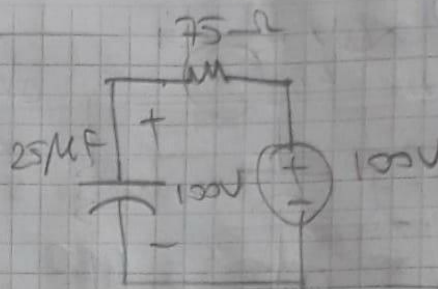
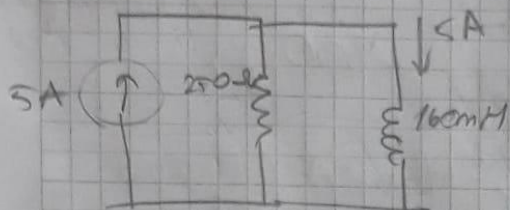


8-11) tLO:

(P2.8)



After a very long time

$$I_0 = 5A, V_0 = 100V$$

$$\alpha = \frac{1}{2RC} = \frac{1}{2 \cdot 50 \cdot (25 \cdot 10^{-6})} = \frac{10^6}{10^2 \cdot 25} = \frac{10^4}{25} = 400 \quad \text{under damp.}$$

$$\omega_0 = \sqrt{\frac{1}{LC}} = \sqrt{\frac{1}{160 \cdot 10^{-3} \cdot 25 \cdot 10^{-6}}} = \sqrt{\frac{10^9}{4 \cdot 10^3}} = 500$$

$$\omega_d = \sqrt{\omega_0^2 - \alpha^2} = \sqrt{500^2 - 400^2} = 300$$

$$V(0^+) = B_1 \cdot e^{-400t} \cdot \cos(300t) + B_2 \cdot e^{-400t} \cdot \sin(300t)$$

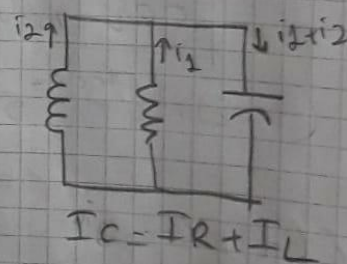
$$V(0^+) = B_1 = 300$$

$$\frac{dV(0^+)}{dt} = -\alpha B_1 + \omega_d B_2 = \frac{1}{C} I_C$$

$$\frac{dV(0^+)}{dt} = -\alpha B_1 + \omega_d B_2 = \frac{1}{C} \left(-I_0 - \frac{V_0}{R} \right)$$

$$= -400 \cdot 100 + 300 B_2 = \frac{1}{25 \cdot 10^{-6}} (-5 - 2)$$

$$\Rightarrow B_2 = -800$$



$$V(t) = 100 e^{-400t} \cdot \cos(300t) - 800 e^{-400t} \cdot \sin(300t) V$$

$$8.27) \alpha = \frac{1}{2RC} = \frac{1}{2 \cdot (125)(62.5)} = 640 \quad \left. \begin{array}{l} (12.5) \\ \text{under damped} \end{array} \right\}$$

$$\omega_0 = \sqrt{\frac{1}{LC}} = \sqrt{\frac{1}{25 \times 10^{-3} \cdot (62.5 \times 10^{-6})}} = 800$$

$$\omega_D = \sqrt{800^2 - 640^2} = 480, \quad I_f = 2A \text{ (Forced Response)}$$

