

# Assignment 2 - Vote Choice in Germany Statistical Inference and Modelling - SIM 1st Semester 2022

Ander Barrio Campos, Odysseas Kyparissis 2023-01-05

# Contents

1	Exp	lanatory Data Analysis - EDA									
	1.1	Loading Voting Data									
	1.2										
	1.3	Checking for Missing Data									
	1.4	Checking for Duplicates									
	1.5	5 Creating Factors for Qualitative Variables									
	1.6	· · · · · · · · · · · · · · · · · · ·									
	1.7	Univariate Descriptive Analysis - UDA									
		1.7.1 Descriptive Analysis for Numerical Variables									
		1.7.2 Standard Deviation									
		1.7.3 Descriptive Analysis for Categorial Variables									
		1.7.4 Bar Plots									
	1.8	Outliers Detection									
		1.8.1 Uni-variate Outliers									
		1.8.2 Multivariate Outliers									
	1.9	Profiling of Target Variable(s)									
	1.0	2 10111119 01 1011901 (0)									
<b>2</b>	Pol	ytomous Modelling 12									
	2.1	Nominal Polytomous Modeling									
		2.1.1 Comparison of Variables' Numerical and Categorical Representation 12									
		2.1.2 Final Nominal Model									
		2.1.2.1 Confusion Matrix and Metrics for Training Set									
		2.1.2.2 Confusion Matrix and Metrics for Testing Set									
	2.2	Ordinal Polytomous Modeling									
		2.2.1 Comparison of Variables' Numerical and Categorical Representation 19									
		2.2.2 Final Ordinal Model									
		2.2.2.1 Confusion Matrix and Metrics for Training Set									
		2.2.2.2 Confusion Matrix and Metrics for Testing Set									
	2.3	Hierarchical Modeling									
		2.3.1 First Layer of Hierarchical Approach									
		2.3.2 Second Layer of Hierarchical Approach									
		2.3.3 Confusion Matrix And Metrics for Training Set									
		2.3.4 Confusion Matrix And Metrics for Testing Set									
		20012 001111111111111111111111111111111									
3	$\mathbf{Bes}$	t Final Model 28									
4	$\mathbf{App}$	pendix 29									
	4.1	EDA									
	4.2	Profiling of Target Variable(s)									
	4.3	Modelling									
		4.3.1 Nominal Models									
		4.3.2 Ordinal Models									
		4.3.3 Hierarchical Models									
		4.3.4 Influential Data									

## 1 Explanatory Data Analysis - EDA

### 1.1 Loading Voting Data

In this part of the report, setting up the working environment and loading of the data into R are taking place. Additionally, a first look at the summary of the raw voting choice in Germany data set is taken.

```
load("gles.RData")
summary(gles)
```

```
##
        vote
                         egoposition_immigration
                                                       ostwest
                                                                     political_interest
    Length: 1000
##
                                 : 0.000
                                                    Min.
                                                            :0.000
                                                                     Min.
                                                                             :0.000
    Class : character
##
                         1st Qu.: 3.000
                                                    1st Qu.:1.000
                                                                     1st Qu.:2.000
##
    Mode
          :character
                         Median: 4.000
                                                    Median :1.000
                                                                     Median :3.000
##
                         Mean
                                 : 4.361
                                                    Mean
                                                            :0.759
                                                                     Mean
                                                                             :2.874
##
                                                    3rd Qu.:1.000
                                                                     3rd Qu.:4.000
                         3rd Qu.: 6.000
                                                            :1.000
##
                         Max.
                                 :10.000
                                                    Max.
                                                                     Max.
                                                                             :4.000
                          gender
##
         income
##
            :0.000
                             :0.000
    Min.
                      Min.
##
    1st Qu.:3.000
                      1st Qu.:0.000
##
    Median :3.000
                      Median : 0.000
##
            :2.906
                              :0.462
    Mean
                      Mean
    3rd Qu.:3.000
##
                      3rd Qu.:1.000
            :4.000
##
    Max.
                      Max.
                              :1.000
```

### 1.2 Data Types

To begin with, the types of the raw variables contained into the data set are being checked. It is clear, that the raw data set consists of 5 numerical variables and 1 categorical. On the one hand, based on the raw data types, the numeric variables are the following: egoposition\_immigration, ostwest, political\_interest, income and gender, while the categorical one is variable vote. On the other hand, if page 3 of the assignment statement (subsection Variables) is taken into account, all of the numerical variables correspond to qualitative concepts. In more detail, variables egoposition\_immigration, political\_interest and income (income-satisfaction) correspond to ordered factors, while ostwest and gender variables are binary ones. In the following sections, all the numerical variables will be transformed into labeled factors (ordered or not).

### 1.3 Checking for Missing Data

To continue with, a check for missing data is conducted on the raw data set. Considering the summary of the data set presented before, there are no NA values in the variables of the data set. The same conclusion is derived when a check is completed for each individual variable.

## 1.4 Checking for Duplicates

By checking if there are duplicate rows inside the raw data set, the result indicates that a total number of 359 occurrences of duplicates exist.

```
dupli <- duplicated(gles); dupli_ind <- which(dupli); length(dupli_ind)
## [1] 359</pre>
```

With the following command, a closer look can be taken into the values of the first 5 duplicate rows (for space saving reasons).

```
gles[dupli ind,][1:5,]
```

```
## # A tibble: 5 x 6
##
     vote
             egoposition immigration ostwest political interest income gender
##
     <chr>>
                                  <dbl>
                                           <dbl>
                                                                 <dbl>
                                                                         <dbl>
                                                                                  <dbl>
                                                                      3
                                                                              3
## 1 Gruene
                                       2
                                                                                      0
                                                1
## 2 SPD
                                       4
                                                1
                                                                      3
                                                                              3
                                                                                      1
## 3 Gruene
                                       4
                                                1
                                                                      3
                                                                              3
                                                                                      1
## 4 LINKE
                                       3
                                                0
                                                                      2
                                                                              3
                                                                                      1
## 5 FDP
                                       6
                                                1
                                                                      3
                                                                              3
                                                                                      0
```

By taking a closer look at the duplicates, one can understand that, it is logical people with the same characteristics to vote for the same party during the elections. For that reason, the duplicates are not removed or treated, but a new factor will be created in the dataset indicating if a row is a duplicate or not.

#### 1.5 Creating Factors for Qualitative Variables

In this subsection of EDA, all qualitative variables are transformed into labeled factors (nominal, ordinal and binary). All variables of the raw data set, as mentioned before, correspond to categorical ones. First of all, their unique values are presented below:

```
unique(gles$vote); unique(gles$egoposition_immigration); unique(gles$ostwest)
```

```
"CDU/CSU" "Gruene"
  [1] "FDP"
                 "SPD"
                                                "AfD"
                                                           "LINKE"
##
    [1]
               3
                 7
                     2
                        1
                                  6 10
        4
                           5 0
## [1] 1 0
```

unique(gles\$political interest); unique(gles\$income); unique(gles\$gender)

```
## [1] 3 2 1 4 0
## [1] 3 2 4 1 0
## [1] 0 1
```

The next step includes the creation of the labeled factors based on the unique values of the categorical variables. Following the practice below, in case a categorical variable includes NA values, they will be transformed into zeros, which is an incorrect approach. In this case, once missing values check indicated that there are no missing data, proceeding with this practice does not result in erroneous data.

Additionally, it is crucial to mention here that the following variables were transformed into ordered factors: income, political interest and egoposition immigration. Moreover gender, vote and ostwest variables were transformed to nominal factors and finally a new nominal factor was generated, named political\_orientation. This new variable discretize the 6 German parties into three political wings with labels Left Wing, Center Wing and Right Wing respectively. In order to accomplish this discretization, page 3 of the assignment statement (subsection Variables - indicating the character of each political party: left, center, right) was taken into account one more time.

In the Polytomous Modelling chapter of the report the generation of new factors for those variables is taking place as well.

#### 1.6 Factor Conversion Check

After checking both manually and by executing commands on the terminal, the conversion of the categorical and numerical variables to factors has been completed correctly. In addition, while the categorical variables *vote*, *ostwest* and *gender* have been transformed into labeled factors, their old versions are discarded from the data frame (in those cases it is sure that their numerical representation does not provide any extra information). The remaining variables were not discarded in order to check if better results could be obtained by using their numerical representation in higher powers (poly function). Below the new structure of the data frame is presented.

```
summary(gles)
```

```
##
    egoposition immigration political interest
                                                       income
                                                                           f.duplicate
##
    Min.
           : 0.000
                                      :0.000
                                                          :0.000
                                                                   No.Duplicate:641
                              Min.
                                                  Min.
    1st Qu.: 3.000
                              1st Qu.:2.000
                                                  1st Qu.:3.000
                                                                   Yes.Duplicate:359
##
    Median: 4.000
                              Median :3.000
                                                  Median :3.000
##
            : 4.361
##
    Mean
                              Mean
                                      :2.874
                                                  Mean
                                                          :2.906
##
    3rd Qu.: 6.000
                              3rd Qu.:4.000
                                                  3rd Qu.:3.000
##
    Max.
            :10.000
                              Max.
                                     :4.000
                                                  Max.
                                                          :4.000
##
##
            f.eastGermany f.gender
                                                    f.income
##
    No.EastGermany:241
                           M:538
                                     Low.Sat
                                                         : 13
                                     Low to Medium.Sat : 28
    Yes.EastGermany:759
                           F:462
##
##
                                     Medium.Sat
                                                         :188
##
                                     Medium_to_High.Sat:582
##
                                     High.Sat
                                                         :189
##
##
##
               f.political_interest
                                            f.egoposition_immigration
                                                                            f.vote
##
    Low.Inter
                             3
                                     4 Level.Imm
                                                          :179
                                                                        AfD
                                                                                : 69
    Low to Medium.Inter: 34
                                                                        CDU/CSU: 289
##
                                     5 Neutral Level.Imm:155
##
    Medium.Inter
                                     3 Level.Imm
                                                                        FDP
                          :308
                                                          :134
                                                                                :121
##
    Medium_to_High.Inter:396
                                     2 Level.Imm
                                                          :130
                                                                        Gruene:143
    High.Inter
                          :259
                                     6 Level.Imm
                                                          : 95
                                                                        LINKE
##
                                                                               :123
##
                                     7 Level.Imm
                                                          : 78
                                                                        SPD
                                                                                :255
##
                                     (Other)
                                                          :229
##
    f.political orientation
##
    Center Wing:665
    Left_Wing
               :266
##
##
    Right Wing: 69
##
##
##
##
```

## 1.7 Univariate Descriptive Analysis - UDA

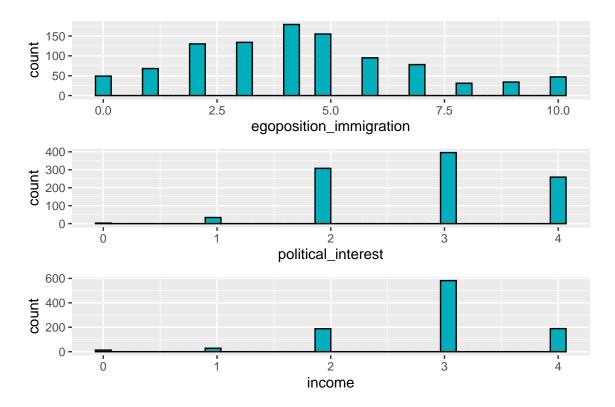
As it is stated in the assignment's statement, but as it was concluded in the previous subsection, data set is unbalanced and it contains individuals who mostly vote for parties belonging in the center wing of politics, followed by left wing and finally left wing respectively. The differences between the numbers of each wing are significant. More details are presented below.

#### 1.7.1 Descriptive Analysis for Numerical Variables

In this subsection, summary statistics, the standard deviation and histograms are presented for the numerical representation of the variables *egoposition\_immigration*, *political\_interest* and *income*.

#### 1.7.2 Standard Deviation

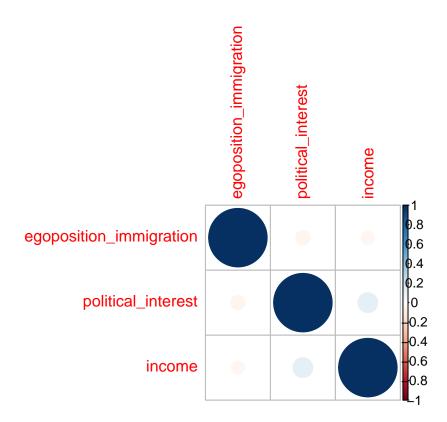
```
lapply(quantiData, sd)
## $egoposition_immigration
## [1] 2.490157
##
## $political interest
## [1] 0.8454814
##
## $income
## [1] 0.7731505
summary(gles$egoposition_immigration)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                 Max.
##
     0.000
              3.000
                      4.000
                               4.361
                                       6.000
                                               10.000
summary(gles$political_interest)
                                                 Max.
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
##
     0.000
              2.000
                      3.000
                                       4.000
                               2.874
                                                4.000
summary(gles$income)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                 Max.
##
     0.000
              3.000
                      3.000
                               2.906
                                       3.000
                                                4.000
```



From the histograms, it is clear that those 1000 German citizens show interest in the political elections since most of the observations belong to categories *Medium* to *High*. The same is true for variable *income* which depicts the satisfaction of the citizens with their income. Concerning variable *egoposition\_immigration* it can be seen that the plot is close to follow a normal distribution with a slight right skewness. This means that most of the citizens in the data set are *Neutral* concerning immigration while the rest of them are scattered through the rest of the variable levels, with a small trend to follow more open ideas for immigration issues.

In addition, the calculation of Spearman correlation is presented for the numerical variables. In the following graph, it is clear that there is not strong correlation between the numerical representation of the variables *egoposition\_immigration*, *political\_interest* and *income*. By checking the correlation matrix the values are extremely low.

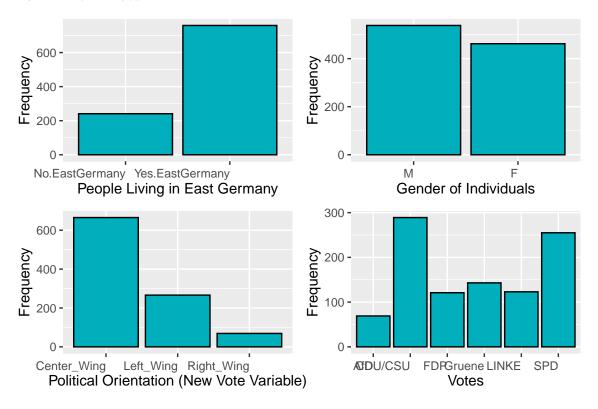
##		egoposition_immigration	<pre>political_interest</pre>	income
##	egoposition_immigration	1.0000000	-0.05861542	-0.04823165
##	political_interest	-0.05861542	1.00000000	0.11449194
##	income	-0.04823165	0.11449194	1.00000000



#### 1.7.3 Descriptive Analysis for Categorial Variables

Moreover, bar plots are generated illustrating the content of the variables ostwest, gender and target variables vote and political\_orientation (new derived factor containing left, center and right wings).

#### 1.7.4 Bar Plots



From the barplots, it is illustrated that most of the observations are from citizens of the Eastern

Gemany, while the gender of them are balanced. In addition, there is a huge difference in the numbers of citizens voting for parties in the center political wing while a smaller number of them vote for the left wing and finally the right one. Finally, party wise, the one with the most votes is party CDU/CSU, followed by SPD with a small difference. At the same time Gruene, LINKE and FDP are pretty close with each other, but with approximately half of the votes of CDU/CSU and SPD.

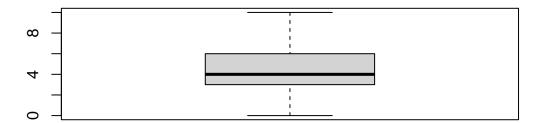
#### 1.8 Outliers Detection

In the following subsections both uni-variate and multivariate outliers will be detected and treated.

#### 1.8.1 Uni-variate Outliers

To start with, in the following subsection the uni-variate outliers will be detected for the numerical variables: *egoposition\_immigration*, *political\_interest* and *income* with the respective order. It is crucial to mention here, that only severe outliers were taken into account and not mild ones. Now, concerning variable *egoposition\_immigration*, as it is depicted in the boxplot of the variable, outliers do not exist. The same result is derived after trying to detect outliers using the IQR method, which is implemented by function calcQ.

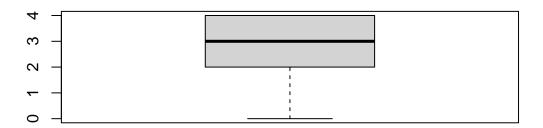
### **Boxplot of Variable Egoposition Inmigration**



**##** [1] 0

Following by, the same approach is used for variable *political\_interest*.

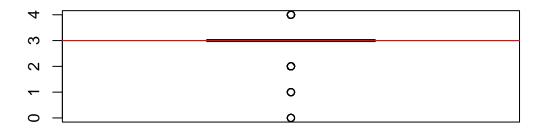
### **Boxplot of Variable Political Interest**



#### ## [1] 0

The results are the same, there are no severe outliers for variable *political\_interest* as well. Finally, the outlier detection for the income is taking place.

### **Boxplot of Variable Income**



#### ## [1] 418

In this case, there are extreme outliers for the income variable, which are presented below (only first 10 rows out of 418 in total).

```
gles[llout_income,][1:10,]
```

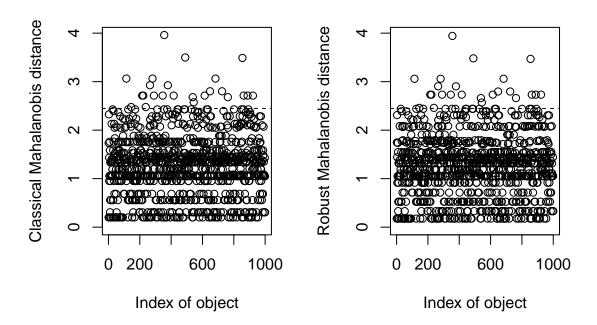
```
## # A tibble: 10 x 11
      egopo~1 polit~2 income f.dup~3 f.eas~4 f.gen~5 f.inc~6 f.pol~7 f.ego~8 f.vote
##
        <dbl>
                 <dbl>
                        <dbl> <fct>
                                       <fct>
                                                                <ord>
                                                                         <ord>
##
                                                        <ord>
            8
                     2
##
    1
                            2 No.Dup~ No.Eas~ F
                                                        Medium~ Medium~ 8_Leve~ SPD
##
    2
            1
                     2
                            4 No.Dup~ Yes.Ea~ F
                                                        High.S~ Medium~ 1 Leve~ Gruene
            2
                     4
                            4 No.Dup~ Yes.Ea~ F
                                                        High.S~ High.I~ 2 Leve~ Gruene
##
    3
    4
            3
                     3
                            2 No.Dup~ Yes.Ea~ M
                                                        Medium~ Medium~ 3_Leve~ AfD
##
    5
            4
                     4
                            4 No.Dup~ Yes.Ea~ M
                                                        High.S~ High.I~ 4_Leve~ CDU/C~
##
                     2
            4
                            2 No.Dup~ No.Eas~ F
                                                        Medium~ Medium~ 4 Leve~ SPD
    6
##
```

```
7
            3
                    3
##
                            2 No.Dup~ Yes.Ea~ M
                                                       Medium~ Medium~ 3_Leve~ CDU/C~
##
            1
                    3
                            1 No.Dup~ Yes.Ea~ F
                                                       Low to~ Medium~ 1 Leve~ SPD
    8
##
    9
            5
                    4
                            1 No.Dup~ Yes.Ea~ M
                                                       Low to~ High.I~ 5 Neut~ FDP
## 10
            5
                    2
                            2 No.Dup~ Yes.Ea~ F
                                                       Medium~ Medium~ 5 Neut~ Gruene
     ... with 1 more variable: f.political_orientation <fct>, and abbreviated
##
       variable names 1: egoposition immigration, 2: political interest,
##
  #
       3: f.duplicate, 4: f.eastGermany, 5: f.gender, 6: f.income,
## #
       7: f.political_interest, 8: f.egoposition_immigration
table(gles$income)
```

Additionally, by taking a look at the figure and the table of occurrences for factor variable *income*, it is clear that by using the IQR method in this case, all categories except *Medium\_to\_High.Sat* (level 3) are considered outliers (13+28+188+189 = 418). For that reason, a new column is generated to indicate the uni-variate outliers for *income*. For now, those outliers are kept into the data set, and in the subsections below, it will be decided if it is necessary to be removed.

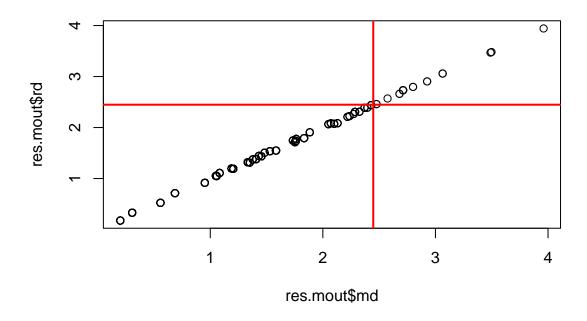
#### 1.8.2 Multivariate Outliers

In this subsection, an attempt for the detection of multivariate outliers took place. To start with, the calculation of the Mahalanobis distance is possible only for numerical variables. At this point, at first, an attempt to calculate the Mahalanobis distance for the numerical representation of egoposition\_immigration, political\_interest and income with a confidence interval of 95% was followed. Due to the fact that those variables create a singular matrix for the calculation of the Mahalanobis distance, its inverse matrix cannot be calculated and in that way an error is thrown. Additionally, an attempt was completed to calculate the distance for all the variables in their raw format (all variables at numerical representation), but the same problem occurred again. The Classical and Robust Mahalanobis distances could be only calculated for the combination of egoposition\_immigration and political\_interest variables of the data set. The results are presented in the following figure:



After calculating Mahalanobis distance at a 95% confidence interval, the cut off given is 2.447747.

Then, all the observations which have a classical and a robust distance bigger than this cut off are marked as multivariate outliers (in this case the term *multivariate* refers only to *egoposition\_immigration* and *political\_interest* variables). After detecting them, a new factor (*f.mout*) is being created in the data set, indicating if an observation belongs to multivariate outliers or not. It can be seen in the final result that 24 observations are marked as multivariate outliers. Further analysis about them will be conducted in the following sections.



## f.mout

## MvOut.No :976 ## MvOut.Yes: 24

### 1.9 Profiling of Target Variable(s)

The goal of this chapter is to discover the relationships between the explanatory variables of the data set and the target variable(s). In order to do so the calculation and presentation of interactions between the target and explanatory variables by using the library FactoMineR and Boxplots is completed.

Moreover, with the usage of the library FactoMineR and specifically the function catdes, which calculate the dependencies of a categorical variable, it is able to check the dependencies of the target variable(s) with the explanatory variables of the data set. At first, the dependency between the target variable *f.vote* and the rest of the variables will take place, followed by the same analysis for the new derived target variable *f.political\_orientation*. Profiling is completed only by using the factor representation of the explanatory variables and the results are presented in the Appendix at the same subsection.

