

CSE 321 Homework 2

Due date: 09 / 11 / 2018

1-) Suppose you are choosing between the following three algorithms:

- a) Algorithm A solves problems by dividing them into five subproblems of half the size, recursively solving each subproblem, and then combining the solutions in linear time.
- b) Algorithm B solves problems of size n by recursively solving two subproblems of size $n - 1$ and then combining the solutions in constant time.
- c) Algorithm C solves problems of size n by dividing them into nine subproblems of size $n/3$, recursively solving each subproblem, and then combining the solutions in $O(n^2)$ time.

What are the running times of each of these algorithms (in big-O notation), and which would you choose?

2-) Solve the following recurrence relations and give a Θ bound for each of them.

- a) $T(n) = 2T(n/3) + 1$
- b) $T(n) = 5T(n/4) + n$
- c) $T(n) = 7T(n/7) + n$
- d) $T(n) = 9T(n/3) + n^2$
- e) $T(n) = 8T(n/2) + n^3$
- f) $T(n) = 49T(n/25) + n^{3/2} \log n$
- g) $T(n) = T(n - 1) + 2$
- h) $T(n) = T(\sqrt{n}) + 1$

3-) Given an array of n elements, and you notice that some of the elements are duplicates; that is, they appear more than once in the array. Show how to remove all duplicates from the array in time $O(n \log n)$.

4-) Consider the task of searching a sorted array $A[1, \dots, n]$ for a given element x : a task we usually perform by binary search in time $O(\log n)$. Show that any algorithm that accesses the array only via comparisons (that is, by asking questions of the form “is $A[i] \leq z$?”), must take $\Omega(\log n)$ steps.

5-) How many lines, as a function of n (in Θ (.) form), does the following program print? Write a recurrence and solve it. You may assume n is a power of 2.

```
function f(n)
    if n > 1:
        print_line("still going")
        f(n/2)
        f(n/2)
```

Note:

- * Your submissions will be handwritten
- * You can deliver your homework to TA Burak Koca until 17:00 on due date (room 119).
- * Do your homework personally, group studies will be considered as cheating.