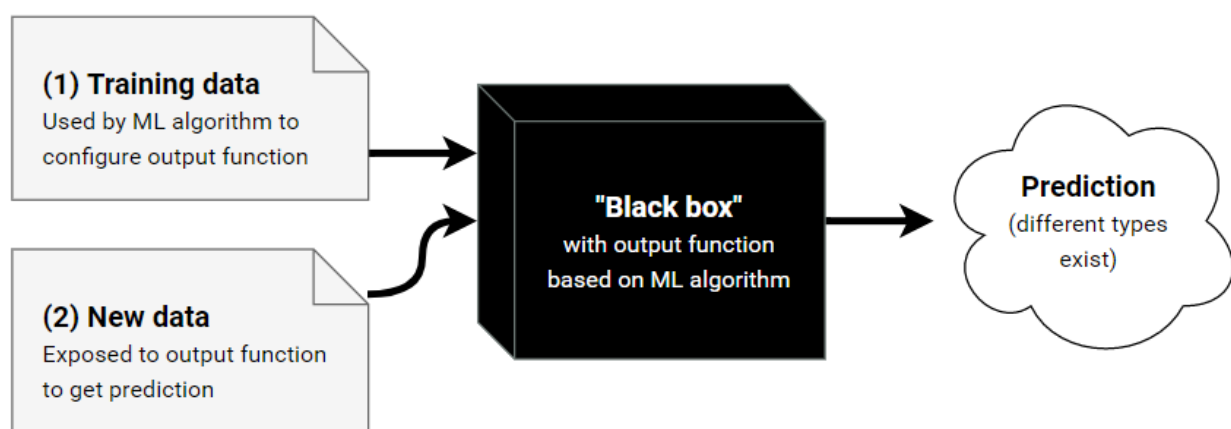


- Lecture 2
 - Linear Regression Models
 - Cat Hearts example:
 - Experience $\$E\$$
 - Learning Task, $\$T\$$
 - Linear Regression Model
 - Performance Measure, $\$P\$$

Lecture 2

Linear Regression Models



Cat Hearts example:

Experience $\$E\$$

- The dataset consists of n data points
 - $((x_1, y_1), \dots, (x_n, y_n)) \in \mathbb{R}^d \times \mathbb{R}$
 - $x_i \in \mathbb{R}^d$ is the "input" for the i^{th} data point as a feature vector with d elements, d being the # of dimensions in the feature space, in this case 1.
 - $y_i \in \mathbb{R}$ is the "output" for the i^{th} data point, in this case the weight of the corresponding cat heart.

Learning Task, $\$T\$$

- In this example, our task is: **Linear Regression**
- Find a "model", i.e. a function:
 - $f : \mathbb{R}^d \rightarrow \mathbb{R}$
- s.t. our future observations produce output "close to" the true output.