The main conclusions derived from profiling the target variables are presented here, starting from target variable *f.vote* following by the second target variable *f.vote* the main conclusions are:

- Party AfD (right wing) is strongly correlated with citizens who have high values for variable egoposition\_imigration (8-10) meaning they have more far-right beliefs, they are mainly males with low\_political\_interest and low\_to\_medium salary satisfaction.
- Party CDU/CSU (center-right) has strong relationship with people who are achieve levels 5 to 7 of egoposition\_imigration meaning that they are mainly neutral with a slight orientation to right beliefs for immigration issues, while they present medium political interest and medium salary satisfaction.
- Party **FDP** (center-right) have strong connection levels 0, 2 and 6 of egoposition\_imigration, which is confusing. In this case, the conclusion is that maybe the data set does not contain data that will provide quality explanatory power for predicting the voting of this party.
- Party **Gruene** (*left*) shows strong relation with level 2 of variable *egoposition\_imigration*, which means that they are open for immigration issues. Additionally, most of the citizens voting this party are females with *medium\_to\_high political interest*.
- Party LINKE (left) is mainly described by observations containing values of No.EastGermany for variable f.eastGermany, level 0 (Very Open) for variable egoposition\_imigration and medium income satisfaction. Also, value Yes.EastGermany appear a lot for this party, so it can concluded that variable f.eastGermany will not provide explanatory power for predicting this party.

For variable f. political orientation the main conclusions are:

- Center Political Wing is mainly described by level 5 of variable egoposition\_imigration (Neutral), people from East Germany (Yes.EastGermany for variable f.eastGermany), high income satisfaction and medium political interest.
- Left Political Wing is strongly connected with levels 0, 2 and 3 of variable egoposition\_imigration meaning that it is open to immigration issues, and high salary satisfaction

(Not sure if this makes sense, but we have no information for demographics and salaries of people voting left parties in Germany).

• Right Political Wing is mainly connected with levels 8 and 10 for egoposition\_imigration (far-right beliefs). Also, those observations are strongly connected with observations of males, with value No.EastGermany for f.eastGermany variable, with low political interest and low to medium salary satisfaction.

Concerning the profiling of target variables with quality metrics of the data set, like number of missing values, number of errors in data, number of univariate or multivariate outliers, is not included in detail while the data set do not contain missing or erroneous data. For the correlation of the target variables with outliers some results are presented during the profiling done by using FactoMineR (presented in Appendix) but the results are not so insightful.

## 2 Polytomous Modelling

In this section of the report, the creation and comparison of multiple models for the prediction of probabilities for voting each party or each political wing is completed. For the sake of this assignment, the goal is to provide three final models following the approaches: nominal response, ordinal response and hierarchical approach. In order to do so, for nominal response model, the variable f.vote containing the 6 different parties will be used. For ordinal response model, f.vote factor will be transformed to an ordinal factor creating an ordinal relationship from far-left parties to far-right ones. More specifically, the order is the following (f.vote\_ord) - the specific order was chosen based on page 3 of assignment's statement:

• LINKE > Gruene > SPD > FDP > CDU/CSU > AfD

Finally, for the hierarchical approach the target variable will be *f.political\_orientation* and in this case 2 nested binary outcome models will be created.

Before proceeding to modeling chapters, the split of the data set into training and test set is necessary and is conducted here.

### 2.1 Nominal Polytomous Modeling

#### 2.1.1 Comparison of Variables' Numerical and Categorical Representation

As a first step in this subsection, it is necessary to check if variables *egoposition\_immigration*, *political\_interest* and *income* provide better explanatory power when they are used as numerical or categorical variables. In order to do so, the following approach has been used:

- 1. Train a nominal polytomous target model containing only one of those variables in a continuous representation.
- 2. Train a nominal polytomous target model containing only one of those variables in a continuous representation, including second, cube and quadratic exponent of the variable.
- 3. Train a nominal polytomous target model containing only one of those variables in a categorical representation.
- 4. Derive new factor for each variable by combining some levels of the already existed factors, and train a new model with it. The new levels are chosen below, based on the allEffects plots.

- 5. Compare those 6 models and the NULL model for each variable by using anova for nested models reduction of deviance, Anova and AIC.
- 6. Keep each variable's representation that provide the best results in each case.

The results of the analysis are presented in the respective subsection of the Appendix for space saving reasons. Finally, during modelling procedure the above-mentioned variables will be used in the following forms, respectively:

• egoposition\_immigration: the new derived factor f.Imm will be used to represent this variable. In this case, the reduction in deviance is approximately equal to 172 units, the second biggest reduction after 224 units belonging to the original factor of the variable containing 10 levels. To continue with, by checking the explanatory power of the variable with Anova function, one can understand that it provides explanatory power to the model, in all of the forms (Appendix). Finally, by checking the allEffects plots for all the 5 models and the AIC comparison of them presented below, it is clear that f.Imm representation provides the better model.

```
## [1] 224.1982
## [1] 172.0104
##
                   df
                            AIC
## nm0
                    5 2378.556
                   10 2256.832
## nm1 imm con
                   15 2253.027
## nm1 imm con sq
## nm1 imm con cb
                   20 2246.187
## nm1 imm con qd
                   25 2247.456
## nm1 imm cat
                    55 2254.358
## nm1 imm cat new 25 2246.546
```

• political\_interest: poly(political\_interest,2), even if the squared form of this variable does not provide significant explanatory power (null model had pretty much the same predictability). For picking this representation of this variable the same approach as before has been followed. AIC values for the 5 models are presented here, the remaining analysis can be found in Appendix. The only reason for using this variable in the squared form is that function Anova, indicates that the squared form of political\_interest has a p-value smaller of 0.05, thus null hypothesis can be rejected.

```
##
                       df
                               AIC
## nm0
                        5 2378.556
## nm1 polint con
                       10 2381.750
## nm1 polint con sq
                       15 2377.448
## nm1 polint con cb
                       20 2378.197
## nm1 polint con qd
                       25 2385.561
## nm1_polint_cat
                       25 2385.557
## nm1_polint_cat_new 15 2388.672
```

• *income*: the continuous representation (*income*) of first order will be used to represent this variable.

```
## nm0 df AIC
## nm0 5 2378.556
## nm1_inc_con 10 2370.628
## nm1 inc con sq 15 2374.321
```

```
## nm1_inc_con_cb 20 2377.178
## nm1_inc_con_qd 25 2386.675
## nm1_inc_cat 25 2386.663
## nm1 inc cat new 20 2386.946
```

#### 2.1.2 Final Nominal Model

## CDU/CSU

Once multiple different combinations of main effects and interactions of factors and the squared form of the numerical variable have been tested, the final model is presented below.

```
summary(nm final)
## Call:
## multinom(formula = f.vote ~ poly(political interest, 2) + income +
       f.Imm + f.eastGermany + f.gender, data = train)
##
##
## Coefficients:
##
             (Intercept) poly(political_interest, 2)1 poly(political_interest, 2)2
            -0.09257836
                                             -5.941845
## CDU/CSU
                                                                           -0.8135103
## FDP
           -13.10876866
                                             -4.007060
                                                                            3.6417160
## Gruene
             0.51181473
                                              1.087766
                                                                           -8.9035984
## LINKE
             3.11883232
                                             -0.199091
                                                                            1.0482878
## SPD
             1.07507231
                                              3.036173
                                                                           -6.5510538
##
                income f.Immlow_medium f.Immmedium f.Immmedium_high f.Immhigh
## CDU/CSU
            0.30897594
                              0.3794200
                                           1.0741356
                                                             -1.614876 -1.641185
## FDP
            0.11260568
                             12.6063799
                                          13.7919676
                                                             10.909124 10.608670
                                                             -4.885834 -4.289655
## Gruene
            0.16462317
                              0.2443429
                                          -0.4785748
## LINKE
           -0.41228020
                             -0.5678470
                                          -1.0749778
                                                             -4.304691 -3.474082
## SPD
           -0.05034817
                              0.4244623
                                           0.2317975
                                                             -2.549853 -2.465248
##
           {\tt f.eastGermanyYes.EastGermany\ f.genderF}
## CDU/CSU
                               0.8480695
                                          1.505285
## FDP
                               1.0859395
                                         1.327414
## Gruene
                               0.7535584
                                          1.970332
## LINKE
                               0.2418049
                                           1.588901
## SPD
                               0.9076119
                                          1.800443
##
## Std. Errors:
           (Intercept) poly(political_interest, 2)1 poly(political_interest, 2)2
##
## CDU/CSU
                                             4.567882
             1.3140067
                                                                            4.118287
## FDP
             0.6787106
                                             5.003145
                                                                            4.386609
             1.3574759
                                             5.469624
                                                                            5.342217
## Gruene
## LINKE
             1.3003537
                                             5.120422
                                                                            4.653212
## SPD
             1.3022998
                                             4.925334
                                                                            4.735253
##
              income f.Immlow_medium f.Immmedium f.Immmedium_high f.Immhigh
## CDU/CSU 0.2396515
                            1.1883878
                                         1.1701492
                                                           1.1253464 1.2027647
## FDP
           0.2640849
                                         0.4208022
                                                           0.3719566 0.5937215
                            0.4983665
## Gruene
           0.2702383
                            1.1700810
                                         1.1623876
                                                           1.3060775 1.5229222
## LINKE
           0.2580925
                            1.1534082
                                                           1.1508066 1.2338791
                                         1.1433739
## SPD
           0.2447612
                            1.1670464
                                         1.1536762
                                                           1.1165164 1.2146920
##
           f.eastGermanyYes.EastGermany f.genderF
```

0.3742758 0.4247466

## FDP 0.4389828 0.4618531 ## Gruene 0.4317185 0.4633330 ## LINKE 0.4172363 0.4637351 ## SPD 0.3919844 0.4346765

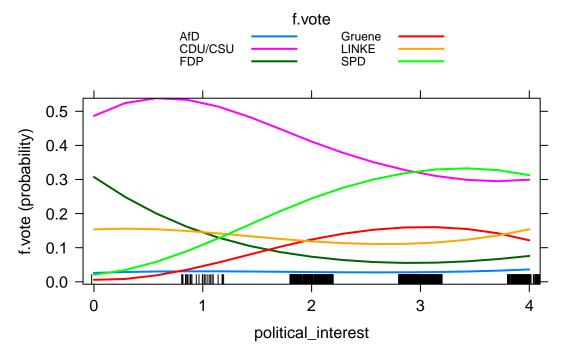
##

## Residual Deviance: 2119.625

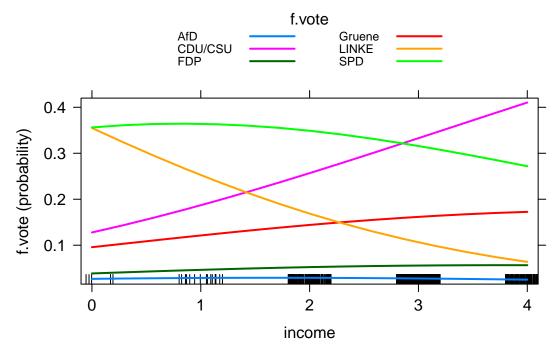
## AIC: 2219.625

From the summary of the final nominal model, after executing the step function on the model containing all main effects and interactions of the factors and the numerical variables it can be concluded that the formula contains only the main effects of factors f.Imm, f.eastGermany, f.gender, the squared form of the numerical representation of variable political\_interest and finally the first order of variable income (numerical representation). Concerning the target variable f.vote, the party AfD is being used as the baseline category and then all the odds for the remaining parties are calculated based on this baseline category, as we have seen it in theory and labs sessions. The following plots indicate how the explanatory variables fluctuate throuhgout the different parties of the target variable. By the allEffects plot it is clear that the available explanatory variables are not enough to distinguish well the voting preferences of the German citizens.

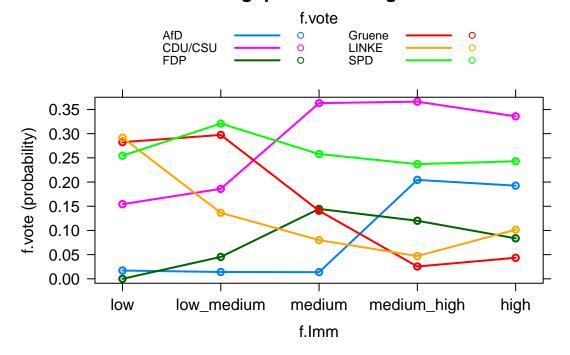
#### **Effects of Political Interest**



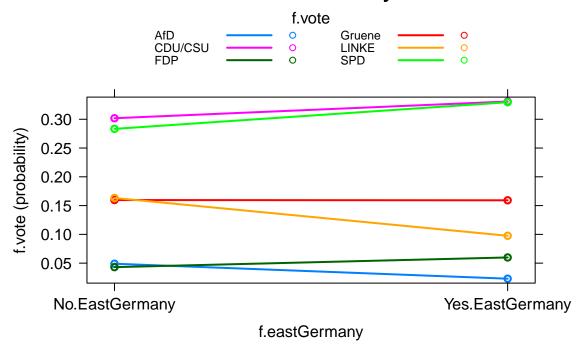
## **Effects of Income**



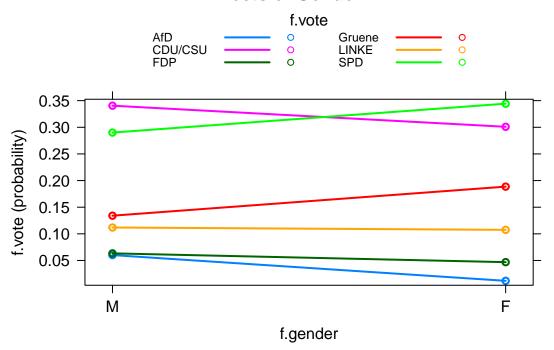
# **Effects of Egoposition Immigration**



### **Effects of East Germany**



#### **Effects of Gender**



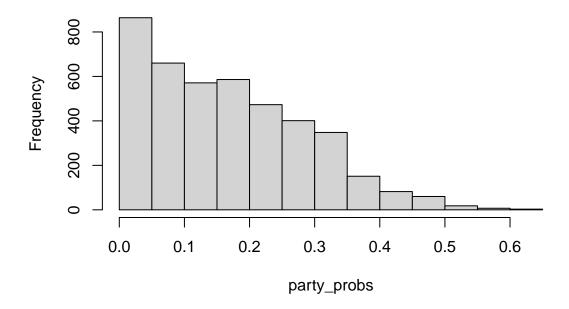
Finally, validation measures and graphs are generated for training and testing set here. Mainly, the confusion matrix has been used to calculate the accuracy, recall and precision of the model, while AUC plots have been generated as well. It can be seen that both training and testing set *FDP*, *Gruene* and *LINKE* cannot be predicted correctly. For those parties we need more variables that could distinguish them from the other parties.

**2.1.2.1** Confusion Matrix and Metrics for Training Set Here the confusion matrix and the appropriate metrics are presented for the training set.

```
##
              AfD CDU/CSU FDP Gruene LINKE SPD
##
##
     AfD
               15
                        11
                              6
                                      0
                                            4
                                                 6
     CDU/CSU
               25
                             57
                                     36
                                           32
                                                79
##
                       144
     FDP
                                      0
##
                1
                          0
                              0
                                            0
                                                 0
     Gruene
                0
                        12
                              3
                                     22
                                            8
                                                20
##
     LINKE
                              3
##
                1
                          8
                                     11
                                            17
                                                12
                             13
##
     SPD
                6
                        36
                                     37
                                           27
                                                52
## [1] "Accuracy:"
## [1] 35.51136
## [1] "Precision:"
##
          AfD
                CDU/CSU
                                FDP
                                        Gruene
                                                    LINKE
                                                                  SPD
## 0.3571429 0.3860590 0.0000000 0.3384615 0.3269231 0.3040936
## [1] "MissClassification Rate:"
## [1] 64.48864
```

Moreover, the plot below depicts the distribution of the predicted probabilities for the training set.

### Histogram of party\_probs



**2.1.2.2** Confusion Matrix and Metrics for Testing Set Here the confusion matrix and the appropriate metrics are presented for the testing set.

##							
##		${\tt AfD}$	CDU/CSU	FDP	${\tt Gruene}$	LINKE	SPD
##	AfD	9	5	3	0	2	3
##	CDU/CSU	10	53	25	17	14	37
##	FDP	1	0	0	0	0	0

```
##
     Gruene
                0
                         4
                             1
                                     9
                                            5
                                               10
     LINKE
                                     2
                0
                         4
                             1
                                            4
                                                8
##
##
     SPD
                1
                        12
                             9
                                     9
                                           10
                                               28
  [1] "Accuracy:"
##
   [1] 34.7973
   [1] "Precision:"
##
         AfD
                CDU/CSU
                                FDP
                                                    LINKE
                                                                 SPD
                                       Gruene
## 0.4090909 0.3397436 0.0000000 0.3103448 0.2105263 0.4057971
   [1] "MissClassification Rate:"
## [1] 65.2027
```

### 2.2 Ordinal Polytomous Modeling

#### 2.2.1 Comparison of Variables' Numerical and Categorical Representation

In this chapter, target variable will be f.vote\_ord which contains the parties in an ordered factor starting from far-left parties to far-right ones. The same approach that has already been followed for nominal models will be applied here as well, in order to generate the optimal model based on the available explanatory variables. The baseline category in this case is party LINKE and it can be seen from the table of the new target variable. Consequently, all odds and cumulative probabilities will be calculated by the model, taking party LINKE as the first reference value of the target variable and continuing with the order indicated by the table below.

#### table(train\$f.vote\_ord)

```
## ## LINKE Gruene SPD FDP CDU/CSU AfD ## 88 106 169 82 211 48
```

The inclusion of different variables and the comparison of the models is taking place in the Appendix for space saving reasons. Below the final model and the validation phase are presented.

From the reduction of deviance and the comparison of the AIC for the different representations of the variable *egoposition\_immigration*, the same conclusions are derived with the analysis for the Nominal Models. Thus, again variable *egoposition\_immigration* will be used with the format of the new vector generated (*f.Imm*). The results are presented here:

```
om0$dev - om1_imm_cat$dev
## [1] 121.6457
om0$dev - om1 imm cat new$dev
## [1] 111.2882
##
                    df
                            AIC
                     5 2378.556
## om0
## om1_imm_con
                     6 2279.716
                     7 2280.979
## om1 imm con sq
                     8 2277.012
## om1 imm con cb
## om1_imm_con_qd
                     9 2277.038
```

```
## om1_imm_cat 15 2276.911
## om1 imm cat new 9 2275.268
```

Moreover, for variable **political\_interest**, as shown below, the lowest AIC value is achieved for the squared form of the numerical representation of the variable, which is approximately the same with the AIC achieved by the new factor generated. Nevertheless, in this case Anova function does not indicate that any of those forms of the variable provide any explanatory power. Thus, in the following analysis, it is anticipated that when full model (with all effects and interactions) will be given as input to the step function will lead to the deletion of this variable.

```
##
                       df
                               AIC
                        5 2378.556
## om0
## om1 polint con
                        6 2377.571
## om1_polint_con_sq
                        7 2377.477
## om1_polint_con_cb
                        8 2379.323
## om1 polint con qd
                        9 2378.822
## om1 polint cat
                        9 2378.822
## om1 polint cat new
                       7 2377.716
```

Finally, for variable *income*, following the same analysis, taking into account the AIC values presented below, the lowest value is achieved when variable *income* is used in a squared form. On the other hand, while using the Anova function (Appendix), only the 1st order and the 2nd order of the variable have a p-value smaller than 0.05. Moreover, when comparing the models of 1st order and 2nd order with anova function, the result indicates that model with 1st order of the variable is better (p-value > 0.05, simpler model is better). For this reason, the first order of variable *income* will be used in this case.

```
##
                            AIC
                     5 2378.556
## om0
## om1 inc con
                     6 2375.977
## om1_inc_con_sq
                     7 2375.961
## om1 inc con cb
                     8 2377.332
## om1 inc con qd
                     9 2379.329
## om1 inc cat
                     9 2379.329
## om1 inc cat new
                    8 2377.488
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote ord
               Model Resid. df Resid. Dev
##
                                              Test
                                                      Df LR stat.
                                                                     Pr(Chi)
## 1
                            698
                                  2363.977
              income
## 2 poly(income, 2)
                                  2361.961 1 vs 2
                                                       1 2.016053 0.1556432
                            697
```

#### 2.2.2 Final Ordinal Model

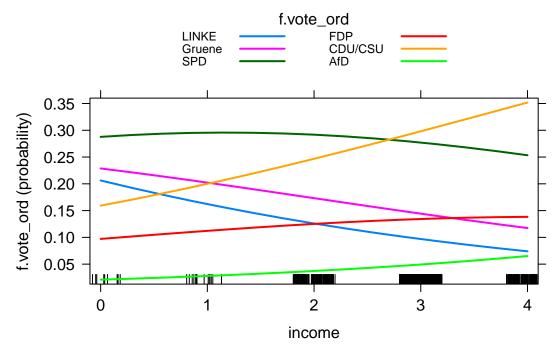
Once multiple different combinations of main effects and interactions of factors and the squared form of the numerical variable have been tested, the final model is presented below.

```
##
## Re-fitting to get Hessian
## Call:
## polr(formula = f.vote_ord ~ poly(political_interest, 2) + income +
```

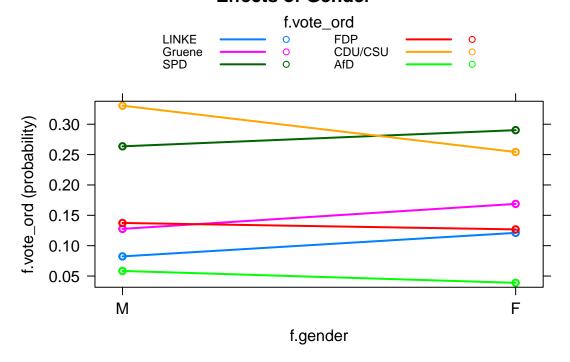
```
##
       f.Imm + f.gender + poly(political_interest, 2):f.Imm, data = train)
##
## Coefficients:
##
                                                      Value Std. Error t value
## poly(political interest, 2)1
                                                               9.07021 -1.9846
                                                   -18.0008
## poly(political interest, 2)2
                                                     7.4740
                                                               9.04420 0.8264
## income
                                                     0.2949
                                                               0.09026
                                                                         3.2678
## f.Immlow_medium
                                                               0.33884
                                                     0.5918
                                                                        1.7466
## f.Immmedium
                                                     1.4948
                                                               0.33865
                                                                        4.4140
## f.Immmedium high
                                                     2.7165
                                                               0.38027
                                                                         7.1437
## f.Immhigh
                                                     2.4998
                                                               0.48377
                                                                         5.1674
## f.genderF
                                                               0.13942 -3.0771
                                                    -0.4290
## poly(political interest, 2)1:f.Immlow medium
                                                    13.6415
                                                               9.57548
                                                                        1.4246
## poly(political_interest, 2)2:f.Immlow_medium
                                                     2.3692
                                                               9.51472
                                                                         0.2490
## poly(political_interest, 2)1:f.Immmedium
                                                    11.4960
                                                               9.48140
                                                                        1.2125
## poly(political interest, 2)2:f.Immmedium
                                                               9.61089 -1.0276
                                                    -9.8759
## poly(political interest, 2)1:f.Immmedium high
                                                    17.3725
                                                              10.21368
                                                                         1.7009
## poly(political interest, 2)2:f.Immmedium high -12.7432
                                                              10.10649 -1.2609
## poly(political interest, 2)1:f.Immhigh
                                                    37.5684
                                                              12.92239
                                                                         2.9072
## poly(political interest, 2)2:f.Immhigh
                                                    -7.2629
                                                              13.03251 -0.5573
##
## Intercepts:
##
                          Std. Error t value
                Value
                 -0.2650
                            0.4222
## LINKE|Gruene
                                      -0.6276
## Gruene | SPD
                  0.8210
                            0.4226
                                       1.9427
## SPD|FDP
                  2.0402
                            0.4286
                                       4.7602
## FDP|CDU/CSU
                  2.5975
                            0.4320
                                       6.0123
## CDU/CSU|AfD
                  4.9260
                            0.4595
                                      10.7198
##
## Residual Deviance: 2212.405
## AIC: 2254.405
```

From the summary of the final ordinal model, after executing the step function on the model containing all main effects and interactions of the factors and the numerical variables it can be concluded that the formula contains the main effects of factors f.Imm, f.gender, the squared form of the numerical representation of variable political\_interest, its interaction with factor f.Imm and finally the first order of variable income (numerical representation). The following plots indicate how the explanatory variables fluctuate throughout the different parties of the target variable. By the allEffects plot it is clear that the available explanatory variables are not enough to distinguish well the all the voting preferences of the German citizens, only specific parties can be differentiated, the far-right and far-left ones.

