

# 3 Minute Student Talks

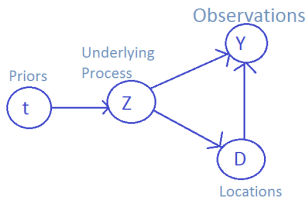
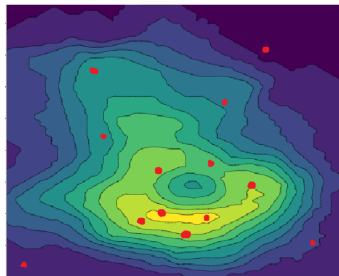


Aoibheann Brady

Attribution of Large Scale Drivers for  
Environmental Change

# Spatial Statistics and Preferential Sampling!

- ▶ Stochastic dependence between unknown underlying process and sampling locations.
- ▶ Dependent on the *utility* of a design.
- ▶ Example: Monitoring pollution levels.



- ▶ How do we deal with this?

Matthew Griffith

An Increased Model Height in the  
Met Office's Unified Model

# Log-Gaussian Cox Processes

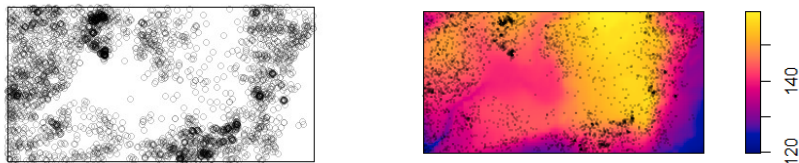


Figure: Locations of 3605 trees in rainforest, bei dataset

Homogeneous Poisson Process	Inhomogeneous Poisson Process	Cox Process
$N(A) \sim Po(\lambda \ A\ )$	$N(A) \sim Po(\int_A \lambda(\mathbf{x}) d\mathbf{x})$	Stochastic intensity function $\Lambda(\mathbf{x})$ $\Lambda(\mathbf{x}) = \lambda(\mathbf{x}) \implies$ Inhom. PP

# Understanding Measure-valued Martingales

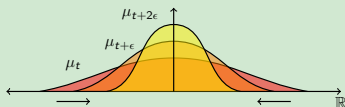
## Definition

A stochastic process  $(\mu_t)_{t \geq 0}$  is said to be a **measure-valued martingale** (MVM), i.e.  $\mu_t \in \mathcal{P}^1(\mathbb{R})$  (integrable)  $\forall t \geq 0$ , and  $\mu_t(A)$  is a martingale  $\forall A \in \mathcal{B}(\mathbb{R})$ .

## Formulation of the Problem

Given that  $\mu_t$  has a constant "speed" (exact sense to be determined...), what is the MVM that makes  $\text{var}(\mu_t) := \int z^2 \mu_t(dz) - (\int z \mu_t(dz))^2$  decrease as fast as possible (on average)? What about general functions  $F$  of  $\mu_t$ , not just variance? The aim is to use the JKO scheme by extending its application to measure-valued processes.

## Example



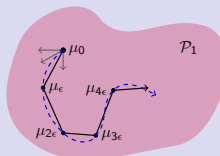
**Fact:** a measure-valued martingale has shrinking support.

## Financial Application

**Variance swaps:** speculating on or hedging the risks associated with the volatility of the underlying financial product (exchange rates, interest rates, stock index).

## Jordan-Kinderlehrer-Otto (JKO) scheme

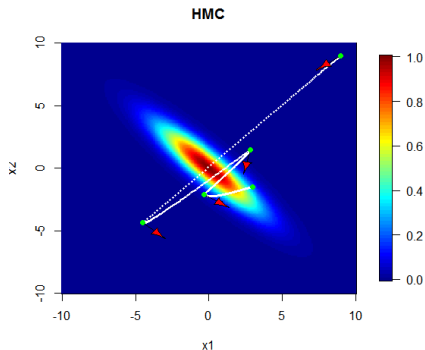
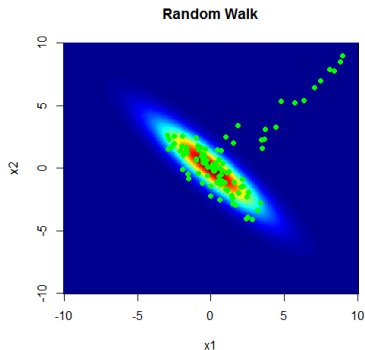
The JKO scheme is a time discretisation scheme that allows us to find the unique (local) minimising direction (gradient flow) of  $F$  at each point in the Wasserstein metric space  $\mathcal{P}_1$ . Optimal transport theory tells us that if we take the mesh size to zero we get a geodesic.



— JKO scheme    - - - Optimal Transport



# Large Scale Differential Geometric MCMC



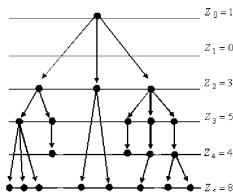
Lizzi Pitt

First in Human Trials



## Simple Branching

Figure: GW Process



$$Z_{n+1} = \sum_{n=1}^{Z_n} A_j^{(n+1)}$$



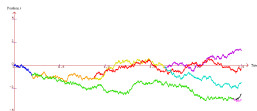
Continuous-time Galton  
Watson process →



Continuous-time BP

## Spatial consideration

Figure: Branching RW



$$X_n(\cdot) = \sum_{n=1}^{Z_n} \delta_{x_i^n}(\cdot)$$

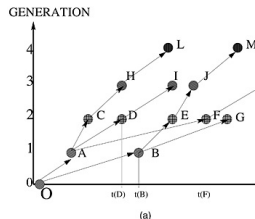
Figure: Branching  
Brownian Motion



$$X_t(\cdot) = \sum_{n=1}^{Z_t} \delta_{x_i^t}(\cdot)$$

Ex: Spatial Position =  
Birth time

Figure: CMJ process



## Definition

A *spatial branching process* is branching phenomenon + spatial motion given by a Markov process.