Heuristic analysis:

First experiment:

Custom 1 is a variation of the Open heurisitc, but instead of the bias towards number of legal moves of the current player, the heurisitic is biased towards limiting number of moves of opponent by returning the negative value of opponet's legal moves. This heuristic performs well against the original Open heurisitc both with Minimax with score 42/8 and Alphabeta with score 27/3. This heurisitic is performing well against other competitiors as well with total win probability of 66% and a good performance against AB_Improved with score 30/20. The definsive nature of the strategy combined with simplicity and high performance gives a good advantage.

Custom 2 tries to enhance the provided improved heuristic by adding a bias towards moves with larger number of open blocks in a 5x5 square. In practice this heuristic performed worse than improved evaluation with overall win rate of 59.7%

Custom 3 is using a hybrid approach with a strategy at the beginning different from the end of game. In this experiment we used the number of legal moves for the first 6 moves, then used improved heurisitic for the rest. This heurisitic seemed to perform well with win rate of 64.7% but with room for enhancement especially against vanilla improved evaluation.

Table 1: first experiment

AB_Custom: negative open AB_Custom_2: AB_Improved with open in proximity AB_Custom_3: First 6 moves: number of legal moves of player, later AB_Improved

Match	Opponent AB	_Improved A	B_Custom AB	S_Custom_2 AB	_Custom_3
		Won Lost	Won Lost	Won Lost	Won Lost
1	MM_Open	39 11	42 8	36 14	37 13
2	MM_Center	41 9	39 11	43 7	39 11
3	MM_Improved	38 12	34 16	35 15	35 15
4	AB_Open	31 19	27 23	22 28	24 26
5	AB_Center	25 25	26 24	24 26	36 14
6	AB_Improved	24 26	30 20	19 31	23 27
	Win Rate:	66.0%	66.0%	59.7%	64.7%

Second experiment

Changing the hybrid heurisite by using the negative open moves as Custom_1 for the first 6 moves. This seems to enhance the results especially agains vanilla improved. The overall win rate is 65% AB_Custom_3: First 6 moves: negative number of legal moves of opponent, later AB_Improved

```
Match
       Opponent
                AB Custom 3
                  Won | Lost
       MM Open
                 39 | 11
      MM_Center 42 | 8
  3 MM Improved 36 | 14
       AB Open
                 24 | 26
  5
       AB Center 28 | 22
       AB Improved 26 | 24
  6
        Win Rate:
                    65.0%
```

Third experiment

Changing the hybrid heurisitic by using a defensive strategy towards the game end by subtracting double the opponent's move from player moves. The end result did not enhance though.

AB_Custom_3: First 10 moves: negative number of legal moves of opponent, later defensive AB_Improved

```
Match #
      Opponent
                 AB Custom 3
                  Won | Lost
  1
       MM Open
                 34 | 16
  2
      MM Center 44 6
      MM_Improved 40 | 10
  3
                  22 | 28
       AB_Open
  4
                27 | 23
  5
       AB_Center
       AB_Improved 26 | 24
  6
        Win Rate:
                   64.3%
```

Fourth experiment

Trying a different configuration for the hybrid heuristic by strating with a strategy favoring center blocks at the beginning, then a defensive negative number of opponent's legal moves, and ending with a defensive variation to the improved heuristic. The overall win rate increased to 66.3%

```
AB Custom 3
Match #
      Opponent
                 Won | Lost
  1
       MM_Open
                35 | 15
      MM Center 46 4
    MM_Improved 38 | 12
       AB Open 26 24
       AB Center 27 | 23
  5
     AB_Improved 27 | 23
  6
       Win Rate:
                 66.3%
```

Fifth experiment

Running all agents at the same experiement with 50 matches against each of the provided heuristics. The hybrid heuristic still seems to perform best with a small margin. AB_Custom: negative open AB_Custom_2: AB_Improved with open in proximity AB_Custom_3: hybrid eval, center 6 moves, negative open 6 moves, then improved

```
AB_Improved AB_Custom AB_Custom_2 AB_Custom_3
Match #
      Opponent
               Won | Lost Won | Lost Won | Lost
      MM_Open 34 | 16 35 | 15 37 | 13
                                         39 | 11
 1
     MM_Center 46 | 4 41 | 9 40 | 10
                                         46 4
  2
  3 MM_Improved 32 | 18 30 | 20 34 | 16
                                         33 | 17
  4
      AB_Open 31 | 19 29 | 21 29 | 21
                                        28 | 22
  5
      AB_Center 28 | 22 26 | 24 20 | 30 25 | 25
      AB_Improved 20 | 30  30  | 20  22  | 28  24  | 26
      Win Rate:
               63.7% 63.7% 60.7%
                                          65.0%
```

Conclusion:

The hybrid approach is promising and make sense to adjust the strategy according to the game state. There is still rooom for improvement with further experimintation towards optimizing the hybrid evaluation function, but for now this is the selected function.