$$i(t) = B_1' e^{-640t} \cos(480t) + B_2' e^{-640t} \sin(480t) + 2$$

$$i(0^+) = 2 + B_1' = 1 \Rightarrow B_1' = -1$$

$$\frac{di(0^+)}{dt} = -\alpha B_1' + \omega_D B_2' = \frac{V_0}{L}$$

$$= 640 + 480 B_2' = \frac{50}{25 \times 10^{-3}} = 2000$$

$$= 480 B_2' = 1360$$

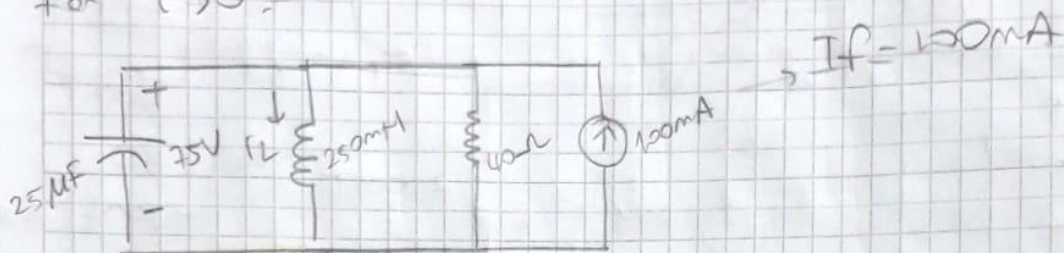
$$\Rightarrow B_2' = 2.83$$

$$i(t) = -e^{-640t} \cos(480t) + 2.83 e^{-640t} \sin(480t) + 2 \text{ A}$$

↙ I_{forced}

8.35) $V_0 = 100 \cdot \frac{3}{4} = 75V$, $I_0 = 100mA$ (fp. 8)

for $t > 0$:



$$\alpha = \frac{1}{2RC} = \frac{1}{2 \cdot 40 \cdot (25 \times 10^{-6})} = 500 \quad \text{overdamped}$$

$$\omega_0 = \sqrt{\frac{1}{LC}} = \sqrt{\frac{1}{250 \times 10^{-3} \cdot 25 \times 10^{-6}}} = 400$$

$$s_{1,2} = -\alpha \pm \sqrt{\alpha^2 - \omega_0^2} \Rightarrow s_{1,2} = -500 \pm \sqrt{500^2 - 400^2}$$

$$s_1 = -200$$

$$s_2 = -800$$

$$a) i(t) = A_1 e^{-200t} + A_2 e^{-800t} + I_f$$

$$i(0) = A_1 + A_2 + 0.1 = 0.1 \Rightarrow A_1 + A_2 = 0$$

$$\frac{di(0^+)}{dt} = -200A_1 - 800A_2 = \frac{V_0}{L} = \frac{75}{0.25} = 300$$

$$\begin{cases} -2A_1 - 8A_2 = 3 \\ 2A_1 + 2A_2 = 0 \end{cases} \Rightarrow \begin{cases} -6A_2 = 3 \\ A_2 = -1/2 \end{cases}$$

$$A_2 = -1/2$$

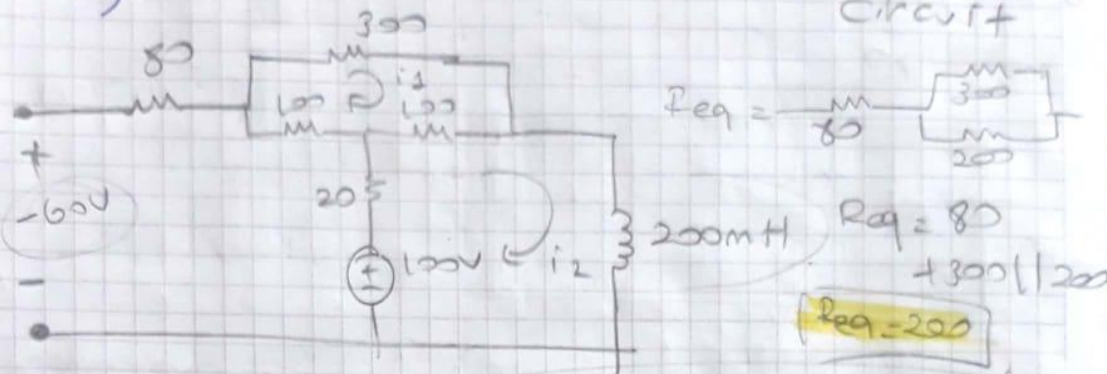
$$A_1 = 1/2$$

$$i(t) = 0.5e^{-200t} - 0.5e^{-800t} + 0.1 \text{ A}$$

$$b) v_L(t) = v_L(t) = L \frac{di_L}{dt} = (0.25) \left[-100e^{-200t} + 400e^{-800t} \right]$$