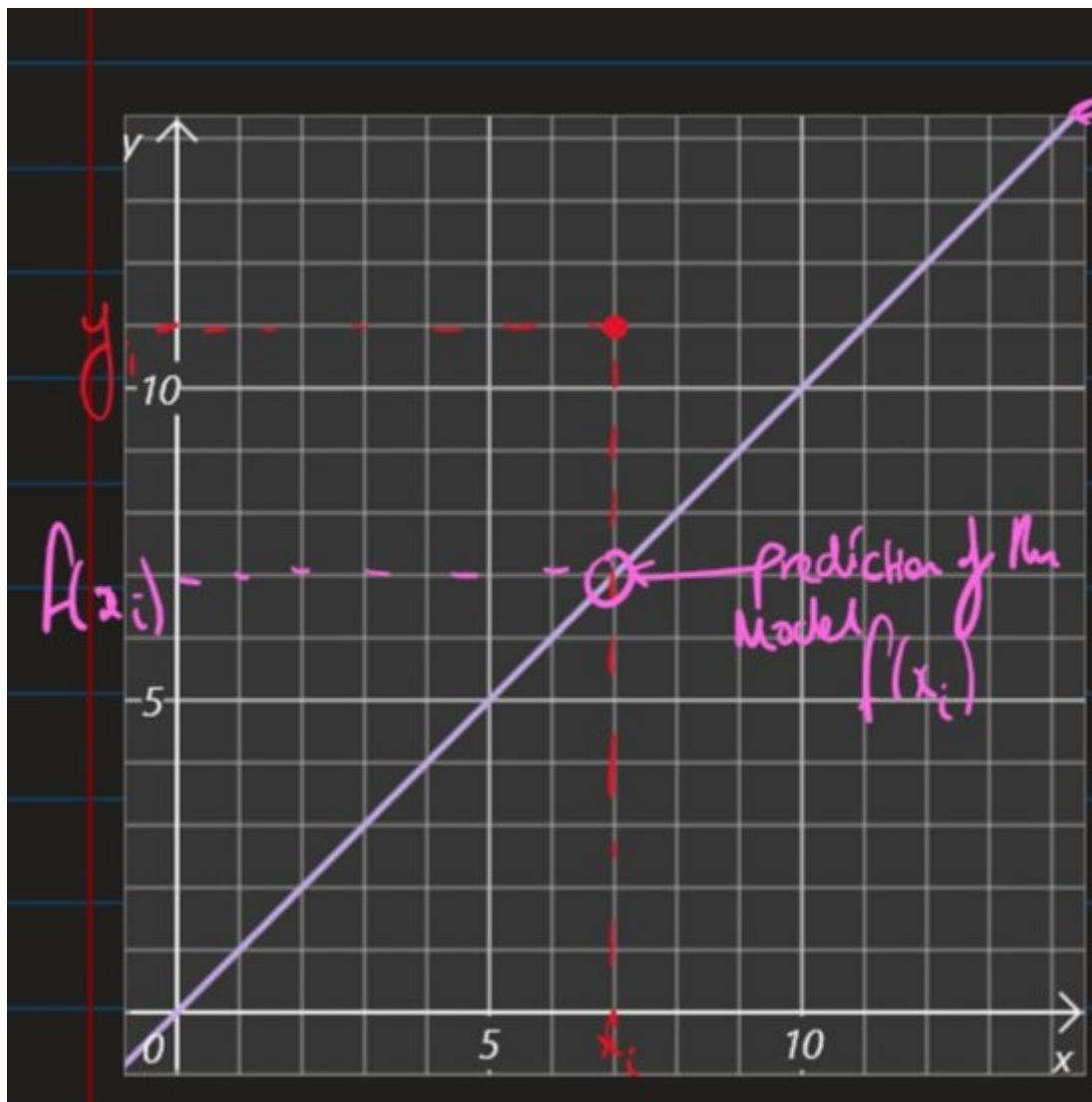
Linear Regression Model

- A linear regression model has the form:
 - $f(x) = (\sum_{i=1}^d w_i \cdot x_i) + b$
 - where:
 - $x \in \mathbb{R}^d$ is the input vector (feature)
 - $w \in \mathbb{R}^d$ is the weight vector (parameters)
 - $b \in \mathbb{R}$ is a bias (parameter)
 - $f(x) \in \mathbb{R}$ is the predicted output

- In our cat example we have:
 - $d=1$ as "body weight" is our only feature
 - $b=0$ as from intuition we expect a cat of 0 weight to have a heart of 0 weight.
 - Our model has one parameter: w

Performance Measure, J

- Want a function, $J(w)$ which quantifies the error in the predictions for a given parameter w



- The following empirical loss function, J takes into account the errors for all n data points.
 - $J(w) = (1/2N) \sum_{i=1}^N (y_i - wx_i)^2$
 - where the summation term is squared so that:

- we ignore the sign
- we penalise large errors more
- To find the optimum weight, solve:
 - $\frac{\partial J}{\partial w} = 0$