

My Notes for AP Calculus BC

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Chapter 1

Limits and Continuity

1.1 Computing Limits

1.2 Limits at Infinity

1.3 Continuity

1.4 Intermediate Value Theorem

1.5 Squeeze Theorem

Chapter 2

Differentiation and the Rate of Change

2.1 Tangent Lines and Rates of Change

2.2 The Derivative Function

2.3 Techniques of Differentiation

2.4 Product Rule and Quotient Rule

2.5 Derivatives of Trig Functions

2.6 The Chain Rule

Chapter 3

Topics in Differentiation

3.1 Implicit Differentiation

3.2 Derivatives of Logarithmic Functions

3.3 Derivatives of Exponential Functions

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3.5 Related Rates

3.6 Local Linear Approximation

3.7 L'Hôpital's Rule and Indeterminate Forms

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The Derivative in Graphing and Applications

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4.2 Relative Extrema

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Chapter 5

Integration

5.1 Overview of Area

5.2 The Indefinite Integral

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5.4 Integration By Substitution

5.5 Area as a Limit and Riemann Sums

5.6 Exact Area Under a Curve (Trapezoid Rule)

5.7 The Definite Integral

5.8 The Accumulation Function

5.9 The Fundamental Theorem of Calculus

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5.11 Average Value

5.12 Definite Integrals by Substitution

Chapter 6

Applications of the Definite Integral

6.1 Area Between Two Curves

6.2 Volumes by Slicing

6.3 Disks and Washers

6.4 Length of a Plane Curve

Chapter 7

Principles of Integral Evaluation

7.1 Integration by Parts

7.2 Integration of Rational Functions by Partial
Fractions

7.3 Improper Integrals

Chapter 8

Differential Equations

8.1 Logistic Growth

8.2 Separable Equations

8.3 Exponential Growth and Decay

8.4 Euler's Method

Chapter 9

Infinite Series

9.1 Defining Convergent and Divergent Infinite Series

9.2 Geometric Series

Definition 1. A series in the form $\sum ar^n = a + ar + ar^2 + ar^3 + \dots + ar^n \dots$ is called a *geometric series* with ratio r .

An infinite geometric series with ratio r diverges if $|r| \geq 1$. If $|r| < 1$, we can say that the series converges by the **geometric series test**. The infinite sum of this series is

$$\sum_{n=0}^{\infty} ar^n = \frac{a}{1-r}$$

9.3 nth Term Test

9.4 Integral Test

9.5 p-series and Harmonic Series

9.6 Comparison Tests

9.7 Polynomial Test

9.8 Alternating Series

Chapter 10

Parametric, Polar, and Vector-Valued Functions

10.1 Parametric Equations

10.2 Vector-Valued Functions

10.3 Polar Functions