$$= -25e^{-200t} + 100e^{-800t} \text{ V}$$

8.47) $t < 0$, capacitor acts like an open circuit



$$500i_1 - 100i_2 = 0 \quad (-100 + 120i_2 - 100i_1 = 0)$$

$$(5i_1 = i_2)$$

$$\Rightarrow i_1 = 0.2A, \quad i_2 = 1A$$

$$V_0 = -100 + 20i_2 + 10i_1$$

$$V_0 = -60V$$

$$\begin{array}{r} A_1 + A_2 = 1 \quad (200) \\ -200A_1 - 800A_2 = -700 \\ \hline -600A_2 = -500 \end{array}$$

$$A_2 = \frac{5}{6}, \quad A_1 = \frac{1}{6}$$

$$\alpha = \frac{R}{2L} = \frac{200}{0.4} = 500$$

$$\omega_0 = \sqrt{\frac{1}{LC}} = \sqrt{\frac{1}{(0.2)(31.25 \times 10^{-6})}}$$

$$\omega_0 = 400$$

overdamped

$$s_{1,2} = -100 \pm \sqrt{500^2 - 400^2} = -200, -800$$

$$i(0) = A_1 + A_2 = 1, \quad \frac{di(0^+)}{dt} = -200A_1 - 800A_2$$

$$= \frac{1}{L} (-V_0 - RI_0) = -700$$

$$\Rightarrow A_1 = 0.167$$

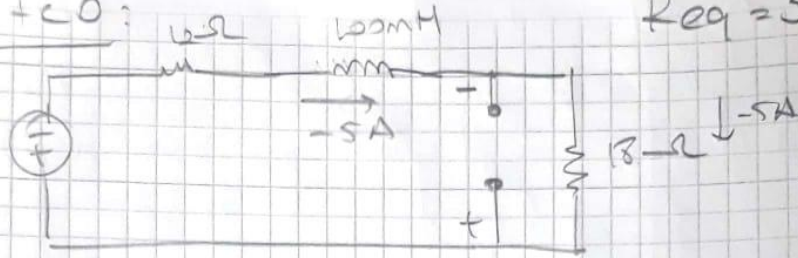
$$A_2 = 0.833$$

$$i(t) = 0.167e^{-200t} + 0.833e^{-800t} \text{ mA} \quad \downarrow$$

$$v(t) = L \frac{di}{dt} \Rightarrow -6.67e^{-200t} - 133.28e^{-800t} \text{ V}$$

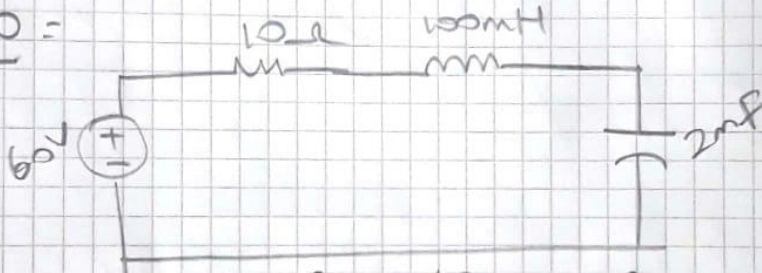
8.54)

$t < 0$:



$$I_0 = \frac{V}{R} = \frac{-150}{30} = -5A \quad V_0 = -90V$$

$t > 0$:



