# Modern Particle Physics Experiments

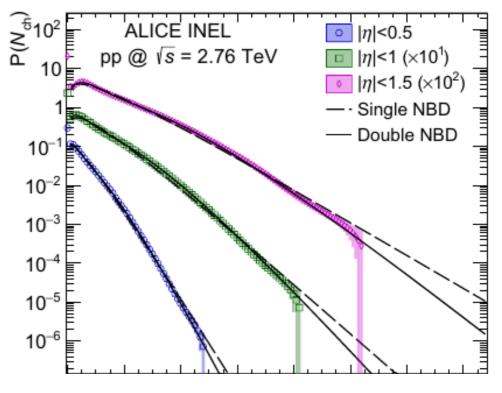




Many aspects of particle physics are of stochastic nature:

• final state properties in particle collisions:

- number of particles
- type of particles
- particle four-momenta



https://arxiv.org/abs/1509.07541

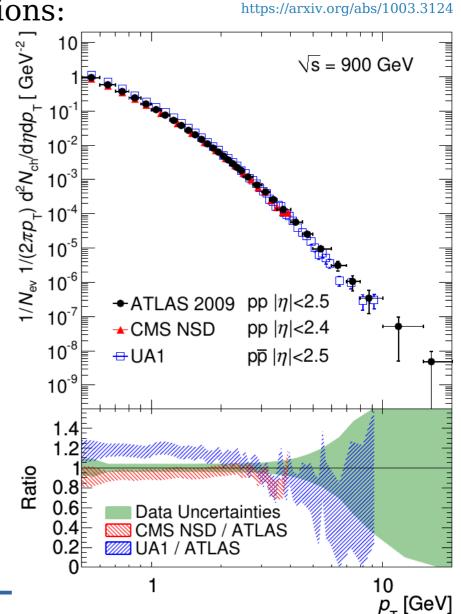




Many aspects of particle physics are of stochastic nature:

• final state properties in particle collisions:

- number of particles
- type of particles
- particle four-momenta

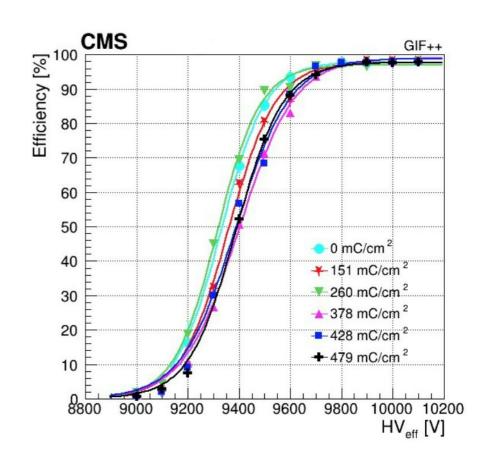






Many aspects of particle physics are of stochastic nature:

- response of the detector:
  - efficiency of
    - detector elements
    - trigger
    - reconstruction algorithms
  - difference of measured values from the true values (resolution)



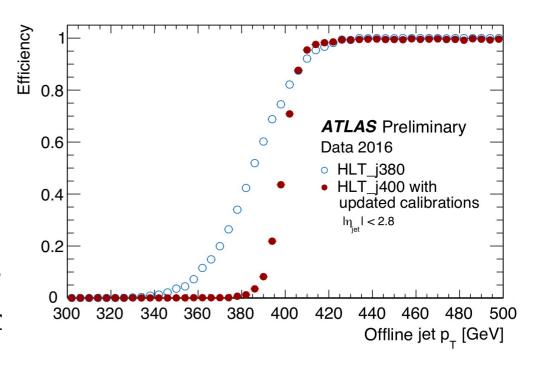
https://arxiv.org/abs/2005.11397





Many aspects of particle physics are of stochastic nature:

- response of the detector:
  - efficiency of
    - detector elements
    - trigger
    - reconstruction algorithms
  - difference of measured values from the true values (resolution



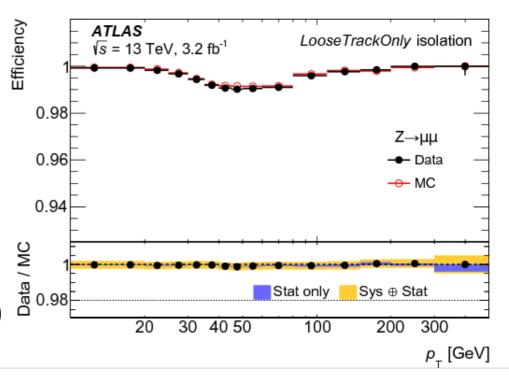
https://arxiv.org/abs/1711.02946





Many aspects of particle physics are of stochastic nature:

- response of the detector:
  - efficiency of
    - detector elements
    - trigger
    - reconstruction algorithms
  - difference of measured values from the true values (resolution)



