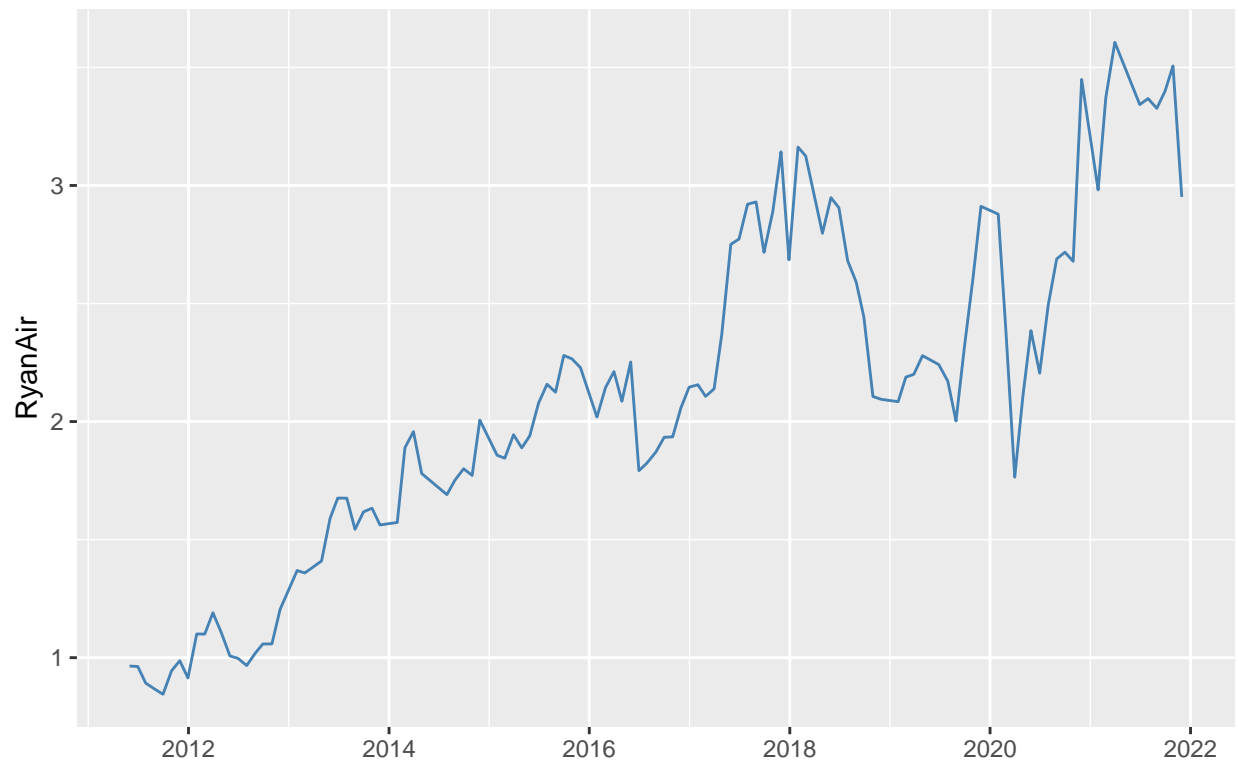
```

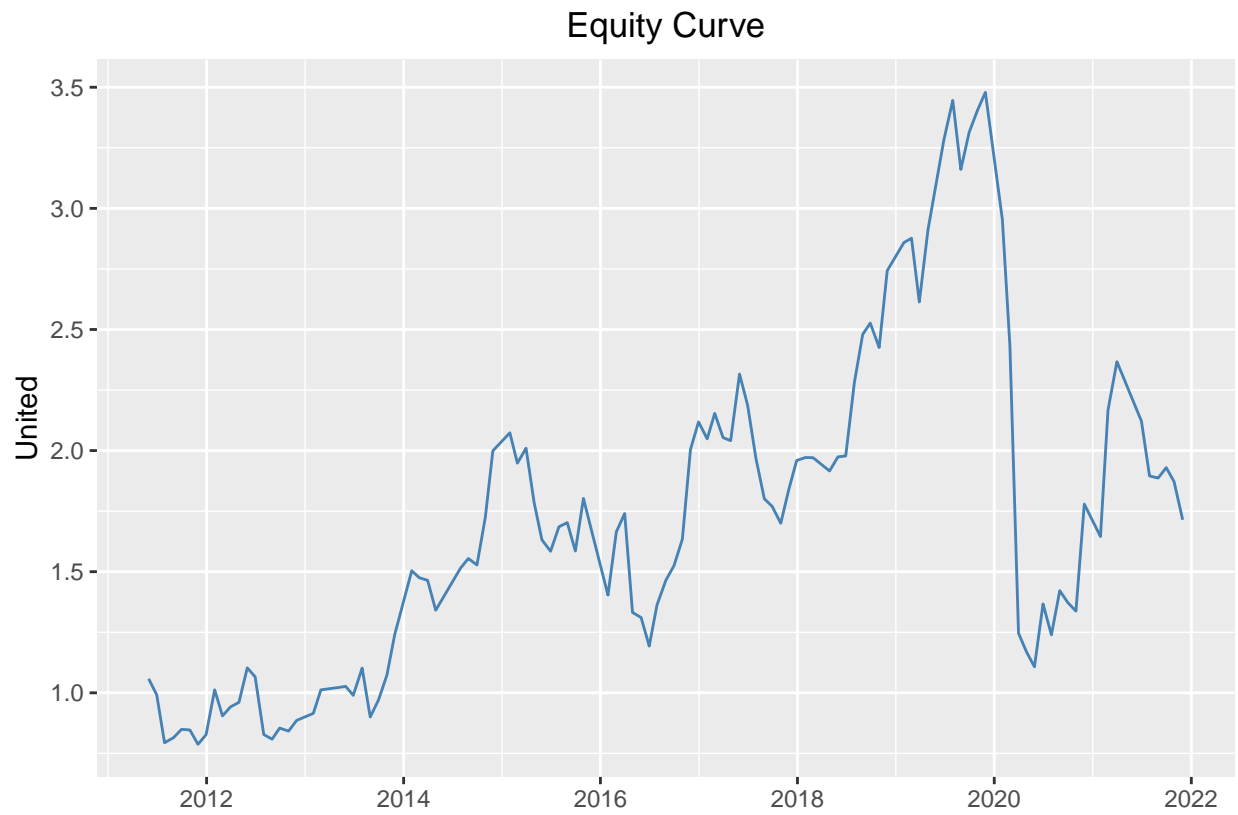




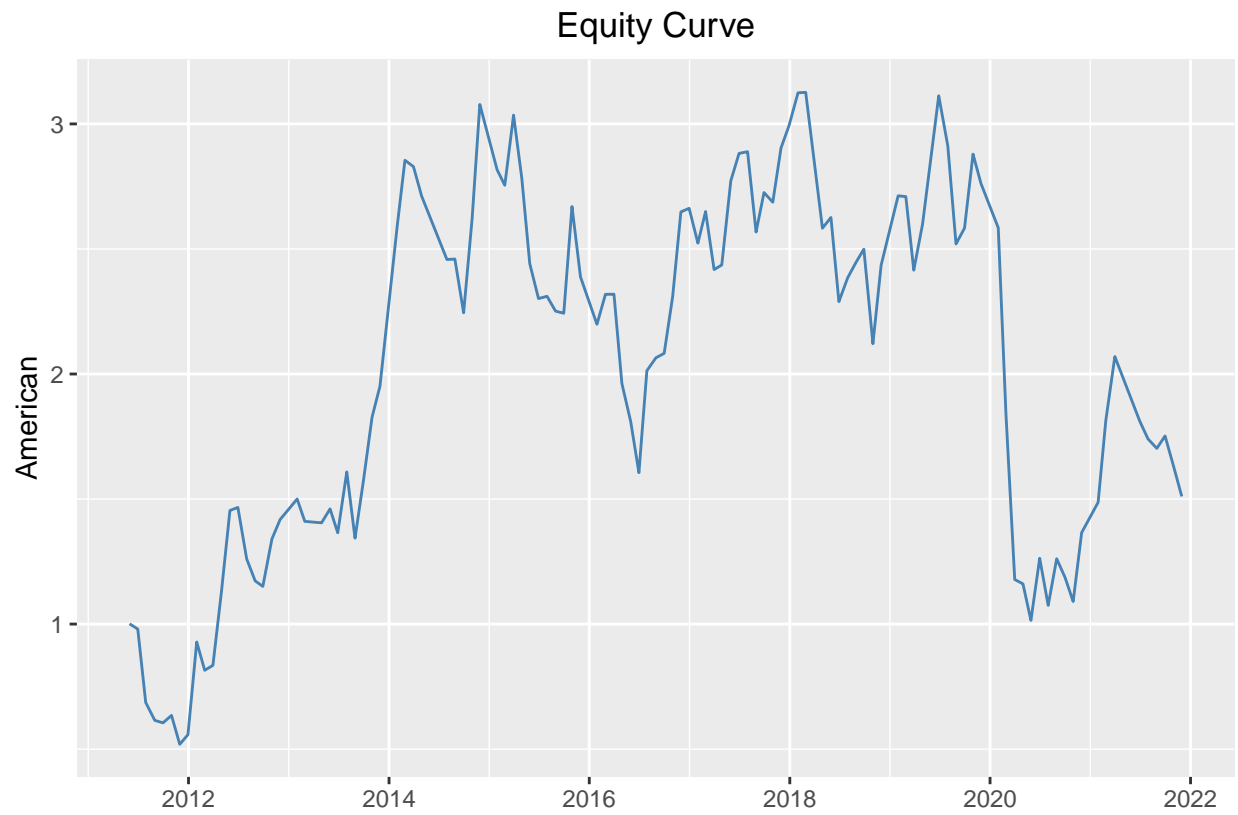


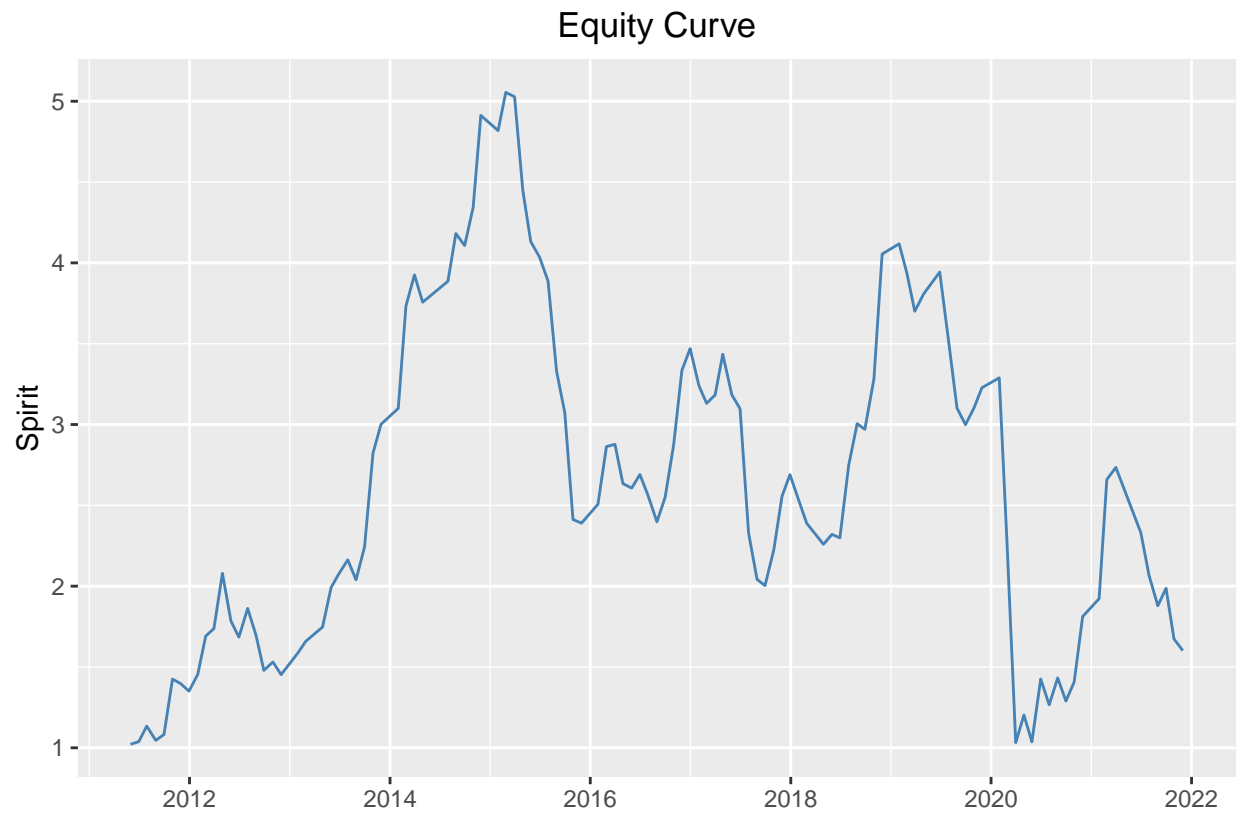
Equity Curve



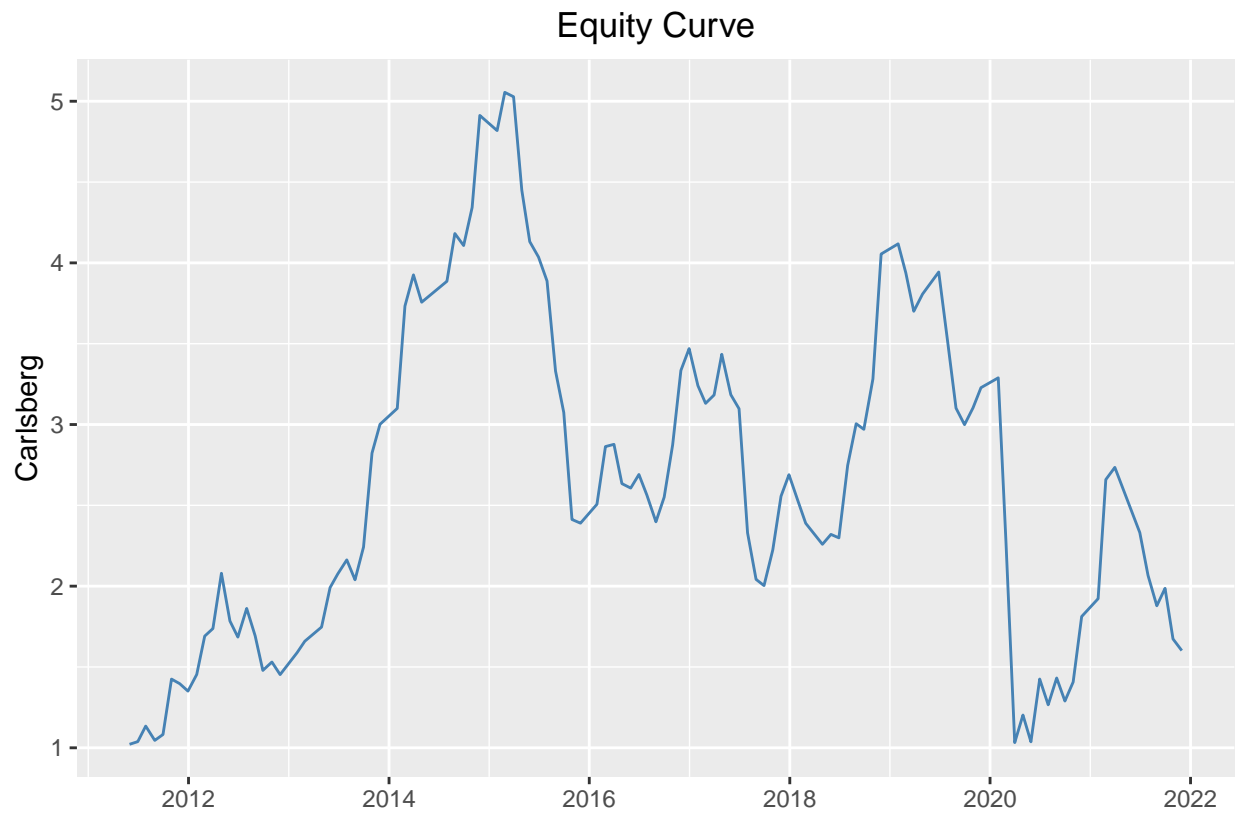




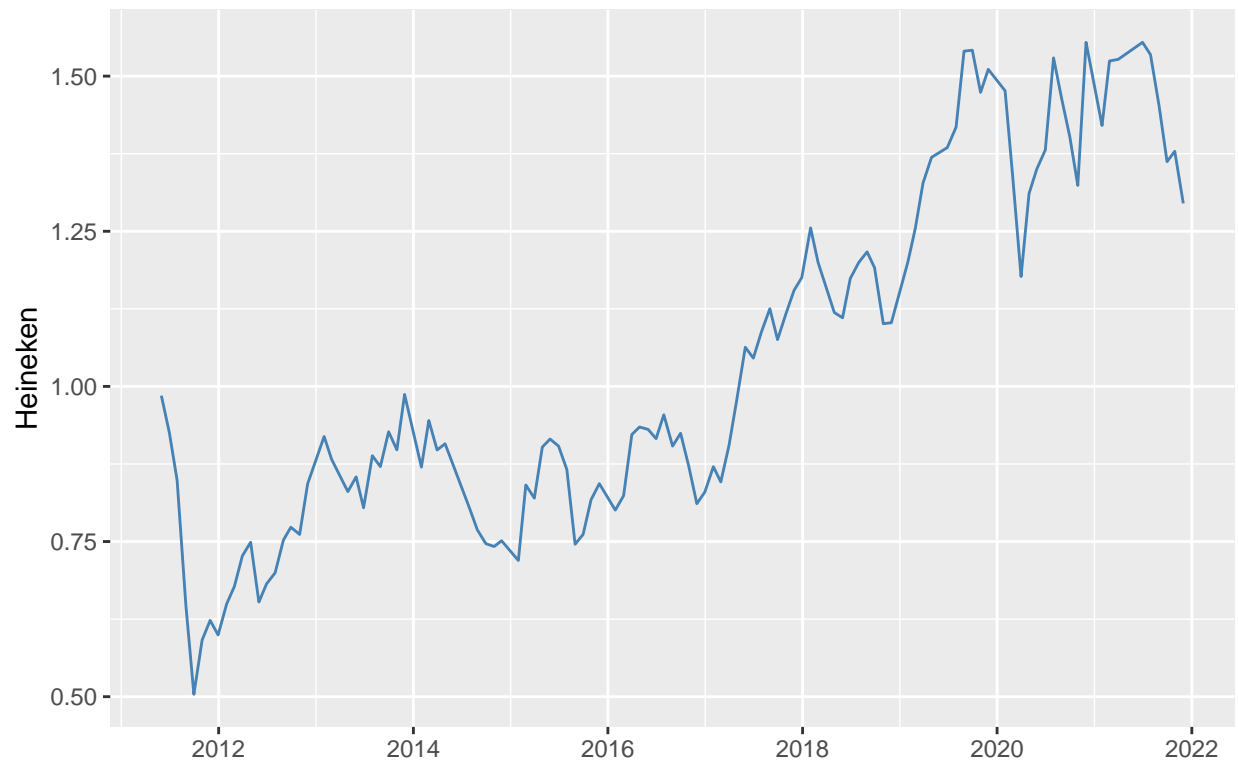


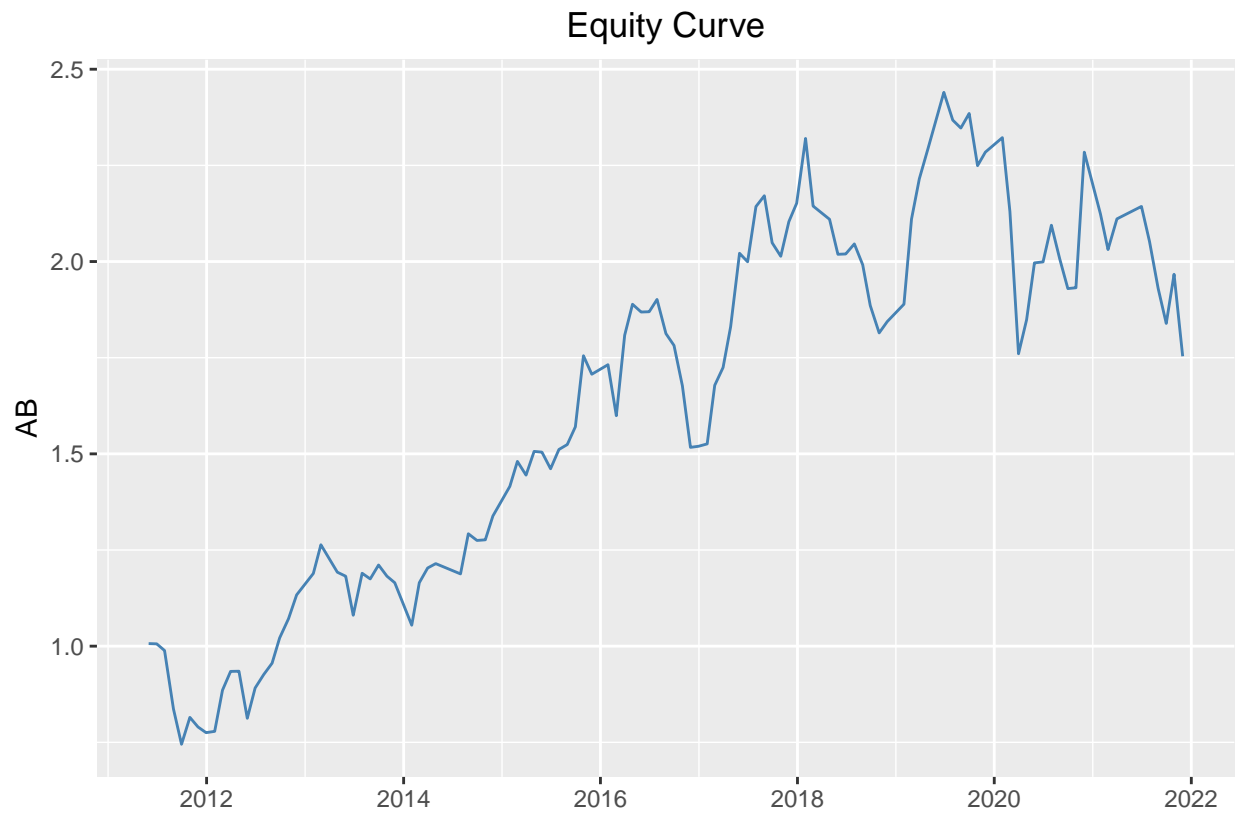


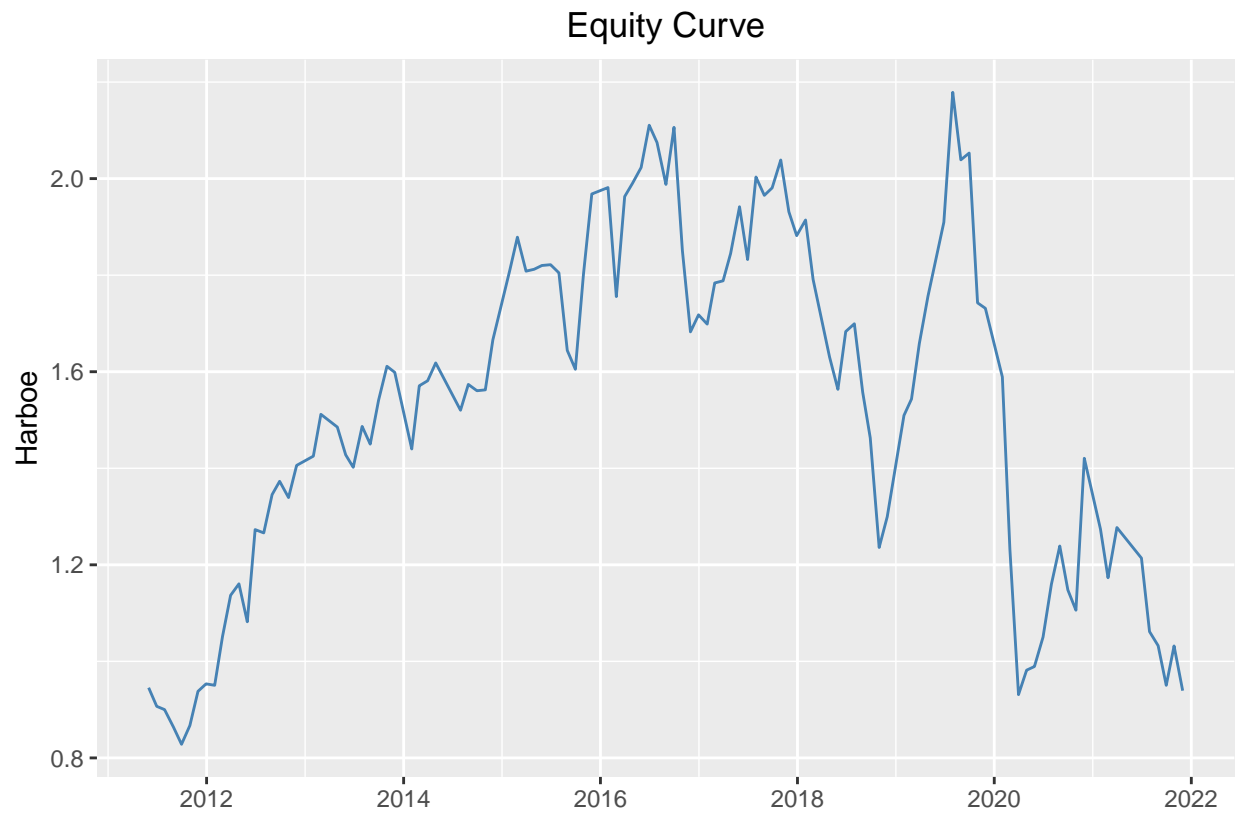
```
#beers
for (i in 1:8)
{
  names <- list(stock_names)
  print(ggplot(equityCurve, aes(x=date, y=equityCurve[,i+7])) +
    ggtitle("Equity Curve") +
    theme(plot.title = element_text(hjust = 0.5)) +
    geom_line(color="steelblue") +
    xlab("") +
    ylab(names[[1]][i+7]))
}
```

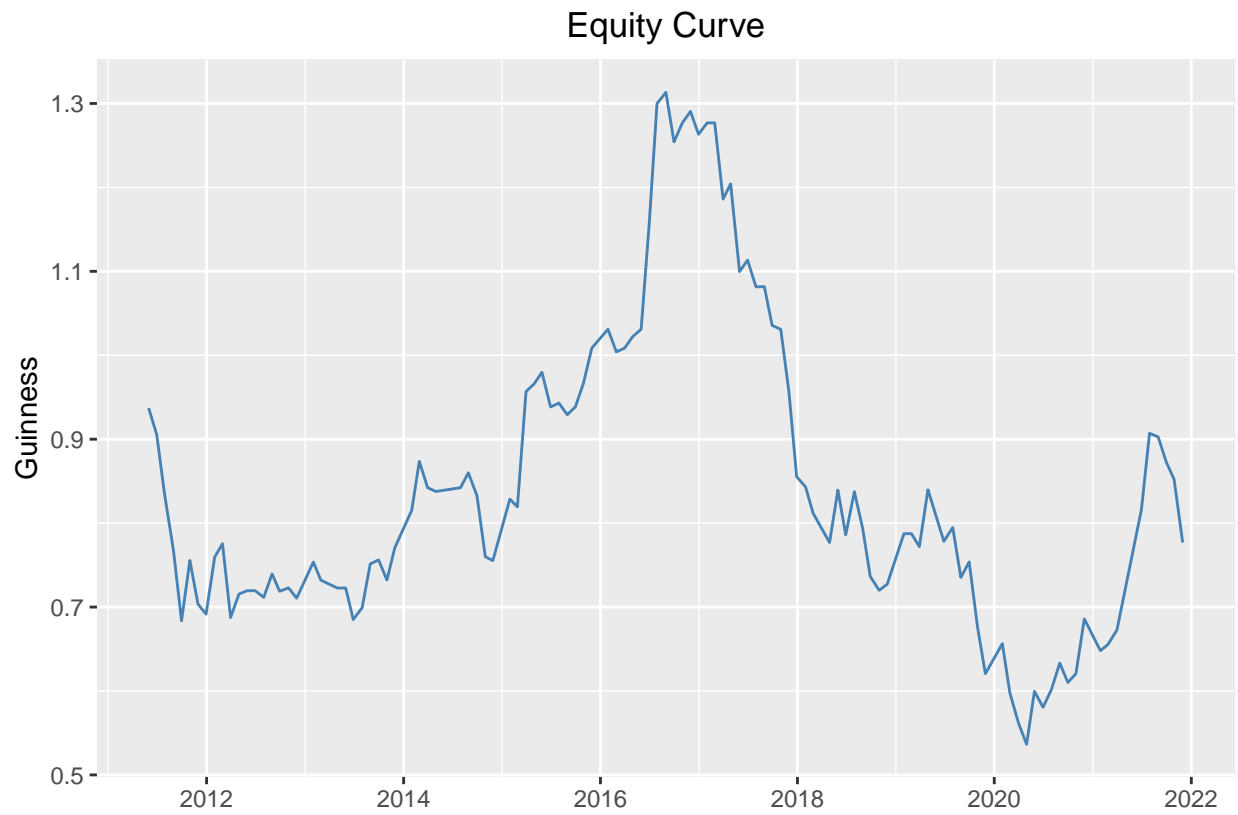


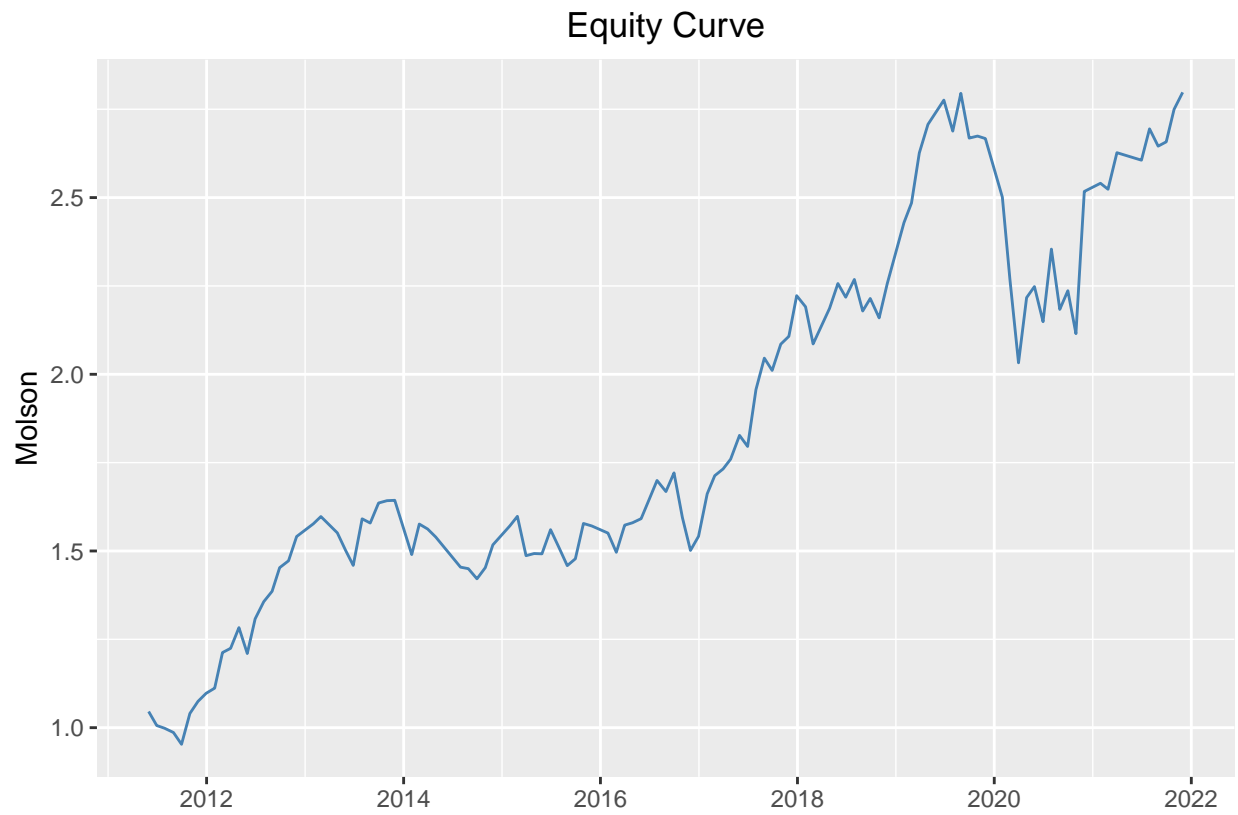
Equity Curve



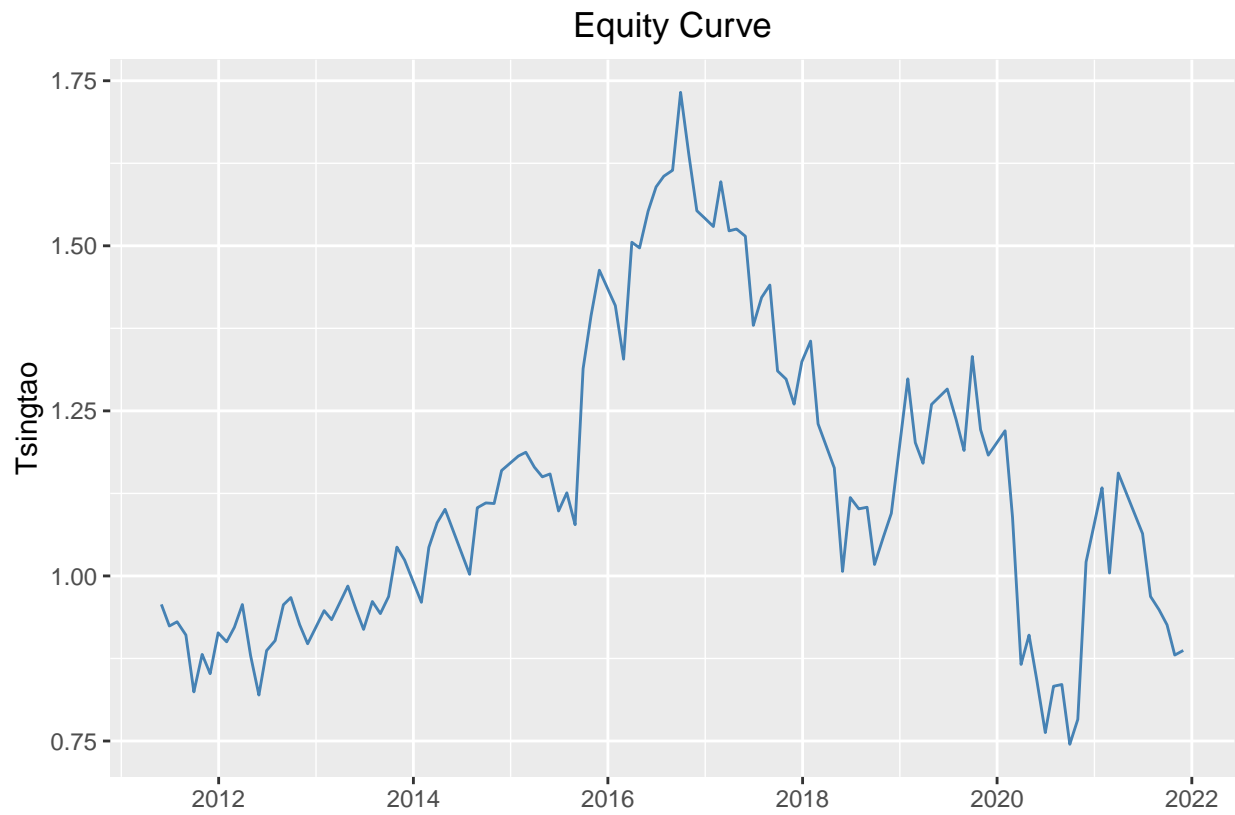


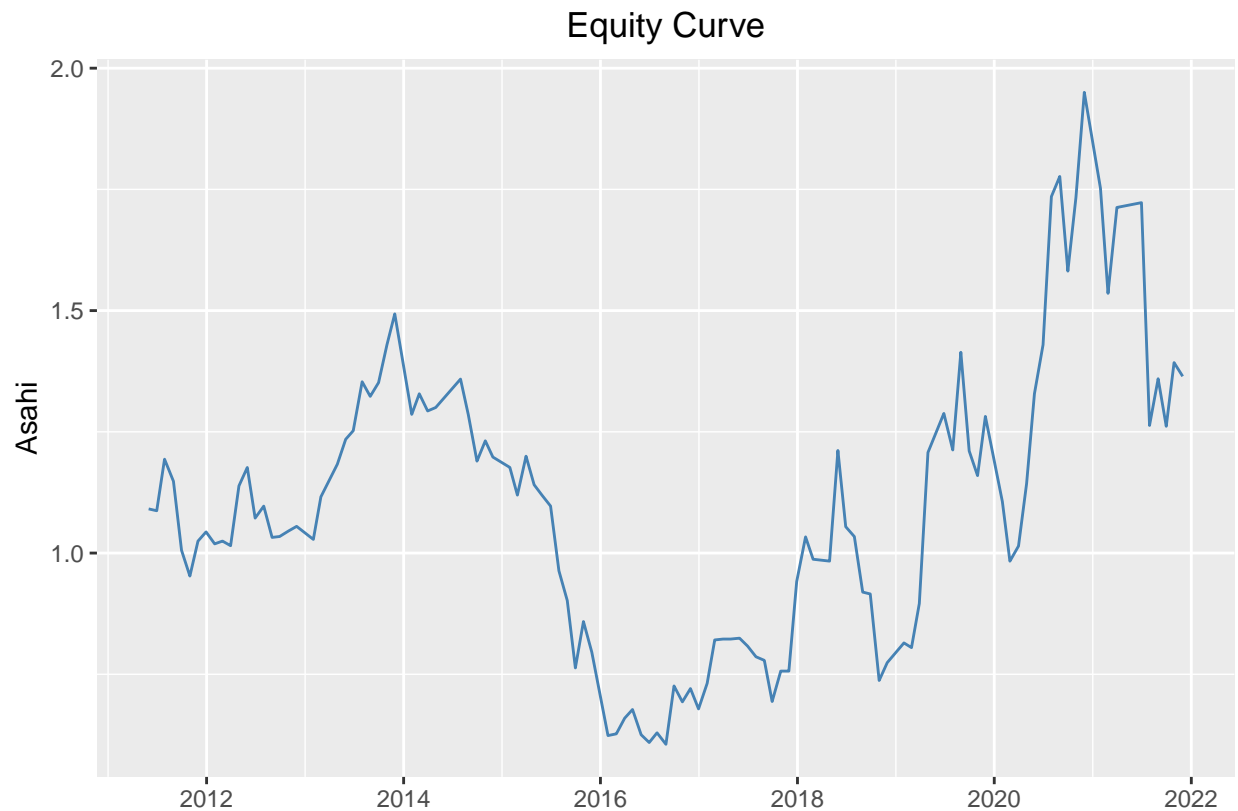












You should also provide an equity curve for each asset (that is, a curve that shows the growth of a \$1 in each of the asset over the time period you chose) and comment of your results. You should do the same for S&P 500 and compare it with the assets.

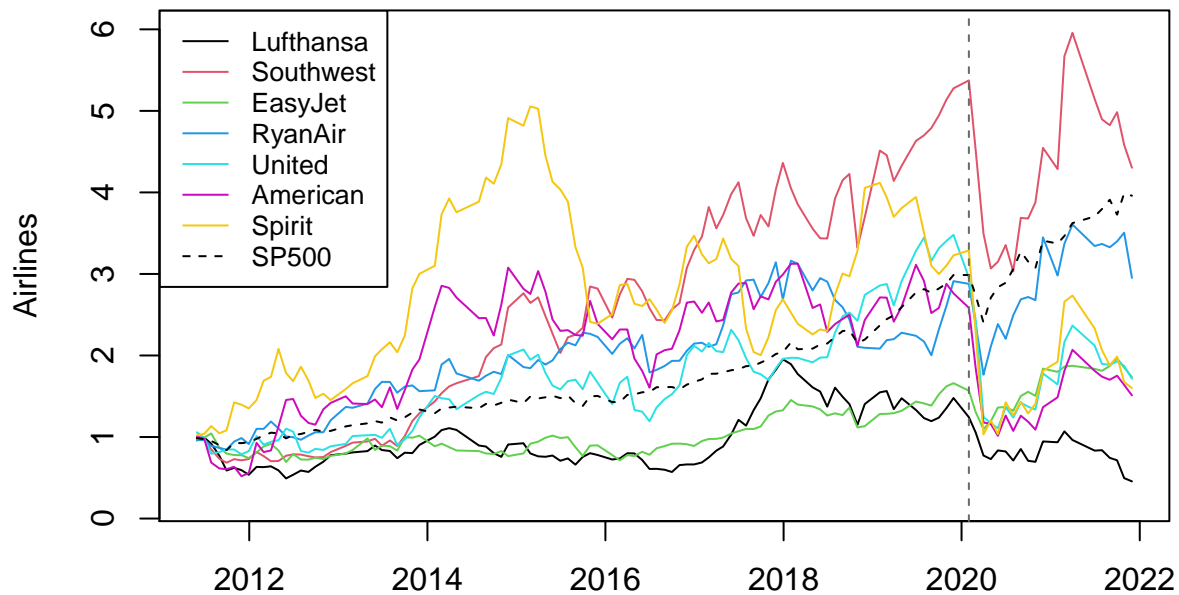
```
equityCurveSP <- cumprod(1 + returnsNA[,17])