In serial form

$$\alpha = \frac{R}{2L} = \frac{10}{2(0.1)} = 50$$

$$\omega_0 = \sqrt{\frac{1}{LC}} = \sqrt{\frac{1}{0.1(2 \times 10^{-6})}} = 70.7$$

$$V(t) = 60 + B_1 e^{-50t} \cos(50t) + B_2 e^{-50t} \sin(50t)$$

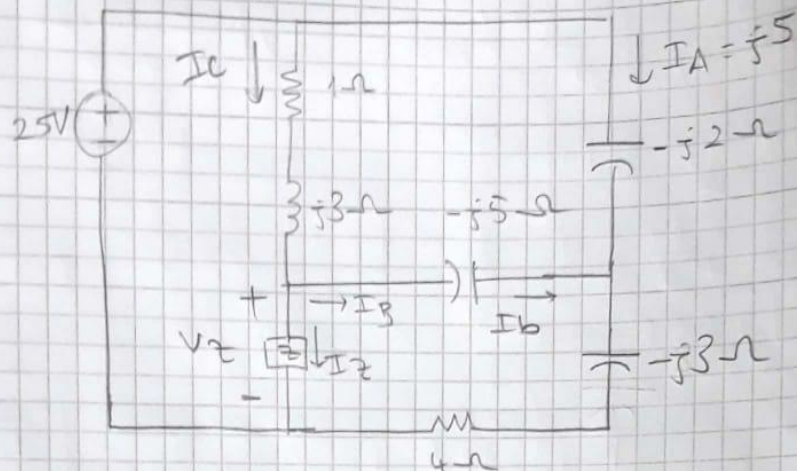
$$V(0^+) = 60 + B_1 = -90 \Rightarrow B_1 = -150$$

$$\frac{dV}{dt} = \frac{I}{C} = \frac{-5}{2 \times 10^{-6}} = -2500$$

$$\frac{dV(0^+)}{dt} = -50B_1 + 50B_2 = -2500 \Rightarrow B_2 = -200$$

$$V(t) = 60 + 150e^{-50t} \cos(50t) - 200e^{-50t} \sin(50t) \text{ V}$$

9.32)