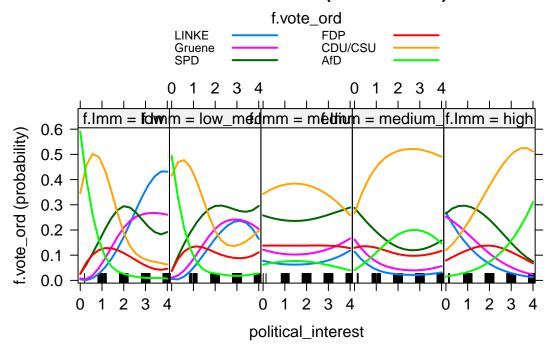
## **Effects of Income**



## **Effects of Gender**



### **Effects of Interactions (Imm - PolInt)**

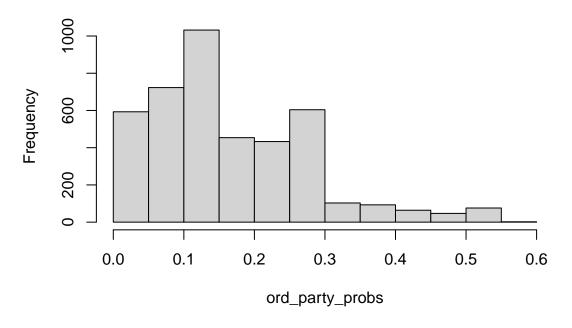


**2.2.2.1** Confusion Matrix and Metrics for Training Set Here the confusion matrix and the appropriate metrics are presented for the training set.

```
##
##
              LINKE Gruene SPD FDP CDU/CSU AfD
##
     LINKE
                 20
                         22
                              14
                                   1
                                            9
##
     Gruene
                   0
                          0
                               0
                                   0
                                            0
                                                 0
##
     SPD
                 37
                         51
                              75
                                  17
                                           55
                                                 5
     FDP
                   0
                          0
##
                               0
                                   0
                                            0
                                                 0
     CDU/CSU
##
                 31
                         33
                              80
                                  64
                                          147
                                                41
                          0
                               0
                                   0
##
     AfD
                   0
                                            0
                                                 1
## [1] "Accuracy:"
## [1] 34.51705
## [1] "Precision:"
                                                  CDU/CSU
##
       LINKE
                 Gruene
                                SPD
                                           FDP
                                                                 AfD
                     NaN 0.3125000
                                           NaN 0.3712121 1.0000000
## 0.2985075
## [1] "MissClassification Rate:"
## [1] 65.48295
```

Moreover, the plot below depicts the distribution of the predicted probabilities for the training set.

### Histogram of ord\_party\_probs



2.2.2.2 Confusion Matrix and Metrics for Testing Set Here the confusion matrix and the appropriate metrics are presented for the ord\_testing set.

```
##
##
              LINKE Gruene SPD FDP CDU/CSU AfD
                   3
                           6
                                              3
##
     LINKE
                               13
                                    4
                                                  0
##
     Gruene
                   0
                           0
                                0
                                    0
                                             0
                                                  0
##
     SPD
                  18
                          17
                               35
                                    6
                                             18
                                                  2
     FDP
                           0
                                                  0
##
                   0
                                0
                                    0
                                             0
##
     CDU/CSU
                  14
                          14
                               38
                                   29
                                            57
                                                 19
                           0
                                0
                                                  0
##
     AfD
                   0
                                    0
                                             0
  [1] "Accuracy:"
##
   [1] 32.09459
## [1] "Precision:"
##
        LINKE
                  Gruene
                                 SPD
                                            FDP
                                                   CDU/CSU
                                                                   AfD
                     NaN 0.3645833
## 0.1034483
                                            NaN 0.3333333
                                                                   NaN
## [1] "MissClassification Rate:"
## [1] 67.90541
```

### 2.3 Hierarchical Modeling

In order to follow the hierarchical approach, it is necessary to create a new variable which will enable the binary split of the data. By checking the table of the generated factor f.political orientation it is derived that 665 observations belong to center wing, 266 to left wing and 69 to the right political wing. For that reason the first layer of the hierarchical approach will deal with the separation of the observations to center wing versus others (left and

right), and the second layer will deal with the discrimination of observations between left and right. Consequently a new factor needs to be created for binary identification of center wing. Once the data is split into <code>Center\_Wing</code> vs <code>Left\_Right\_Wings</code>, the same approach as before will be followed in order to choose the right representation of the explanatory variables. Due to repetition of the idea, the whole analysis of variables representation will take place in Appendix or the analysis chunks will not be included in this report (include=FALSE). Consequently the final model and its validation metrics will be presented directly.

#### 2.3.1 First Layer of Hierarchical Approach

The format of the variables being used for training the first layer of the hierarchical approach is the following: f.Imm, poly(political\_interest,3), income.

```
##
## Call:
## glm(formula = bwing ~ income + f.Imm + f.eastGermany + income:f.Imm,
##
       family = binomial, data = train)
##
## Deviance Residuals:
##
       Min
                  10
                       Median
                                    30
                                             Max
## -1.8258
            -1.1463
                       0.6878
                                0.8629
                                          1.5708
##
## Coefficients:
##
                                 Estimate Std. Error z value Pr(>|z|)
                                                       -0.764
## (Intercept)
                                 -1.02051
                                              1.33582
                                                                0.44489
## income
                                  0.06552
                                              0.44330
                                                        0.148
                                                               0.88249
## f.Immlow medium
                                 -0.75659
                                              1.46862
                                                       -0.515
                                                               0.60644
## f.Immmedium
                                                        1.328
                                  1.89378
                                              1.42596
                                                                0.18415
## f.Immmedium high
                                  0.10100
                                              1.54920
                                                        0.065
                                                               0.94802
                                                        1.316
## f.Immhigh
                                  2.46921
                                              1.87635
                                                               0.18819
                                                        2.779
## f.eastGermanyYes.EastGermany
                                  0.52471
                                              0.18879
                                                               0.00545 **
## income:f.Immlow medium
                                  0.47267
                                              0.48693
                                                        0.971
                                                                0.33169
## income:f.Immmedium
                                                       -0.192
                                 -0.09122
                                              0.47485
                                                                0.84767
## income:f.Immmedium high
                                  0.38232
                                              0.52346
                                                        0.730
                                                                0.46517
## income:f.Immhigh
                                 -0.58147
                                              0.63207
                                                       -0.920
                                                               0.35760
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 906.04
                               on 703
                                       degrees of freedom
## Residual deviance: 849.75
                               on 693
                                       degrees of freedom
## AIC: 871.75
##
## Number of Fisher Scoring iterations: 4
```

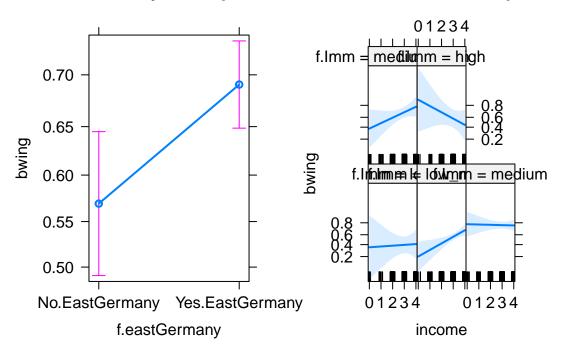
From the Anova analysis of the model and the all effects plot, we can see which explanatory variables are significant for the discrimination of central vs right and left wings, as well as how those variables affect the predictability of the first layer binary model.

```
## Analysis of Deviance Table (Type II tests)
##
```

```
## Response: bwing
##
                  LR Chisq Df Pr(>Chisq)
## income
                     3.261
                            1
                                0.070961 .
## f.Imm
                    38.445
                            4
                               9.069e-08 ***
## f.eastGermany
                     7.655
                            1
                                0.005663 **
## income:f.Imm
                     8.488
                            4
                                0.075244 .
## ---
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

### f.eastGermany effect plot

### income\*f.lmm effect plot



### 2.3.2 Second Layer of Hierarchical Approach

For the second layer of the hierarchical approach the separation between right and left parties is necessary. The representations of the variables after the analysis for this step is: poly(egoposition\_immigration,4), f.PolInt (null model is better), poly(income,3) (null model is better).

```
bh2m0 <- glm( f.political_orientation ~ 1, family = binomial, data = train[train$bwing==
##
## Call:</pre>
```

```
## glm(formula = f.political_orientation ~ f.Imm + f.PolInt + f.gender,
       family = binomial, data = train[train$bwing == "Left Right Wings",
##
##
           1)
##
## Deviance Residuals:
##
       Min
                 1Q
                       Median
                                    3Q
                                            Max
## -2.1494
            -0.4360
                     -0.1862
                              -0.1317
                                         2.3271
##
## Coefficients:
##
                       Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                       15.53200 1455.39800
                                              0.011 0.991485
```

```
## f.Immlow_medium
                         0.03407
                                      1.16288
                                                 0.029 0.976628
## f.Immmedium
                         0.73118
                                      1.13031
                                                 0.647 0.517710
## f.Immmedium high
                         4.87808
                                      1.18292
                                                 4.124 3.73e-05 ***
## f.Immhigh
                         3.57605
                                      1.23106
                                                 2.905 0.003674 **
## f.PolIntmedium
                       -18.20467 1455.39764
                                                -0.013 0.990020
## f.PolInthigh
                       -17.87140 1455.39766
                                                -0.012 0.990203
## f.genderF
                         -2.10501
                                      0.61681
                                                -3.413 0.000643 ***
## ---
## Signif. codes:
                     0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 241.08
                                 on 241
                                          degrees of freedom
## Residual deviance: 121.70
                                 on 234
                                          degrees of freedom
##
  AIC: 137.7
##
## Number of Fisher Scoring iterations: 14
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political orientation
             LR Chisq Df Pr(>Chisq)
##
## f.Imm
               97.782
                        4
                            < 2.2e-16 ***
## f.PolInt
                5.371
                        2
                              0.06819 .
## f.gender
               15.279
                        1
                           9.272e-05 ***
## ---
                     0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
                                                f.Polint effect plot
         f.Imm effect plot
  f.political_orientation
                                         political_orientation
      0.8
                                             0.8
          loow_merationationation_thiggth
                                                          medium
                                                                      high
                                                  low
                   f.Imm
                                                          f.PolInt
        f.gender effect plot
 f.political_orientation
      0,8
           Μ
                  f.gender
```

From the Anova analysis of the second layer of the hierarchical model and the all effects plot, we can see which explanatory variables are significant for the discrimination of right vs left wings,

as well as how those variables affect the predictability of the second layer of the binary model.

#### 2.3.3 Confusion Matrix And Metrics for Training Set

```
##
                       Left_Right_Wings Center_Wing
##
##
                                      168
                                                   403
     Center_Wing
     Left_Right_Wings
                                       74
                                                    59
##
##
                train y
                 Center_Wing Left_Wing Right_Wing
##
  train_pred
     Left Wing
                            0
                                     182
##
     Right Wing
                            0
                                      12
                                                 35
##
## [1] "Accuracy:"
## [1] 35.79545
```

#### 2.3.4 Confusion Matrix And Metrics for Testing Set

```
##
##
                       Left_Right_Wings Center_Wing
##
     Center_Wing
                                       74
                                                   165
##
     Left Right Wings
                                       19
                                                    38
##
                test y
## test pred
                 Center Wing Left Wing Right Wing
     Left Wing
                                      68
##
                            0
     Right_Wing
                            0
                                       4
                                                  14
##
## [1] "Accuracy:"
   [1] 63.49614
```

### 3 Best Final Model

In order to select the final best model from the three different approaches, the comparison is completed by using the AIC method and by checking the accuracy of all the models. As it is depicted below, the best model is the Hierarchical Approach.

```
AIC(nm0,om0,nm_final,om_final)
```

```
## df AIC

## nm0 5 2378.556

## om0 5 2378.556

## nm_final 50 2219.625

## om_final 21 2254.405

AIC(layer1) + AIC(layer2)
```

```
## [1] 1009.448
```

Improvements to this work could be done by adding more detailed influential data analysis and retraining of the models without them. In this version of the report influential data plots can be found in the last subsection of the Appendix for the hierarchical approach. Also, better results

could be generated by checking in more detail the interactions between all the variables and by creating new factors in all the different approaches followed.

# 4 Appendix

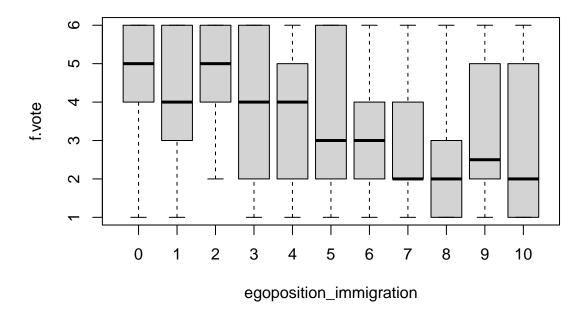
#### 4.1 EDA

### 4.2 Profiling of Target Variable(s)

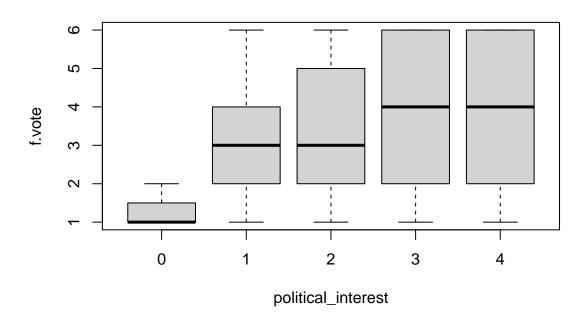
In the following plots the levels of variable *f.vote* and *f.political\_orientation* follow the structure presented below.

```
## [1] "Parties:"
## [1] 1 2 3 4 5 6
## [1] "AfD" "CDU/CSU" "FDP" "Gruene" "LINKE" "SPD"
## [1] "Political Wings:"
## [1] 1 2 3
## [1] "Center_Wing" "Left_Wing" "Right_Wing"
```

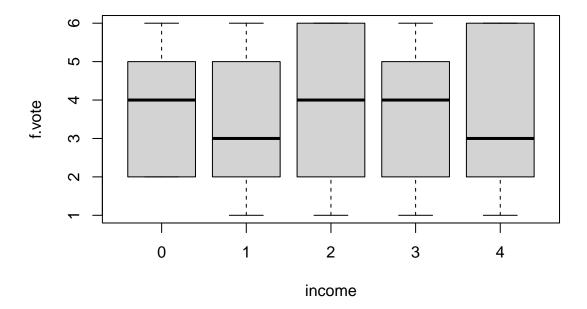
### **Association of f.vote and Egoposition Immigration**



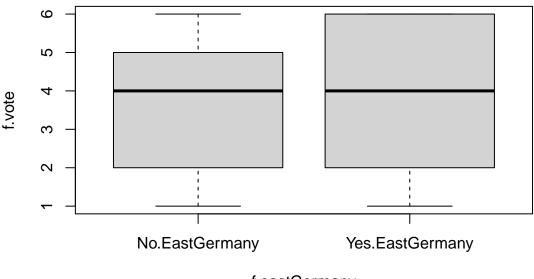
## **Association of f.vote and Political Interest**



## **Association of f.vote and Income Satisfaction**

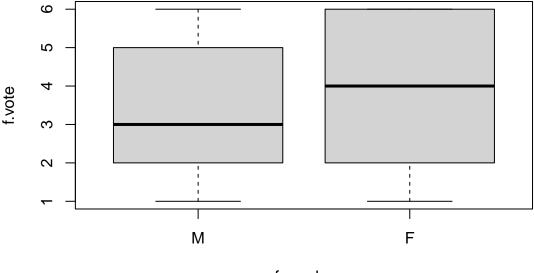


# **Association of f.vote and East Germany**



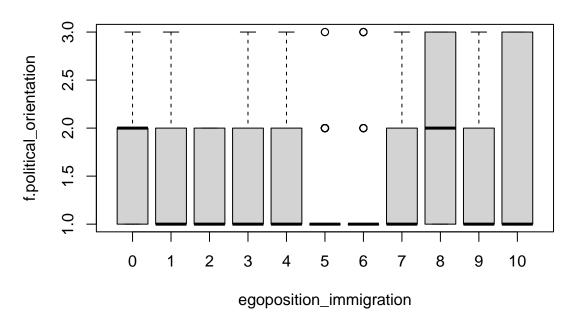
f.eastGermany

### **Association of f.vote and Gender**

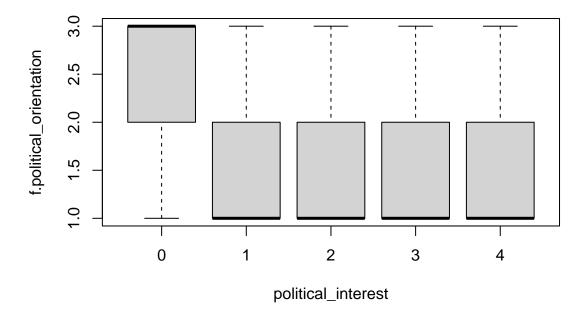


f.gender

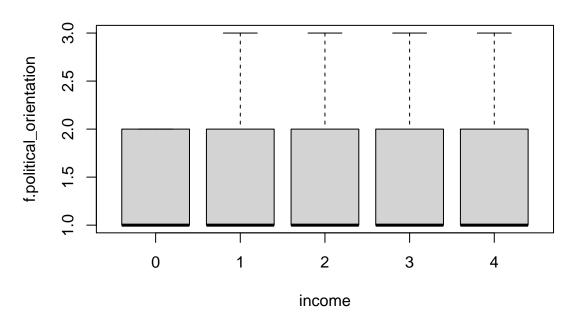
# **Association of Political Wings and Egoposition Immigration**



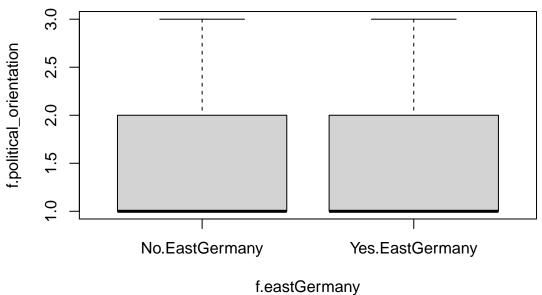
# **Association of Political Wings and Political Interest**



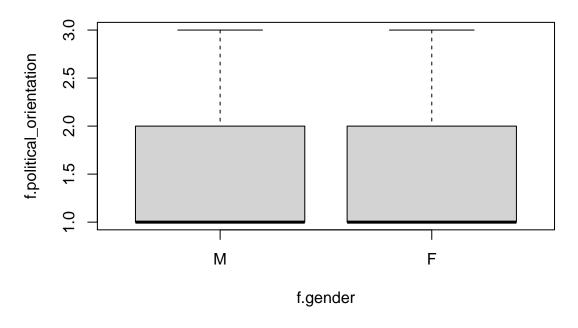
# **Association of Political Wings and Income Satisfaction**



# **Association of Political Wings and East Germany**



### **Association of Political Wings and Gender**



```
res.cat<-catdes(gles, 10)
res.cat$category
```

```
## $AfD
##
                                                                Cla/Mod
                                                                           Mod/Cla
## f.vote_ord=AfD
                                                             100.000000 100.000000
## f.political_orientation=Right_Wing
                                                             100.000000 100.000000
## bwing=Left Right Wings
                                                              20.597015 100.000000
## f.Imm=medium_high
                                                             25.174825
                                                                         52.173913
## f.egoposition_immigration=8_Level.Imm
                                                                         20.289855
                                                             45.161290
## f.Imm=high
                                                              34.042553
                                                                         23.188406
## f.egoposition immigration=10 Very Restrictive Level.Imm
                                                             34.042553
                                                                         23.188406
## f.gender=M
                                                                         81.159420
                                                              10.408922
## f.mout=MvOut.Yes
                                                              37.500000
                                                                         13.043478
## f.duplicate=No.Duplicate
                                                               8.892356
                                                                         82.608696
## f.egoposition immigration=7 Level.Imm
                                                              17.948718
                                                                         20.289855
## f.egoposition_immigration=9_Level.Imm
                                                             23.529412
                                                                         11.594203
## f.eastGermany=No.EastGermany
                                                              11.618257
                                                                         40.579710
## f.PolInt=low
                                                              66.666667
                                                                          2.898551
## f.political interest=Low.Inter
                                                             66.666667
                                                                          2.898551
## f.IncSat=low_to_medium
                                                              17.857143
                                                                          7.246377
## f.income=Low_to_Medium.Sat
                                                              17.857143
                                                                          7.246377
## f.egoposition immigration=1 Level.Imm
                                                               1.470588
                                                                          1.449275
## f.egoposition_immigration=3_Level.Imm
                                                               2.985075
                                                                          5.797101
## f.eastGermany=Yes.EastGermany
                                                                         59.420290
                                                               5.401845
## f.egoposition immigration=5 Neutral Level.Imm
                                                               1.290323
                                                                          2.898551
## f.duplicate=Yes.Duplicate
                                                               3.342618
                                                                         17.391304
## f.egoposition immigration=4 Level.Imm
                                                               1.117318
                                                                          2.898551
## f.vote_ord=FDP
                                                               0.000000
                                                                          0.00000
## f.vote_ord=LINKE
                                                               0.000000
                                                                          0.00000
```