namesair <- names[[1]][1:7]
namesair <- append(namesair, "SP500")

colors <- c(1,2,3,4,5,6,7,1)
lt <- c(1,1,1,1,1,1,1,2)

#airlines
plot(equityCurve[,1], equityCurve[,2], type = "l", ylim= c(0.2,6), xlab="", ylab="Airlines", main="Equity Curve")
for(i in 1:6)
{
  lines(equityCurve[,1], equityCurve[,i+2], type = "l", col = i+1)
}
lines(equityCurve[,1],equityCurveSP,type="l", lty=2, lwd=1, col="black")
abline(v=as.Date("2020-01-31"), lty=2, col="dimgrey")
legend(x='topleft', legend=namesair,col=colors, lty=lt, cex=0.8)
```

## Equity Curves of Airlines

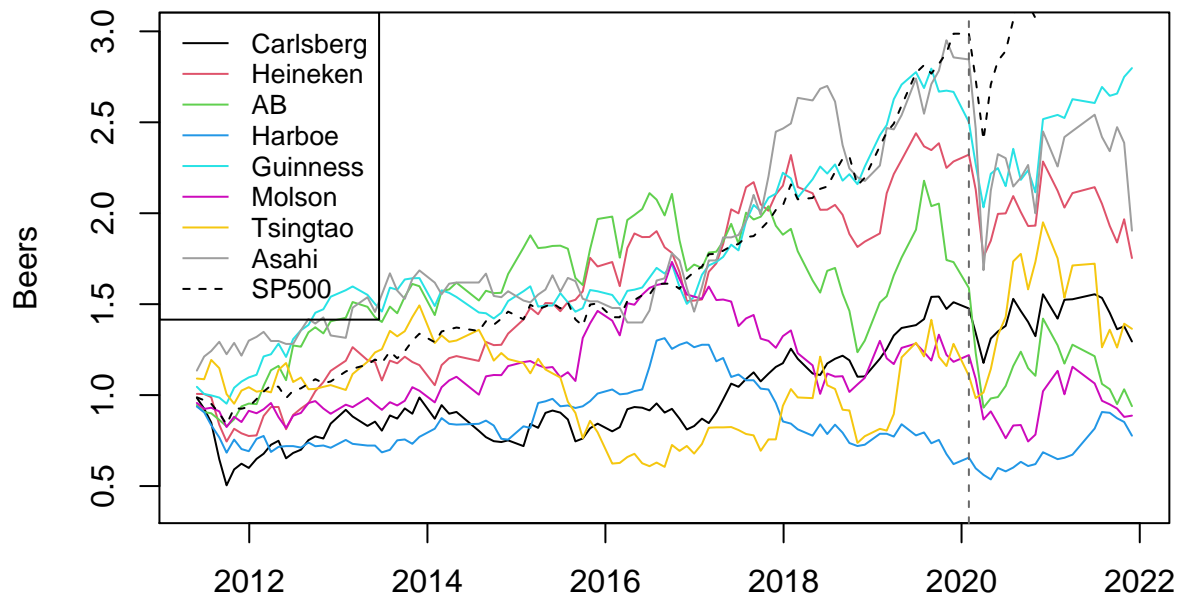


```
#####

colors <- c(1,2,3,4,5,6,7,8,1)
lt <- c(1,1,1,1,1,1,1,1,2)

