

$$f(x,y) = \frac{2xy}{x^2 + 2y^2}$$

$$\begin{matrix} x^2 & + & 2y^2 & = & 0 \\ \geq 0 & & \geq 0 \end{matrix} \Rightarrow \begin{matrix} x^2 & = & -2y^2 \\ \geq 0 & & \geq 0 \end{matrix}$$

$$\Rightarrow \underline{x=0 \text{ e } y=0}$$

$$\begin{matrix} (-2) \cdot y^2 & \leq & 0 \\ < 0 & \geq 0 \end{matrix} \underline{\leq 0}$$

$$x=-y \Rightarrow f(x,y) = \frac{2(-y)y}{(-y)^2 + 2y^2} = \frac{-2y^2}{3y^2} = -\frac{2}{3}$$

$$x=y \Rightarrow f(x,y) = \frac{2x \cdot x}{x^2 + 2x^2} = \frac{2x^2}{3x^2} = \frac{2}{3}$$

$$D = \mathbb{R}^2 - \{(0,0)\}$$

$$D = \{(x,y) \in \mathbb{R}^2 \mid x \neq 0 \text{ e } y \neq 0\}$$

$$f(x,y) = 9 - x^2 - 9y^2, \quad \underline{\underline{z = 9 - x^2 - 9y^2}}$$

plano xz: $(x, 0, z)$

$$z = 9 - x^2 \Rightarrow z = -x^2 + \underline{9} \text{ (parábola)}$$

plano yz: $(0, y, z)$

$$z = 9 - 9y^2 \Rightarrow z = -9y^2 + \underline{9} \text{ (parábola)}$$

plano xy: $(x, y, 0) \quad \underline{z=0}$

$$0 = 9 - x^2 - 9y^2 \Rightarrow x^2 + 9y^2 = 9 \stackrel{(\div 9)}{\Rightarrow} \boxed{\frac{x^2}{\underline{3^2}} + \frac{y^2}{\underline{1^2}} = 1} \text{ (elipse)}$$

$z = \underline{1}$:

$$\underline{1 = 9 - x^2 - 9y^2} \Rightarrow x^2 + 9y^2 = 8 \stackrel{(\div 8)}{\Rightarrow} \frac{x^2}{8} + \frac{9y^2}{8} = 1 \Rightarrow \frac{x^2}{(\underline{\sqrt{8}})^2} + \frac{y^2}{(\underline{\sqrt{\frac{8}{9}}})^2} = 1$$