```
## f.egoposition_immigration=2_Level.Imm
                                                             0.000000
                                                                        0.000000
## f.vote ord=Gruene
                                                             0.000000
                                                                        0.000000
## f.mout=MvOut.No
                                                             6.147541
                                                                       86.956522
## f.gender=F
                                                             2.813853
                                                                       18.840580
## f.Imm=medium
                                                             2.564103
                                                                       15.942029
## f.Imm=low medium
                                                             1.506024
                                                                        7.246377
## f.vote ord=SPD
                                                             0.000000
                                                                        0.000000
## f.political_orientation=Left_Wing
                                                             0.000000
                                                                        0.000000
## f.vote ord=CDU/CSU
                                                             0.000000
                                                                        0.000000
## bwing=Center_Wing
                                                             0.000000
                                                                        0.000000
## f.political_orientation=Center_Wing
                                                             0.000000
                                                                        0.000000
                                                           Global
##
                                                                        p.value
## f.vote ord=AfD
                                                              6.9 1.889108e-108
## f.political orientation=Right Wing
                                                              6.9 1.889108e-108
## bwing=Left_Right_Wings
                                                             33.5 9.958160e-36
## f.Imm=medium high
                                                             14.3 7.616170e-15
## f.egoposition immigration=8 Level.Imm
                                                              3.1 1.675803e-09
## f.Imm=high
                                                              4.7 1.468400e-08
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm
                                                              4.7 1.468400e-08
## f.gender=M
                                                             53.8 1.101835e-06
## f.mout=MvOut.Yes
                                                              2.4 1.316568e-05
## f.duplicate=No.Duplicate
                                                             64.1 5.540764e-04
## f.egoposition_immigration=7_Level.Imm
                                                              7.8 5.783367e-04
## f.egoposition immigration=9 Level.Imm
                                                              3.4 1.731296e-03
## f.eastGermany=No.EastGermany
                                                             24.1 1.731634e-03
## f.PolInt=low
                                                              0.3 1.377478e-02
## f.political_interest=Low.Inter
                                                              0.3 1.377478e-02
## f.IncSat=low to medium
                                                              2.8 4.793709e-02
## f.income=Low to Medium.Sat
                                                              2.8 4.793709e-02
## f.egoposition_immigration=1_Level.Imm
                                                              6.8 4.815760e-02
## f.egoposition immigration=3 Level.Imm
                                                             13.4 4.305493e-02
## f.eastGermany=Yes.EastGermany
                                                             75.9 1.731634e-03
                                                             15.5 6.970986e-04
## f.egoposition immigration=5 Neutral Level.Imm
## f.duplicate=Yes.Duplicate
                                                             35.9 5.540764e-04
## f.egoposition_immigration=4_Level.Imm
                                                             17.9 1.193747e-04
## f.vote ord=FDP
                                                             12.1 9.721535e-05
## f.vote_ord=LINKE
                                                             12.3 8.254390e-05
## f.egoposition immigration=2 Level.Imm
                                                             13.0 4.641675e-05
## f.vote ord=Gruene
                                                             14.3 1.573110e-05
## f.mout=MvOut.No
                                                             97.6 1.316568e-05
## f.gender=F
                                                             46.2 1.101835e-06
## f.Imm=medium
                                                             42.9 9.629260e-07
## f.Imm=low medium
                                                             33.2 1.727176e-07
                                                             25.5 6.459324e-10
## f.vote ord=SPD
## f.political_orientation=Left_Wing
                                                             26.6 2.200779e-10
## f.vote_ord=CDU/CSU
                                                             28.9 2.190738e-11
## bwing=Center Wing
                                                             66.5 9.958160e-36
## f.political orientation=Center Wing
                                                             66.5 9.958160e-36
##
                                                               v.test
## f.vote ord=AfD
                                                            22.123229
```

```
## f.political_orientation=Right_Wing
                                                             22.123229
## bwing=Left Right Wings
                                                             12.477072
## f.Imm=medium high
                                                              7.773807
## f.egoposition immigration=8 Level.Imm
                                                              6.026469
## f.Imm=high
                                                              5.665215
## f.egoposition immigration=10 Very Restrictive Level.Imm
                                                              5.665215
## f.gender=M
                                                              4.872520
## f.mout=MvOut.Yes
                                                              4.357333
## f.duplicate=No.Duplicate
                                                              3.453152
## f.egoposition immigration=7 Level.Imm
                                                              3.441576
## f.egoposition immigration=9 Level.Imm
                                                              3.132830
## f.eastGermany=No.EastGermany
                                                              3.132773
## f.PolInt=low
                                                              2.463084
## f.political_interest=Low.Inter
                                                              2.463084
## f.IncSat=low_to_medium
                                                              1.977926
## f.income=Low to Medium.Sat
                                                              1.977926
## f.egoposition immigration=1 Level.Imm
                                                             -1.975975
## f.egoposition immigration=3 Level.Imm
                                                             -2.023177
## f.eastGermany=Yes.EastGermany
                                                             -3.132773
## f.egoposition_immigration=5_Neutral_Level.Imm
                                                             -3.390718
## f.duplicate=Yes.Duplicate
                                                             -3.453152
## f.egoposition immigration=4 Level.Imm
                                                             -3.847407
## f.vote_ord=FDP
                                                             -3.897439
## f.vote ord=LINKE
                                                             -3.936892
## f.egoposition immigration=2 Level.Imm
                                                             -4.072973
## f.vote ord=Gruene
                                                             -4.318194
## f.mout=MvOut.No
                                                             -4.357333
## f.gender=F
                                                             -4.872520
## f.Imm=medium
                                                             -4.899067
                                                             -5.226533
## f.Imm=low medium
## f.vote ord=SPD
                                                             -6.178794
## f.political orientation=Left Wing
                                                             -6.346633
## f.vote ord=CDU/CSU
                                                             -6.692711
## bwing=Center Wing
                                                            -12.477072
## f.political_orientation=Center_Wing
                                                            -12.477072
##
## $`CDU/CSU`
##
                                                    Cla/Mod
                                                               Mod/Cla Global
## f.vote ord=CDU/CSU
                                                  100.00000 100.000000
                                                                         28.9
## bwing=Center Wing
                                                   43.45865 100.000000
                                                                         66.5
## f.political_orientation=Center_Wing
                                                   43.45865 100.000000
                                                                         66.5
## f.Imm=medium
                                                   35.89744 53.287197
                                                                         42.9
## f.duplicate=Yes.Duplicate
                                                   36.21170 44.982699
                                                                         35.9
## f.egoposition immigration=5 Neutral Level.Imm
                                                   39.35484 21.107266
                                                                         15.5
## f.egoposition_immigration=7_Level.Imm
                                                   43.58974 11.764706
                                                                          7.8
## f.egoposition_immigration=6_Level.Imm
                                                   40.00000 13.148789
                                                                         9.5
## f.political interest=Medium.Inter
                                                   33.44156 35.640138
                                                                         30.8
## f.egoposition immigration=1 Level.Imm
                                                   17.64706
                                                              4.152249
                                                                         6.8
## f.income=Medium.Sat
                                                   22.34043 14.532872
                                                                         18.8
## f.duplicate=No.Duplicate
                                                   24.80499 55.017301
                                                                         64.1
```

```
6.574394
## f.egoposition_immigration=2_Level.Imm
                                                  14.61538
                                                                        13.0
## f.Imm=low medium
                                                  18.67470
                                                            21.453287
                                                                        33.2
## f.vote ord=AfD
                                                   0.00000
                                                             0.000000
                                                                         6.9
## f.political_orientation=Right_Wing
                                                   0.00000
                                                             0.000000
                                                                         6.9
## f.vote_ord=FDP
                                                   0.00000
                                                             0.000000
                                                                        12.1
## f.vote ord=LINKE
                                                   0.00000
                                                             0.000000
                                                                        12.3
## f.vote ord=Gruene
                                                   0.00000
                                                             0.000000
                                                                        14.3
## f.vote_ord=SPD
                                                             0.000000
                                                   0.00000
                                                                        25.5
## f.political orientation=Left Wing
                                                   0.00000
                                                             0.000000
                                                                        26.6
## bwing=Left Right Wings
                                                   0.00000
                                                             0.000000
                                                                        33.5
##
                                                       p.value
                                                                   v.test
## f.vote_ord=CDU/CSU
                                                 2.718794e-260 34.464630
## bwing=Center Wing
                                                  4.312957e-64 16.902491
## f.political orientation=Center Wing
                                                  4.312957e-64 16.902491
## f.Imm=medium
                                                  2.568896e-05 4.208660
## f.duplicate=Yes.Duplicate
                                                  1.578900e-04
                                                                 3.778320
## f.egoposition immigration=5 Neutral Level.Imm
                                                  2.326304e-03
                                                                 3.045064
## f.egoposition immigration=7 Level.Imm
                                                  4.123963e-03
                                                                 2.868521
## f.egoposition immigration=6 Level.Imm
                                                  1.484342e-02
                                                                 2.436177
## f.political_interest=Medium.Inter
                                                  3.612343e-02 2.095535
## f.egoposition_immigration=1_Level.Imm
                                                  2.975586e-02 -2.173325
## f.income=Medium.Sat
                                                  2.589708e-02 -2.227752
## f.duplicate=No.Duplicate
                                                  1.578900e-04 -3.778320
## f.egoposition_immigration=2 Level.Imm
                                                  5.395182e-05 -4.037813
## f.Imm=low medium
                                                  2.862253e-07 -5.132298
## f.vote ord=AfD
                                                  2.190738e-11 -6.692711
## f.political_orientation=Right_Wing
                                                  2.190738e-11 -6.692711
## f.vote ord=FDP
                                                  4.521871e-20 -9.174854
## f.vote ord=LINKE
                                                  2.036114e-20 -9.260430
## f.vote_ord=Gruene
                                                  6.155171e-24 -10.089389
## f.vote ord=SPD
                                                  9.555546e-46 -14.197047
## f.political_orientation=Left_Wing
                                                  4.116942e-48 -14.573901
## bwing=Left_Right_Wings
                                                  4.312957e-64 -16.902491
##
## $FDP
##
                                                      Cla/Mod
                                                                  Mod/Cla Global
## f.vote ord=FDP
                                                   100.000000 100.0000000
                                                                             12.1
## bwing=Center Wing
                                                    18.195489 100.0000000
                                                                             66.5
## f.political orientation=Center Wing
                                                    18.195489 100.0000000
                                                                             66.5
## f.Imm=medium
                                                    17.016317
                                                               60.3305785
                                                                             42.9
## f.egoposition_immigration=6_Level.Imm
                                                                              9.5
                                                    22.105263
                                                               17.3553719
## f.Imm=low
                                                     2.040816
                                                               0.8264463
                                                                              4.9
## f.egoposition_immigration=0_Very_Open_Level.Imm
                                                                0.8264463
                                                                             4.9
                                                     2.040816
## f.Imm=low medium
                                                     6.927711 19.0082645
                                                                             33.2
## f.egoposition_immigration=2_Level.Imm
                                                     3.076923
                                                                3.3057851
                                                                             13.0
## f.vote ord=AfD
                                                     0.000000
                                                                0.0000000
                                                                              6.9
## f.political orientation=Right Wing
                                                     0.000000
                                                                0.0000000
                                                                              6.9
## f.vote_ord=LINKE
                                                     0.000000
                                                                0.0000000
                                                                             12.3
## f.vote_ord=Gruene
                                                     0.000000
                                                                0.0000000
                                                                             14.3
## f.vote ord=SPD
                                                     0.000000
                                                                0.0000000
                                                                             25.5
```

```
## f.political_orientation=Left_Wing
                                                     0.000000
                                                                0.0000000
                                                                            26.6
## f.vote ord=CDU/CSU
                                                     0.000000
                                                                0.0000000
                                                                             28.9
## bwing=Left Right Wings
                                                     0.00000
                                                                0.0000000
                                                                            33.5
##
                                                         p.value
                                                                     v.test
## f.vote ord=FDP
                                                   1.570479e-159
                                                                  26.912447
## bwing=Center Wing
                                                    6.200298e-24
                                                                  10.088671
## f.political orientation=Center Wing
                                                    6.200298e-24 10.088671
## f.Imm=medium
                                                    4.272470e-05 4.092229
## f.egoposition immigration=6 Level.Imm
                                                    3.784565e-03
                                                                 2.895582
## f.Imm=low
                                                    1.390975e-02 -2.459586
## f.egoposition_immigration=0_Very_Open_Level.Imm 1.390975e-02 -2.459586
## f.Imm=low_medium
                                                    2.581352e-04
                                                                  -3.654051
## f.egoposition immigration=2 Level.Imm
                                                    1.560324e-04 -3.781267
## f.vote ord=AfD
                                                    9.721535e-05 -3.897439
## f.political_orientation=Right_Wing
                                                    9.721535e-05 -3.897439
## f.vote ord=LINKE
                                                    4.155458e-08 -5.484114
## f.vote ord=Gruene
                                                    2.059483e-09 -5.993045
                                                    2.177390e-17 -8.483916
## f.vote ord=SPD
## f.political orientation=Left Wing
                                                    3.054680e-18 -8.709407
## f.vote_ord=CDU/CSU
                                                    4.521871e-20 -9.174854
## bwing=Left_Right_Wings
                                                    6.200298e-24 -10.088671
##
## $Gruene
##
                                                              Cla/Mod
                                                                          Mod/Cla
                                                           100.000000 100.0000000
## f.vote ord=Gruene
## f.political orientation=Left Wing
                                                            53.759398 100.0000000
## bwing=Left_Right_Wings
                                                            42.686567 100.0000000
## f.Imm=low medium
                                                            23.795181 55.2447552
## f.egoposition immigration=2 Level.Imm
                                                            28.461538 25.8741259
## f.gender=F
                                                            17.748918 57.3426573
## f.political interest=Medium to High.Inter
                                                            17.676768 48.9510490
## f.egoposition immigration=1 Level.Imm
                                                            25.000000 11.8881119
## f.egoposition immigration=6 Level.Imm
                                                             7.368421
                                                                        4.8951049
## f.egoposition immigration=8 Level.Imm
                                                             0.000000
                                                                       0.0000000
## f.Imm=high
                                                             2.127660
                                                                        0.6993007
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm
                                                                        0.6993007
                                                             2.127660
## f.egoposition immigration=9 Level.Imm
                                                             0.000000
                                                                        0.0000000
## f.gender=M
                                                            11.338290 42.6573427
## f.egoposition immigration=7 Level.Imm
                                                             2.564103
                                                                        1.3986014
## f.vote ord=AfD
                                                             0.000000
                                                                        0.0000000
## f.political_orientation=Right_Wing
                                                             0.000000
                                                                        0.0000000
## f.Imm=medium_high
                                                             1.398601
                                                                        1.3986014
## f.vote ord=FDP
                                                             0.000000
                                                                        0.0000000
## f.vote ord=LINKE
                                                             0.000000
                                                                        0.0000000
## f.vote ord=SPD
                                                             0.000000
                                                                        0.0000000
## f.vote_ord=CDU/CSU
                                                             0.000000
                                                                        0.000000
## bwing=Center Wing
                                                             0.000000
                                                                        0.000000
## f.political orientation=Center Wing
                                                             0.000000
                                                                        0.0000000
##
                                                           Global
                                                                        p.value
## f.vote ord=Gruene
                                                             14.3 1.663892e-177
```

```
## f.political_orientation=Left_Wing
                                                              26.6 4.555935e-99
## bwing=Left Right Wings
                                                              33.5 1.406134e-79
## f.Imm=low medium
                                                             33.2 4.705371e-09
## f.egoposition_immigration=2_Level.Imm
                                                             13.0 5.773018e-06
                                                              46.2 4.072838e-03
## f.gender=F
## f.political interest=Medium to High.Inter
                                                             39.6 1.459058e-02
## f.egoposition immigration=1 Level.Imm
                                                              6.8 1.540367e-02
## f.egoposition_immigration=6_Level.Imm
                                                               9.5 3.395532e-02
## f.egoposition immigration=8 Level.Imm
                                                               3.1 7.725865e-03
## f.Imm=high
                                                               4.7 6.044056e-03
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm
                                                              4.7 6.044056e-03
## f.egoposition_immigration=9_Level.Imm
                                                               3.4 4.782805e-03
## f.gender=M
                                                              53.8 4.072838e-03
## f.egoposition immigration=7 Level.Imm
                                                              7.8 4.551511e-04
## f.vote_ord=AfD
                                                               6.9 1.573110e-05
## f.political orientation=Right Wing
                                                               6.9 1.573110e-05
## f.Imm=medium high
                                                              14.3 1.816764e-08
## f.vote ord=FDP
                                                              12.1 2.059483e-09
## f.vote ord=LINKE
                                                              12.3 1.443577e-09
## f.vote ord=SPD
                                                              25.5 1.039117e-20
## f.vote ord=CDU/CSU
                                                              28.9 6.155171e-24
## bwing=Center Wing
                                                             66.5 1.406134e-79
## f.political_orientation=Center_Wing
                                                             66.5 1.406134e-79
##
                                                               v.test
## f.vote ord=Gruene
                                                            28.406856
## f.political orientation=Left Wing
                                                            21.126332
## bwing=Left_Right_Wings
                                                             18.888951
## f.Imm=low medium
                                                             5.857270
## f.egoposition_immigration=2_Level.Imm
                                                             4.534536
## f.gender=F
                                                             2.872465
## f.political interest=Medium to High.Inter
                                                             2.442385
## f.egoposition immigration=1 Level.Imm
                                                             2.422746
## f.egoposition immigration=6 Level.Imm
                                                            -2.120602
## f.egoposition immigration=8 Level.Imm
                                                            -2.663821
## f.Imm=high
                                                             -2.745382
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm
                                                            -2.745382
## f.egoposition immigration=9 Level.Imm
                                                            -2.821309
## f.gender=M
                                                            -2.872465
## f.egoposition immigration=7 Level.Imm
                                                            -3.505850
## f.vote ord=AfD
                                                            -4.318194
## f.political_orientation=Right_Wing
                                                            -4.318194
## f.Imm=medium_high
                                                            -5.628602
## f.vote ord=FDP
                                                            -5.993045
## f.vote_ord=LINKE
                                                            -6.050544
## f.vote ord=SPD
                                                            -9.331980
## f.vote_ord=CDU/CSU
                                                           -10.089389
## bwing=Center Wing
                                                           -18.888951
## f.political_orientation=Center_Wing
                                                           -18.888951
##
## $LINKE
```

```
##
                                                       Cla/Mod
                                                                  Mod/Cla Global
## f.vote ord=LINKE
                                                    100.000000 100.000000
                                                                             12.3
## f.political orientation=Left Wing
                                                     46.240602 100.000000
                                                                             26.6
## bwing=Left_Right_Wings
                                                     36.716418 100.000000
                                                                             33.5
## f.eastGermany=No.EastGermany
                                                     19.087137
                                                                37.398374
                                                                             24.1
## f.Imm=low
                                                     28.571429
                                                                11.382114
                                                                              4.9
## f.egoposition_immigration=0_Very_Open_Level.Imm
                                                                 11.382114
                                                                              4.9
                                                     28.571429
## f.IncSat=medium
                                                     13.896104
                                                                86.991870
                                                                             77.0
## f.Imm=low medium
                                                     16.566265
                                                                             33.2
                                                                44.715447
## f.egoposition immigration=3 Level.Imm
                                                     19.402985
                                                                21.138211
                                                                             13.4
## f.duplicate=No.Duplicate
                                                                             64.1
                                                     14.196568
                                                                73.983740
## f.income=Medium.Sat
                                                     17.553191
                                                                26.829268
                                                                             18.8
## f.Imm=medium high
                                                      6.993007
                                                                             14.3
                                                                 8.130081
## f.duplicate=Yes.Duplicate
                                                      8.913649
                                                                26.016260
                                                                             35.9
## f.Imm=medium
                                                      9.324009
                                                                32.520325
                                                                             42.9
## f.egoposition_immigration=6_Level.Imm
                                                      4.210526
                                                                 3.252033
                                                                              9.5
## f.egoposition immigration=5 Neutral Level.Imm
                                                                             15.5
                                                      5.161290
                                                                 6.504065
## f.eastGermany=Yes.EastGermany
                                                     10.144928
                                                                62.601626
                                                                             75.9
## f.IncSat=high
                                                      4.761905
                                                                 7.317073
                                                                             18.9
## f.income=High.Sat
                                                      4.761905
                                                                 7.317073
                                                                             18.9
## f.vote_ord=AfD
                                                      0.000000
                                                                 0.000000
                                                                              6.9
## f.political orientation=Right Wing
                                                      0.000000
                                                                 0.000000
                                                                              6.9
## f.vote_ord=FDP
                                                      0.000000
                                                                 0.000000
                                                                             12.1
## f.vote ord=Gruene
                                                                             14.3
                                                      0.000000
                                                                 0.000000
## f.vote ord=SPD
                                                      0.000000
                                                                  0.000000
                                                                             25.5
## f.vote_ord=CDU/CSU
                                                      0.000000
                                                                  0.000000
                                                                             28.9
## bwing=Center_Wing
                                                      0.000000
                                                                  0.000000
                                                                             66.5
## f.political orientation=Center Wing
                                                      0.000000
                                                                  0.000000
                                                                             66.5
##
                                                          p.value
                                                                       v.test
## f.vote_ord=LINKE
                                                    3.053611e-161
                                                                    27.058260
## f.political orientation=Left Wing
                                                     8.361150e-83
                                                                   19.277115
## bwing=Left Right Wings
                                                     6.141124e-67
                                                                    17.284633
## f.eastGermany=No.EastGermany
                                                     4.265885e-04
                                                                    3.523064
## f.Imm=low
                                                     1.737035e-03
                                                                     3.131859
## f.egoposition_immigration=0_Very_Open_Level.Imm
                                                     1.737035e-03
                                                                    3.131859
## f.IncSat=medium
                                                     3.395906e-03
                                                                     2.929424
## f.Imm=low medium
                                                     4.615992e-03
                                                                    2.832678
## f.egoposition_immigration=3_Level.Imm
                                                     1.099556e-02
                                                                    2.542840
## f.duplicate=No.Duplicate
                                                     1.345692e-02
                                                                     2.471442
## f.income=Medium.Sat
                                                     1.925059e-02
                                                                     2.340643
## f.Imm=medium_high
                                                     3.007057e-02 -2.169160
## f.duplicate=Yes.Duplicate
                                                     1.345692e-02
                                                                   -2.471442
## f.Imm=medium
                                                     1.252121e-02
                                                                   -2.497104
## f.egoposition immigration=6 Level.Imm
                                                     6.136722e-03
                                                                   -2.740385
## f.egoposition_immigration=5_Neutral_Level.Imm
                                                     1.585127e-03
                                                                   -3.158630
## f.eastGermany=Yes.EastGermany
                                                     4.265885e-04
                                                                   -3.523064
## f.IncSat=high
                                                     1.536281e-04
                                                                   -3.785130
## f.income=High.Sat
                                                     1.536281e-04
                                                                   -3.785130
## f.vote_ord=AfD
                                                     8.254390e-05
                                                                    -3.936892
## f.political orientation=Right Wing
                                                     8.254390e-05
                                                                   -3.936892
```