#beers
plot(equityCurve[,1], equityCurve[,9], type = "l", ylim= c(0.4,3), xlab="", ylab="Beers", main="Equity C
for(i in 1:7)
{
  lines(equityCurve[,1], equityCurve[,i+9], type = "l", col = i+1)
}
lines(equityCurve[,1],equityCurveSP,type="l", lty=2, lwd=1, col="black")
abline(v=as.Date("2020-01-31"), lty=2, col="dimgrey")
legend(x='topleft', legend=names[[1]][8:16],col=colors, lty=lt, cex=0.8)
```

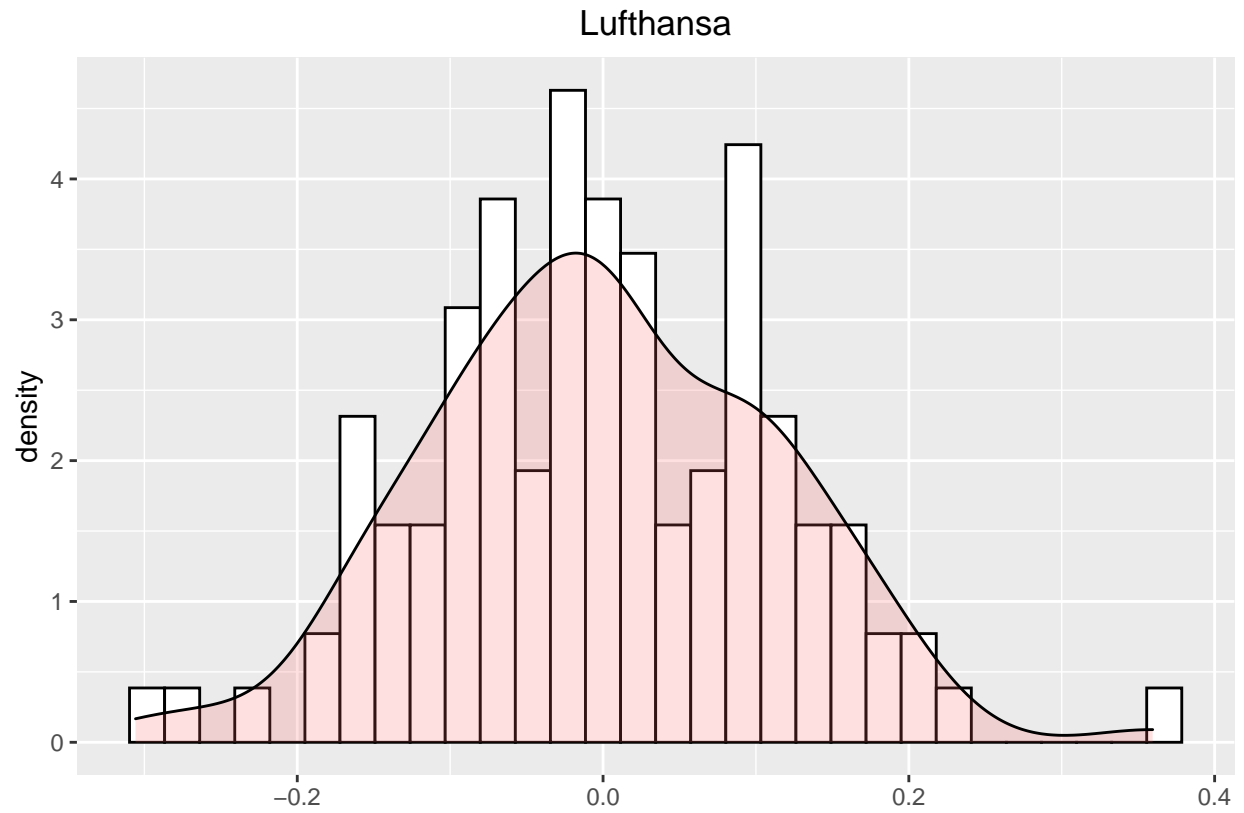
## Equity Curves of Beers



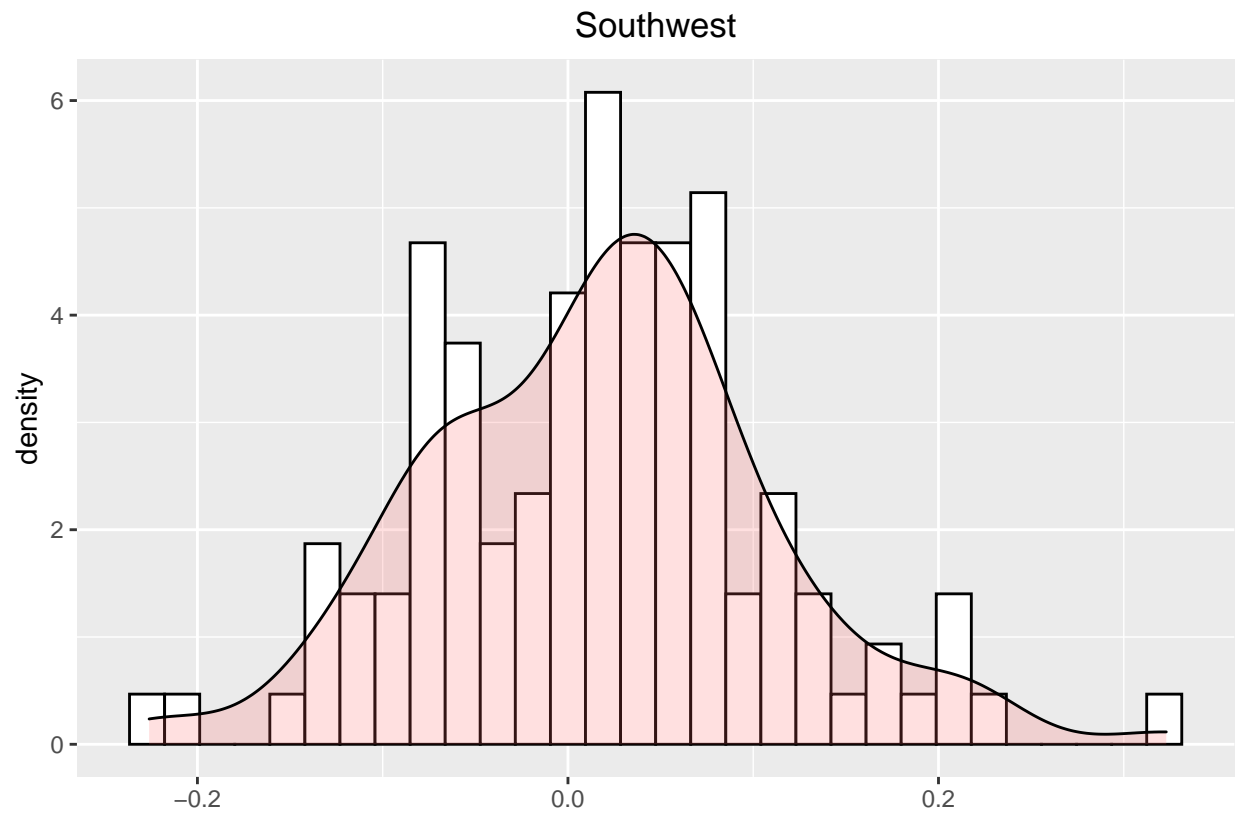
### 4. Histograms for each return series

```
for (i in 1:15)
{
  names <- list(stock_names)
  print(ggplot(returnsNA, aes(x=returnsNA[,i+1])) +
    geom_histogram(aes(y=..density..), colour="black", fill="white") +
    geom_density(alpha=.2, fill="#FF6666")+
    xlab("") +
    ggtitle(names[[1]][i])+
    theme(plot.title = element_text(hjust = 0.5)))
}
```

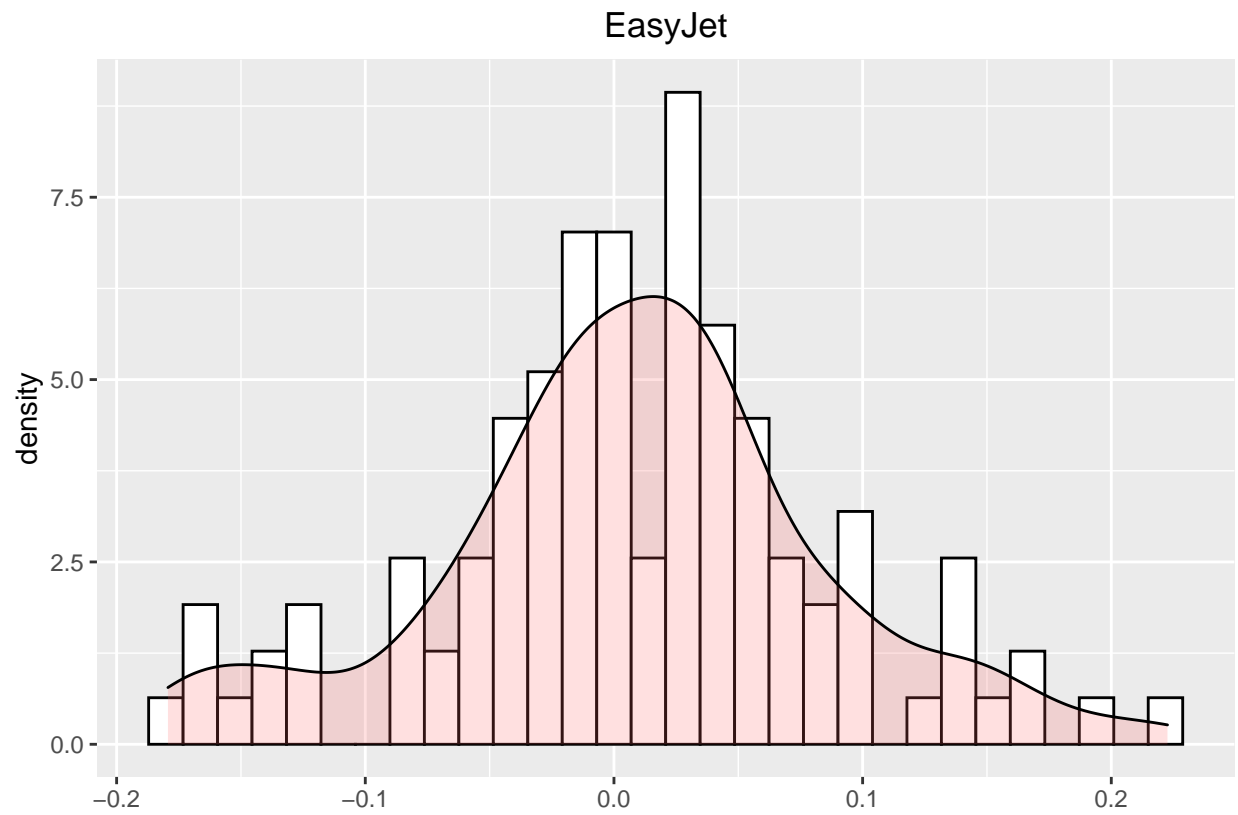
## 'stat\_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



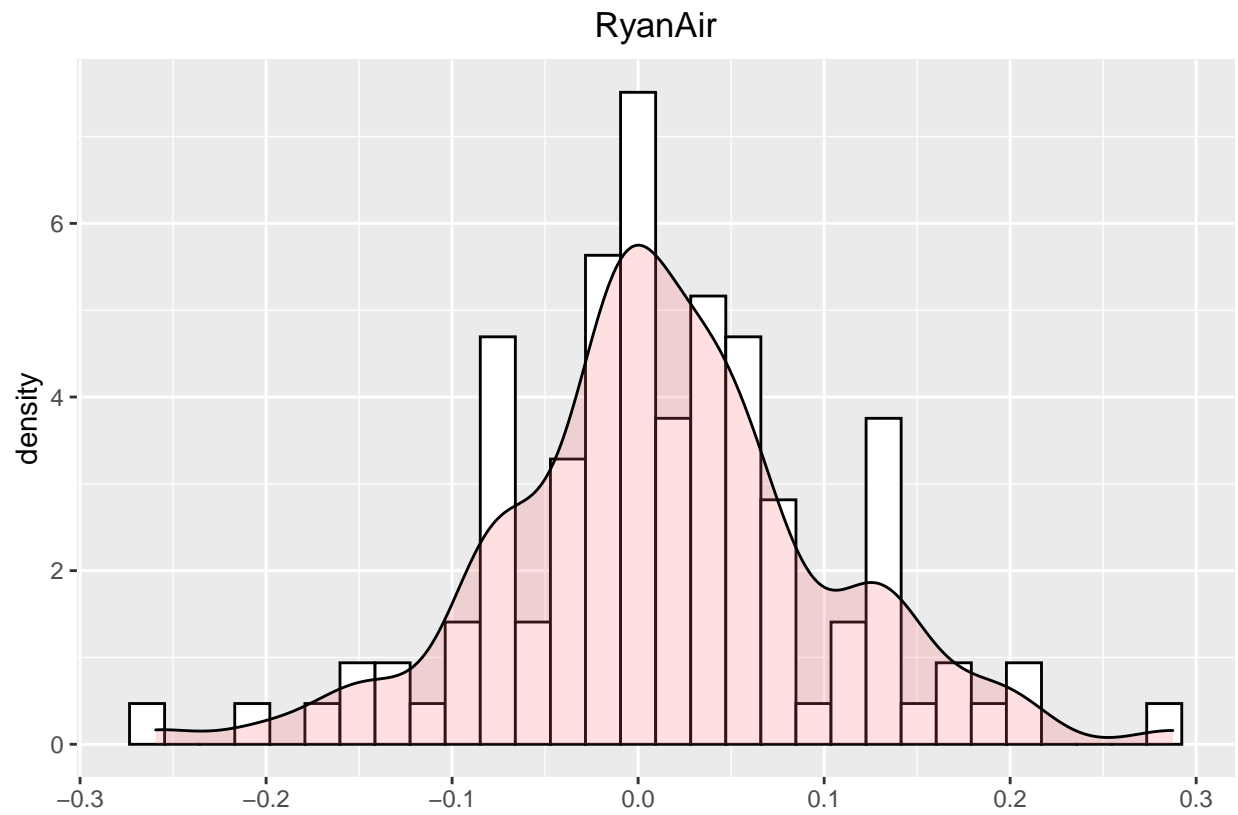
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

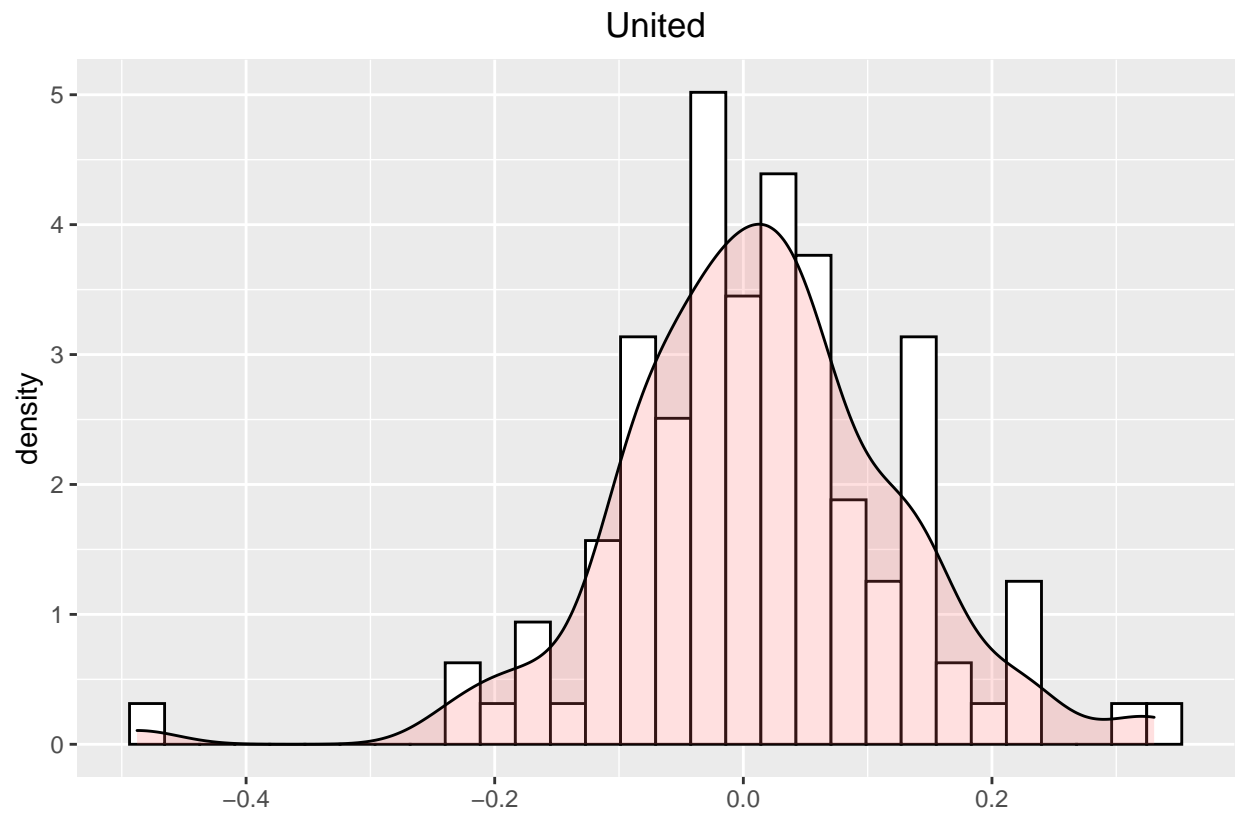


