# Lecture 2: Causality, potential outcomes and experiments



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ECU 33091 Econometrics A Trinity College Dublin Michaelmas Term 2024 We are primarily interested in answering causal questions

## We are primarily interested in answering causal questions

- When thinking about causal Qs, it's often easier to split the problem in two
- Identification: what could we learn about the parameters we care about (causal effects) if we had the observable data for the entire population
  - Need to make assumptions about how observed outcomes relate to outcomes that would have been realized under different treatments
- **Statistics**: what can we learn about the full population that we care about from the finite sample that we have?
  - Need to understand the process by which our data is generated from the full population

- Sample: the data that you actually observe
  - A survey of students from Brown and URI graduates about their earnings

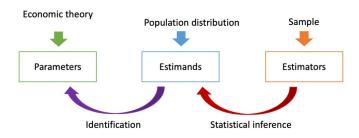
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- The process of learning about the *parameter* from the *estimand* is called **identification**.



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- ullet We can write the observed outcome as  $Y_i=D_i\,Y_i(1)+(1-D_i)\,Y_i(0)$

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- Example estimator:
  - Difference in sample mean of earnings for people who went to Brown and people who went to URI:

$$\underbrace{\frac{1}{N_1} \sum_{i:D_i=1} Y_i}_{i:D_i=1} Y_i \qquad - \underbrace{\frac{1}{N_0} \sum_{i:D_i=0} Y_i}_{i:D_i=0} Y_i$$

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- Example estimand:
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- Example target parameter:
  - Causal effect of Brown for Brown students:

$$E[Y_i(1)|D_i=1] - E[Y_i(0)|D_i=1]$$

Earnings at Brown for Brown students in pop 
Earnings at URI for Brown students in pop

- Thought experiment: suppose we had data on earnings for every Brown and URI graduate
- We can learn from the data:

$$\underbrace{E[Y_i(1)|D_i=1]}_{\text{Earnings at Brown for Brown Students}} \quad \text{and} \quad \underbrace{E[Y_i(0)|D_i=0]}_{\text{Earnings at URI for URI students}}$$

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The causal effect of Brown for Brown students is

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• The data doesn't tell us  $\underbrace{E[Y_i(0)|D_i=1]}_{\text{Earnings at URI for Brown Students}}. \text{ Why not?}$ 

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$$E[Y_i(0)|D_i=1]$$
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Earnings at URI for Brown Students

Because we never see Brown students going to URI!

• One idea to solve this problem would be to assume that:

$$\underbrace{E[Y_i(0)|D_i=1]}_{\text{Earnings at URI for Brown Students}} = \underbrace{E[Y_i(0)|D_i=0]}_{\text{Earnings at URI for URI Students}}$$

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- Why might this give us the wrong answer?
- Because Brown students may be different from URI students in other ways that would affect their earnings (regardless of where they went to college)
  - Academic ability, family background, career goals, etc.
- These differences are referred to as omitted variables or confounding factors

## What about experiments?

- The gold standard for learning about causal effects is a randomized controlled trial (RCT), aka experiment
- Suppose that the Brown and URI administration randomized who got into which college (assume these are the only 2 colleges for simplicity)
- Since college is randomly assigned, the only thing that differs between Brown and URI students is the college they went to
- Hence,

$$\underbrace{E[Y_i(0)|D_i=1]}_{\text{Earnings at URI for Brown Students}} = \underbrace{E[Y_i(0)|D_i=0]}_{\text{Earnings at URI for URI Students}}$$

since we've eliminated any confounding factors

## But running experiments is often hard/impossible

- Unfortunately, Brown/URI have not let us randomize who gets into which college
  - At least not yet! If you could convince them to do this, it'd make for a cool senior thesis!
- Likewise, it is difficult to convince states to randomize their minimum wages, or other policies
- In some cases, randomization is not just difficult but would be immoral
  - "What is the causal effect of spousal death on labor supply?"

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- In some cases, randomization is not just difficult but would be immoral
  - "What is the causal effect of spousal death on labor supply?"
- In this course, we'll discuss tools economists try to use when running experiments is not possible.

# Course Roadmap - Where we're going

- Part I ( $\sim$  7 lectures): Review of probability/statistics. This will give us a mathematical language to talk about:
  - Statistical estimation/inference: how does the sample we observe relate to the population of interest
  - 2 *Identification:* how do observable features of the population relate to (causal) parameters we care about

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- Part III (~ 7 lectures:) Other "quasi-experimental" strategies:
   We'll discuss other strategies for "mimicking" an experiment when it's
   not available, including instrumental variables (IV) and regression
   discontinuity (RD)