$$-25 - (-j2 \cdot j5) + (4 - j3)(j5 + I_B) = 0$$

$$-25 + 10 + (4 - j3)(j5 + I_B) = 0$$

$$\Rightarrow I_B = (2.4 - j3.2) \text{ A}$$

$$V_Z = -j5(2.4 - j3.2) + (4 - j3)(\underbrace{2.4 + j1.8}_{I_A + I_B}) = 0$$

$$\Rightarrow V_Z = (-1 - j12) \text{ V}$$

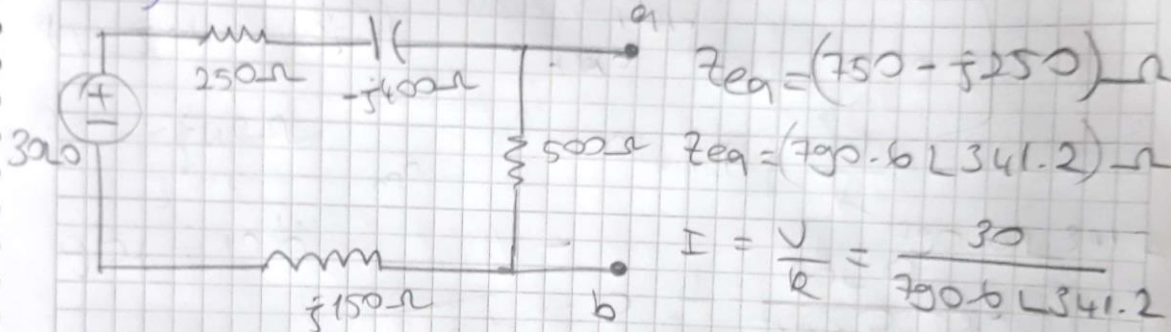
$$-25 + (1 + j3)I_C + (-1 - j12) = 0$$

$$\Rightarrow I_C = (6.2 - j6.6) \text{ A}$$

$$I_Z = I_C - I_B = (6.2 - j6.6) - (2.4 - j3.2) = (3.8 - j3.4) \text{ A}$$

$$Z = \frac{V_Z}{I_Z} = \frac{-1 - j12}{3.8 - j3.4} = (1.42 - j1.88) \Omega$$

9.45) $V = (120 \angle 0) \cdot (250 \angle 0) = 30 \text{ V}$



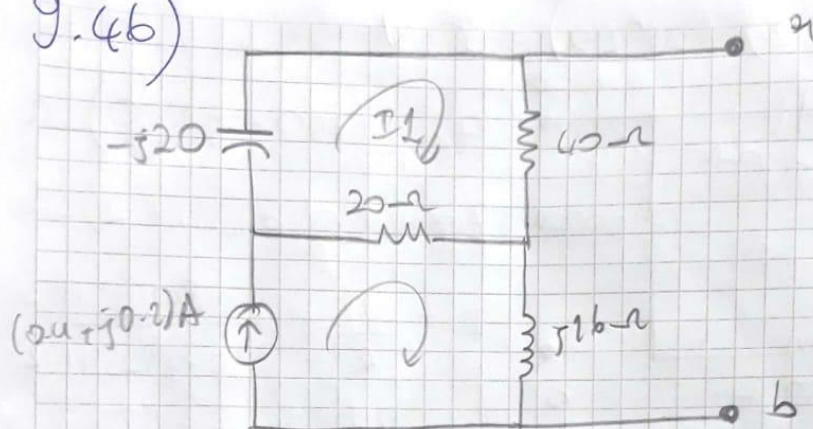
$$I = \frac{V}{Z} = \frac{30}{790.6 \angle -341.2}$$

$$I = 0.038 \angle -341.2$$

$$V_{ab} = 500 \cdot (0.038 \angle -341.2)$$

$$V_{ab} = 19 \angle -341.2 = 18 - j6 \text{ V}$$

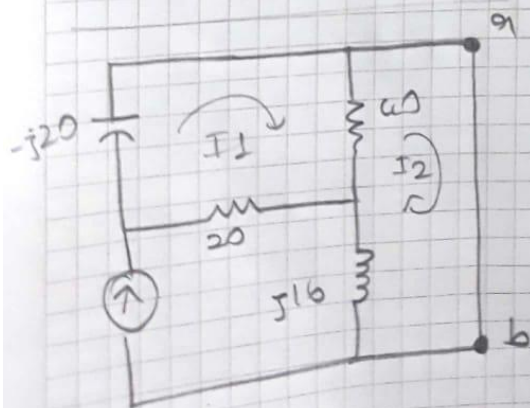
9.46)



$$-j20I_1 + 40I_1 + 20(I_1 - 0.4 - j0.2) = 0$$

$$\Rightarrow I_1 = \frac{20(0.4 + j0.2)}{60 - j20} = 0.1 + j0.1 \text{ A}$$

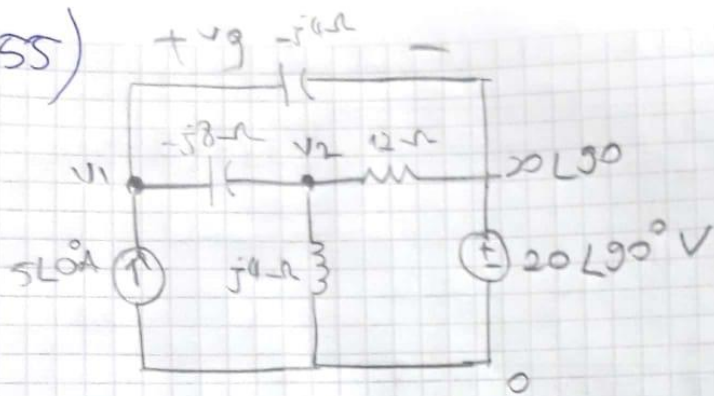
$$V_{ab} = 40I_1 + j16(0.4 + j0.2) = 0.8 + j10.4 \text{ V}$$