```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

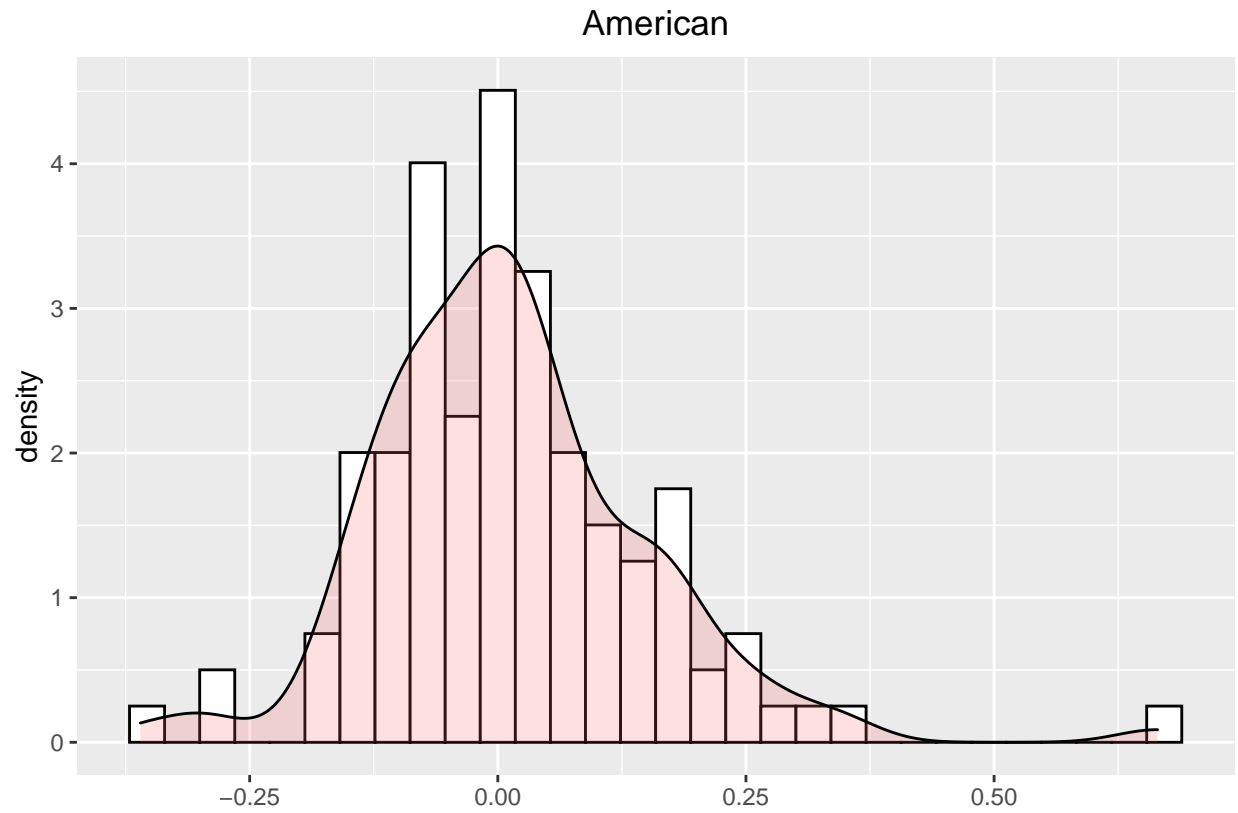


```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

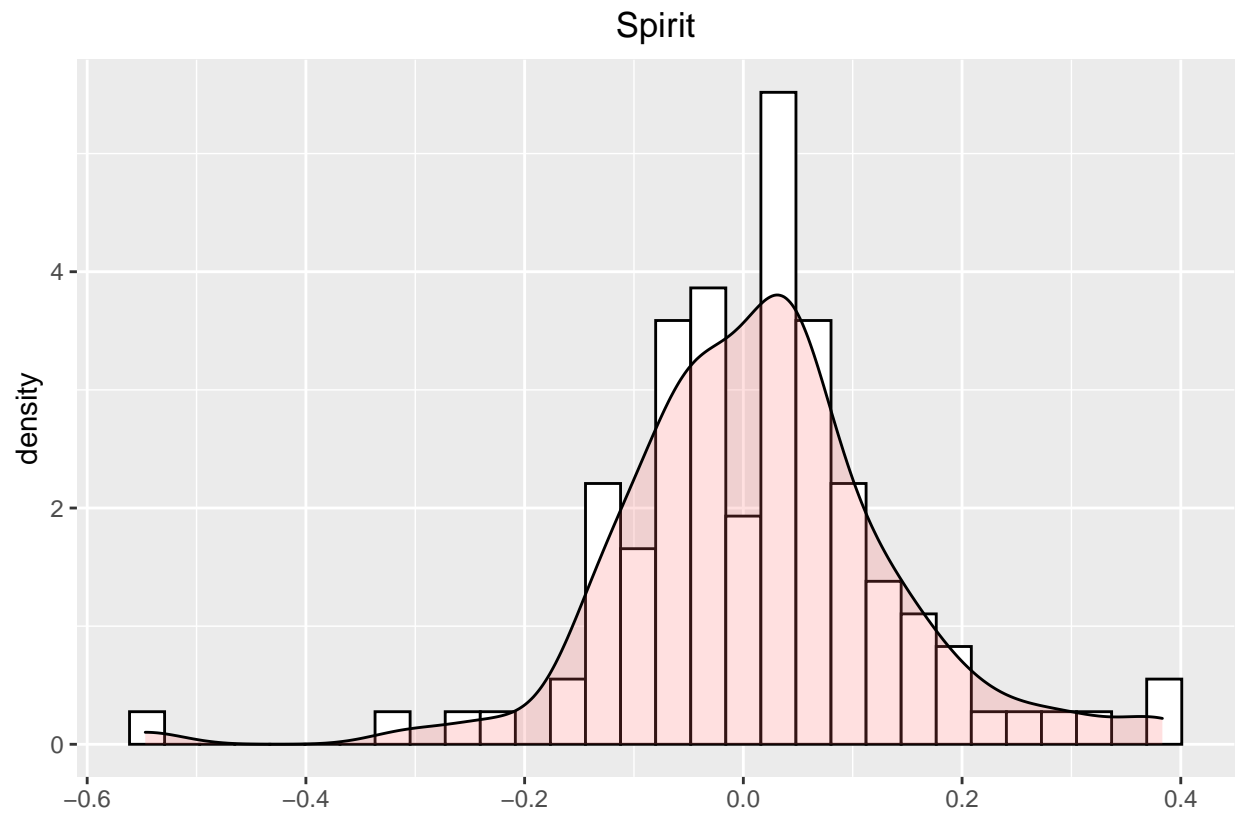




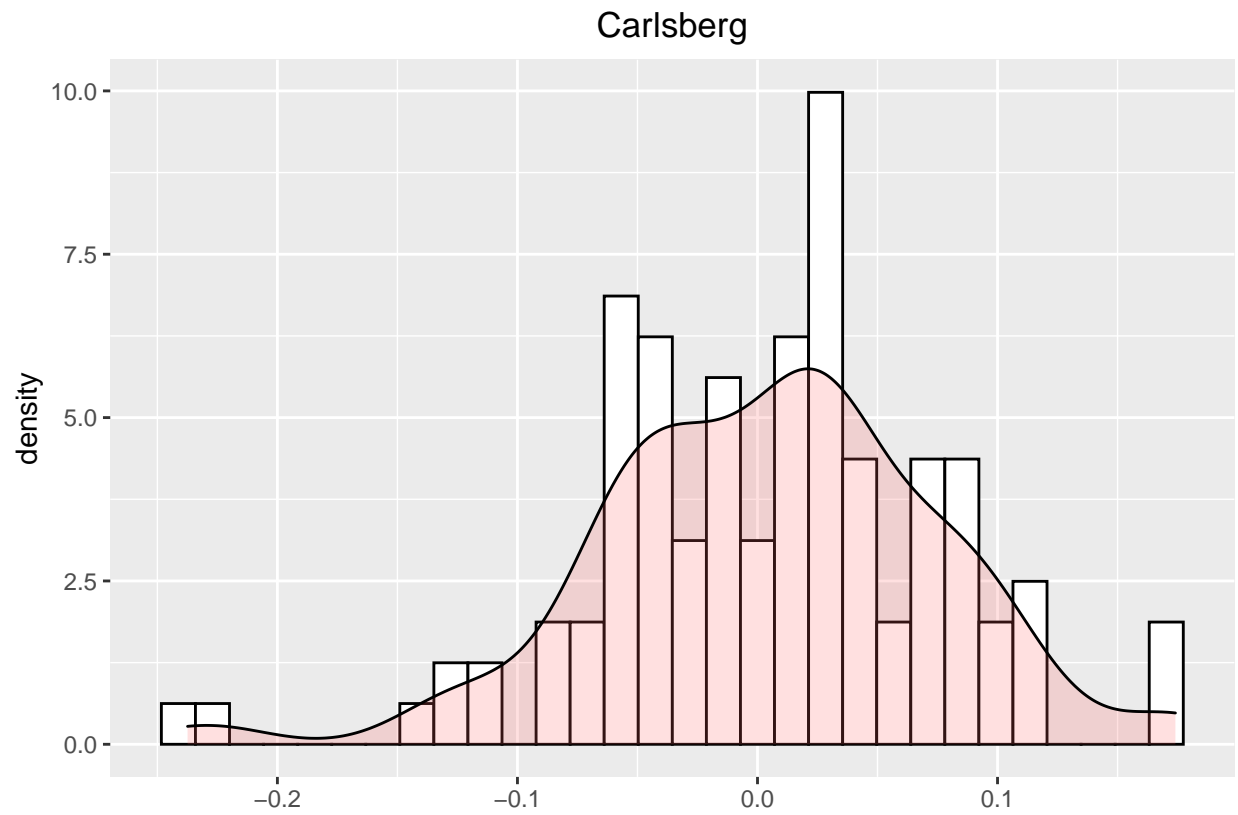
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



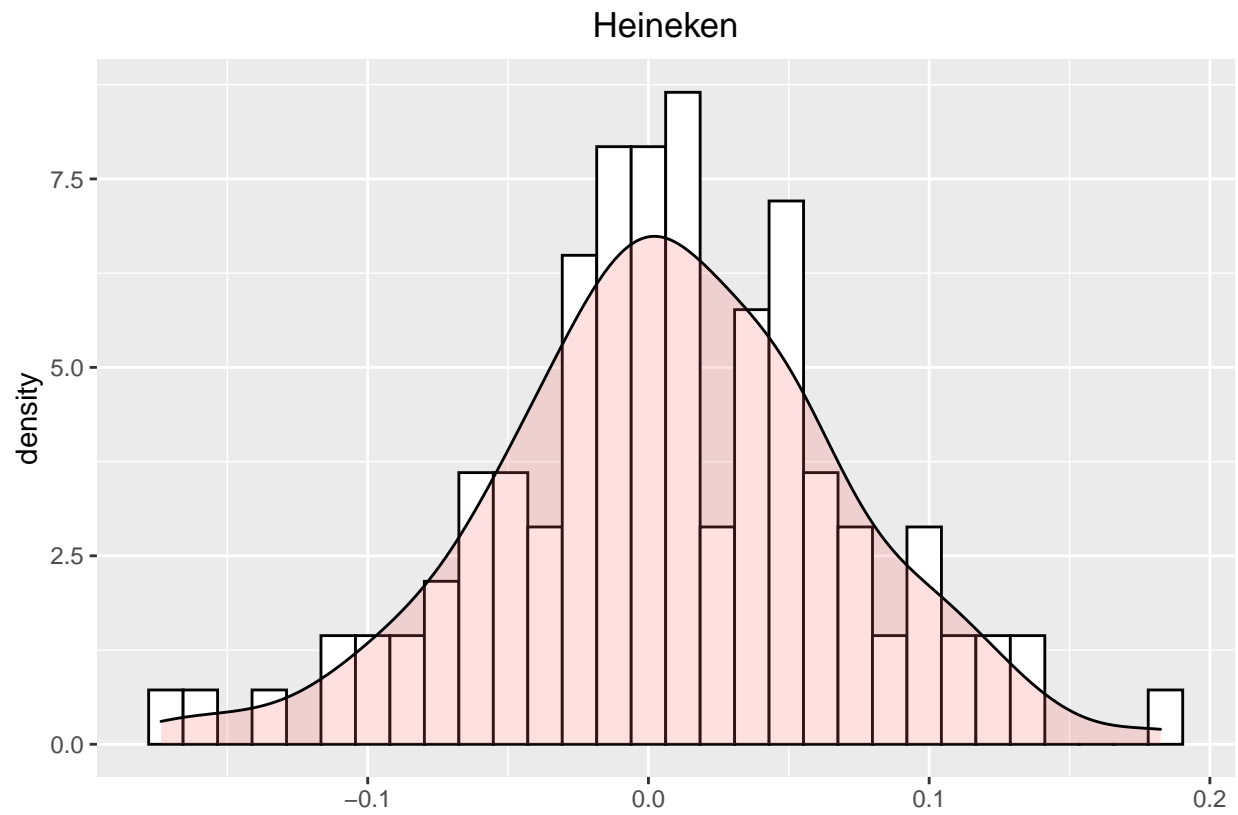
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



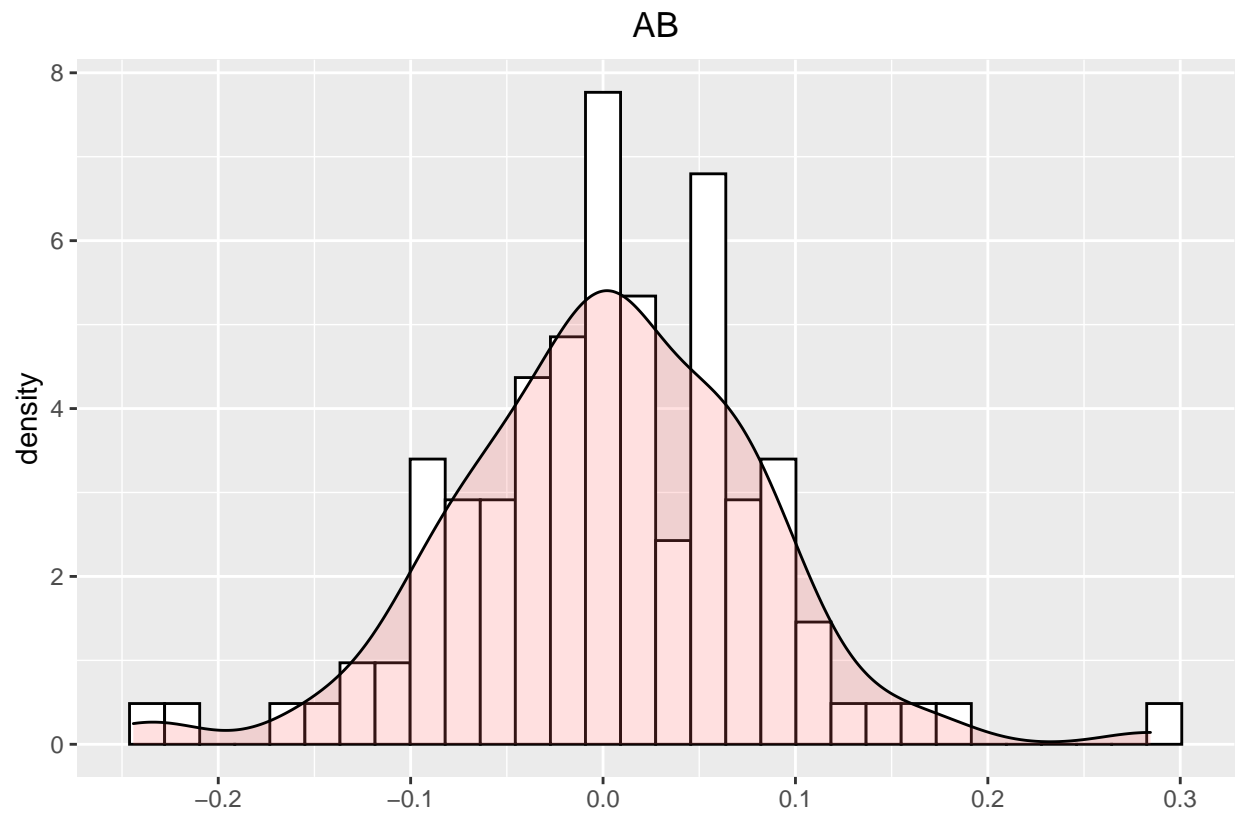
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



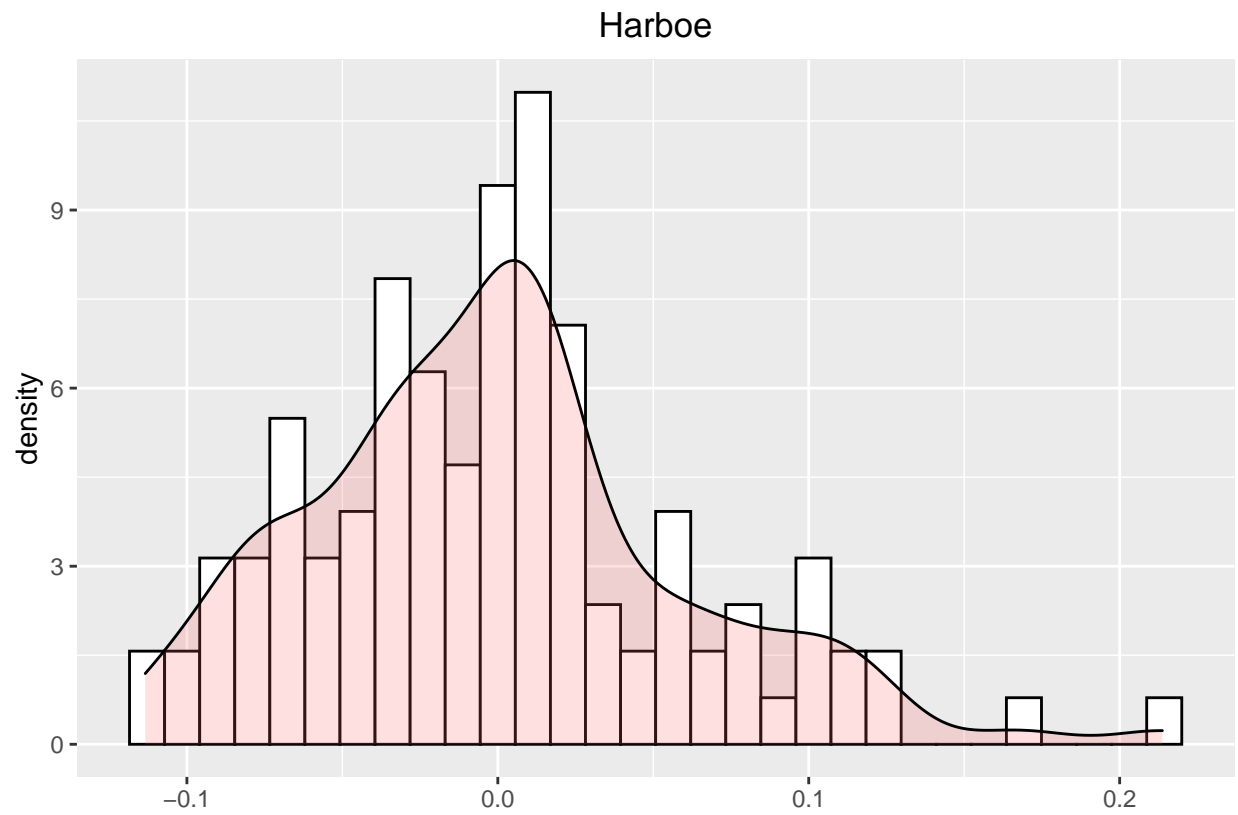
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



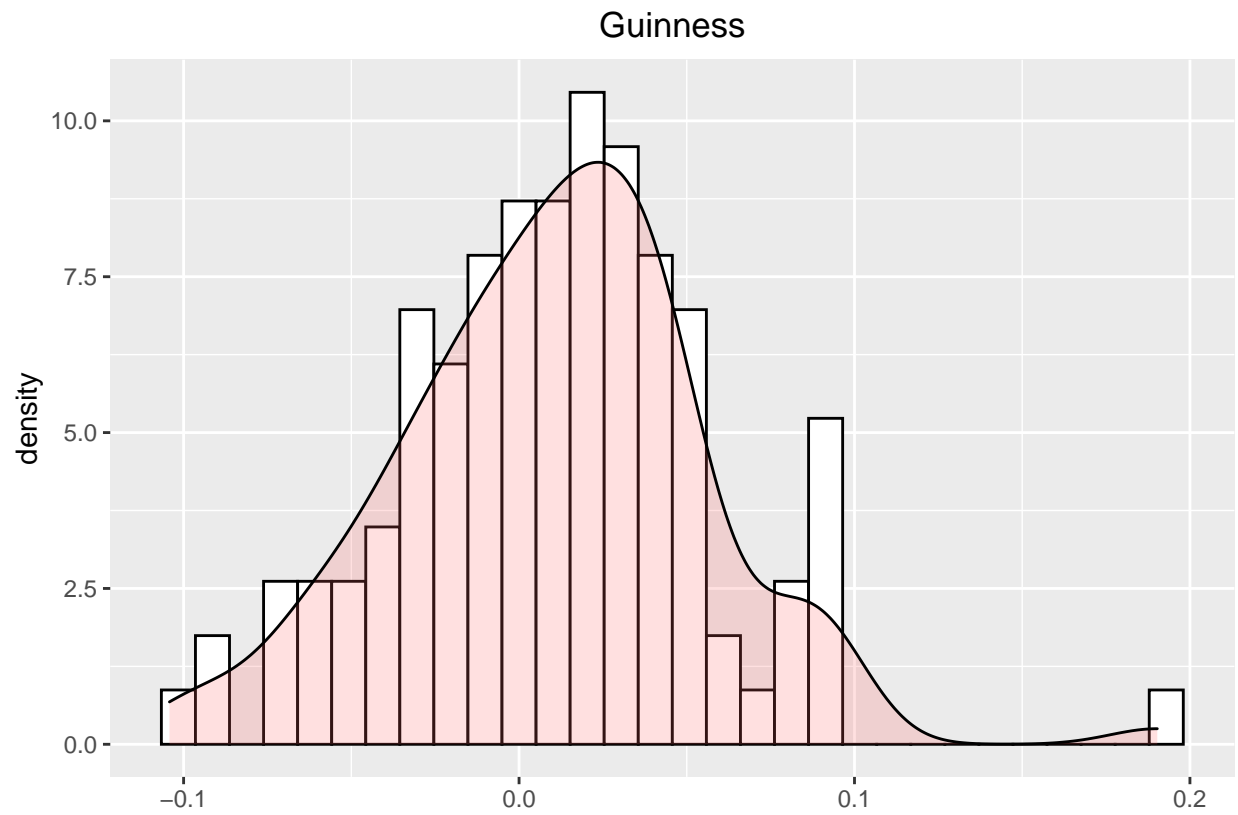
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

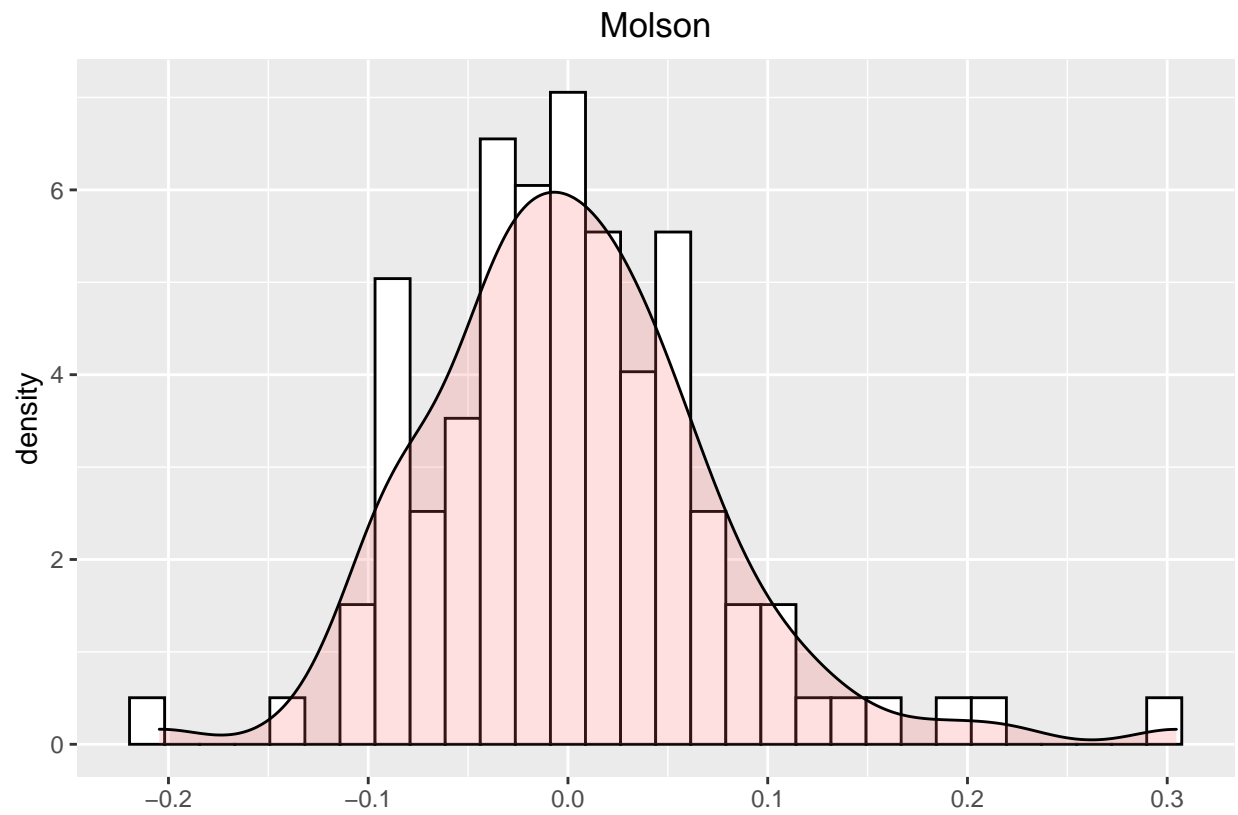


```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

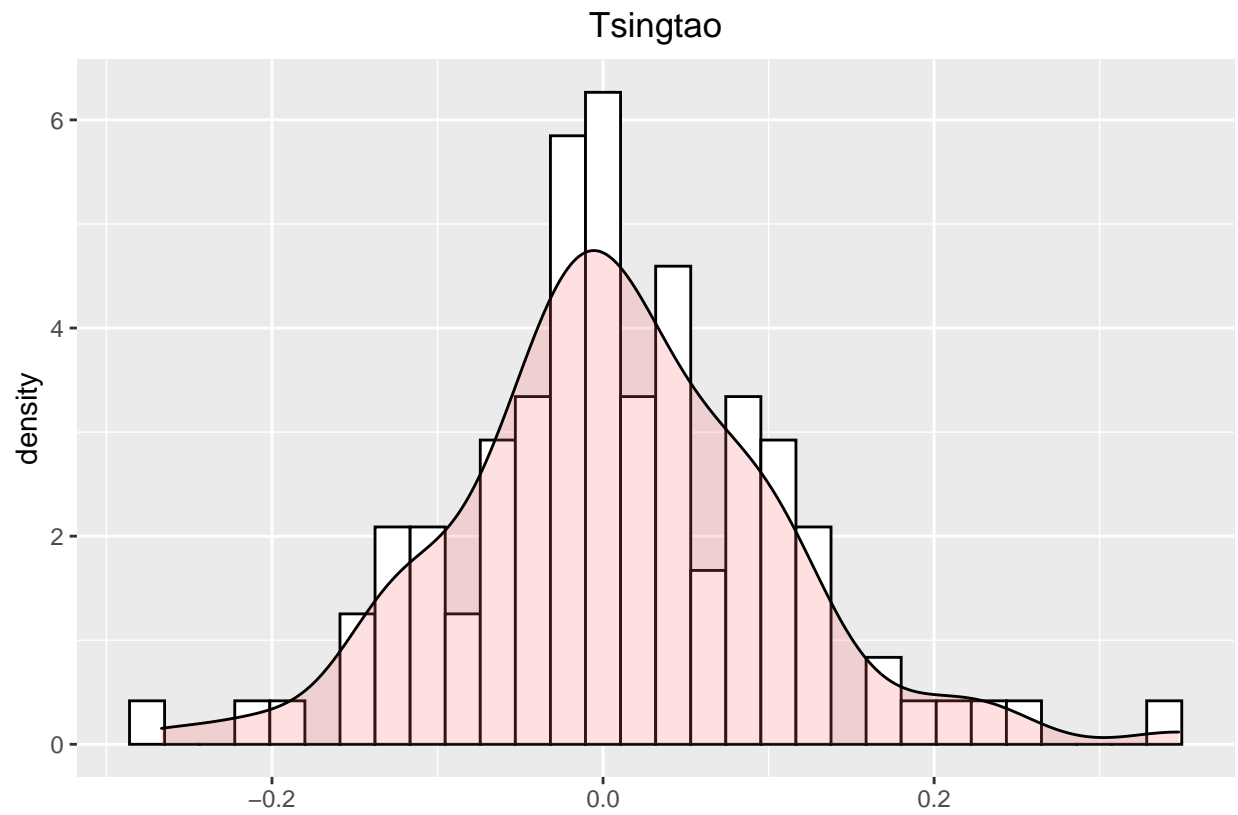


```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

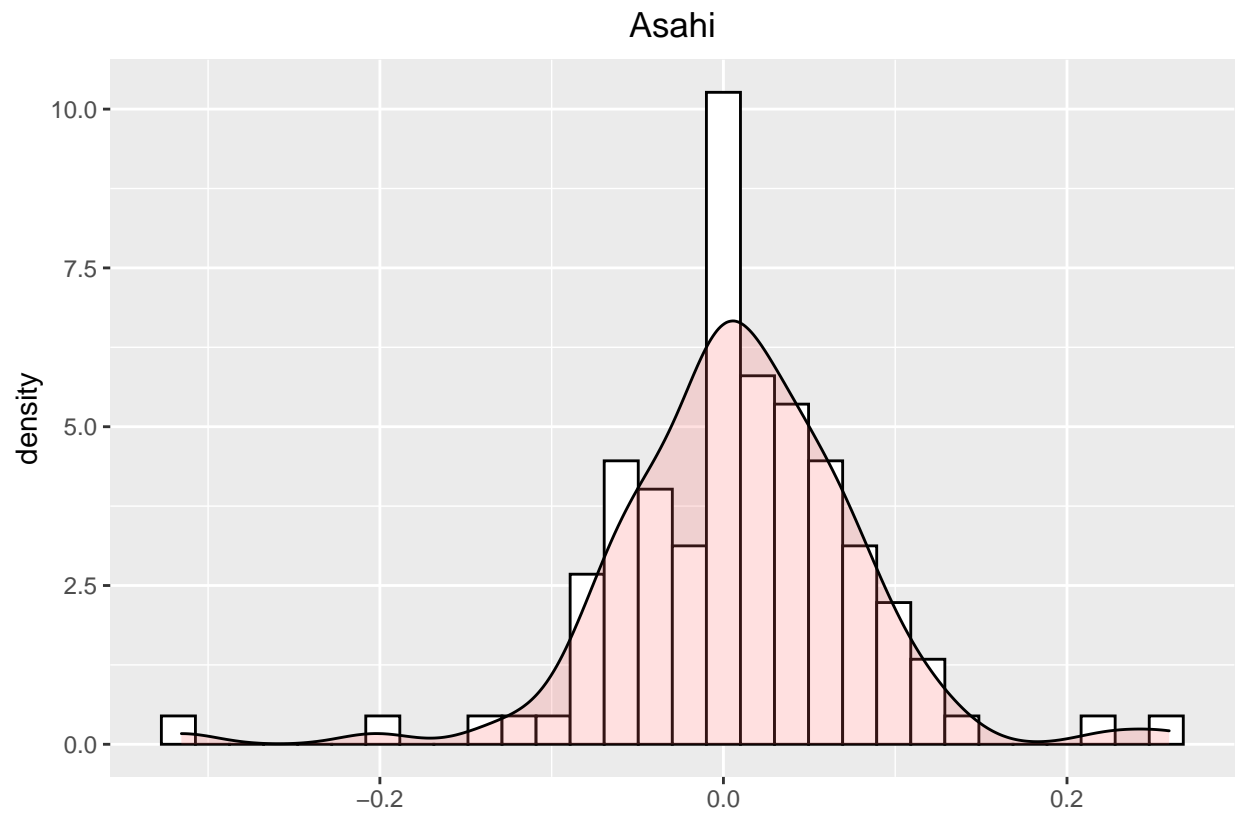