```
4.155458e-08 -5.484114
## f.vote_ord=FDP
## f.vote ord=Gruene
                                                    1.443577e-09 -6.050544
## f.vote ord=SPD
                                                    1.096795e-17 -8.563303
## f.vote ord=CDU/CSU
                                                    2.036114e-20 -9.260430
## bwing=Center_Wing
                                                    6.141124e-67 -17.284633
## f.political_orientation=Center_Wing
                                                    6.141124e-67 -17.284633
##
## $SPD
##
                                               Cla/Mod
                                                           Mod/Cla Global
## f.vote ord=SPD
                                            100.000000 100.0000000
                                                                     25.5
## bwing=Center_Wing
                                             38.345865 100.0000000
                                                                     66.5
## f.political_orientation=Center_Wing
                                             38.345865 100.0000000
                                                                     66.5
## f.Imm=low medium
                                             32.530120
                                                        42.3529412
                                                                     33.2
## f.egoposition immigration=2 Level.Imm
                                             36.923077
                                                        18.8235294
                                                                     13.0
                                             26.024590 99.6078431
## f.mout=MvOut.No
                                                                     97.6
## f.egoposition_immigration=1_Level.Imm
                                             38.235294 10.1960784
                                                                      6.8
## f.political interest=Low to Medium.Inter
                                                                      3.4
                                              8.823529 1.1764706
## f.mout=MvOut.Yes
                                              4.166667
                                                         0.3921569
                                                                      2.4
## f.Imm=medium_high
                                             16.783217
                                                         9.4117647
                                                                    14.3
## f.vote_ord=AfD
                                              0.00000
                                                         0.0000000
                                                                      6.9
                                              0.00000
## f.political_orientation=Right_Wing
                                                         0.0000000
                                                                      6.9
## f.vote ord=FDP
                                              0.000000
                                                         0.0000000
                                                                     12.1
## f.vote_ord=LINKE
                                                                     12.3
                                              0.00000
                                                         0.0000000
## f.vote ord=Gruene
                                                                     14.3
                                              0.000000
                                                         0.0000000
## f.political_orientation=Left_Wing
                                              0.000000
                                                         0.0000000
                                                                     26.6
## f.vote_ord=CDU/CSU
                                              0.000000
                                                         0.0000000
                                                                     28.9
## bwing=Left_Right_Wings
                                              0.000000
                                                         0.0000000
                                                                     33.5
##
                                                  p.value
                                                              v.test
## f.vote ord=SPD
                                            9.178288e-246 33.480784
## bwing=Center_Wing
                                             5.401466e-55 15.619038
## f.political orientation=Center Wing
                                             5.401466e-55 15.619038
## f.Imm=low medium
                                             3.909839e-04
                                                            3.546096
## f.egoposition immigration=2 Level.Imm
                                             1.985233e-03
                                                            3.092433
## f.mout=MvOut.No
                                             8.131457e-03 2.646562
## f.egoposition_immigration=1_Level.Imm
                                             1.674243e-02
                                                            2.392316
## f.political_interest=Low_to_Medium.Inter
                                             1.626155e-02 -2.402992
## f.mout=MvOut.Yes
                                             8.131457e-03 -2.646562
## f.Imm=medium high
                                             7.988755e-03 -2.652545
## f.vote ord=AfD
                                             6.459324e-10 -6.178794
## f.political orientation=Right Wing
                                             6.459324e-10 -6.178794
## f.vote_ord=FDP
                                             2.177390e-17 -8.483916
## f.vote_ord=LINKE
                                             1.096795e-17 -8.563303
## f.vote ord=Gruene
                                             1.039117e-20 -9.331980
## f.political orientation=Left Wing
                                             2.115265e-41 -13.477726
## f.vote_ord=CDU/CSU
                                             9.555546e-46 -14.197047
## bwing=Left_Right_Wings
                                             5.401466e-55 -15.619038
res.cat<-catdes(gles, 11) #11 for new factor
res.cat$category
```

## \$Center\_Wing

```
##
                                                       Cla/Mod
                                                                  Mod/Cla Global
## bwing=Center Wing
                                                     100.00000 100.000000
                                                                            66.5
## f.vote ord=CDU/CSU
                                                     100.00000
                                                                43.458647
                                                                            28.9
## f.vote=CDU/CSU
                                                     100.00000
                                                                43.458647
                                                                            28.9
## f.vote ord=SPD
                                                     100.00000
                                                                38.345865
                                                                            25.5
## f.vote=SPD
                                                     100.00000
                                                                38.345865
                                                                            25.5
## f.vote ord=FDP
                                                                            12.1
                                                     100.00000
                                                                18.195489
## f.vote=FDP
                                                     100.00000
                                                                18.195489
                                                                            12.1
## f.Imm=medium
                                                                            42.9
                                                      76.22378 49.172932
## f.egoposition immigration=5 Neutral Level.Imm
                                                      83.22581
                                                                            15.5
                                                                19.398496
## f.eastGermany=Yes.EastGermany
                                                      69.43347
                                                                79.248120
                                                                            75.9
## f.duplicate=Yes.Duplicate
                                                      73.25905
                                                                39.548872
                                                                            35.9
## f.egoposition immigration=6 Level.Imm
                                                      81.05263
                                                                             9.5
                                                                11.578947
## f.IncSat=high
                                                      74.07407
                                                                21.052632
                                                                            18.9
## f.income=High.Sat
                                                      74.07407
                                                                21.052632
                                                                            18.9
## f.political_interest=Medium.Inter
                                                      71.75325
                                                                33.233083
                                                                            30.8
## f.egoposition immigration=8 Level.Imm
                                                                             3.1
                                                      48.38710
                                                                 2.255639
## f.Imm=low
                                                      48.97959
                                                                 3.609023
                                                                             4.9
## f.egoposition_immigration=0_Very_Open_Level.Imm
                                                     48.97959
                                                                 3.609023
                                                                             4.9
## f.egoposition_immigration=2_Level.Imm
                                                      54.61538 10.676692
                                                                            13.0
## f.duplicate=No.Duplicate
                                                      62.71451
                                                                60.451128
                                                                            64.1
                                                                            24.1
## f.eastGermany=No.EastGermany
                                                      57.26141
                                                                20.751880
## f.Imm=low_medium
                                                      58.13253
                                                                29.022556
                                                                            33.2
## f.vote ord=AfD
                                                                             6.9
                                                       0.00000
                                                                 0.000000
## f.vote=AfD
                                                       0.00000
                                                                 0.000000
                                                                             6.9
## f.vote_ord=LINKE
                                                       0.00000
                                                                 0.000000
                                                                            12.3
## f.vote=LINKE
                                                       0.00000
                                                                 0.000000
                                                                            12.3
## f.vote ord=Gruene
                                                       0.00000
                                                                 0.000000
                                                                            14.3
## f.vote=Gruene
                                                       0.00000
                                                                 0.000000
                                                                            14.3
## bwing=Left_Right_Wings
                                                       0.00000
                                                                 0.000000
                                                                            33.5
##
                                                           p.value
                                                                       v.test
## bwing=Center Wing
                                                     4.360677e-276
                                                                    35.503370
## f.vote ord=CDU/CSU
                                                      4.312957e-64
                                                                    16.902491
## f.vote=CDU/CSU
                                                      4.312957e-64
                                                                    16.902491
## f.vote_ord=SPD
                                                      5.401466e-55
                                                                    15.619038
## f.vote=SPD
                                                      5.401466e-55
                                                                    15.619038
## f.vote ord=FDP
                                                      6.200298e-24
                                                                    10.088671
## f.vote=FDP
                                                      6.200298e-24
                                                                    10.088671
## f.Imm=medium
                                                      1.257853e-08
                                                                     5.691694
## f.egoposition immigration=5 Neutral Level.Imm
                                                      5.513189e-07
                                                                     5.007534
## f.eastGermany=Yes.EastGermany
                                                      5.849772e-04
                                                                     3.438486
## f.duplicate=Yes.Duplicate
                                                      6.507953e-04
                                                                     3.409511
## f.egoposition_immigration=6_Level.Imm
                                                      1.102026e-03
                                                                     3.263095
## f.IncSat=high
                                                      1.331258e-02
                                                                     2.475296
## f.income=High.Sat
                                                                     2.475296
                                                      1.331258e-02
## f.political_interest=Medium.Inter
                                                      1.837781e-02
                                                                     2.357917
## f.egoposition immigration=8 Level.Imm
                                                      3.695876e-02
                                                                    -2.086219
## f.Imm=low
                                                      1.008813e-02
                                                                    -2.572794
## f.egoposition_immigration=0_Very_Open_Level.Imm 1.008813e-02
                                                                    -2.572794
## f.egoposition immigration=2 Level.Imm
                                                      2.600362e-03
                                                                   -3.011411
```

```
## f.duplicate=No.Duplicate
                                                     6.507953e-04 -3.409511
## f.eastGermany=No.EastGermany
                                                     5.849772e-04 -3.438486
## f.Imm=low medium
                                                     9.076070e-05 -3.914050
## f.vote ord=AfD
                                                     9.958160e-36 -12.477072
## f.vote=AfD
                                                     9.958160e-36 -12.477072
## f.vote ord=LINKE
                                                     6.141124e-67 -17.284633
## f.vote=LINKE
                                                     6.141124e-67 -17.284633
## f.vote_ord=Gruene
                                                     1.406134e-79 -18.888951
## f.vote=Gruene
                                                     1.406134e-79 -18.888951
## bwing=Left Right Wings
                                                    4.360677e-276 -35.503370
##
## $Left_Wing
##
                                                               Cla/Mod
                                                                           Mod/Cla
## bwing=Left_Right_Wings
                                                             79.402985 100.0000000
## f.vote_ord=Gruene
                                                            100.000000
                                                                        53.7593985
## f.vote=Gruene
                                                            100.000000
                                                                        53.7593985
## f.vote ord=LINKE
                                                            100.000000
                                                                        46.2406015
## f.vote=LINKE
                                                            100.000000
                                                                        46.2406015
## f.Imm=low medium
                                                             40.361446
                                                                        50.3759398
## f.egoposition_immigration=2_Level.Imm
                                                             45.384615
                                                                        22.1804511
## f.Imm=low
                                                             48.979592
                                                                         9.0225564
## f.egoposition immigration=0 Very Open Level.Imm
                                                             48.979592
                                                                         9.0225564
## f.egoposition_immigration=3_Level.Imm
                                                             38.059701
                                                                        19.1729323
## f.gender=F
                                                             30.086580
                                                                        52.2556391
## f.IncSat=medium
                                                             28.311688
                                                                        81.9548872
## f.gender=M
                                                             23.605948
                                                                        47.7443609
## f.IncSat=high
                                                             19.576720
                                                                        13.9097744
## f.income=High.Sat
                                                             19.576720
                                                                        13.9097744
## f.Imm=high
                                                             10.638298
                                                                        1.8796992
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm
                                                                         1.8796992
                                                             10.638298
## f.egoposition immigration=8 Level.Imm
                                                              6.451613
                                                                         0.7518797
## f.egoposition immigration=9 Level.Imm
                                                              5.882353
                                                                         0.7518797
## f.Imm=medium
                                                             21.212121
                                                                        34.2105263
## f.egoposition immigration=5 Neutral Level.Imm
                                                             15.483871
                                                                         9.0225564
## f.egoposition_immigration=7_Level.Imm
                                                             10.256410
                                                                         3.0075188
## f.egoposition immigration=6 Level.Imm
                                                             11.578947
                                                                         4.1353383
## f.Imm=medium high
                                                                         4.5112782
                                                              8.391608
## f.vote ord=AfD
                                                              0.000000
                                                                         0.0000000
## f.vote=AfD
                                                              0.000000
                                                                         0.0000000
## f.vote ord=FDP
                                                              0.000000
                                                                         0.000000
## f.vote=FDP
                                                              0.000000
                                                                         0.0000000
## f.vote_ord=SPD
                                                              0.000000
                                                                         0.0000000
## f.vote=SPD
                                                              0.000000
                                                                         0.0000000
## f.vote ord=CDU/CSU
                                                              0.000000
                                                                         0.0000000
## f.vote=CDU/CSU
                                                              0.000000
                                                                         0.0000000
## bwing=Center_Wing
                                                              0.000000
                                                                         0.0000000
                                                            Global
                                                                         p.value
## bwing=Left_Right_Wings
                                                              33.5 5.080116e-178
## f.vote_ord=Gruene
                                                              14.3 4.555935e-99
## f.vote=Gruene
                                                              14.3 4.555935e-99
```

```
12.3 8.361150e-83
## f.vote_ord=LINKE
## f.vote=LINKE
                                                              12.3 8.361150e-83
## f.Imm=low medium
                                                             33.2 9.856340e-12
## f.egoposition_immigration=2_Level.Imm
                                                              13.0 7.347278e-07
                                                              4.9 6.479798e-04
## f.Imm=low
## f.egoposition immigration=0 Very Open Level.Imm
                                                              4.9 6.479798e-04
## f.egoposition immigration=3 Level.Imm
                                                              13.4 1.798442e-03
## f.gender=F
                                                              46.2 2.119615e-02
## f.IncSat=medium
                                                             77.0 2.344145e-02
## f.gender=M
                                                              53.8 2.119615e-02
## f.IncSat=high
                                                              18.9 1.362802e-02
                                                              18.9 1.362802e-02
## f.income=High.Sat
## f.Imm=high
                                                               4.7 7.300975e-03
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm
                                                               4.7 7.300975e-03
## f.egoposition_immigration=8_Level.Imm
                                                               3.1 5.282681e-03
## f.egoposition_immigration=9_Level.Imm
                                                               3.4 2.382574e-03
## f.Imm=medium
                                                              42.9 7.895011e-04
## f.egoposition immigration=5 Neutral Level.Imm
                                                              15.5 4.059018e-04
## f.egoposition immigration=7 Level.Imm
                                                              7.8 2.687651e-04
## f.egoposition_immigration=6_Level.Imm
                                                               9.5 2.154814e-04
## f.Imm=medium high
                                                              14.3 6.708713e-09
## f.vote ord=AfD
                                                               6.9 2.200779e-10
## f.vote=AfD
                                                               6.9 2.200779e-10
## f.vote ord=FDP
                                                              12.1 3.054680e-18
## f.vote=FDP
                                                              12.1 3.054680e-18
## f.vote ord=SPD
                                                              25.5 2.115265e-41
## f.vote=SPD
                                                              25.5 2.115265e-41
## f.vote ord=CDU/CSU
                                                              28.9 4.116942e-48
## f.vote=CDU/CSU
                                                              28.9 4.116942e-48
## bwing=Center_Wing
                                                              66.5 5.080116e-178
##
                                                                v.test
## bwing=Left Right Wings
                                                             28.448539
## f.vote ord=Gruene
                                                             21.126332
## f.vote=Gruene
                                                            21.126332
## f.vote_ord=LINKE
                                                             19.277115
## f.vote=LINKE
                                                             19.277115
## f.Imm=low medium
                                                              6.808585
## f.egoposition_immigration=2_Level.Imm
                                                             4.951952
## f.Imm=low
                                                             3.410693
## f.egoposition immigration=0_Very_Open_Level.Imm
                                                             3.410693
## f.egoposition_immigration=3_Level.Imm
                                                             3.121644
## f.gender=F
                                                              2.304472
## f.IncSat=medium
                                                             2.266162
## f.gender=M
                                                             -2.304472
## f.IncSat=high
                                                             -2.466922
## f.income=High.Sat
                                                            -2.466922
## f.Imm=high
                                                             -2.682795
## f.egoposition_immigration=10_Very_Restrictive_Level.Imm -2.682795
## f.egoposition_immigration=8_Level.Imm
                                                             -2.789271
## f.egoposition immigration=9 Level.Imm
                                                            -3.037869
```

```
## f.Imm=medium
                                                             -3.356450
## f.egoposition immigration=5 Neutral Level.Imm
                                                             -3.536217
## f.egoposition immigration=7 Level.Imm
                                                             -3.643682
## f.egoposition immigration=6 Level.Imm
                                                             -3.700139
## f.Imm=medium high
                                                             -5.798058
## f.vote ord=AfD
                                                             -6.346633
## f.vote=AfD
                                                             -6.346633
## f.vote_ord=FDP
                                                             -8.709407
## f.vote=FDP
                                                             -8.709407
                                                            -13.477726
## f.vote ord=SPD
## f.vote=SPD
                                                            -13.477726
## f.vote_ord=CDU/CSU
                                                            -14.573901
## f.vote=CDU/CSU
                                                            -14.573901
## bwing=Center Wing
                                                            -28.448539
##
## $Right_Wing
##
                                                                           Mod/Cla
                                                                Cla/Mod
## f.vote ord=AfD
                                                            100.000000 100.000000
## f.vote=AfD
                                                             100.000000 100.000000
## bwing=Left_Right_Wings
                                                             20.597015 100.000000
## f.Imm=medium high
                                                             25.174825
                                                                         52.173913
## f.egoposition immigration=8 Level.Imm
                                                             45.161290
                                                                         20.289855
## f.Imm=high
                                                             34.042553
                                                                         23.188406
## f.egoposition immigration=10 Very Restrictive Level.Imm
                                                             34.042553
                                                                         23.188406
## f.gender=M
                                                              10.408922
                                                                         81.159420
## f.mout=MvOut.Yes
                                                             37.500000
                                                                         13.043478
## f.duplicate=No.Duplicate
                                                              8.892356
                                                                         82.608696
## f.egoposition immigration=7 Level.Imm
                                                             17.948718
                                                                         20.289855
## f.egoposition immigration=9 Level.Imm
                                                             23.529412
                                                                         11.594203
## f.eastGermany=No.EastGermany
                                                                        40.579710
                                                             11.618257
## f.PolInt=low
                                                             66.666667
                                                                          2.898551
## f.political interest=Low.Inter
                                                             66.666667
                                                                          2.898551
## f.IncSat=low to medium
                                                              17.857143
                                                                          7.246377
## f.income=Low to Medium.Sat
                                                             17.857143
                                                                          7.246377
## f.egoposition_immigration=1_Level.Imm
                                                              1.470588
                                                                          1.449275
## f.egoposition immigration=3 Level.Imm
                                                              2.985075
                                                                          5.797101
## f.eastGermany=Yes.EastGermany
                                                                         59.420290
                                                              5.401845
## f.egoposition immigration=5 Neutral Level.Imm
                                                              1.290323
                                                                          2.898551
## f.duplicate=Yes.Duplicate
                                                              3.342618
                                                                        17.391304
## f.egoposition immigration=4 Level.Imm
                                                              1.117318
                                                                          2.898551
## f.vote ord=FDP
                                                              0.000000
                                                                          0.000000
## f.vote=FDP
                                                              0.000000
                                                                          0.000000
## f.vote ord=LINKE
                                                              0.000000
                                                                          0.000000
## f.vote=LINKE
                                                              0.000000
                                                                          0.000000
## f.egoposition_immigration=2_Level.Imm
                                                              0.000000
                                                                          0.000000
## f.vote_ord=Gruene
                                                              0.000000
                                                                          0.000000
## f.vote=Gruene
                                                              0.000000
                                                                          0.000000
## f.mout=MvOut.No
                                                              6.147541
                                                                         86.956522
## f.gender=F
                                                              2.813853
                                                                         18.840580
## f.Imm=medium
                                                              2.564103
                                                                         15.942029
```

```
1.506024
                                                                        7.246377
## f.Imm=low_medium
## f.vote ord=SPD
                                                             0.000000
                                                                        0.000000
## f.vote=SPD
                                                             0.000000
                                                                        0.000000
## f.vote ord=CDU/CSU
                                                             0.000000
                                                                        0.000000
## f.vote=CDU/CSU
                                                             0.000000
                                                                        0.000000
## bwing=Center Wing
                                                             0.000000
                                                                        0.000000
##
                                                           Global
                                                                        p.value
## f.vote_ord=AfD
                                                               6.9 1.889108e-108
## f.vote=AfD
                                                               6.9 1.889108e-108
                                                             33.5 9.958160e-36
## bwing=Left Right Wings
## f.Imm=medium high
                                                              14.3 7.616170e-15
                                                              3.1 1.675803e-09
## f.egoposition_immigration=8_Level.Imm
## f.Imm=high
                                                              4.7 1.468400e-08
                                                              4.7 1.468400e-08
## f.egoposition immigration=10 Very Restrictive Level.Imm
## f.gender=M
                                                             53.8 1.101835e-06
## f.mout=MvOut.Yes
                                                               2.4 1.316568e-05
                                                             64.1 5.540764e-04
## f.duplicate=No.Duplicate
## f.egoposition immigration=7 Level.Imm
                                                              7.8 5.783367e-04
## f.egoposition immigration=9 Level.Imm
                                                              3.4 1.731296e-03
## f.eastGermany=No.EastGermany
                                                             24.1 1.731634e-03
## f.PolInt=low
                                                              0.3 1.377478e-02
## f.political_interest=Low.Inter
                                                              0.3 1.377478e-02
## f.IncSat=low_to_medium
                                                              2.8 4.793709e-02
## f.income=Low to Medium.Sat
                                                              2.8 4.793709e-02
## f.egoposition immigration=1 Level.Imm
                                                              6.8 4.815760e-02
## f.egoposition immigration=3 Level.Imm
                                                             13.4 4.305493e-02
## f.eastGermany=Yes.EastGermany
                                                             75.9 1.731634e-03
## f.egoposition immigration=5 Neutral Level.Imm
                                                             15.5 6.970986e-04
## f.duplicate=Yes.Duplicate
                                                             35.9 5.540764e-04
## f.egoposition_immigration=4_Level.Imm
                                                             17.9 1.193747e-04
## f.vote ord=FDP
                                                             12.1 9.721535e-05
## f.vote=FDP
                                                             12.1 9.721535e-05
                                                             12.3 8.254390e-05
## f.vote ord=LINKE
## f.vote=LINKE
                                                             12.3 8.254390e-05
## f.egoposition_immigration=2_Level.Imm
                                                             13.0 4.641675e-05
## f.vote ord=Gruene
                                                             14.3 1.573110e-05
## f.vote=Gruene
                                                             14.3 1.573110e-05
## f.mout=MvOut.No
                                                             97.6 1.316568e-05
## f.gender=F
                                                             46.2 1.101835e-06
## f.Imm=medium
                                                             42.9 9.629260e-07
## f.Imm=low medium
                                                             33.2 1.727176e-07
## f.vote_ord=SPD
                                                             25.5 6.459324e-10
## f.vote=SPD
                                                             25.5 6.459324e-10
## f.vote ord=CDU/CSU
                                                             28.9 2.190738e-11
## f.vote=CDU/CSU
                                                             28.9 2.190738e-11
## bwing=Center_Wing
                                                             66.5 9.958160e-36
                                                               v.test
## f.vote ord=AfD
                                                            22.123229
## f.vote=AfD
                                                            22.123229
                                                             12.477072
## bwing=Left Right Wings
```

```
## f.Imm=medium_high
                                                               7.773807
## f.egoposition_immigration=8_Level.Imm
                                                               6.026469
## f.Imm=high
                                                               5.665215
## f.egoposition immigration=10 Very Restrictive Level.Imm
                                                               5.665215
## f.gender=M
                                                               4.872520
## f.mout=MvOut.Yes
                                                               4.357333
## f.duplicate=No.Duplicate
                                                               3.453152
## f.egoposition_immigration=7_Level.Imm
                                                               3.441576
## f.egoposition immigration=9 Level.Imm
                                                               3.132830
## f.eastGermany=No.EastGermany
                                                               3.132773
## f.PolInt=low
                                                               2.463084
## f.political_interest=Low.Inter
                                                               2.463084
## f.IncSat=low to medium
                                                               1.977926
## f.income=Low to Medium.Sat
                                                               1.977926
## f.egoposition_immigration=1_Level.Imm
                                                              -1.975975
## f.egoposition immigration=3 Level.Imm
                                                              -2.023177
## f.eastGermany=Yes.EastGermany
                                                              -3.132773
## f.egoposition immigration=5 Neutral Level.Imm
                                                              -3.390718
## f.duplicate=Yes.Duplicate
                                                              -3.453152
## f.egoposition immigration=4 Level.Imm
                                                              -3.847407
## f.vote ord=FDP
                                                              -3.897439
## f.vote=FDP
                                                              -3.897439
## f.vote_ord=LINKE
                                                              -3.936892
## f.vote=LINKE
                                                              -3.936892
## f.egoposition_immigration=2 Level.Imm
                                                              -4.072973
## f.vote ord=Gruene
                                                              -4.318194
## f.vote=Gruene
                                                              -4.318194
## f.mout=MvOut.No
                                                              -4.357333
## f.gender=F
                                                              -4.872520
                                                              -4.899067
## f.Imm=medium
## f.Imm=low medium
                                                              -5.226533
## f.vote ord=SPD
                                                              -6.178794
## f.vote=SPD
                                                              -6.178794
## f.vote ord=CDU/CSU
                                                              -6.692711
## f.vote=CDU/CSU
                                                              -6.692711
                                                             -12.477072
## bwing=Center_Wing
```

### 4.3 Modelling

#### 4.3.1 Nominal Models

Comparison of Variables' Numerical and Categorical Representation for Nominal Models