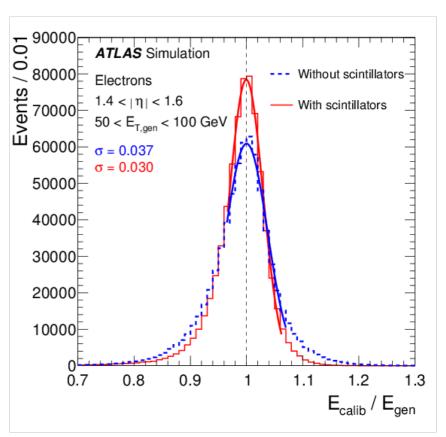
https://arxiv.org/abs/1603.05598





Many aspects of particle physics are of stochastic nature:

- response of the detector:
  - efficiency of
    - detector elements
    - trigger
    - reconstruction algorithms
  - difference of measured values from the true values (resolution)



https://arxiv.org/abs/1812.03848





Probability distribution, or probability density for results of particle interactions are proportional to differential cross sections:

$$\frac{d\sigma}{dN} = \dots, \quad \frac{d\sigma}{dp_T} = \dots, \quad \frac{d\sigma}{d\eta} = \dots$$

Probability distribution has to correctly normalized:

$$p(\eta) = \frac{1}{\sigma_{tot}} \frac{d\sigma}{d\eta}$$

total cross section
- normalization
constant

differential cross section - the distribution shape



### FIRST Electron spectrum from $\mu$ decay



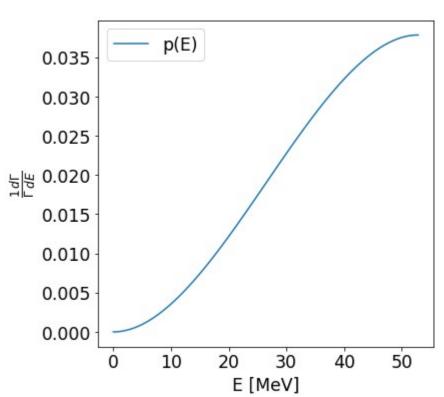
What is the probability distribution for the electron energy for electrons from muon decay?

• the differential decay width section is as follows:

$$\frac{d\Gamma}{dE_e} = \frac{G_F^2}{4\pi^3} m_{\mu}^2 E_e^2 \left(1 - \frac{4E_e}{3m_{\mu}}\right)$$

• the total decay width is as follows:

$$\Gamma_{\mu} = \frac{G_F^2 m_{\mu}^5}{192 \, \pi^3}$$



• the probability is:  $p(E)dE = \frac{1}{\Gamma} \frac{d\Gamma}{dE} dE$ 



### Event generation



How to generate fake dataset (energy values only for now) of electrons from  $\mu$  decay?

• draw numbers (energy values) from correct probability distribution. How? Let's look at cumulative distribution function (CDF):

$$F(x) = \int_{-\infty}^{x} p(x) dx, \quad 0 \le F(x) \le 1$$
$$p(x) = \frac{dF(x)}{dx}$$

•what is probability distribution for F(x)?



#### PHYSICS Probability distribution for CDF



$$P(x_{0} < x < x_{1}) = \int_{x_{0}}^{x_{1}} p(x) dx = \int_{F(x_{0})}^{F(x_{1})} p(F) dF$$

$$\int_{x_{0}}^{x_{1}} \frac{dF(x)}{dx} dx = \int_{F(x_{0})}^{F(x_{1})} \frac{dF}{dx} \left(\frac{dF}{dx}\right)^{-1} dF =$$

$$\int_{F(x_{0})}^{F(x_{1})} \frac{dF}{dx} \frac{dx}{dF} dF = \int_{F(x_{0})}^{F(x_{1})} \frac{dF}{dx} \left(\frac{dF}{dx}\right)^{-1} dF =$$

$$\int_{F(x_{0})}^{F(x_{1})} 1 dF$$

$$\int_{F(x_{0})}^{F(x_{1})} 1 dF$$

$$p(F) = \frac{dF}{dx} \left(\frac{dF}{dx}\right)^{-1} = 1$$

CDF has a flat distribution over [0,1] range.



### FACULTY OF How to generate a number from arbitrary distribution?



- 1) draw a random number z, from flat distribution in [0,1]
- 2) pretend this is a CDF value for your distribution at some x:

$$z = \int_0^x p(x) dx$$

3) calculate x using functional form of  $F^{-1}(z)$ :

$$x=F^{-1}(z)$$

**Problem:** F<sup>-1</sup>(z) is often not easy (or possible) to calculate.



#### Hit-or-miss method



- 1) draw the value of number of interest (e.g. energy, E) from flat distribution in desired range:  $[E_{min}, E_{max}]$
- 2) draw a second number, z, from flat distribution in [0,1]
- 3) calculate p(E)
- 4) accept the "event" if x < p(E)



## Materials



#### Review articles of probability and statistics on PDG portal:

The Review of Particle Physics

#### **Python packages:**

• Scikit-HEP Project