```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

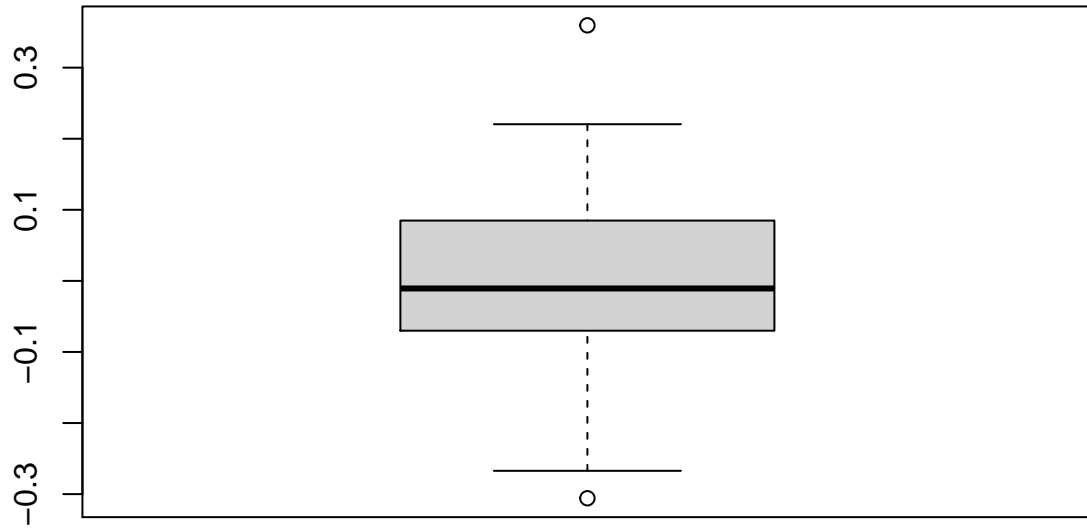


#### 5. Boxplots for each return series

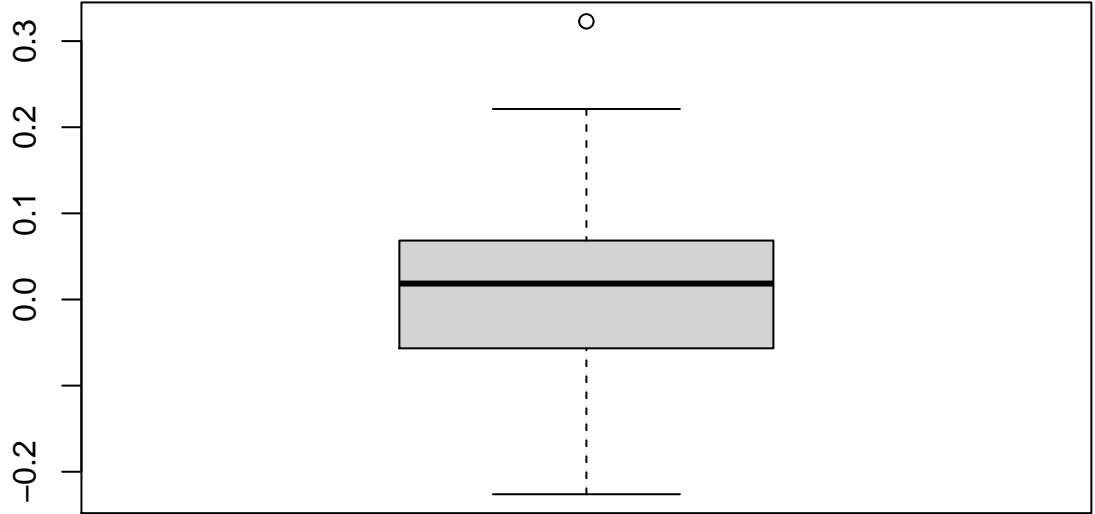
*#individual boxplots*

```
for (i in 1:15)
{
  names <- list(stock_names)
  boxplot(returnsIVV[,i+1], xlab="", main = names[[1]][i])
}
```