```
nm0$dev - nm1_imm_con$dev

## [1] 131.7249

nm0$dev - nm1_imm_con_sq$dev
```

## [1] 145.5295

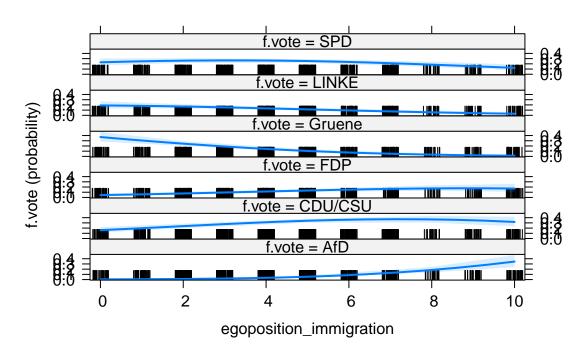
nmO\$dev - nm1\_imm\_con\_cb\$dev

```
## [1] 162.3689
nm0$dev - nm1 imm con qd$dev
## [1] 171.1001
nm0$dev - nm1_imm_cat$dev
## [1] 224.1982
nm0$dev - nm1_imm_cat_new$dev
## [1] 172.0104
anova(nm1 imm con, nm1 imm con sq, test="Chisq")
## Likelihood ratio tests of Multinomial Models
## Response: f.vote
##
                                Model Resid. df Resid. Dev
                                                             Test
                                                                    Df LR stat.
## 1
             egoposition_immigration
                                           3510
                                                  2236.832
                                                  2223.027 1 vs 2 5 13.80457
## 2 poly(egoposition immigration, 2)
                                           3505
       Pr(Chi)
##
## 1
## 2 0.01689968
anova(nm1_imm_con_sq, nm1_imm_con_cb, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
                                Model Resid. df Resid. Dev
##
                                                             Test
                                                                    Df LR stat.
## 1 poly(egoposition_immigration, 2)
                                           3505
                                                  2223.027
## 2 poly(egoposition_immigration, 3)
                                           3500
                                                  2206.187 1 vs 2 5 16.83944
##
        Pr(Chi)
## 1
## 2 0.004814587
anova(nm1_imm_con_cb, nm1_imm_con_qd, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
##
                                Model Resid. df Resid. Dev
                                                             Test Df LR stat.
## 1 poly(egoposition_immigration, 3)
                                           3500
                                                  2206.187
## 2 poly(egoposition_immigration, 4)
                                           3495
                                                  2197.456 1 vs 2 5 8.731158
      Pr(Chi)
##
## 1
## 2 0.1202799
Anova(nm1_imm_con, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
```

```
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
##
                          LR Chisq Df Pr(>Chisq)
                            131.72 5 < 2.2e-16 ***
## egoposition immigration
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Anova(nm1_imm_con_sq, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
##
                                   LR Chisq Df Pr(>Chisq)
## poly(egoposition immigration, 2) 145.53 10 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1 imm con cb, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
                                   LR Chisq Df Pr(>Chisq)
##
                                   162.37 15 < 2.2e-16 ***
## poly(egoposition immigration, 3)
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1 imm con qd, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
## Response: f.vote
```

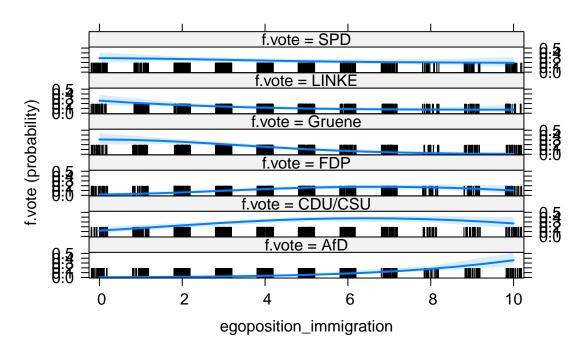
```
##
                                   LR Chisq Df Pr(>Chisq)
## poly(egoposition_immigration, 4) 171.1 20 < 2.2e-16 ***</pre>
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_imm_cat, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
                            LR Chisq Df Pr(>Chisq)
## f.egoposition immigration
                               224.2 50 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1 imm cat new, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
        LR Chisq Df Pr(>Chisq)
## f.Imm 172.01 20 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(allEffects(nm1 imm con),ask=FALSE, main="Effects Imm Continuous")
```

### **Effects Imm Continuous**



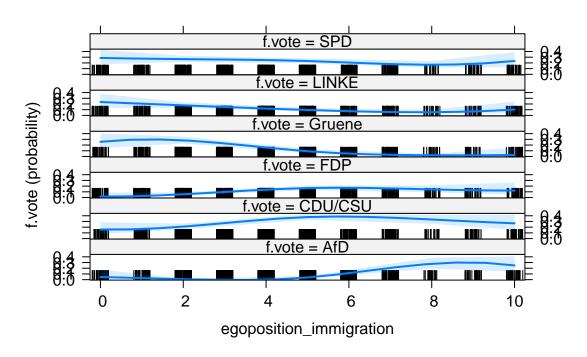
plot(allEffects(nm1\_imm\_con\_sq),ask=FALSE,main="Effects Imm Continuous Squared")

### **Effects Imm Continuous Squared**



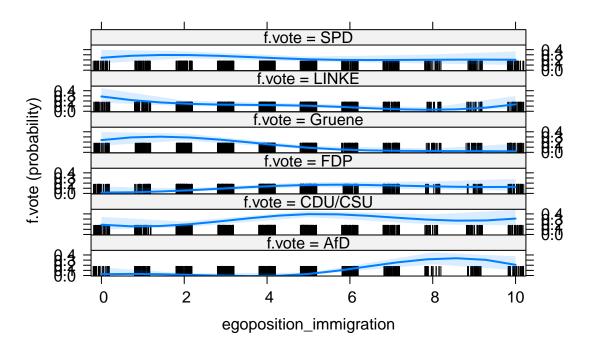
plot(allEffects(nm1\_imm\_con\_cb),ask=FALSE, main="Effects Imm Continuous Cubed")

# **Effects Imm Continuous Cubed**



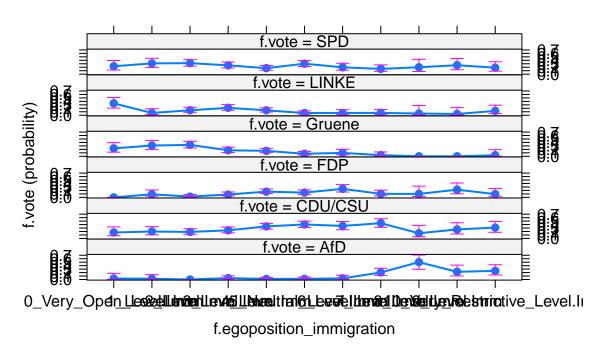
plot(allEffects(nm1\_imm\_con\_qd),ask=FALSE, main="Effects Imm Continuous Quadratic")

### **Effects Imm Continuous Quadratic**



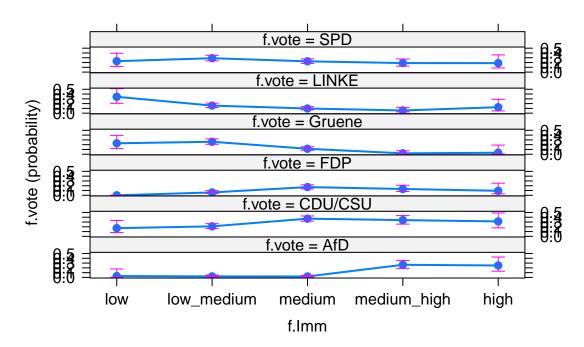
plot(allEffects(nm1\_imm\_cat),ask=FALSE, main="Effects Imm Categorical")

### **Effects Imm Categorical**



plot(allEffects(nm1\_imm\_cat\_new),ask=FALSE, main="Effects Imm Categorical")

### **Effects Imm Categorical**



# nm1\_imm\_con\_cb is better concerning AIC but we lose 5 df that compared to new factor
#step(nm1\_imm\_cat\_new)

nm0\$dev - nm1\_polint\_con\$dev

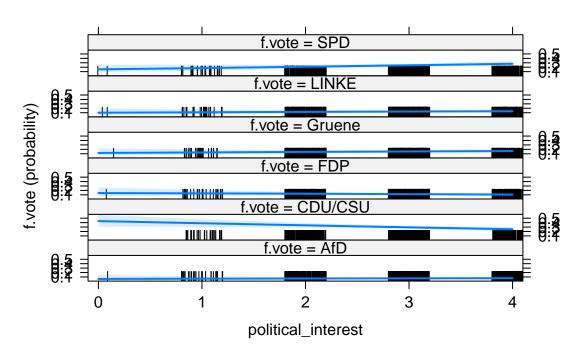
## [1] 6.806457

```
nm0$dev - nm1_polint_con_sq$dev
## [1] 21.10837
nm0$dev - nm1 polint con cb$dev
## [1] 30.35926
nmO$dev - nm1_polint_con_qd$dev
## [1] 32.99533
nm0$dev - nm1_polint_cat$dev
## [1] 32.99949
nmO$dev - nm1_polint_cat_new$dev
## [1] 9.884028
anova(nm1_polint_con, nm1_polint_con_sq, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
##
                           Model Resid. df Resid. Dev
                                                        Test
                                                                Df LR stat.
## 1
              political_interest
                                      3510
                                             2361.750
## 2 poly(political interest, 2)
                                      3505
                                             2347.448 1 vs 2 5 14.30191
##
        Pr(Chi)
## 1
## 2 0.01380121
anova(nm1 polint con sq, nm1 polint con cb, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
##
                           Model Resid. df Resid. Dev
                                                        Test
                                                                Df LR stat.
## 1 poly(political_interest, 2)
                                      3505
                                             2347.448
## 2 poly(political_interest, 3)
                                      3500
                                             2338.197 1 vs 2 5 9.250894
##
        Pr(Chi)
## 1
## 2 0.09946569
anova(nm1 polint con cb, nm1 polint con qd, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
                           Model Resid. df Resid. Dev
##
                                                        Test
                                                                Df LR stat.
## 1 poly(political_interest, 3)
                                      3500
                                             2338.197
                                      3495
## 2 poly(political_interest, 4)
                                             2335.561 1 vs 2 5 2.636069
##
      Pr(Chi)
## 1
## 2 0.7558777
```

```
Anova(nm1_polint_con, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
## Response: f.vote
##
                     LR Chisq Df Pr(>Chisq)
## political interest
                       6.8065
                              5
                                     0.2354
Anova(nm1_polint_con_sq, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
                              LR Chisq Df Pr(>Chisq)
## poly(political_interest, 2)
                                21.108 10
                                            0.02035 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_polint_con_cb, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
                              LR Chisq Df Pr(>Chisq)
## poly(political interest, 3)
                                30.359 15
                                             0.01069 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_polint_con_qd, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
```

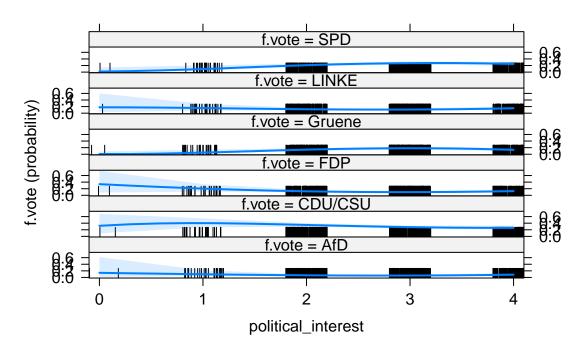
```
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
##
                              LR Chisq Df Pr(>Chisq)
## poly(political_interest, 4)
                                32.995 20
                                             0.03378 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_polint_cat, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
##
                       LR Chisq Df Pr(>Chisq)
## f.political interest
                         32.999 20
                                      0.03375 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_polint_cat_new, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
## Response: f.vote
           LR Chisq Df Pr(>Chisq)
              9.884 10
                           0.4507
## f.PolInt
plot(allEffects(nm1_polint_con),ask=FALSE, main="Effects Pol Int Continuous")
```

# **Effects Pol Int Continuous**



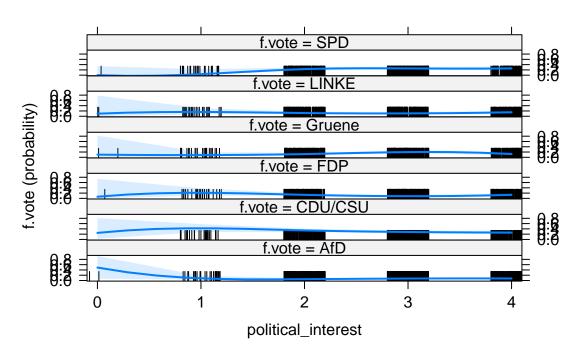
plot(allEffects(nm1\_polint\_con\_sq),ask=FALSE,main="Effects Pol Int Continuous Squared")

# **Effects Pol Int Continuous Squared**



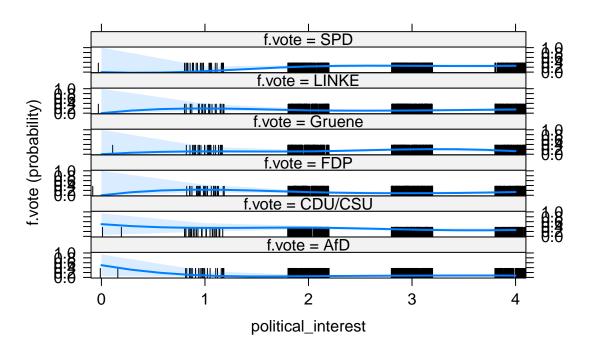
plot(allEffects(nm1\_polint\_con\_cb), ask=FALSE, main="Effects Pol Int Continuous Cubed")

# **Effects Pol Int Continuous Cubed**



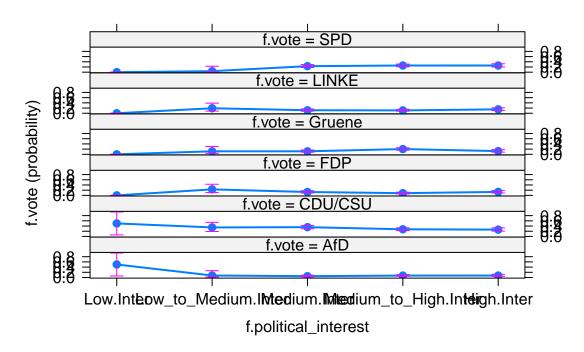
plot(allEffects(nm1\_polint\_con\_qd),ask=FALSE, main="Effects Pol Int Continuous Quadratic

### **Effects Pol Int Continuous Quadratic**



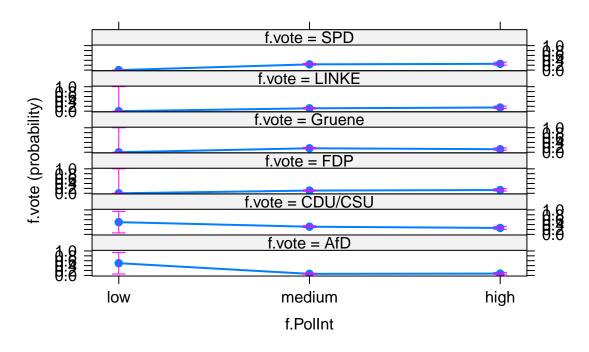
plot(allEffects(nm1\_polint\_cat),ask=FALSE, main="Effects Pol Int Categorical")

# **Effects Pol Int Categorical**



plot(allEffects(nm1\_polint\_cat\_new),ask=FALSE, main="Effects Pol Int Categorical")

### **Effects Pol Int Categorical**



#step(nm1\_polint\_con\_sq)

nmO\$dev - nm1\_inc\_con\$dev

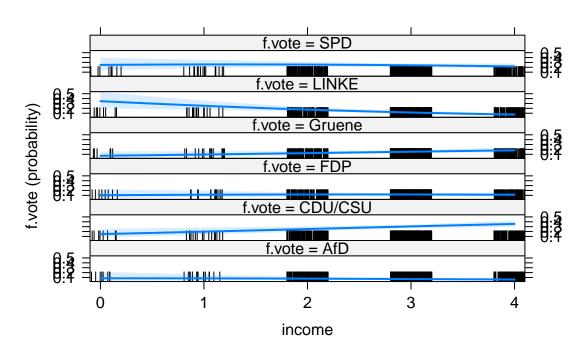
## [1] 17.92852

```
nm0$dev - nm1_inc_con_sq$dev
## [1] 24.23512
nm0$dev - nm1_inc_con_cb$dev
## [1] 31.37888
nm0$dev - nm1_inc_con_qd$dev
## [1] 31.88161
nm0$dev - nm1_inc_cat$dev
## [1] 31.89324
nm0$dev - nm1_inc_cat_new$dev
## [1] 21.60993
anova(nm1 inc con, nm1 inc con sq, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
##
               Model Resid. df Resid. Dev
                                            Test Df LR stat.
                                                                  Pr(Chi)
## 1
              income
                          3510
                                 2350.628
## 2 poly(income, 2)
                          3505
                                 2344.321 1 vs 2
                                                     5 6.306599 0.2775181
anova(nm1 inc con sq, nm1 inc con cb, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
               Model Resid. df Resid. Dev
##
                                            Test Df LR stat.
                                                                  Pr(Chi)
## 1 poly(income, 2)
                          3505
                                 2344.321
## 2 poly(income, 3)
                          3500
                                 2337.178 1 vs 2
                                                     5 7.143764 0.2101661
anova(nm1_inc_con_cb, nm1_inc_con_qd, test="Chisq")
## Likelihood ratio tests of Multinomial Models
##
## Response: f.vote
               Model Resid. df Resid. Dev
                                                                   Pr(Chi)
##
                                            Test
                                                    Df LR stat.
## 1 poly(income, 3)
                                 2337.178
                          3500
                                 2336.675 1 vs 2 5 0.5027325 0.9920229
## 2 poly(income, 4)
                          3495
Anova(nm1_inc_con, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
```

```
##
## Response: f.vote
         LR Chisq Df Pr(>Chisq)
## income 17.928 5 0.003037 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_inc_con_sq, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
## Response: f.vote
##
                  LR Chisq Df Pr(>Chisq)
## poly(income, 2) 24.235 10
                                 0.007 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_inc_con_cb, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
##
                  LR Chisq Df Pr(>Chisq)
## poly(income, 3)
                    31.379 15 0.007814 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_inc_con_qd, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
## Response: f.vote
##
                  LR Chisq Df Pr(>Chisq)
## poly(income, 4)
                    31.882 20
                               0.04458 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

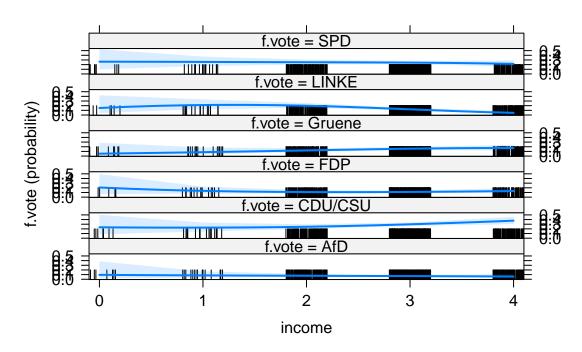
```
Anova(nm1_inc_cat, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
## Response: f.vote
           LR Chisq Df Pr(>Chisq)
##
             31.893 20
                           0.04445 *
## f.income
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(nm1_inc_cat_new, test="Chisq")
## # weights: 12 (5 variable)
## initial value 1261.398666
## iter 10 value 1184.278222
## final value 1184.278203
## converged
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote
           LR Chisq Df Pr(>Chisq)
## f.IncSat
              21.61 15
                            0.1184
plot(allEffects(nm1_inc_con),ask=FALSE, main="Effects Inc Sat Continuous")
```

#### **Effects Inc Sat Continuous**



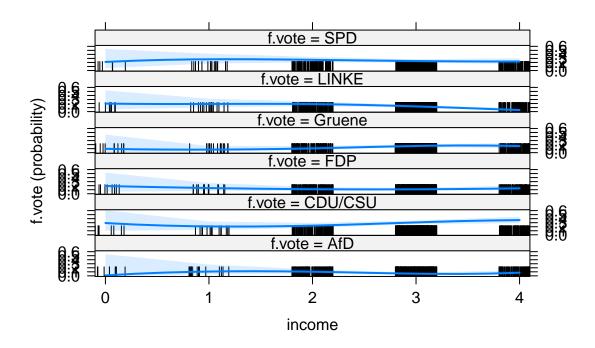
plot(allEffects(nm1\_inc\_con\_sq),ask=FALSE,main="Effects Inc Sat Continuous Squared")

# **Effects Inc Sat Continuous Squared**



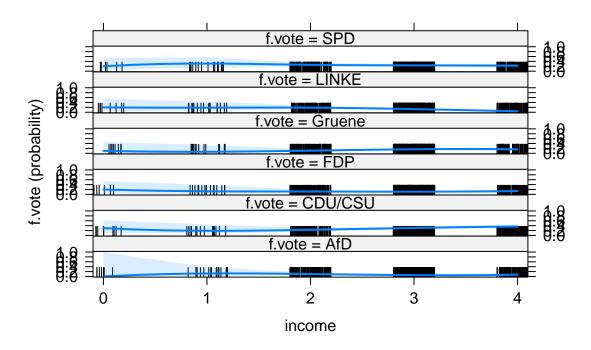
plot(allEffects(nm1\_inc\_con\_cb), ask=FALSE, main="Effects Inc Sat Continuous Cubed")

### **Effects Inc Sat Continuous Cubed**



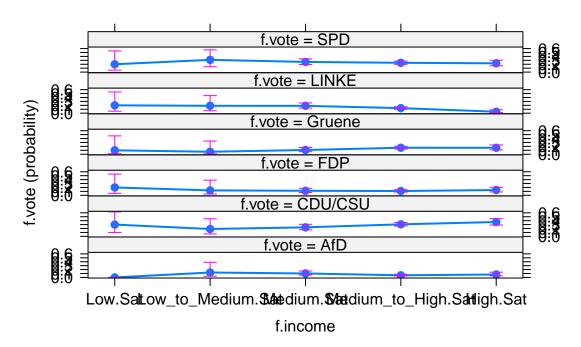
plot(allEffects(nm1\_inc\_con\_qd),ask=FALSE, main="Effects Inc Sat Continuous Quadratic")

