

Lecture 2- Induction



$$\forall x \in \mathbb{N} : \text{all } P(n) \text{ is true}$$

Note

- Important propositions are called **theorems**.
- A **lemma** is a preliminary proposition useful for proving later propositions.
- A **corollary** is a proposition that follows in just a few logical steps from a lemma or a theorem

Tip

Because a conditionals contrapositive equals to itself proving contrapositive proves also the theorem.

Sets

$S \subseteq T$ indicates that set S is a subset of set T and S may be equal to T.

$S \subset T$ indicates that set S is a subset of set.

\overline{A} is consists from every element not in set A. Henceforth that is called **complement**

Cardinality

$$|\{1,2,3\}| = 3$$

Power set

Every subset of a set A.

Cross product

A product of sets, $S_1 S_2$, is a new set consisting of all sequences where the first component is drawn from S_1 , the second from S_2 , and so forth.

$$\mathbb{N} \times \{a, b\} = \{0, a\}, \{0, b\}, \{1, a\}, \{1, b\}, \dots$$

Lecture 3- Strong Induction