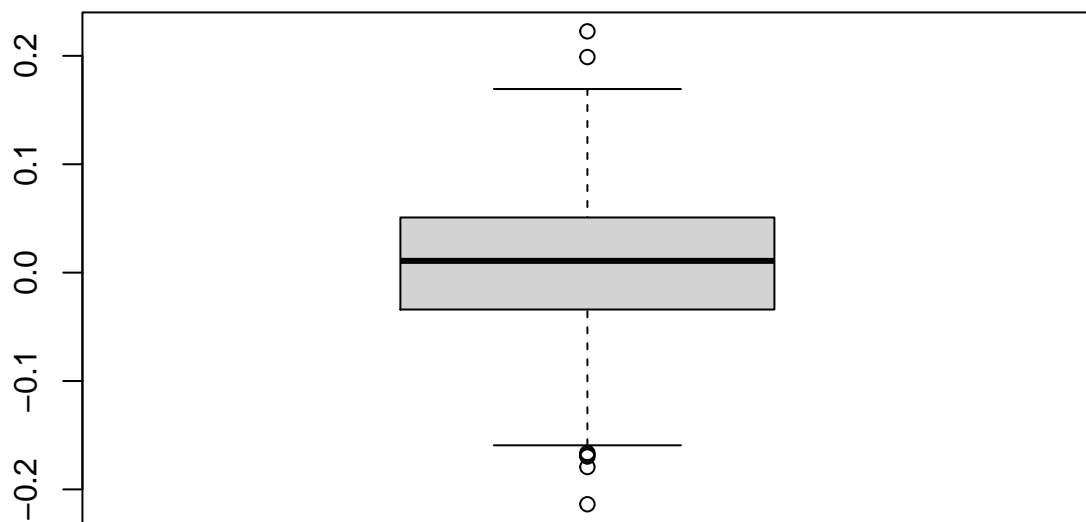
## Lufthansa



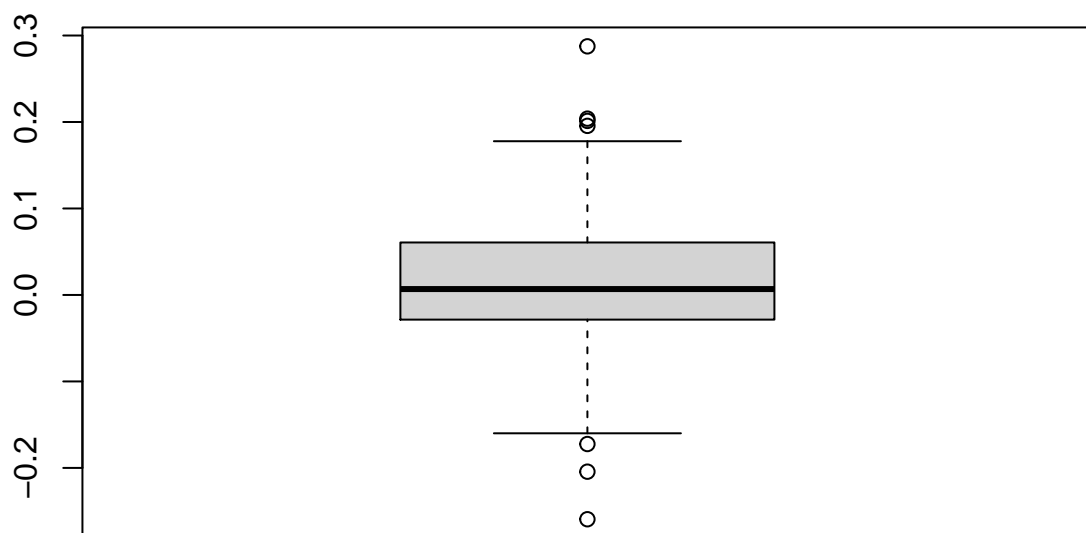
**Southwest**



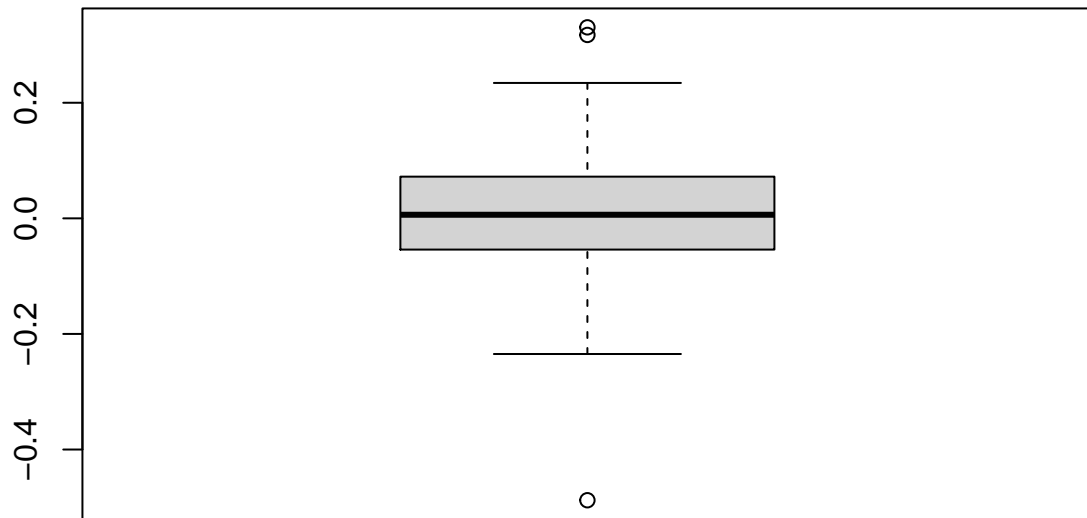
## EasyJet



## RyanAir

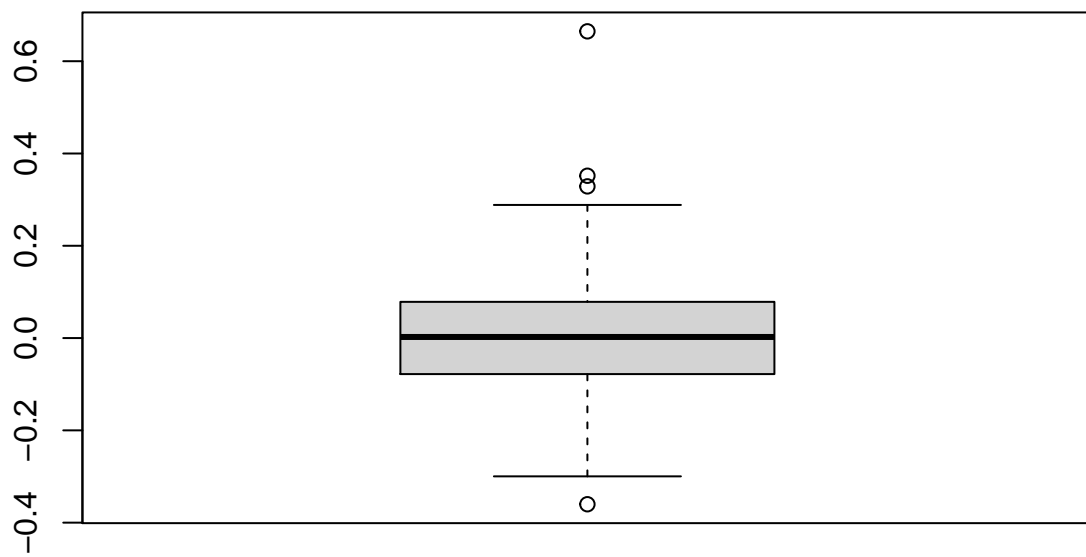


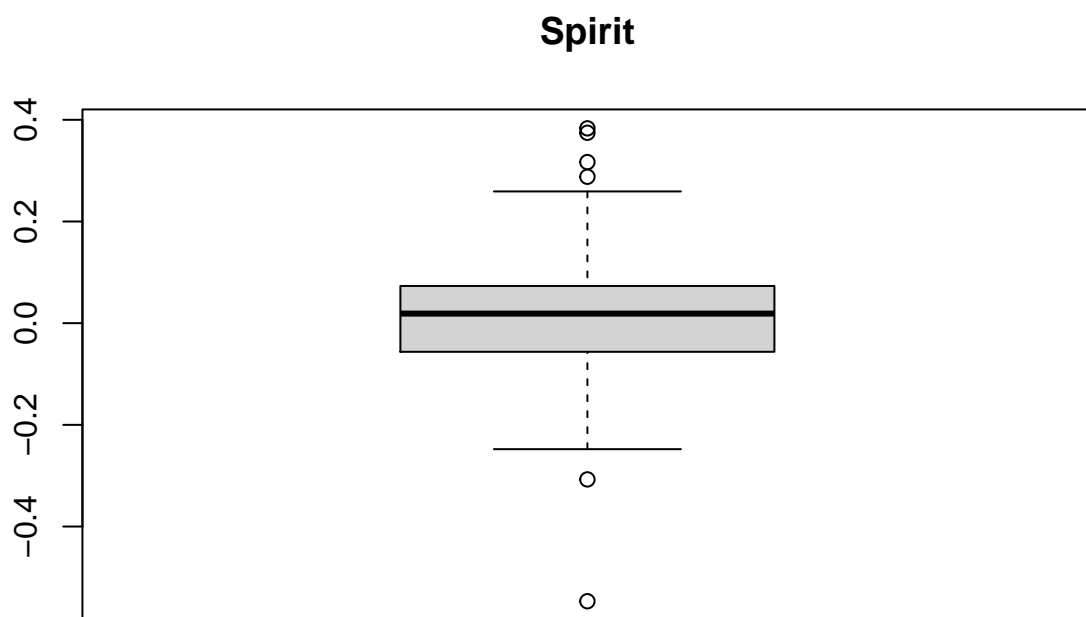
## United



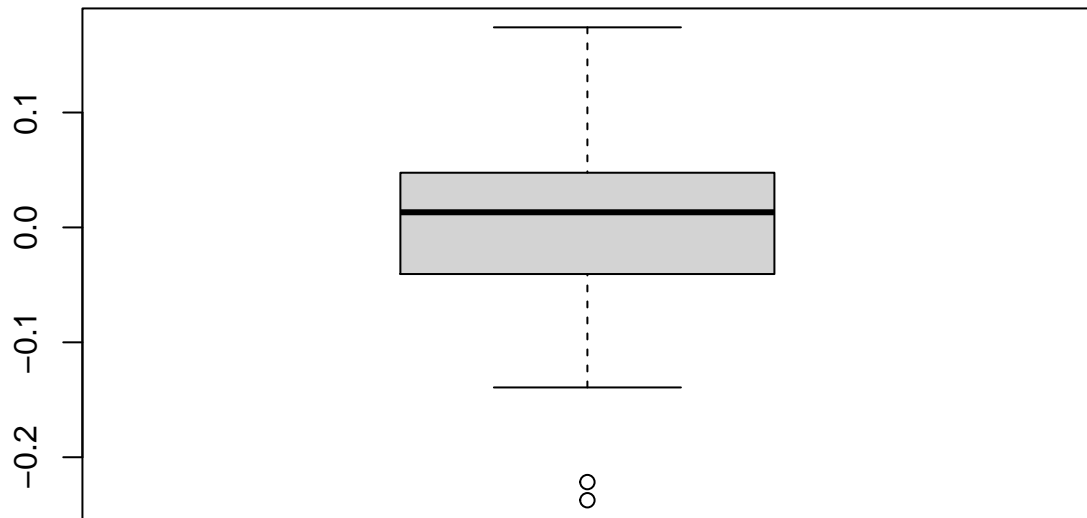


## American

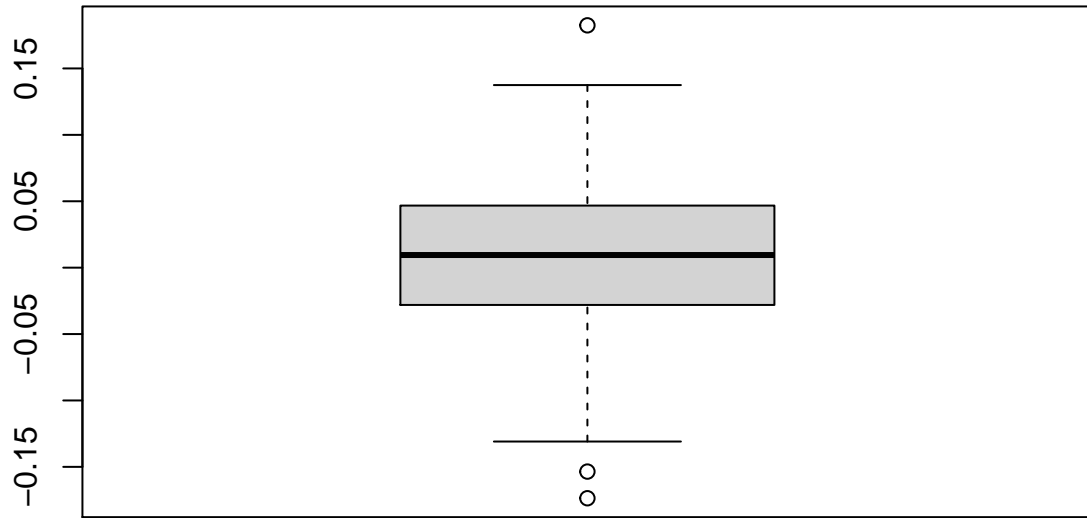


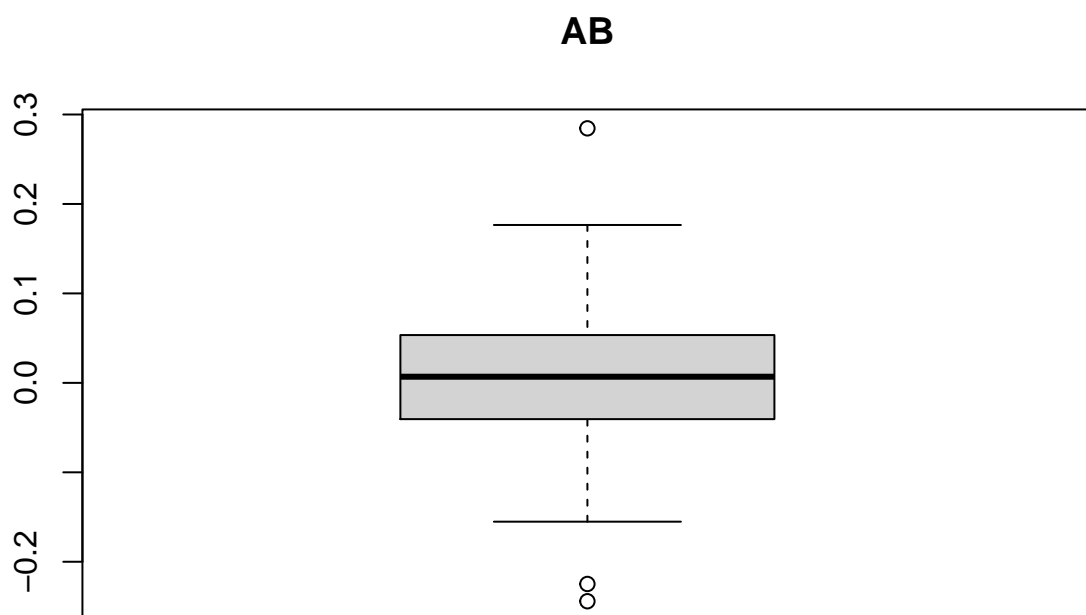


## Carlsberg

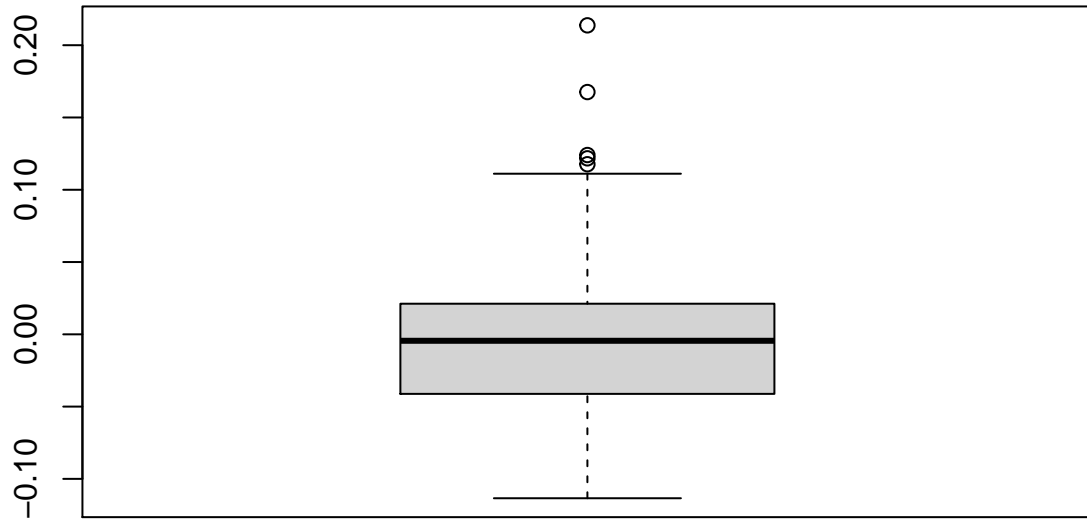


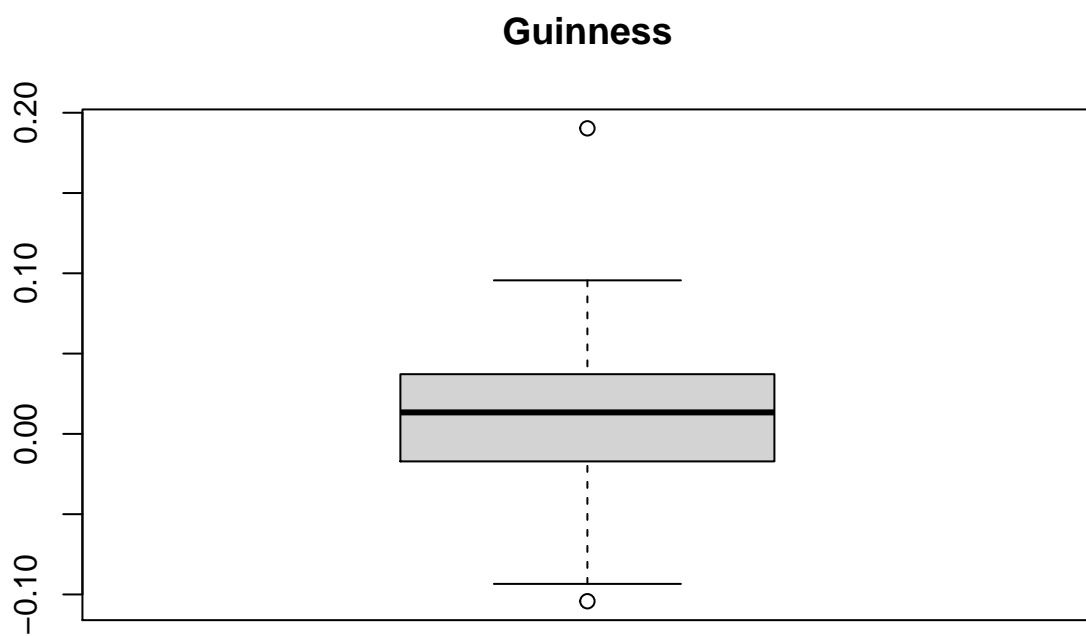
## Heineken



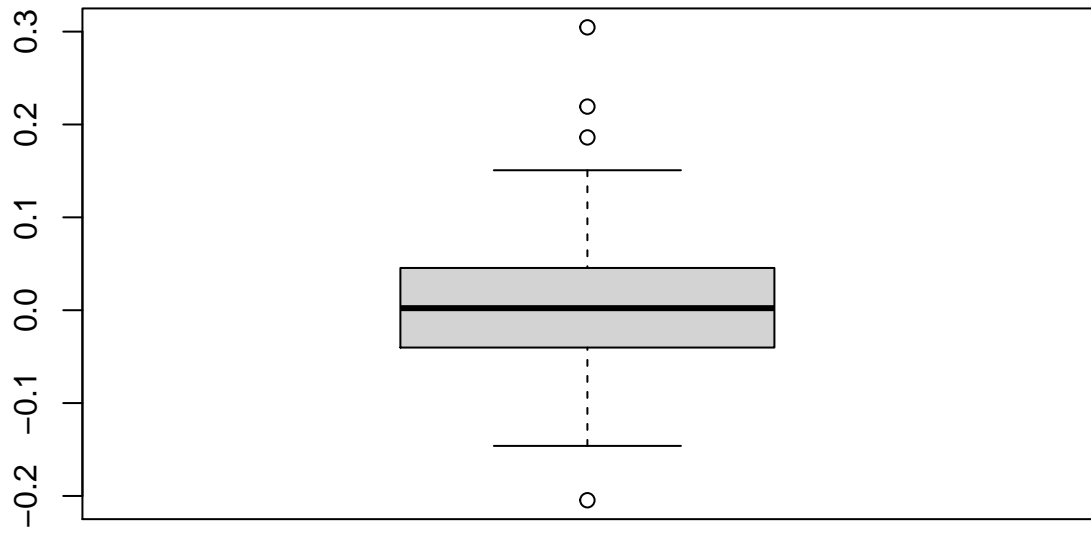


## Harboe



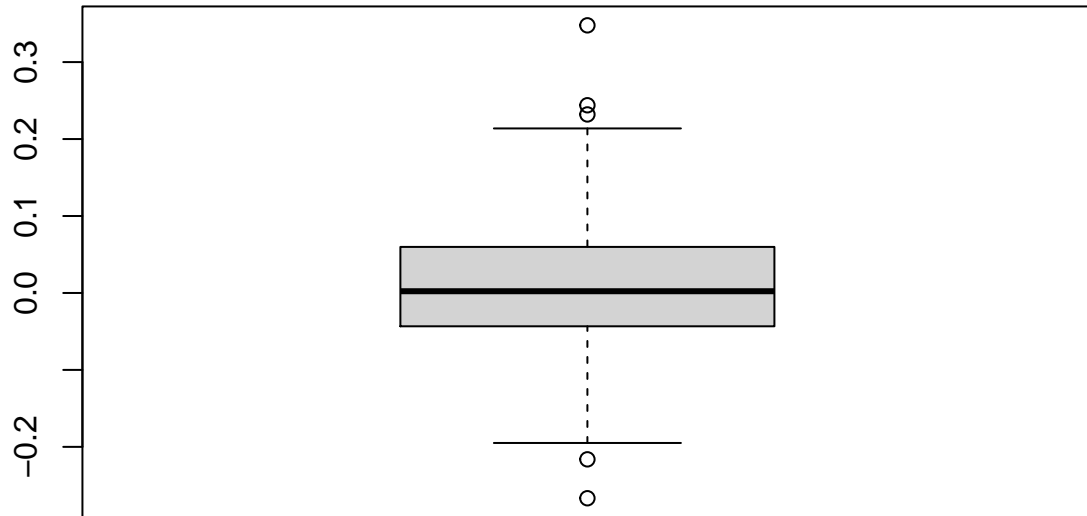


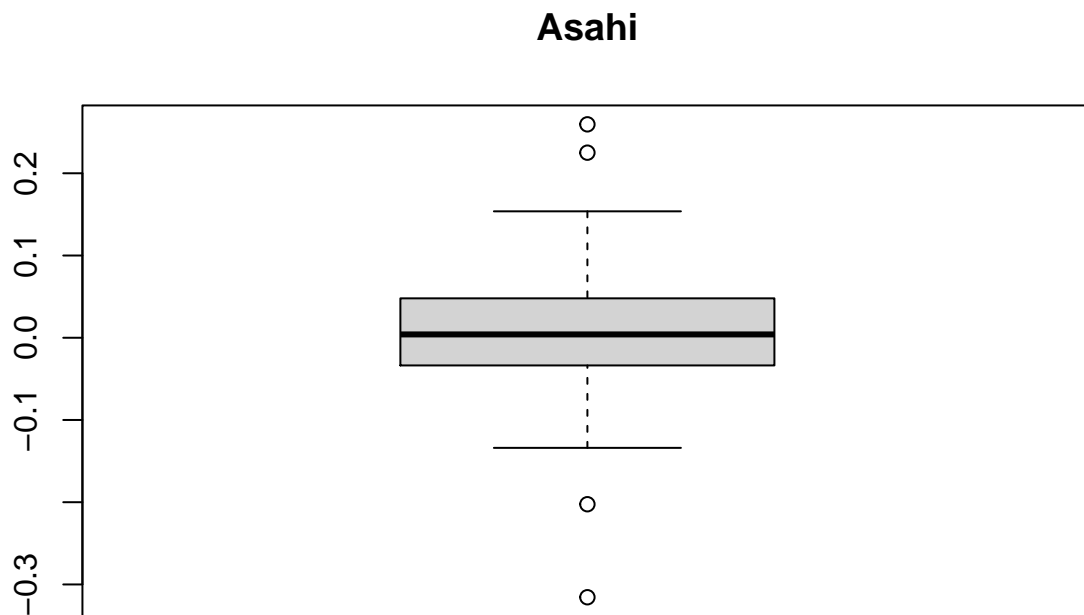
## Molson





## Tsingtao





```
returnsbox <- returnsIVV  
colnames(returnsbox)[2:16] <- names[[1]]
```

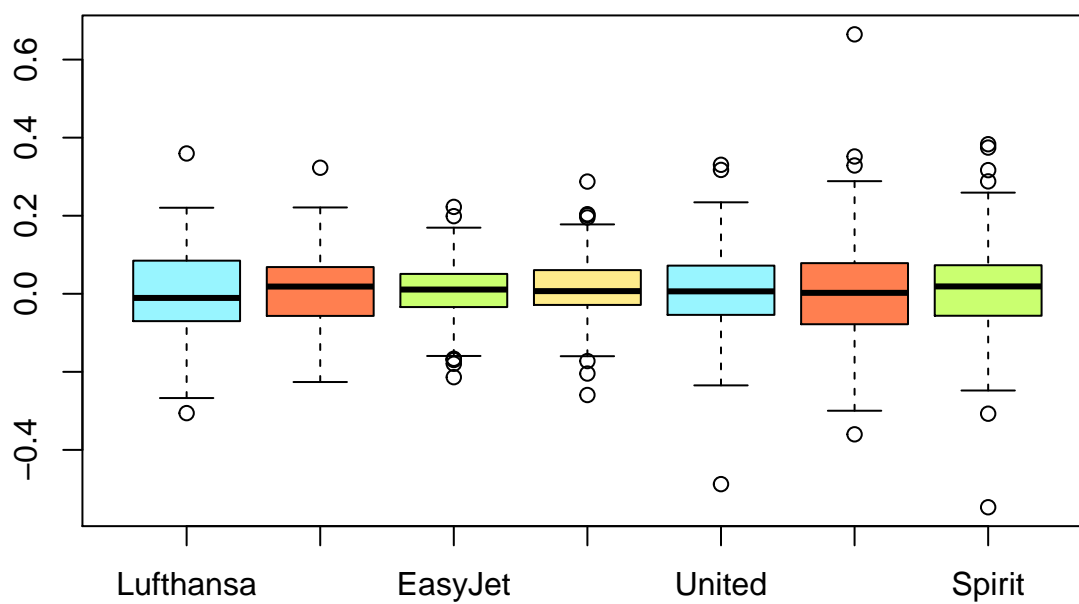
```
## Warning in colnames(returnsbox)[2:16] <- names[[1]]: number of items to replace  
## is not a multiple of replacement length
```

```
colors <- c('cadetblue1', 'coral', 'darkolivegreen1', 'lightgoldenrod1')
```

```
#airlines
```

```
boxplot(returnsbox[,2:8], col = colors, main= "Boxplots of Airlines")
```

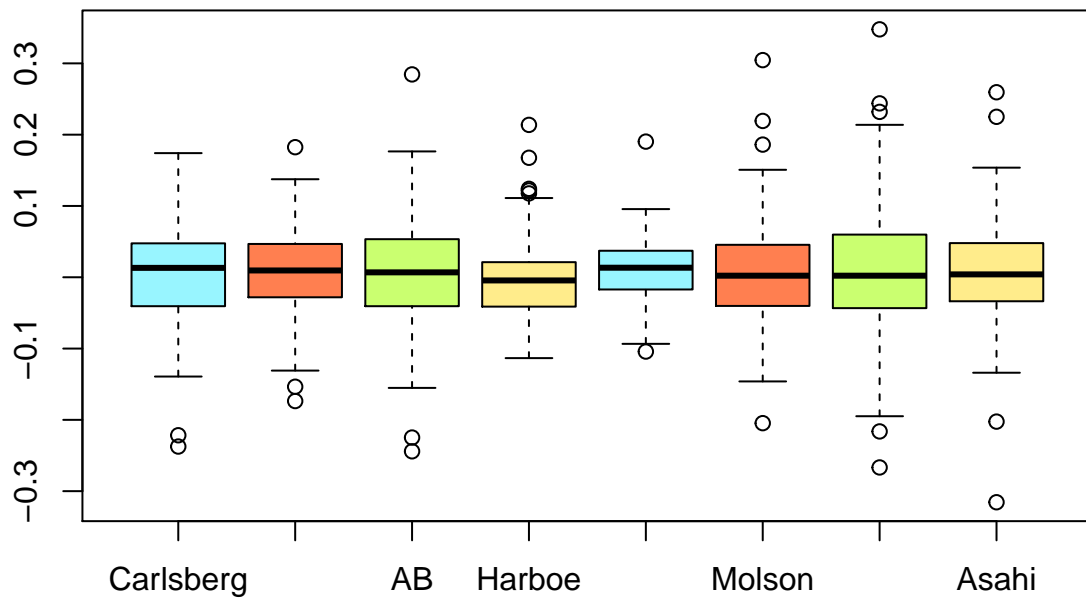
## Boxplots of Airlines



```
#beers
```

```
boxplot(returnsbox[,9:16], col= colors, main = "Boxplots of Beers")
```

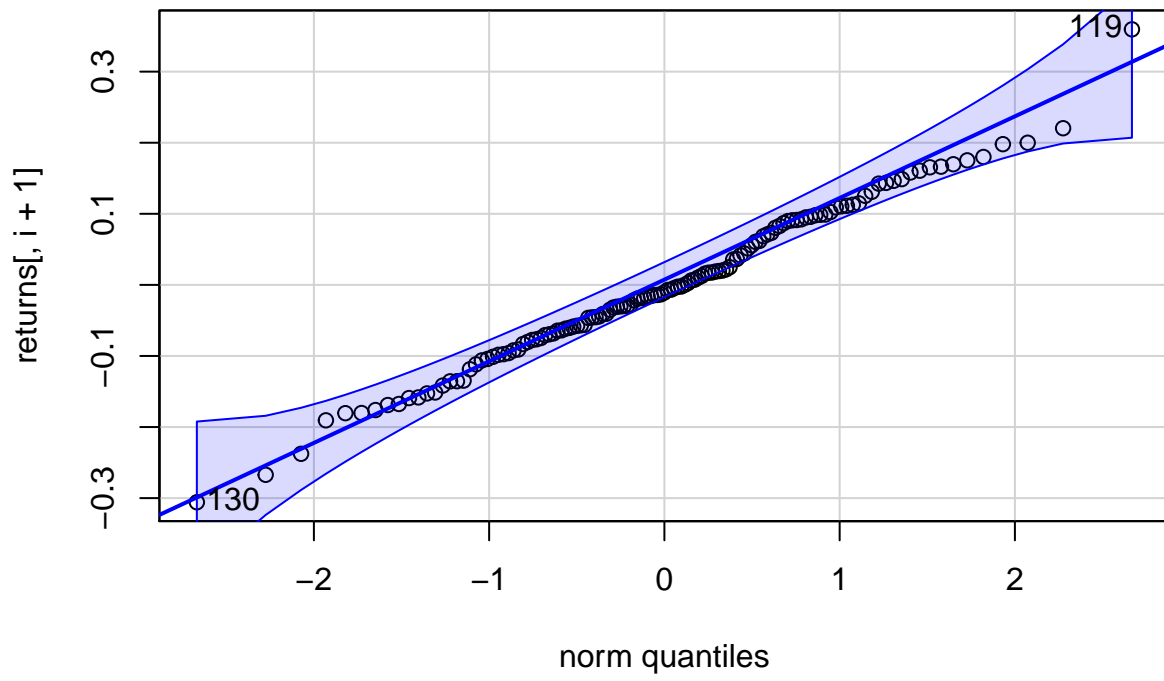
## Boxplots of Beers



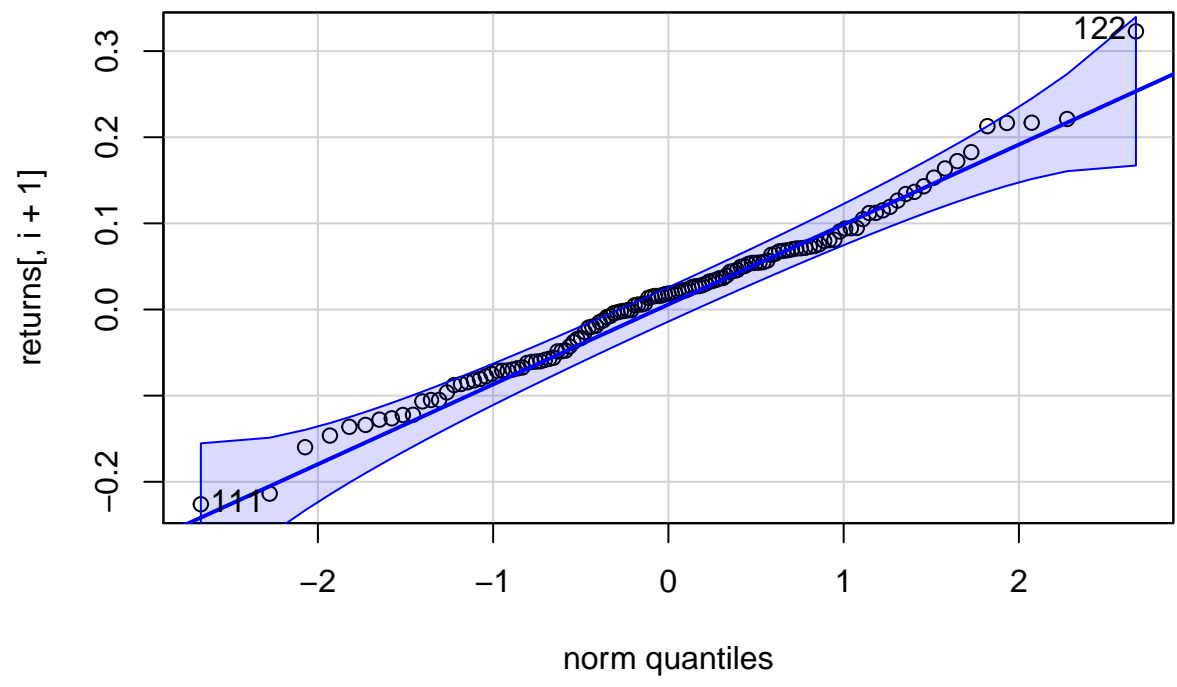
6. qqplots for each return series

```
for (i in 1:15)
{
  qqPlot(returns[,i+1], main = names[[1]][i])
}
```