# **Effects Inc Sat Continuous Quadratic**



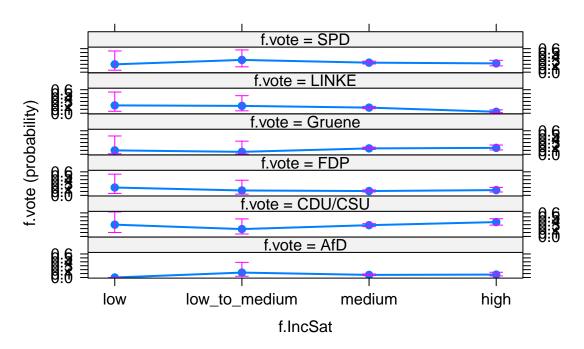
plot(allEffects(nm1\_inc\_cat),ask=FALSE, main="Effects Inc Sat Categorical")

### **Effects Inc Sat Categorical**



plot(allEffects(nm1\_inc\_cat\_new),ask=FALSE, main="Effects Inc Sat Categorical")

### **Effects Inc Sat Categorical**



#step(nm1\_imm\_cat\_new)

#### 4.3.2 Ordinal Models

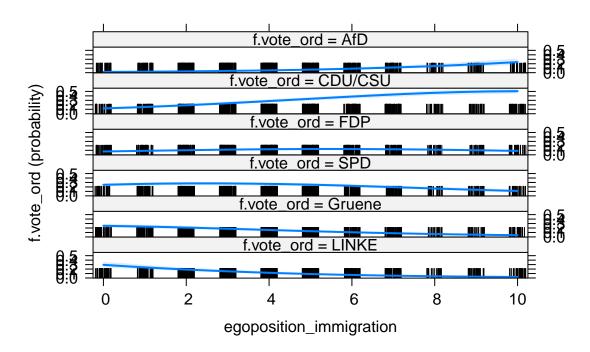
## 2 0.3907153

```
Comparison of Variables' Numerical and Categorical Representation for Ordinal Models
om0$dev - om1_imm_con$dev
## [1] 100.8407
\verb|om0\$dev - om1_imm_con_sq\$dev|\\
## [1] 101.5774
omO$dev - om1_imm_con_cb$dev
## [1] 107.5449
om0$dev - om1_imm_con_qd$dev
## [1] 109.5187
anova(om1_imm_con, om1_imm_con_sq, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote ord
##
                                  Model Resid. df Resid. Dev
                                                                Test
                                                                         Df
                                                                             LR stat.
              egoposition_immigration
                                              698
                                                     2267.716
## 2 poly(egoposition_immigration, 2)
                                                                          1 0.7367148
                                              697
                                                     2266.979 1 vs 2
       Pr(Chi)
##
## 1
```

```
anova(om1_imm_con_sq, om1_imm_con_cb, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote ord
                               Model Resid. df Resid. Dev
##
                                                            Test
                                                                   Df LR stat.
## 1 poly(egoposition immigration, 2)
                                           697
                                                 2266.979
## 2 poly(egoposition immigration, 3)
                                           696
                                                 2261.012 1 vs 2 1 5.967445
##
       Pr(Chi)
## 1
## 2 0.01457238
anova(om1_imm_con_cb, om1_imm_con_qd, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote_ord
                                                            Test Df LR stat.
                               Model Resid. df Resid. Dev
## 1 poly(egoposition immigration, 3)
                                           696
                                                 2261.012
## 2 poly(egoposition_immigration, 4)
                                           695
                                                 2259.038 1 vs 2 1 1.973788
      Pr(Chi)
##
## 1
## 2 0.1600463
Anova(om1 imm con, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
                          LR Chisq Df Pr(>Chisq)
                            100.84 1 < 2.2e-16 ***
## egoposition_immigration
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1_imm_con_sq, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
                                   LR Chisq Df Pr(>Chisq)
##
## poly(egoposition_immigration, 2)
                                     101.58 2 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Anova(om1 imm con cb, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
##
                                   LR Chisq Df Pr(>Chisq)
## poly(egoposition_immigration, 3) 107.55 3 < 2.2e-16 ***</pre>
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

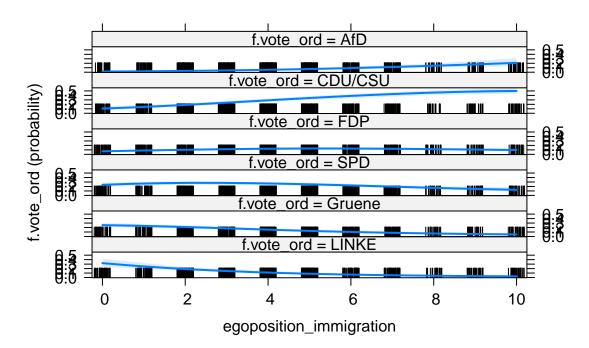
```
Anova(om1_imm_con_qd, test="Chisq")
## Analysis of Deviance Table (Type II tests)
## Response: f.vote ord
                                   LR Chisq Df Pr(>Chisq)
##
## poly(egoposition_immigration, 4) 109.52 4 < 2.2e-16 ***</pre>
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1 imm cat, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
                            LR Chisq Df Pr(>Chisq)
##
## f.egoposition_immigration 121.65 10 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1 imm cat new, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote_ord
        LR Chisq Df Pr(>Chisq)
## f.Imm 111.29 4 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(allEffects(om1_imm_con),ask=FALSE, main="Effects Imm Continuous")
##
## Re-fitting to get Hessian
```

### **Effects Imm Continuous**



plot(allEffects(om1\_imm\_con\_sq),ask=FALSE,main="Effects Imm Continuous Squared")
##
## Re-fitting to get Hessian

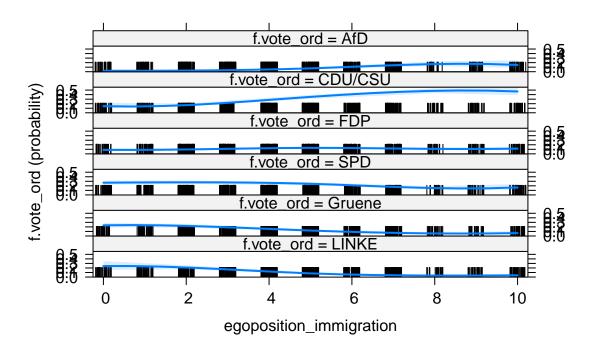
### **Effects Imm Continuous Squared**



plot(allEffects(om1\_imm\_con\_cb),ask=FALSE, main="Effects Imm Continuous Cubed")
##

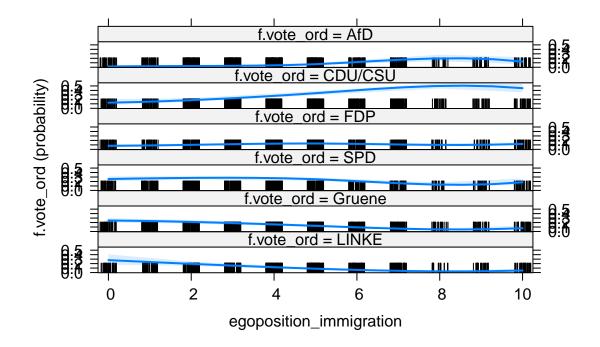
## Re-fitting to get Hessian

### **Effects Imm Continuous Cubed**



plot(allEffects(om1\_imm\_con\_qd),ask=FALSE, main="Effects Imm Continuous Quadratic")
##
## Re-fitting to get Hessian

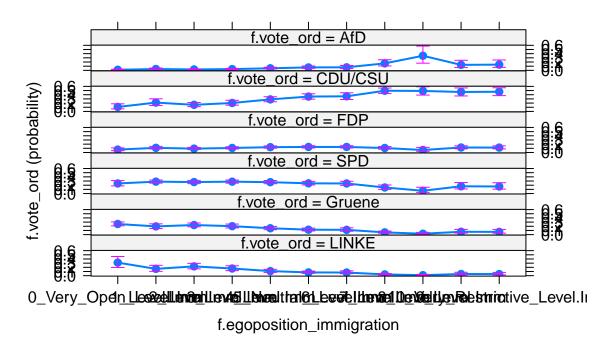
#### **Effects Imm Continuous Quadratic**



plot(allEffects(om1\_imm\_cat),ask=FALSE, main="Effects Imm Categorical")

##
## Re-fitting to get Hessian

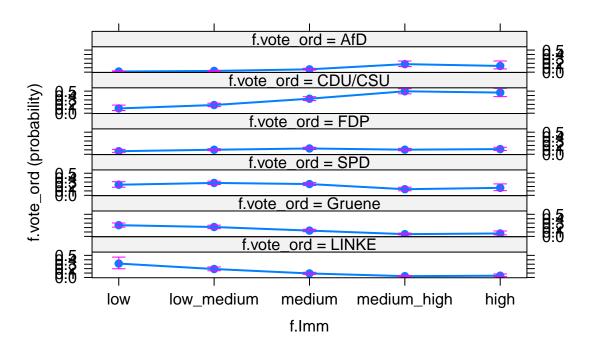
### **Effects Imm Categorical**



plot(allEffects(om1\_imm\_cat\_new),ask=FALSE, main="Effects Imm Categorical")

##
## Re-fitting to get Hessian

### **Effects Imm Categorical**



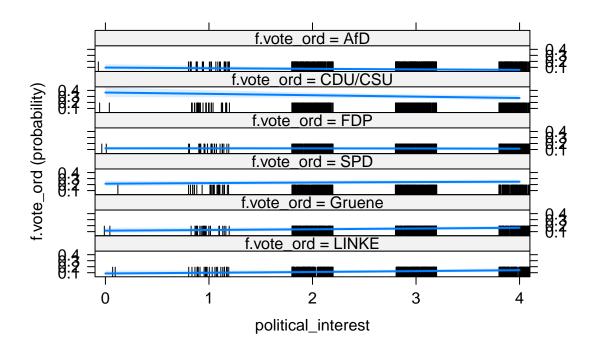
# om1\_imm\_con\_cb is better concerning AIC but we lose 5 df that compared to new factor
#step(om1\_imm\_cat\_new)

```
om0$dev - om1_polint_con$dev
## [1] 2.985803
om0$dev - om1_polint_con_sq$dev
## [1] 5.079863
om0$dev - om1_polint_con_cb$dev
## [1] 5.232933
om0$dev - om1_polint_con_qd$dev
## [1] 7.734318
om0$dev - om1_polint_cat$dev
## [1] 7.73432
om0$dev - om1 polint cat new$dev
## [1] 4.840537
anova(om1_polint_con, om1_polint_con_sq, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote_ord
                           Model Resid. df Resid. Dev
##
                                                        Test
                                                                Df LR stat.
                                     698
                                             2365.571
## 1
              political interest
## 2 poly(political_interest, 2) 697
                                             2363.477 1 vs 2 1 2.094061
##
       Pr(Chi)
## 1
## 2 0.1478726
anova(om1_polint_con_sq, om1_polint_con_cb, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote_ord
                           Model Resid. df Resid. Dev
                                                                   LR stat.
##
                                                        Test
                                                                Df
## 1 poly(political_interest, 2)
                                       697
                                             2363.477
## 2 poly(political_interest, 3)
                                       696
                                             2363.323 1 vs 2
                                                                1 0.1530697
##
       Pr(Chi)
## 1
## 2 0.6956189
anova(om1_polint_con_cb, om1_polint_con_qd, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote_ord
##
                           Model Resid. df Resid. Dev
                                                                Df LR stat.
                                                        Test
## 1 poly(political_interest, 3)
                                             2363.323
                                       696
## 2 poly(political interest, 4)
                                       695
                                             2360.822 1 vs 2
                                                                 1 2.501385
```

```
##
       Pr(Chi)
## 1
## 2 0.1137462
Anova(om1_polint_con, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
##
                      LR Chisq Df Pr(>Chisq)
## political interest
                        2.9858 1
                                       0.084 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1_polint_con_sq, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote_ord
##
                               LR Chisq Df Pr(>Chisq)
## poly(political_interest, 2)
                                5.0799 2
                                             0.07887 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1 polint con cb, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
##
                               LR Chisq Df Pr(>Chisq)
## poly(political interest, 3)
                                               0.1555
                                 5.2329
                                        3
Anova(om1_polint_con_qd, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
                               LR Chisq Df Pr(>Chisq)
## poly(political interest, 4)
                                7.7343
                                               0.1018
Anova(om1_polint_cat, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote_ord
                        LR Chisq Df Pr(>Chisq)
## f.political interest 7.7343 4
                                        0.1018
Anova(om1 polint cat new, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
           LR Chisq Df Pr(>Chisq)
## f.PolInt
             4.8405 2
                            0.0889 .
```

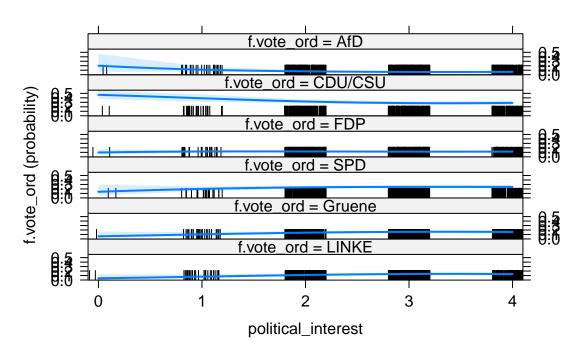
```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(allEffects(om1_polint_con),ask=FALSE, main="Effects Pol Int Continuous")
##
## Re-fitting to get Hessian
```

### **Effects Pol Int Continuous**



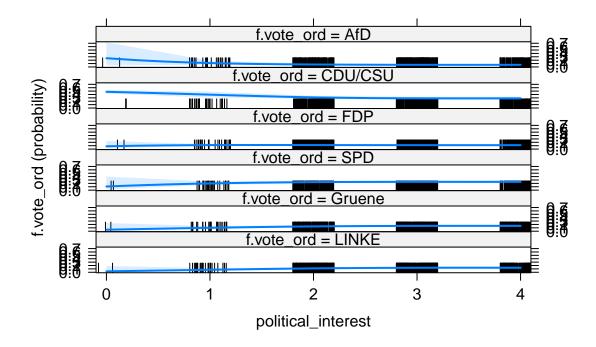
plot(allEffects(om1\_polint\_con\_sq),ask=FALSE,main="Effects Pol Int Continuous Squared")
##
## Re-fitting to get Hessian

## **Effects Pol Int Continuous Squared**



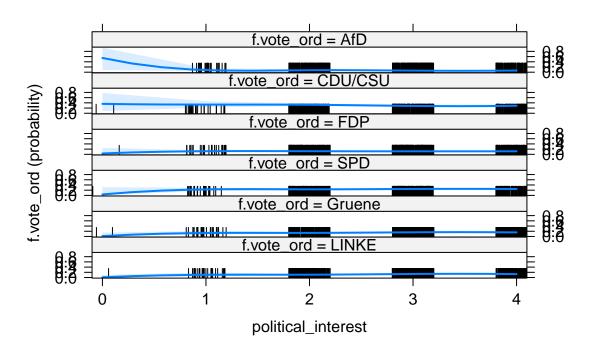
plot(allEffects(om1\_polint\_con\_cb),ask=FALSE, main="Effects Pol Int Continuous Cubed")
##
## Re-fitting to get Hessian

#### **Effects Pol Int Continuous Cubed**



plot(allEffects(om1\_polint\_con\_qd),ask=FALSE, main="Effects Pol Int Continuous Quadratic
##
## Re-fitting to get Hessian

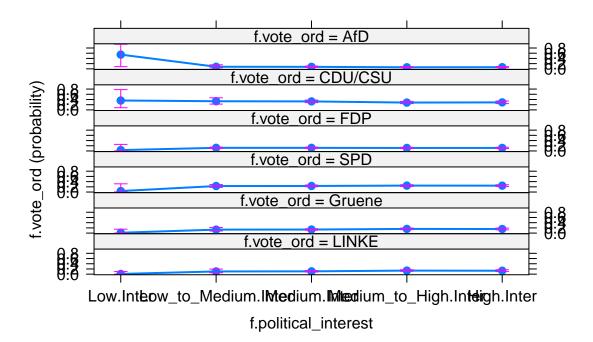
### **Effects Pol Int Continuous Quadratic**



plot(allEffects(om1\_polint\_cat),ask=FALSE, main="Effects Pol Int Categorical")

##
## Re-fitting to get Hessian

### **Effects Pol Int Categorical**

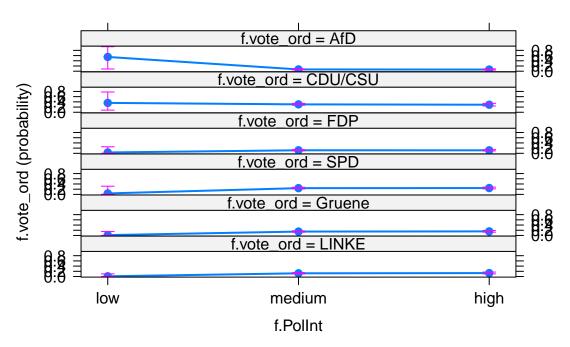


plot(allEffects(om1\_polint\_cat\_new),ask=FALSE, main="Effects Pol Int Categorical")

##

## Re-fitting to get Hessian

#### **Effects Pol Int Categorical**



```
om0$dev - om1_inc_con$dev
## [1] 4.579493
om0$dev - om1_inc_con_sq$dev
## [1] 6.595547
om0$dev - om1_inc_con_cb$dev
## [1] 7.224751
om0$dev - om1_inc_con_qd$dev
## [1] 7.226956
om0$dev - om1_inc_cat$dev
## [1] 7.226959
om0$dev - om1_inc_cat_new$dev
## [1] 7.068024
anova(om1_inc_con_sq, om1_inc_con_cb, test="Chisq")
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote_ord
               Model Resid. df Resid. Dev
                                            Test
                                                                   Pr(Chi)
##
                                                        LR stat.
## 1 poly(income, 2)
                           697
                                 2361.961
                                                     1 0.6292041 0.4276474
## 2 poly(income, 3)
                           696
                                 2361.332 1 vs 2
anova(om1 inc con cb, om1 inc con qd, test="Chisq")
```

```
## Likelihood ratio tests of ordinal regression models
##
## Response: f.vote ord
##
              Model Resid. df Resid. Dev
                                           Test
                                                   Df
                                                         LR stat.
                                                                    Pr(Chi)
## 1 poly(income, 3)
                     696
                                2361.332
                                2361.329 1 vs 2 1 0.002204762 0.9625492
## 2 poly(income, 4)
                          695
Anova(om1_inc_con, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
         LR Chisq Df Pr(>Chisq)
           4.5795 1
## income
                        0.03236 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1 inc con sq, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote_ord
##
                  LR Chisq Df Pr(>Chisq)
## poly(income, 2)
                    6.5955 2
                                 0.03697 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1 inc con cb, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote_ord
                  LR Chisq Df Pr(>Chisq)
## poly(income, 3) 7.2248 3
                                 0.06507 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(om1 inc con qd, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
                  LR Chisq Df Pr(>Chisq)
## poly(income, 4)
                     7.227
                            4
                                  0.1244
Anova(om1 inc cat, test="Chisq")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.vote ord
           LR Chisq Df Pr(>Chisq)
##
              7.227 4
                           0.1244
## f.income
```

```
Anova(om1_inc_cat_new, test="Chisq")

## Analysis of Deviance Table (Type II tests)

##

## Response: f.vote_ord

## LR Chisq Df Pr(>Chisq)

## f.IncSat 7.068 3 0.06976 .

## ---

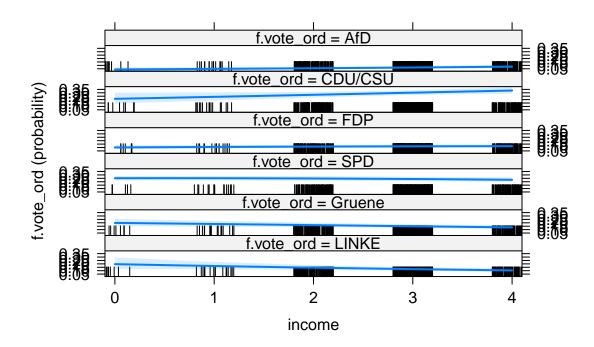
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

plot(allEffects(om1_inc_con),ask=FALSE, main="Effects Inc Sat Continuous")

##

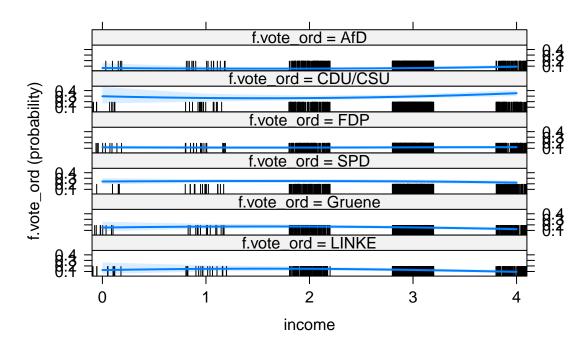
## Re-fitting to get Hessian
```

#### **Effects Inc Sat Continuous**



plot(allEffects(om1\_inc\_con\_sq),ask=FALSE,main="Effects Inc Sat Continuous Squared")
##
## Re-fitting to get Hessian

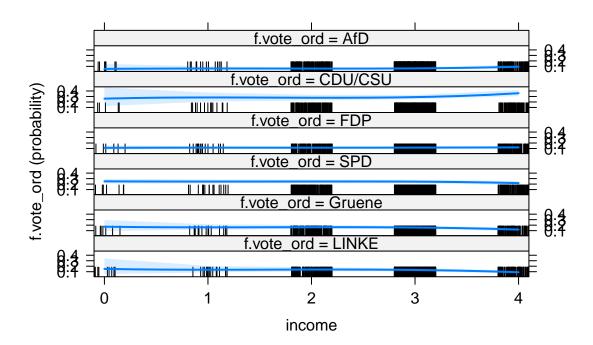
## **Effects Inc Sat Continuous Squared**



plot(allEffects(om1\_inc\_con\_cb), ask=FALSE, main="Effects Inc Sat Continuous Cubed")
##

## Re-fitting to get Hessian

#### **Effects Inc Sat Continuous Cubed**

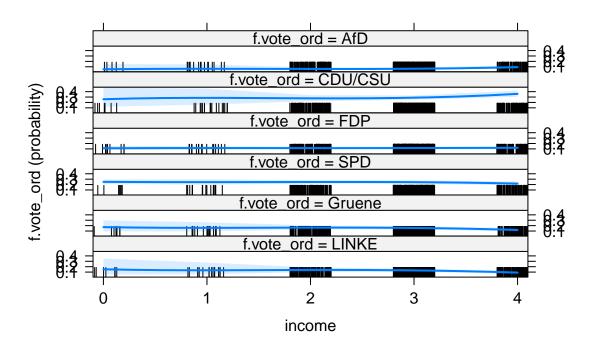


plot(allEffects(om1\_inc\_con\_qd),ask=FALSE, main="Effects Inc Sat Continuous Quadratic")

##

## Re-fitting to get Hessian

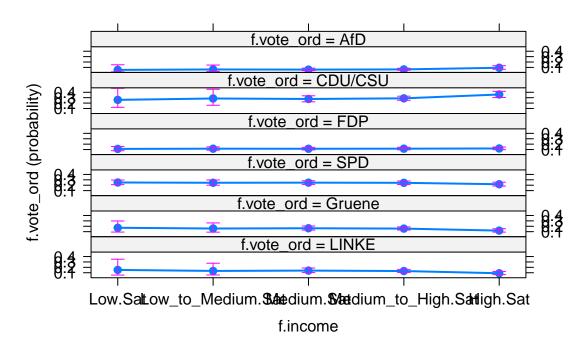
### **Effects Inc Sat Continuous Quadratic**



plot(allEffects(om1 inc cat),ask=FALSE, main="Effects Inc Sat Categorical")

##
## Re-fitting to get Hessian

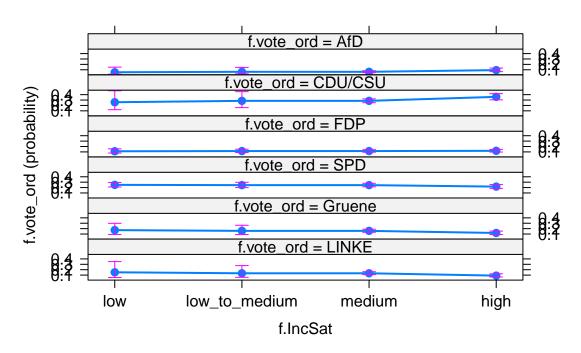
### **Effects Inc Sat Categorical**



plot(allEffects(om1\_inc\_cat\_new),ask=FALSE, main="Effects Inc Sat Categorical")

##
## Re-fitting to get Hessian

#### **Effects Inc Sat Categorical**



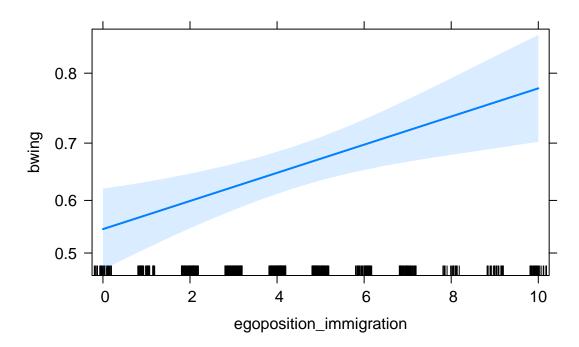
#### 4.3.3 Hierarchical Models

