Algorithms and Complexity: Online session week 2

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1 Points on formative assignment

- Before trying to answer a question, make sure you understand it.
- Try and unpack the question. Expand on all assumptions you are given.
 - 1. Need to give a logspace TM that decides this language We are not expected to fully describe the Turing machine and work out the precise space usage or running time. The amount of detail seen in the model answer.
 - The worse case $WS_M(n) \leq c \cdot \log n$, this **must** hold for all bitstrings whether in the language or not.
 - 2. Suppose L is a language in **NP**. Then we want to show L is in PSPACE **Note: We must be sure to say 'we want to show' when talking about something we are yet to prove.

We have a polynomial p and a polytime machine M s.t. $\forall x \in \{0,1\}^*, x \in L \iff \exists u M(x,u) = 1$ where u is a bitstring whose length is p(|x|)

We want to show it is in PSPACE, so we want to provide a TM N that decides L and uses polynomial space.

Algorithm to decide whether $x \in L$:

Step 1. work out p(|x|)

Step 2. go through each bit string u of that length & check whether M(x,u)=1

Step 1: uses polynomial space.

Step 2: uses p(|x|) space to hold u, it reuses this same space for each u that we test. M uses polynomial time, we know that

anything that is polytime is polyspace! Therefore, overall we must be using polynomial space.

	n 5	6 7	8	9 10		
Is $f(n) \leq$	2g(n)?	No	Yes	Yes	No	
18 J (10) <u> </u>	- g(,,).	110	100	100	110	•••