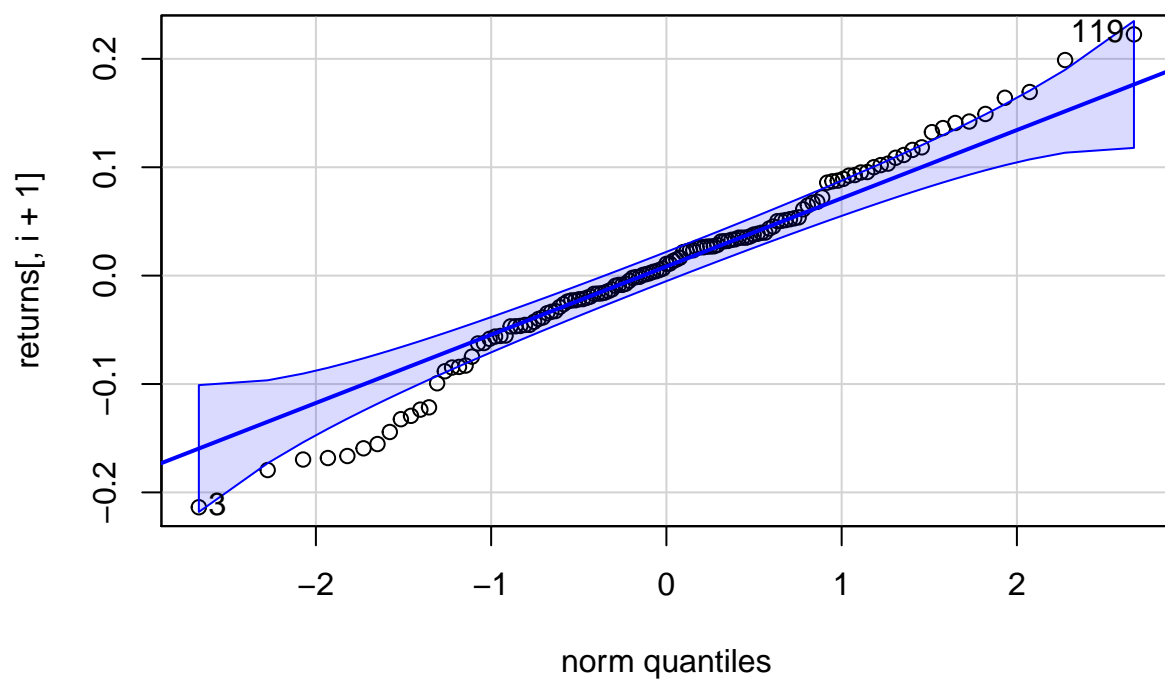
## Lufthansa



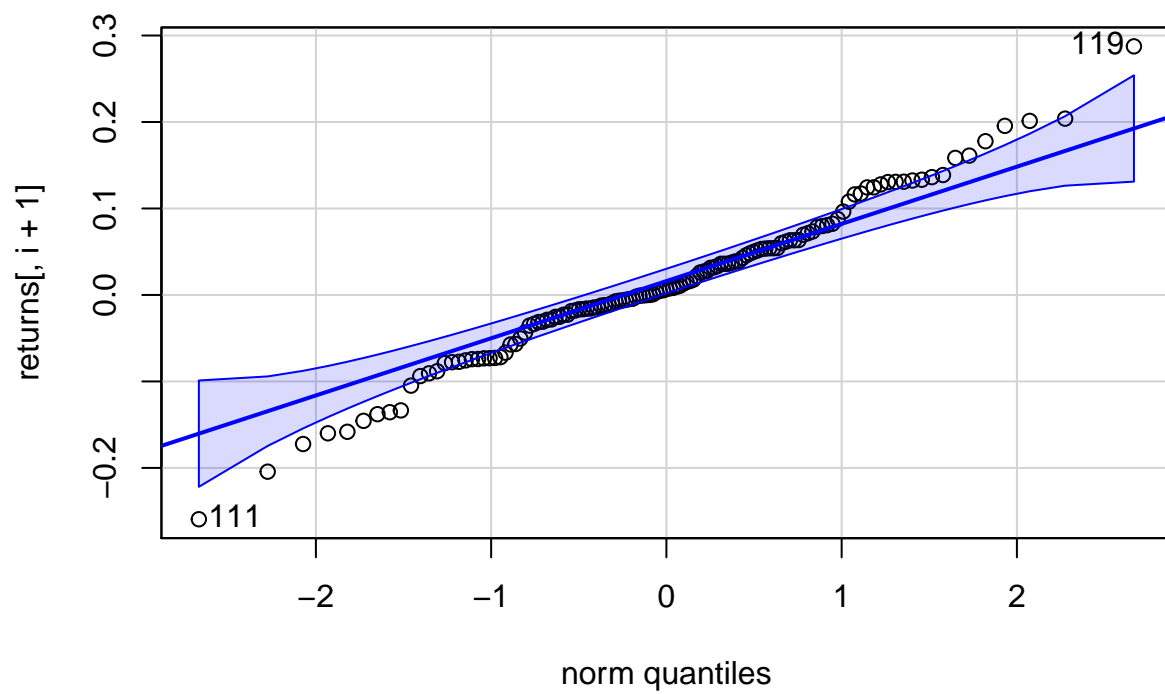
Southwest



## EasyJet

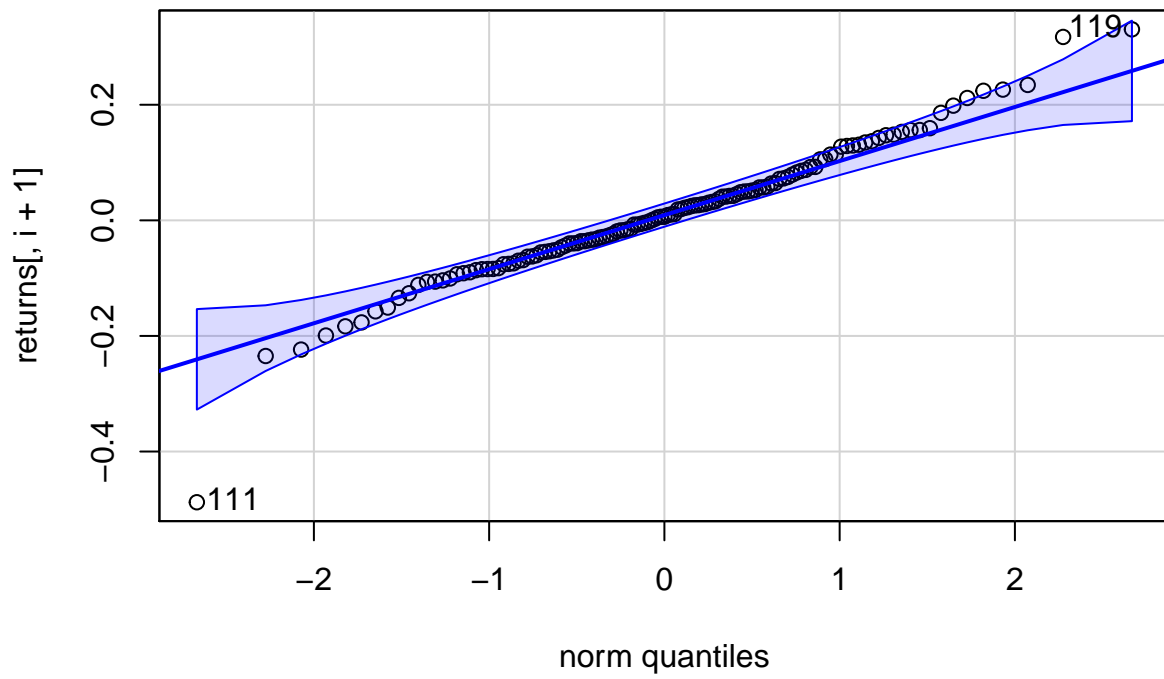


## RyanAir

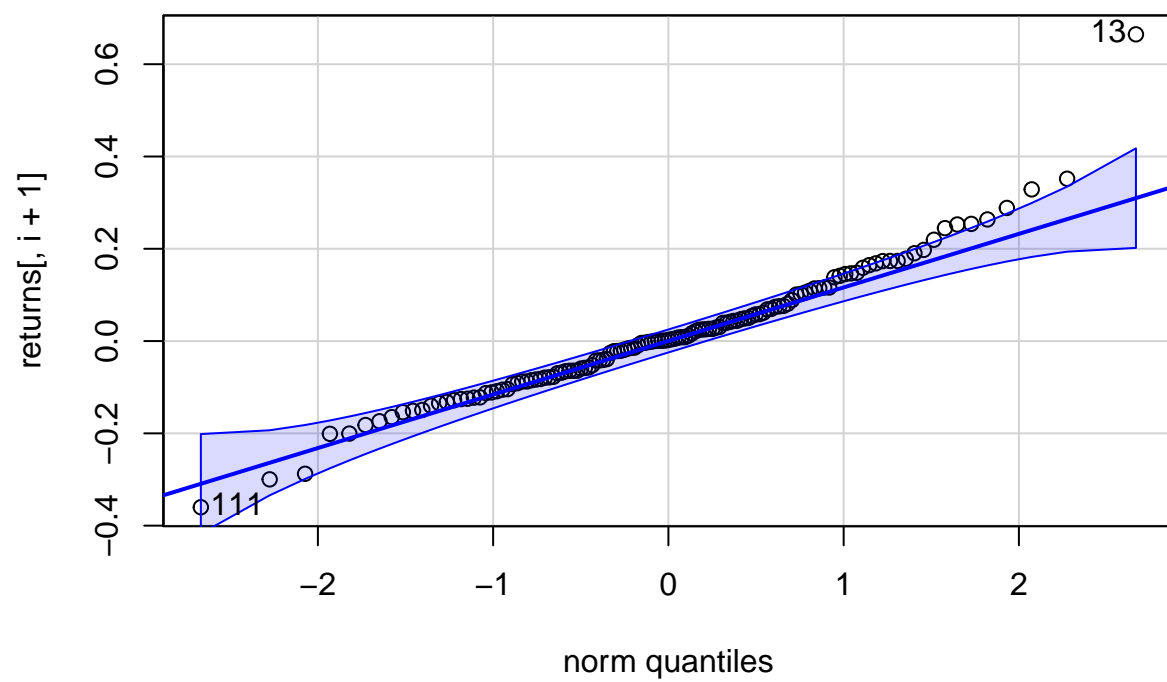




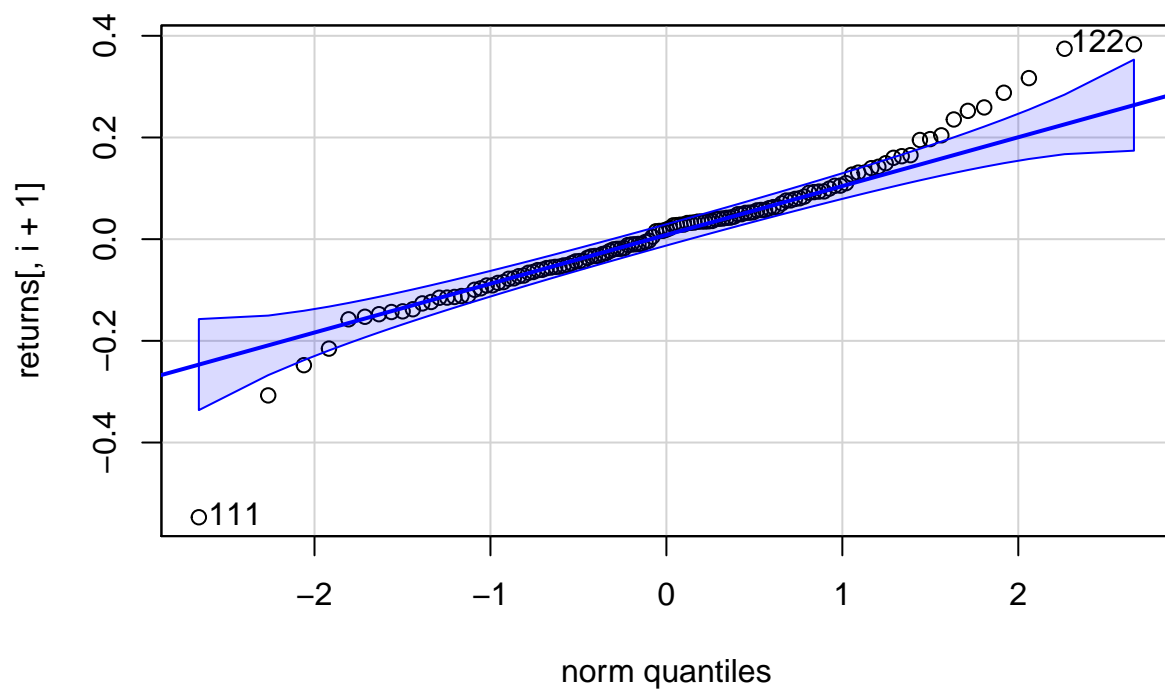
# United



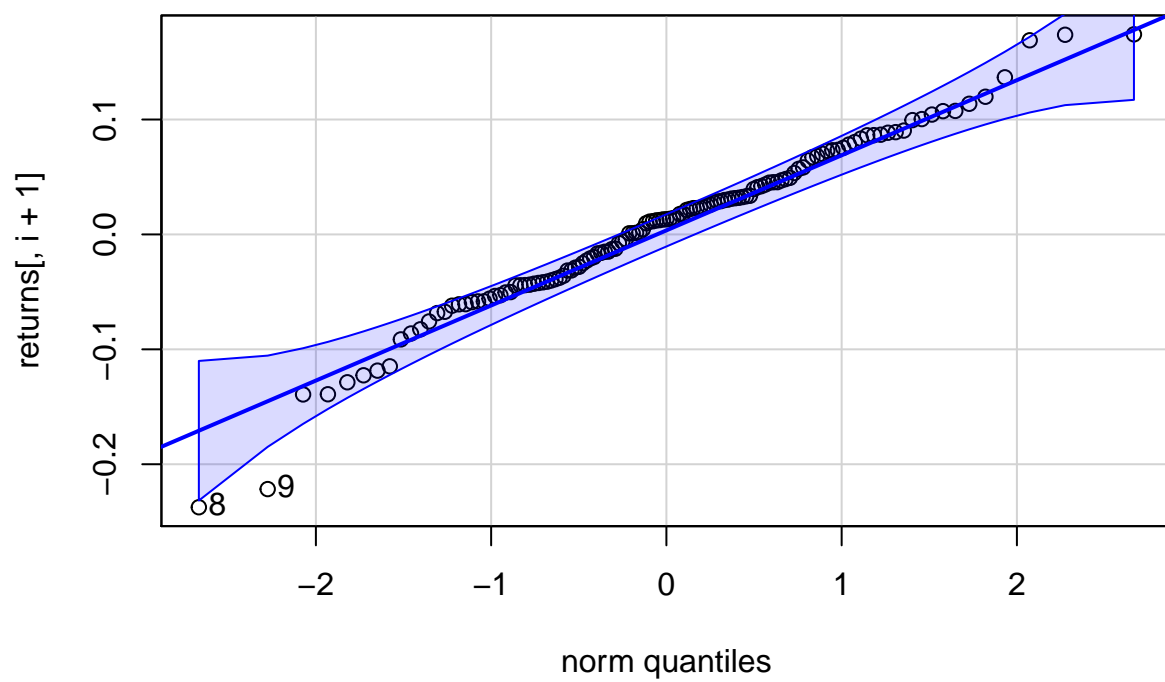
# American



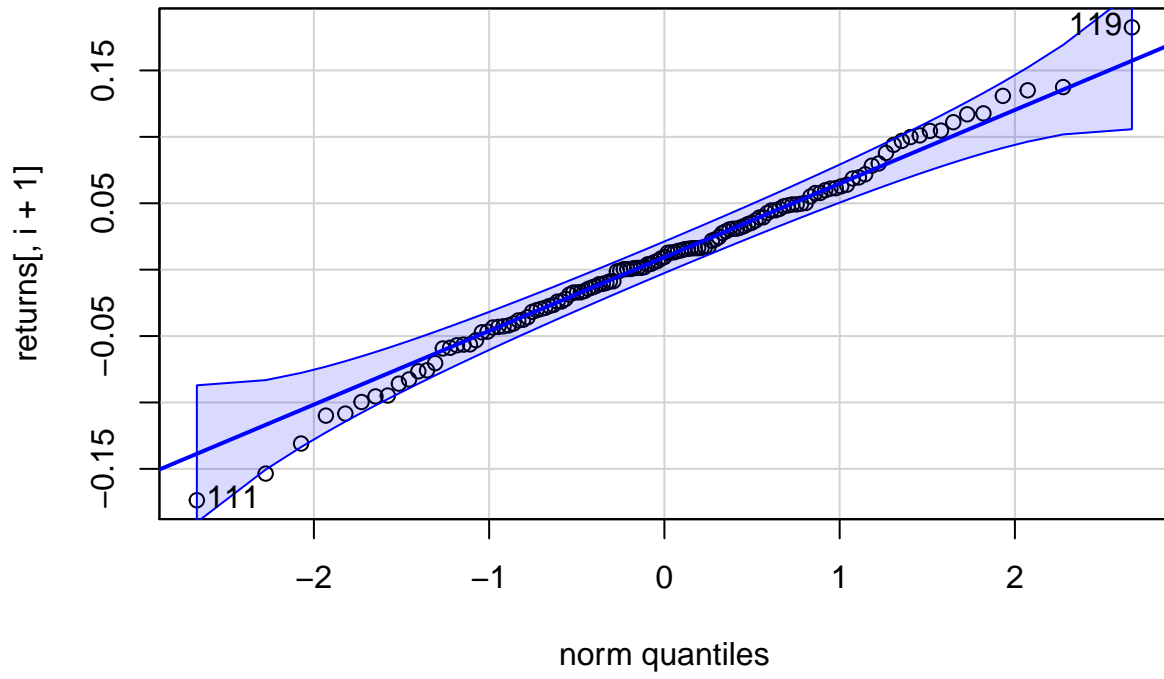
## Spirit



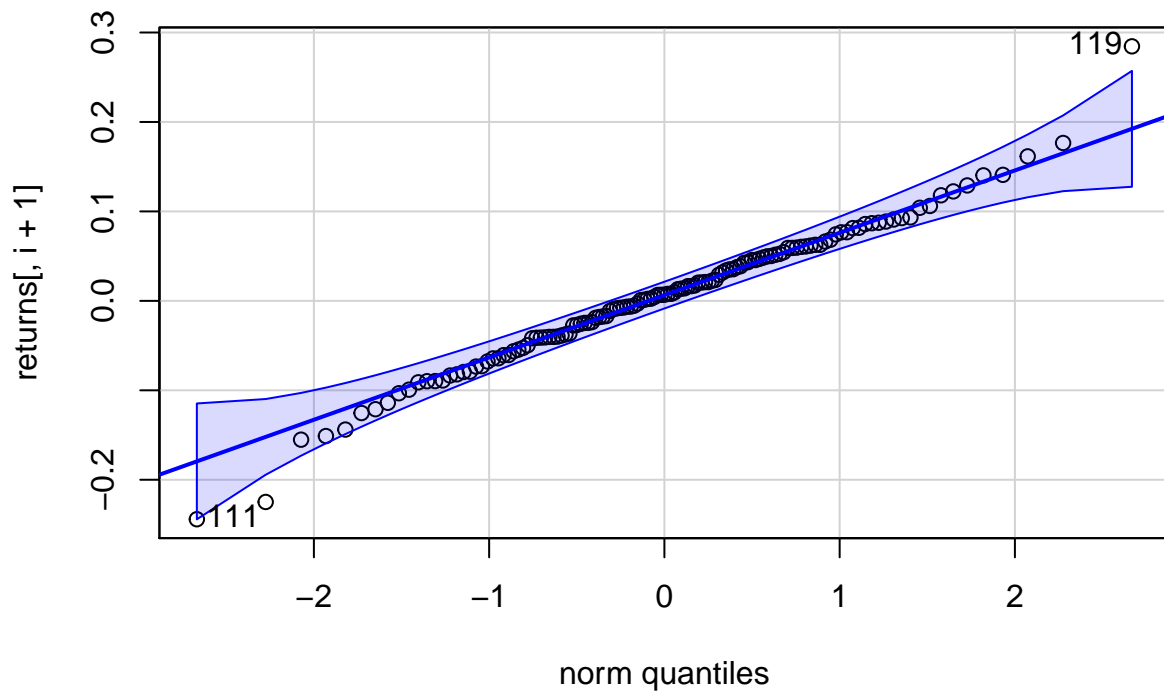
# Carlsberg



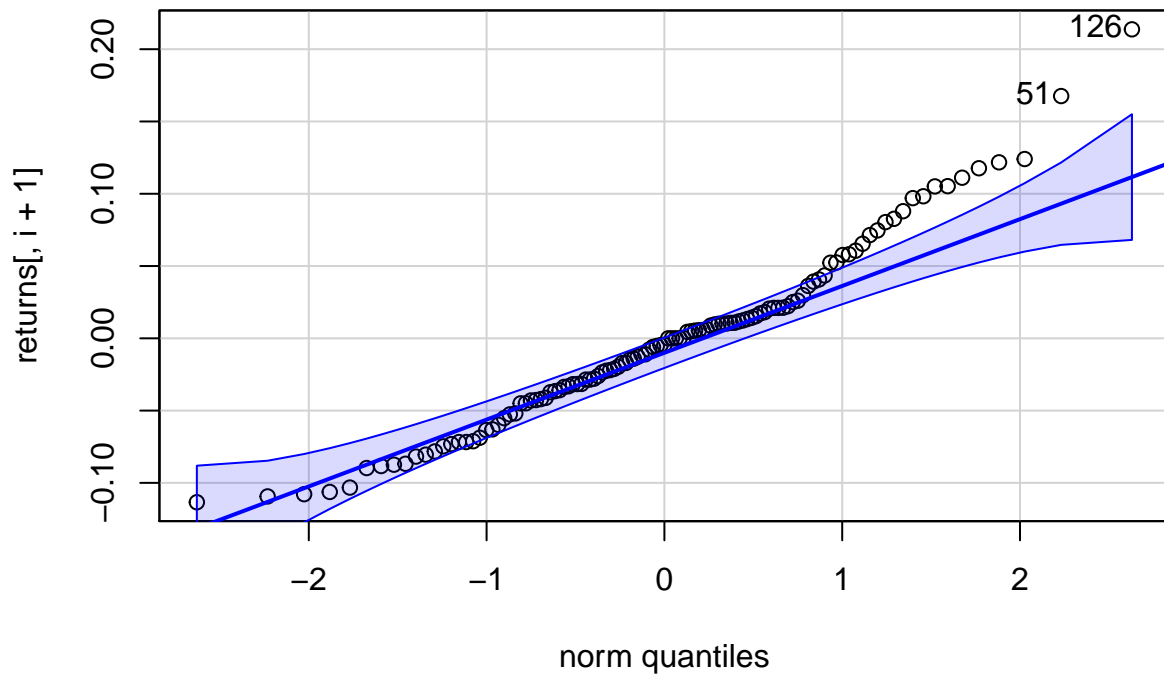
## Heineken



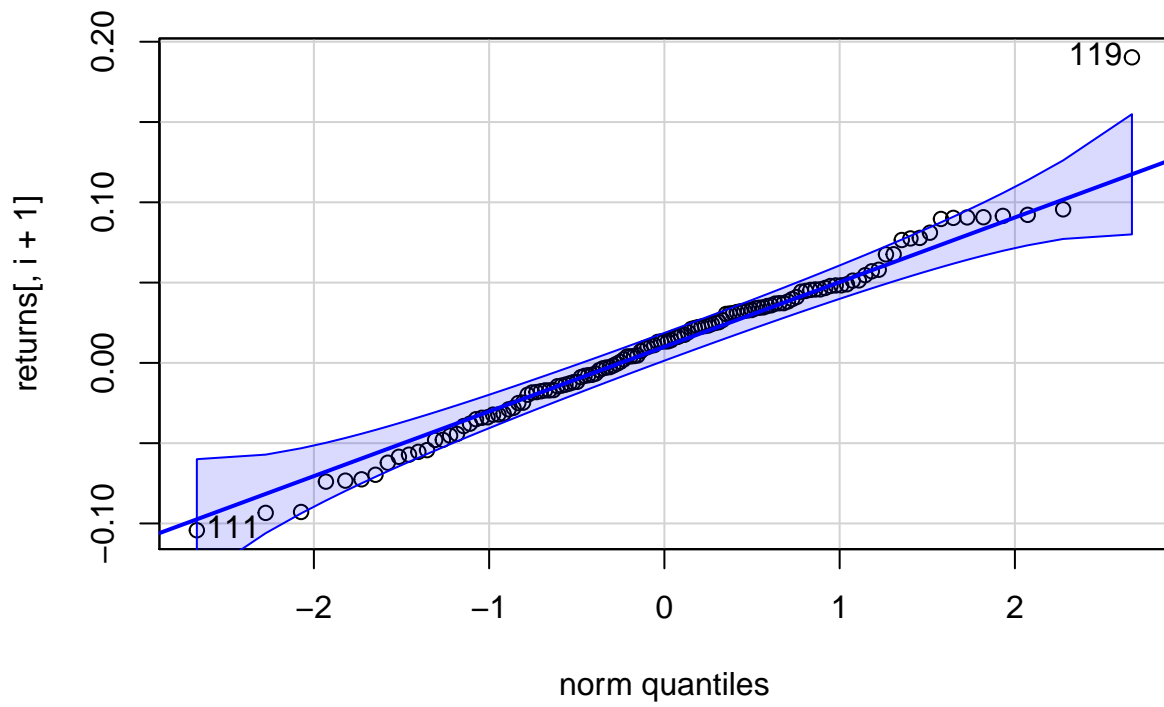
AB



## Harboe

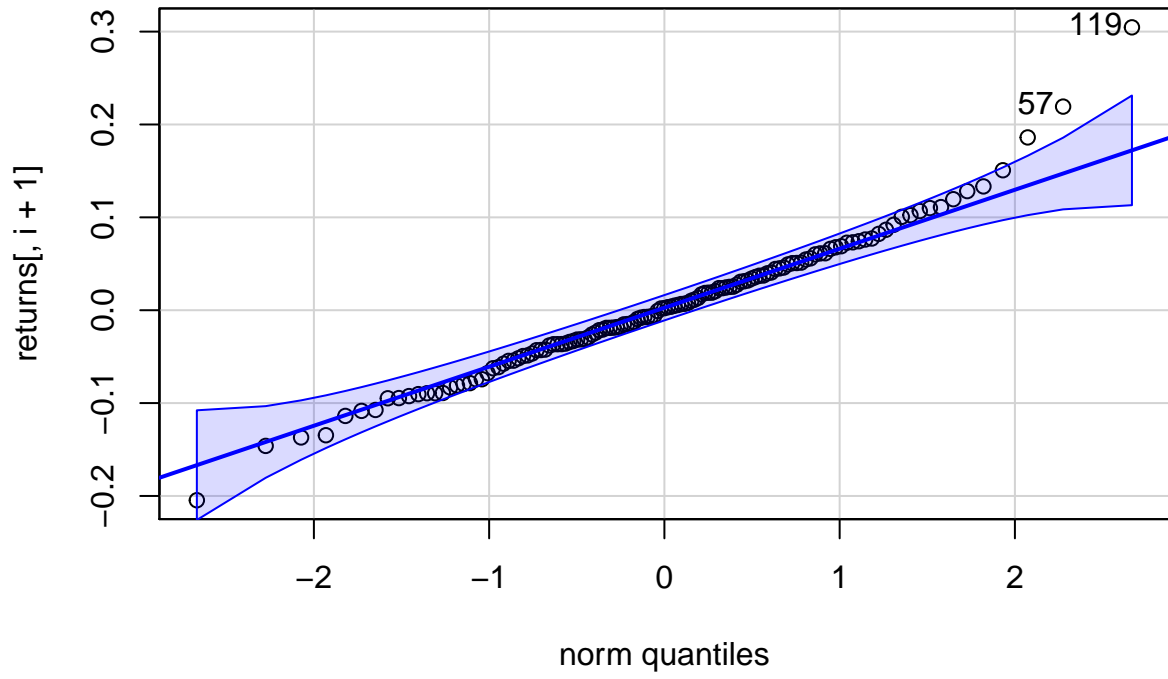


## Guinness

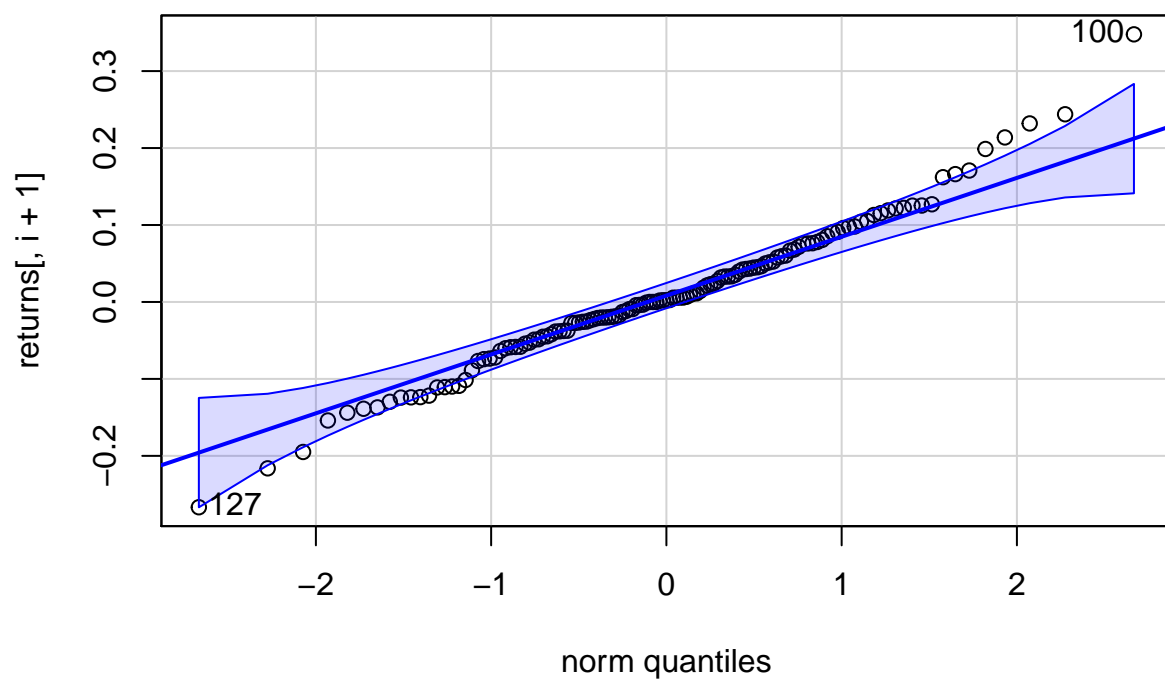




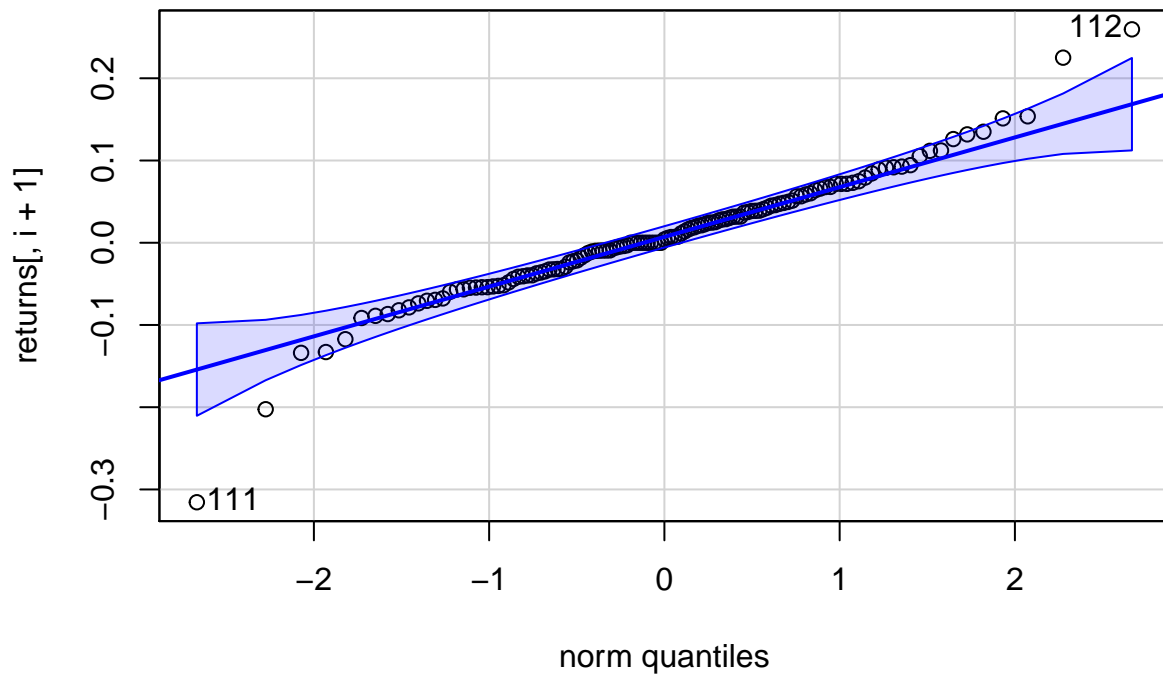
## Molson



# Tsingtao



## Asahi



### 7. Run tests for stationarity

*#null hypothesis is series is non stationary*

```
for (i in 1:15)
{
  print(adf.test(returnsNA[,i+1]))
}
```

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##

## Augmented Dickey-Fuller Test

##

## data: returnsNA[, i + 1]

## Dickey-Fuller = -4.4488, Lag order = 4, p-value = 0.01

## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##

## Augmented Dickey-Fuller Test

##

## data: returnsNA[, i + 1]

## Dickey-Fuller = -4.8884, Lag order = 4, p-value = 0.01

## alternative hypothesis: stationary

```

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -5.0885, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -5.7205, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -4.6744, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -4.9571, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -4.2524, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -7.2601, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

```

```

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -5.5502, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -4.8581, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -5.1527, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -4.5603, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -5.0268, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value

##
## Augmented Dickey-Fuller Test
##
## data: returnsNA[, i + 1]
## Dickey-Fuller = -4.9261, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

```

```
## Warning in adf.test(returnsNA[, i + 1]): p-value smaller than printed p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: returnsNA[, i + 1]  
## Dickey-Fuller = -5.4737, Lag order = 4, p-value = 0.01  
## alternative hypothesis: stationary
```

```
#all pvalues are less than 0.01 and so p-value<0.05 hence we reject the null hypothesis and conclude th  
#graphically we can see that all the returns have no trends and the oscillations between the returns se
```

8. Check if returns are normally distributed

```
#From the histograms the returns appear to have the normal distribution shape, where most of them appear  
#Looking at the qqplots we can see a few of the returns have values outside the interval which means th  
#lastly we do the Shapiro test  
#null hypothesis: normal
```

```
for (i in 1:15)  
{  
  print(shapiro.test(returnsNA[,i+1]))  
}
```

```
##  
## Shapiro-Wilk normality test  
##  
## data: returnsNA[, i + 1]  
## W = 0.99245, p-value = 0.7962  
##  
##  
## Shapiro-Wilk normality test  
##  
## data: returnsNA[, i + 1]  
## W = 0.98699, p-value = 0.3485  
##  
##  
## Shapiro-Wilk normality test  
##  
## data: returnsNA[, i + 1]  
## W = 0.9802, p-value = 0.09229  
##  
##  
## Shapiro-Wilk normality test  
##  
## data: returnsNA[, i + 1]  
## W = 0.9842, p-value = 0.2053  
##  
##  
## Shapiro-Wilk normality test  
##  
## data: returnsNA[, i + 1]
```

```

## W = 0.96322, p-value = 0.003369
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.94478, p-value = 0.0001491
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.94954, p-value = 0.0003182
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.97806, p-value = 0.05991
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.9946, p-value = 0.9422
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.98093, p-value = 0.1071
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.96791, p-value = 0.008096
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.9787, p-value = 0.06814
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.96058, p-value = 0.002092
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]

```

```
## W = 0.98392, p-value = 0.1943
##
##
## Shapiro-Wilk normality test
##
## data:  returnsNA[, i + 1]
## W = 0.93592, p-value = 3.924e-05
```

```
#normal <- 1,2,3,4,9,10,12,14,8 barely with 0.05991
#not normal <- 5,6,7,11,13,15
```

9. Fit different distributions to your data, which one fits better?

```
#t distribution
```

```
AIC_t <- c(rep(NA), 15)
BIC_t <- c(rep(NA), 15)

for (i in 1:15)
{
  x <- diff(returnsNA[,i+1])
  n = length(x)
  start = c(mean(x), sd(x), 5)
  loglik_t = function(beta) sum( - dt((x - beta[1]) / beta[2], beta[3], log = TRUE) + log(beta[2]) )
  fit_t = optim(start, loglik_t, hessian = T, method = "L-BFGS-B", lower = c(-1, 0.001, 1))
  AIC_t[i] = 2 * fit_t$value + 2 * 3
  BIC_t[i] = 2 * fit_t$value + log(n) * 3
}
```

```
#skewed student t
```

```
#not work: Harboe=11
```

```
AIC_sstd <- c(rep(NA), 15)
BIC_sstd <- c(rep(NA), 15)
```

```
for (i in 1:10)
{
  x <- diff(returnsNA[,i+1])
  n = length(x)
  loglik_sstd = function(beta) sum(- dsstd(x, mean = beta[1], sd = beta[2], nu = beta[3], xi = beta[4],
  start = c(mean(x), sd(x), 5, 1)