$$40(I_2 - I_1) + j16(I_2 - 0.4 - j0.2) = 0$$

$$\Rightarrow I_2 = 0.3 + j0.5 \text{ A}$$

9.55)



$$V_1: -5\angle 0^\circ + \frac{V_1 - V_2}{-j8} + \frac{V_2 - 20\angle 90^\circ}{-j4} = 0$$

$$V_2: \frac{V_2 - V_1}{-j8} + \frac{V_2}{j4} + \frac{V_2 - 20\angle 90^\circ}{12} = 0$$

$$V_1 \left(\frac{1}{-j8} - \frac{1}{j4} \right) + V_2 \left(\frac{1}{j8} \right) - 5\angle 0^\circ + \frac{20\angle 90^\circ}{j4} = 0$$

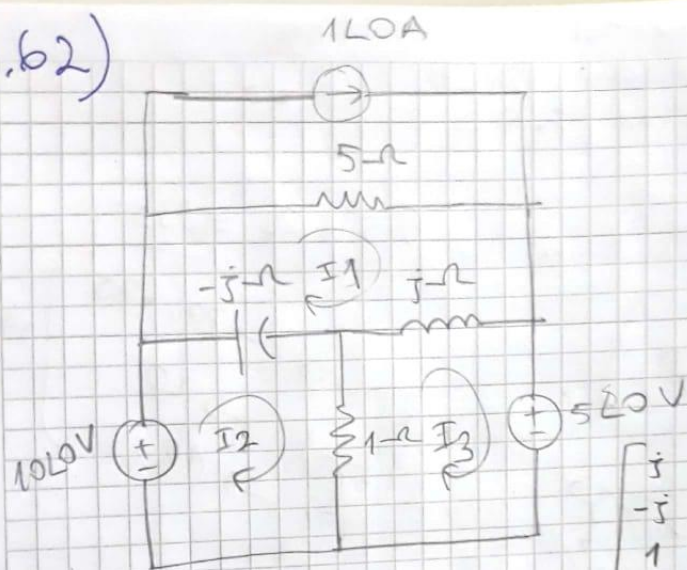
$$V_1 \left(\frac{1}{j8} \right) + V_2 \left(\frac{1}{j4} - \frac{1}{j8} + \frac{1}{12} \right) - \frac{20\angle 90^\circ}{12} = 0$$

$$\Rightarrow V_1 = -\frac{8}{3} + j\frac{4}{3}, \quad V_2 = -8 + j4$$

$$V_g = V_1 - 20\angle 90^\circ = \left(-\frac{8}{3} + j\frac{4}{3} \right) - (j20)$$

$$= \left(-\frac{8}{3} - j18.67 \right) V$$

9.62)



$$\begin{bmatrix} j & -j+1 & -1 \\ -j & -1 & j+1 \\ 1 & -1 & -j \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} 10L0 \\ -5L0 \\ 1 \end{bmatrix}$$

$$-10L0 + I_2(-j+1) - I_1(-j) - I_3(1) = 0$$

$$5L0 + (1+j)I_3 - jI_1 - I_2 = 0$$

$$-1 - jI_2 - jI_3 + I_1 = 0$$

$$\Rightarrow I_1 = 6A, I_2 = 11+j10, I_3 = 11+j5$$

$$I_{a1} = I_1 - 1 = 5A$$

$$I_{b3} = I_2 - I_1 = (5+j10)A$$

$$I_{c0} = I_3 - I_1 = (5+j5)A$$

$$I_{d0} = I_2 - I_3 = j5A$$