  fit_sstd = optim(start, loglik_sstd, hessian = T, method = "L-BFGS-B", lower = c(-0.1, 0.01, 2.1, -2))
  AIC_sstd[i] = 2*fit_sstd$value + 2 * 4
  BIC_sstd[i]= 2*fit_sstd$value + log(n) * 4
}
```

```
for (i in 1:4)
{
  x <- diff(returnsNA[,i+12])
  n = length(x)
  loglik_sstd = function(beta) sum(- dsstd(x, mean = beta[1], sd = beta[2], nu = beta[3], xi = beta[4],
  start = c(mean(x), sd(x), 5, 1)
  fit_sstd = optim(start, loglik_sstd, hessian = T, method = "L-BFGS-B", lower = c(-0.1, 0.01, 2.1, -2))
```



```

AIC_sstd[i+11] = 2*fit_sstd$value + 2 * 4
BIC_sstd[i+11]= 2*fit_sstd$value + log(n) * 4
}

#ged

AIC_ged <- c(rep(NA), 15)
BIC_ged <- c(rep(NA), 15)

for (i in 1:15)
{
x <- diff(returnsNA[,i+1])
n = length(x)
loglik_ged = function(beta) sum( - dged(x,mean=beta[1],sd=beta[2],nu=beta[3],log=TRUE) )
start = c(mean(x),sd(x),1)
fit_ged = optim(start,loglik_ged,hessian=T,method="L-BFGS-B",lower = c(-.1,.01,1))
AIC_ged[i] = 2*fit_ged$value+2*4
BIC_ged[i] = 2*fit_ged$value+log(n)*4
}

#normal

AIC_n <- c(rep(NA), 15)
BIC_n <- c(rep(NA), 15)

for (i in 1:15)
{
x <- diff(returnsNA[,i+1])
n = length(x)
start = c(mean(x),sd(x),1)
loglik_n = function(beta) sum( - dnorm(x,mean=beta[1],sd=beta[2],log=TRUE) )
fit_n = optim(start, loglik_n, hessian = T,
method = "L-BFGS-B", lower = c(-1, 0.001, 1))
AIC_n[i] = 2 * fit_n$value + 2 * 3
BIC_n[i] = 2 * fit_n$value + log(n) * 3
}

#####

table <- data.frame(AIC_t,AIC_sstd,AIC_ged,AIC_n,BIC_t,BIC_sstd,BIC_ged,BIC_n)
table <- cbind(Stocks, table)
table

```

```

##      Stocks      AIC_t  AIC_sstd  AIC_ged      AIC_n      BIC_t  BIC_sstd
## 1  Lufthansa -101.29256 -103.37211  -99.83794 -101.18741  -93.13707  -92.49812
## 2  Southwest -153.09917 -151.38061 -151.98968 -151.38767 -144.94367 -140.50662
## 3   EasyJet -166.23519 -164.47357 -166.30879 -164.09265 -158.07969 -153.59958
## 4   RyanAir -143.43542 -143.47498 -141.94782 -135.58773 -135.27993 -132.60098
## 5    United  -92.86558  -91.84959  -91.88617  -92.40196  -84.71008  -80.97559
## 6  American  -54.19922  -52.85083  -51.01658  -48.25515  -46.04373  -41.97684
## 7   Spirit  -84.69354  -84.58365  -79.86794  -75.45280  -76.53804  -73.70966
## 8  Carlsberg -195.03689 -195.95710 -192.57583 -190.49990 -186.88139 -185.08310
## 9  Heineken -228.57643 -227.35985 -226.72998 -225.91525 -220.42094 -216.48586
## 10         AB -184.98238 -184.19720 -181.40210 -179.18697 -176.82689 -173.32321

```



```
## 9      -216.48586 -215.85599 -217.75975      t Dist      t Dist
## 10     -173.32321 -170.52811 -171.03148      t Dist      t Dist
## 11              NA -221.07002 -225.66598      Normal      Normal
## 12     -272.09431 -267.40128 -269.11246 Skewed Sd t      t Dist
## 13     -166.32066 -165.44613 -168.62527 Skewed Sd t      t Dist
## 14     -107.89309 -107.91192 -112.55908      Normal      Normal
## 15     -197.19801 -190.19567 -176.26297      t Dist      t Dist
```

10. Compute Sharpe's slope for each asset. Which asset has the highest slope? If  $E(R_P)$  and  $\sigma_{R_P}$  are the expected return and standard deviation of the return on a portfolio and  $\mu_f$  is the risk-free rate, then Sharpe's slope =  $\frac{E(R_P) - \mu_f}{\sigma_{R_P}}$

```
riskfree <- 0.04
```

```
SharpesSlope <- rep(NA,15)
```

```
for (i in 1:15)
{
  SharpesSlope[i] <- (mean(returnsNA[,i+1]) - riskfree)/sd(returnsNA[,i+1])
}
```

*#If the analysis results in a negative Sharpe ratio, it either means the risk-free rate is greater than*

```
SharpesSlope
```

```
## [1] -0.3611148 -0.2458842 -0.4103832 -0.3012443 -0.2466343 -0.1938094
## [7] -0.2113170 -0.4910430 -0.5343287 -0.4788517 -0.6687074 -0.6470281
## [13] -0.5263983 -0.3381888 -0.4398642
```

```
max(SharpesSlope) #highest slope
```

```
## [1] -0.1938094
```

11. Convert the monthly sample means into annual estimates by multiplying by 12 and convert the monthly sample SDs into annual estimates by multiplying by the square root of 12. Comment on the values of these annual numbers.

```
#?
```

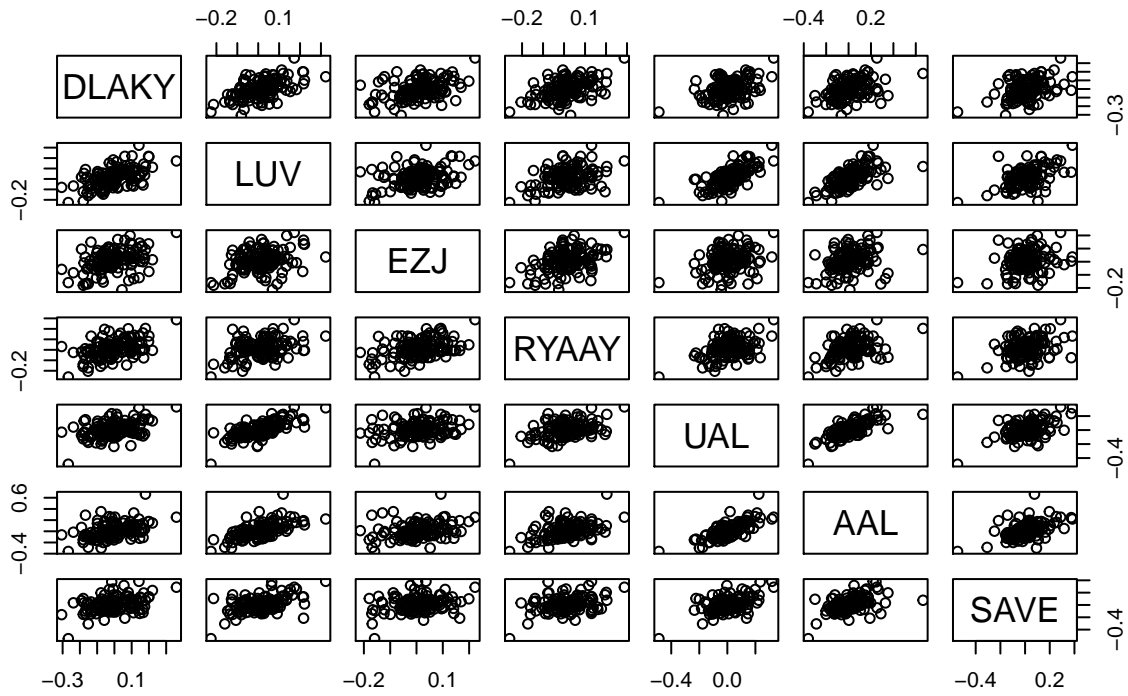
```
#annualsamplemeans <- returns[,2:16] *12
```

```
#annualsamplesd <- sd(returns[,2:16])*sqrt(12)
```

12. Construct pairwise scatter plots between your assets returns and comment on any relationships you see.

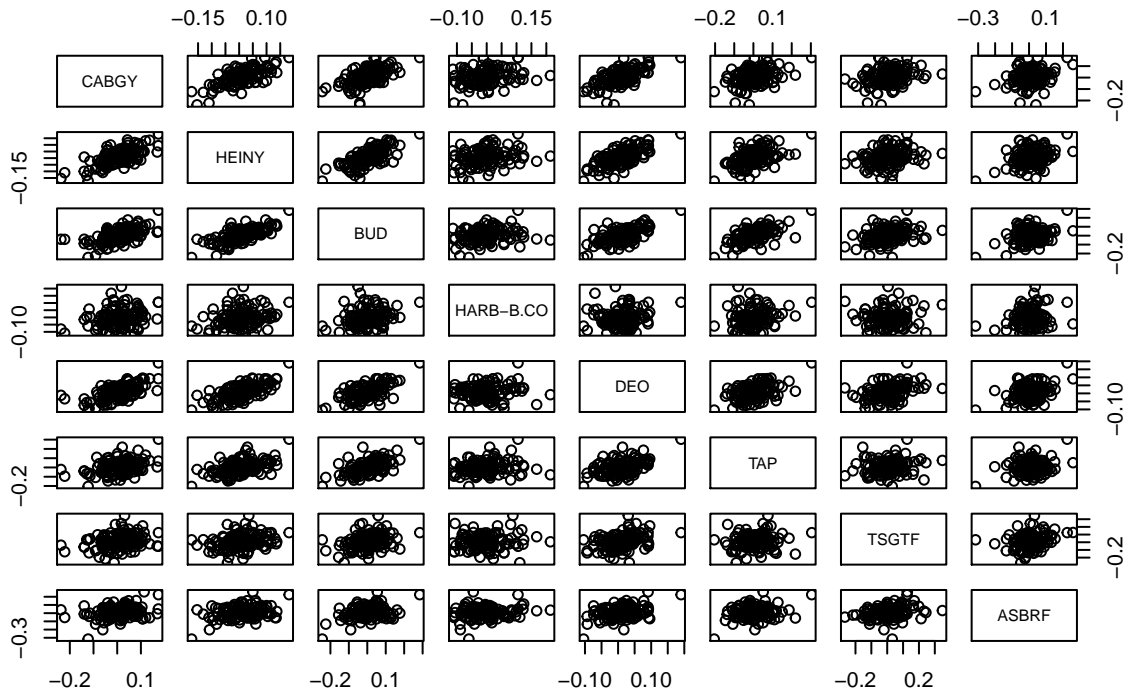
```
#airlines
pairs(returns[,2:8], main="Scatterplot of Airline Returns")
```

## Scatterplot of Airline Returns



```
#beers
pairs(returns[,9:16], main="Scatterplot of Beer Returns")
```

## Scatterplot of Beer Returns



13. You should also compute the sample covariance matrix of the returns on your assets and comment on the direction of linear association between the asset returns.

```
# covariance monthly data

Covariances <- as.data.frame(cov(returnsNA[2:16]))

#they all have positive covariances hence the returns all move together, vary in the same direction.

Covariancesair <- Covariances[1:7,1:7]
Covariancesbeers <- Covariances[8:15,8:15]

# covariance annualized data

annualreturns <- returnsNA[,2:16]*12

Covariancesannual <- as.data.frame(cov(annualreturns[1:15]))

#they all have positive covariances hence the returns all move together, vary in the same direction.

Covariancesairannual <- Covariancesannual[1:7,1:7]
Covariancesbeersannual <- Covariancesannual[8:15,8:15]

#####
```

```
#correlation for monthly data

Correlations <- as.data.frame(cor(returnsNA[2:16]))

#they all have positive covariances hence the returns all move together, vary in the same direction.

Correlationsair <- Correlations[1:7,1:7]
Correlationsbeers <- Correlations[8:15,8:15]
```