```
bhm0$dev - bhm1 imm con$dev
## [1] 11.06988
bhm0$dev - bhm1_imm_con_sq$dev
## [1] 28.21052
bhm0$dev - bhm1_imm_con_cb$dev
## [1] 29.49081
bhm0$dev - bhm1_imm_con_qd$dev
## [1] 32.86867
anova(bhm1 imm con, bhm1 imm con sq, test="Chisq")
## Analysis of Deviance Table
## Model 1: bwing ~ egoposition immigration
## Model 2: bwing ~ poly(egoposition_immigration, 2)
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
          702
                  894.97
## 2
           701
                  877.83 1
                            17.141 3.471e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(bhm1 imm con sq, bhm1 imm con cb, test="Chisq")
## Analysis of Deviance Table
```

```
##
## Model 1: bwing ~ poly(egoposition_immigration, 2)
## Model 2: bwing ~ poly(egoposition immigration, 3)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          701
                  877.83
                  876.55 1
## 2
           700
                              1.2803
                                       0.2578
anova(bhm1_imm_con_cb, bhm1_imm_con_qd, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: bwing ~ poly(egoposition_immigration, 3)
## Model 2: bwing ~ poly(egoposition_immigration, 4)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          700
                  876.55
## 2
           699
                  873.17
                         1
                              3.3779 0.06608 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm1 imm con, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
                          Df Chisq Pr(>Chisq)
## egoposition immigration 1 10.701
                                      0.001071 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm1_imm_con_sq, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                                   Df Chisq Pr(>Chisq)
## poly(egoposition_immigration, 2) 2 27.359 1.145e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Anova(bhm1_imm_con_cb, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
                                   Df Chisq Pr(>Chisq)
##
## poly(egoposition_immigration, 3) 3 28.743 2.536e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm1 imm con qd, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
```

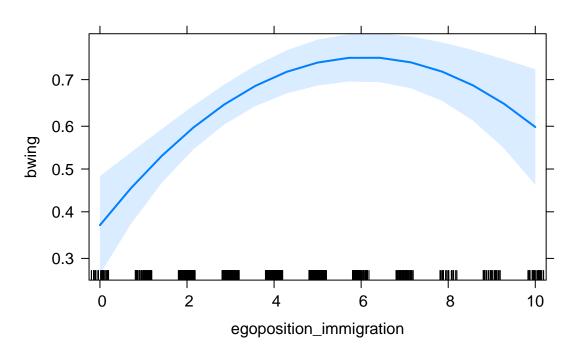
```
##
                                  Df Chisq Pr(>Chisq)
## poly(egoposition_immigration, 4) 4 32.007 1.907e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm1_imm_cat, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                            Df
                               Chisq Pr(>Chisq)
## f.egoposition immigration 10 46.032 1.415e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm1_imm_cat_new, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
        Df Chisq Pr(>Chisq)
## f.Imm 4 35.157 4.313e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(allEffects(bhm1_imm_con),ask=FALSE, main="Effects Imm Continuous")
```

#### **Effects Imm Continuous**



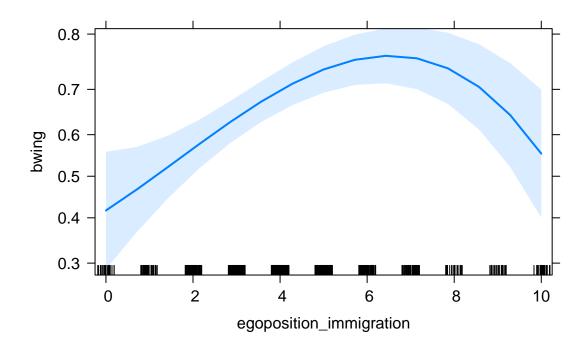
plot(allEffects(bhm1\_imm\_con\_sq), ask=FALSE, main="Effects Imm Continuous Squared")

# **Effects Imm Continuous Squared**



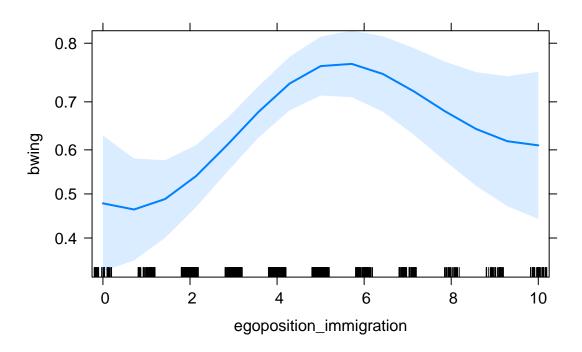
plot(allEffects(bhm1\_imm\_con\_cb),ask=FALSE, main="Effects Imm Continuous Cubed")

### **Effects Imm Continuous Cubed**



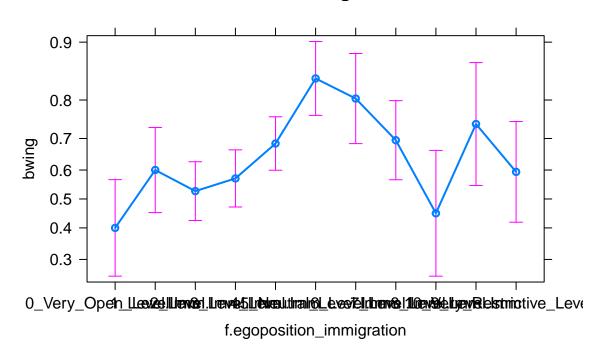
plot(allEffects(bhm1\_imm\_con\_qd),ask=FALSE, main="Effects Imm Continuous Quadratic")

## **Effects Imm Continuous Quadratic**



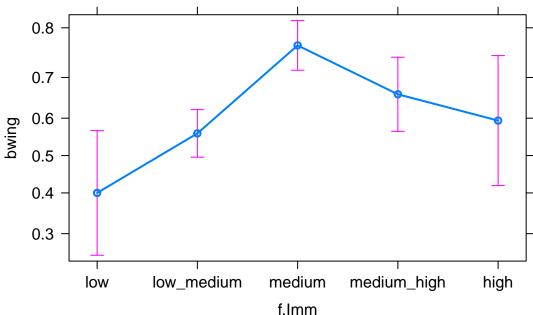
plot(allEffects(bhm1\_imm\_cat),ask=FALSE, main="Effects Imm Categorical")

## **Effects Imm Categorical**



plot(allEffects(bhm1\_imm\_cat\_new),ask=FALSE, main="Effects Imm Categorical")

### **Effects Imm Categorical**



```
hm0$dev - bhm1_polint_con$dev

## [1] 1.027896

bhm0$dev - bhm1_polint_con_sq$dev

## [1] 1.034385

bhm0$dev - bhm1_polint_con_cb$dev

## [1] 5.069252

bhm0$dev - bhm1_polint_con_qd$dev

## [1] 6.113992

bhm0$dev - bhm1_polint_cat$dev

## [1] 6.113992

bhm0$dev - bhm1_polint_cat_new$dev

## [1] 0.2269066

anova(bhm1_polint_con, bhm1_polint_con_sq, test="Chisq")

## Analysis of Deviance Table
```

0.9358

## Model 1: bwing ~ political\_interest

702

701

##

## 1

## 2

## Model 2: bwing ~ poly(political\_interest, 2)

905.01

Resid. Df Resid. Dev Df Deviance Pr(>Chi)

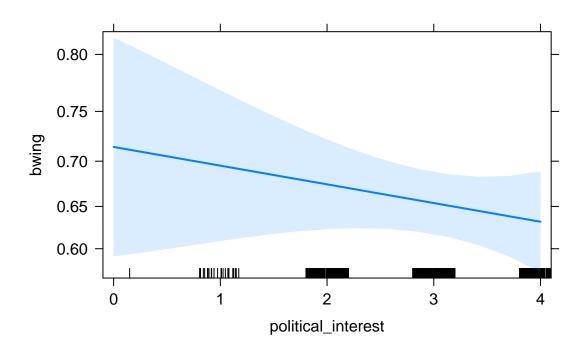
905.00 1 0.0064891

```
anova(bhm1_polint_con_sq, bhm1_polint_con_cb, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: bwing ~ poly(political_interest, 2)
## Model 2: bwing ~ poly(political interest, 3)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           701
                   905.00
## 2
           700
                   900.97 1
                             4.0349 0.04457 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(bhm1_polint_con_cb, bhm1_polint_con_qd, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: bwing ~ poly(political_interest, 3)
## Model 2: bwing ~ poly(political_interest, 4)
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           700
                   900.97
## 2
           699
                   899.92 1
                               1.0447
                                        0.3067
Anova(bhm1 polint con, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                      Df Chisq Pr(>Chisq)
## political interest 1 1.0241
Anova(bhm1_polint_con_sq, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                               Df Chisq Pr(>Chisq)
## poly(political interest, 2) 2 1.0277
                                             0.5982
Anova(bhm1 polint con cb, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                                  Chisq Pr(>Chisq)
                               Df
## poly(political_interest, 3)
                                3 4.8836
                                             0.1805
Anova(bhm1_polint_con_qd, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
                               Df Chisq Pr(>Chisq)
##
## poly(political_interest, 4) 4 6.0009
                                             0.1991
```

```
Anova(bhm1_polint_cat, test="Wald")
## Analysis of Deviance Table (Type II tests)
## Response: bwing
##
                            Chisq Pr(>Chisq)
                        Df
## f.political_interest 4 6.0009
                                      0.1991
Anova(bhm1_polint_cat_new, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
               Chisq Pr(>Chisq)
            Df
            2 0.2305
## f.PolInt
                          0.8912
```

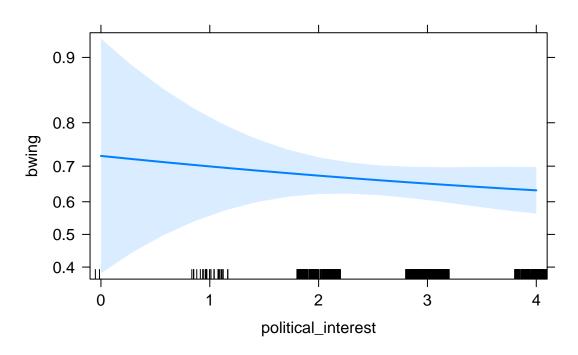
plot(allEffects(bhm1 polint con), ask=FALSE, main="Effects Political Interest Continuous"

### Effects Political Interest Continuous



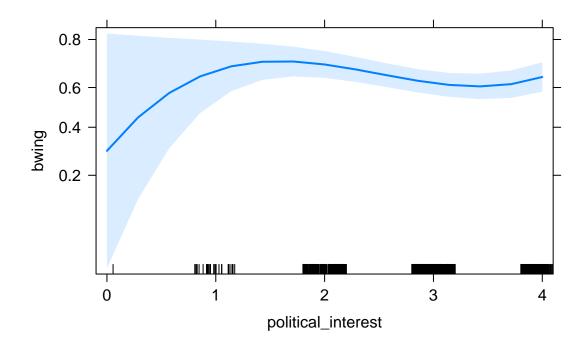
plot(allEffects(bhm1\_polint\_con\_sq), ask=FALSE, main="Effects Political Interest Continuous Plot(allEffects(bhm1\_polint\_con\_sq), ask=FALSE, main="Effects(bhm1\_polint\_con\_sq), ask=Effects(bhm1\_polint\_con\_sq), ask=Effects(bhm

# **Effects Political Interest Continuous Squared**



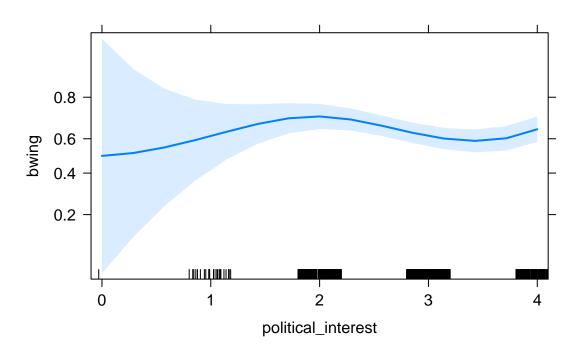
plot(allEffects(bhm1\_polint\_con\_cb), ask=FALSE, main="Effects Political Interest Continue

### **Effects Political Interest Continuous Cubed**



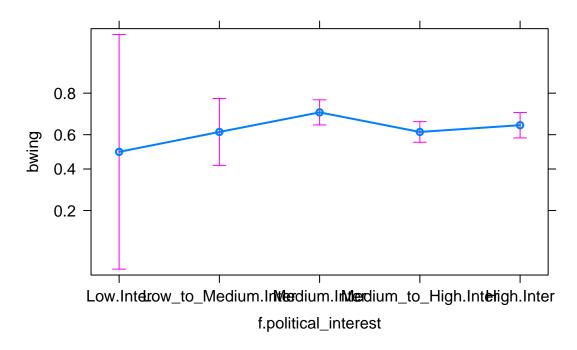
plot(allEffects(bhm1\_polint\_con\_qd), ask=FALSE, main="Effects Political Interest Continuo

### **Effects Political Interest Continuous Quadratic**



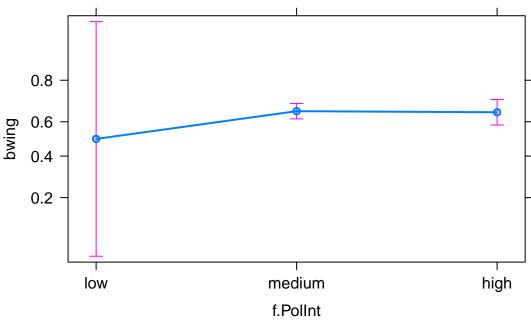
plot(allEffects(bhm1\_polint\_cat),ask=FALSE, main="Effects Political Interest Categorical")

## **Effects Political Interest Categorical**



plot(allEffects(bhm1\_polint\_cat\_new),ask=FALSE, main="Effects Political Interest Categor")

### **Effects Political Interest Categorical**



```
bhm0$dev - bhm1_inc_con$dev
## [1] 2.66419
bhm0$dev - bhm1_inc_con_sq$dev
## [1] 4.560265
bhm0$dev - bhm1_inc_con_cb$dev
## [1] 4.625955
bhm0$dev - bhm1_inc_con_qd$dev
## [1] 4.632596
bhm0$dev - bhm1_inc_cat$dev
## [1] 4.632596
bhm0$dev - bhm1_inc_cat_new$dev
## [1] 3.626678
anova(bhm1_inc_con, bhm1_inc_con_sq, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: bwing ~ income
## Model 2: bwing ~ poly(income, 2)
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           702
                   903.37
## 2
           701
                   901.48 1 1.8961
                                        0.1685
```

```
anova(bhm1_inc_con_sq, bhm1_inc_con_cb, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: bwing ~ poly(income, 2)
## Model 2: bwing ~ poly(income, 3)
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           701
                   901.48
## 2
           700
                   901.41 1 0.065689
                                        0.7977
anova(bhm1 inc con cb, bhm1 inc con qd, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: bwing ~ poly(income, 3)
## Model 2: bwing ~ poly(income, 4)
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           700
                   901.41
## 2
           699
                   901.40 1 0.0066418
                                          0.935
Anova(bhm1 inc con, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
          Df Chisq Pr(>Chisq)
## income 1 2.6707
                        0.1022
Anova(bhm1_inc_con_sq, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                   Df Chisq Pr(>Chisq)
## poly(income, 2) 2 4.4295
Anova(bhm1_inc_con_cb, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
                   Df Chisq Pr(>Chisq)
## poly(income, 3) 3 4.5237
                                 0.2102
Anova(bhm1_inc_con_qd, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
##
                   Df Chisq Pr(>Chisq)
## poly(income, 4) 4 4.5337
                                 0.3386
Anova(bhm1_inc_cat, test="Wald")
```

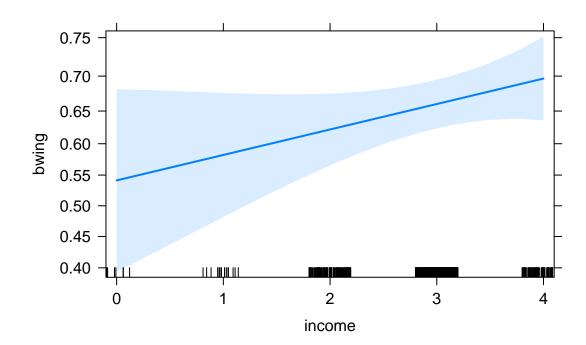
```
## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
## Df Chisq Pr(>Chisq)
## f.income 4 4.5337   0.3386

Anova(bhm1_inc_cat_new, test="Wald")

## Analysis of Deviance Table (Type II tests)
##
## Response: bwing
## Df Chisq Pr(>Chisq)
## f.IncSat 3 3.5048   0.3201

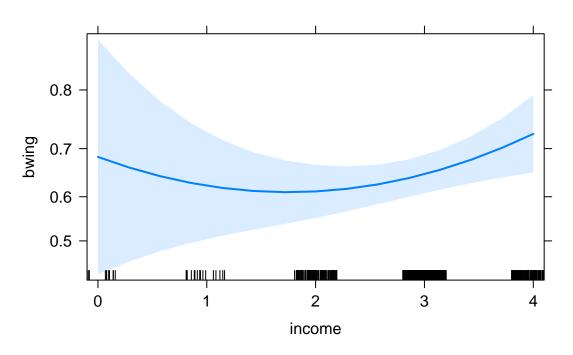
plot(allEffects(bhm1_inc_con),ask=FALSE, main="Effects Income Continuous")
```

#### **Effects Income Continuous**



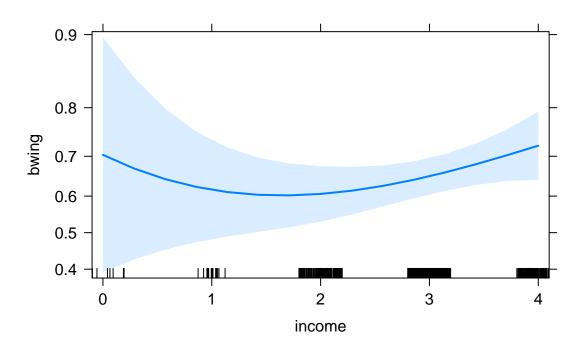
plot(allEffects(bhm1\_inc\_con\_sq),ask=FALSE,main="Effects Income Continuous Squared")

# **Effects Income Continuous Squared**



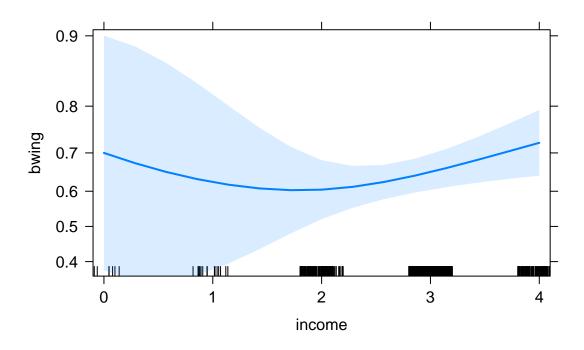
plot(allEffects(bhm1\_inc\_con\_cb),ask=FALSE, main="Effects Income Continuous Cubed")

## **Effects Income Continuous Cubed**



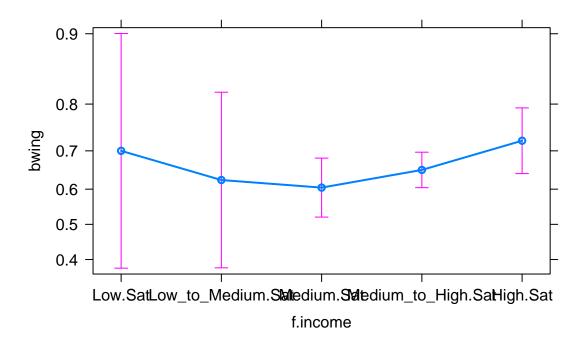
plot(allEffects(bhm1\_inc\_con\_qd), ask=FALSE, main="Effects Income Interest Continuous Qua

## **Effects Income Interest Continuous Quadratic**



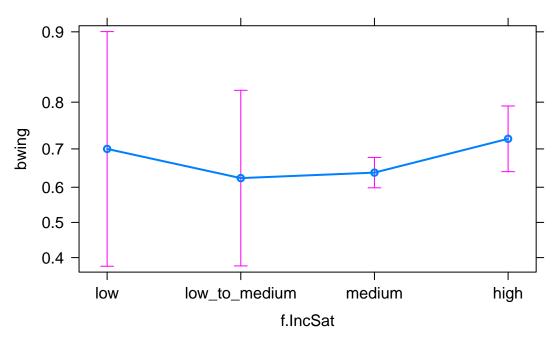
plot(allEffects(bhm1\_inc\_cat),ask=FALSE, main="Effects Income Interest Categorical")

## **Effects Income Interest Categorical**



plot(allEffects(bhm1\_inc\_cat\_new),ask=FALSE, main="Effects Income Interest Categorical")

## **Effects Income Interest Categorical**

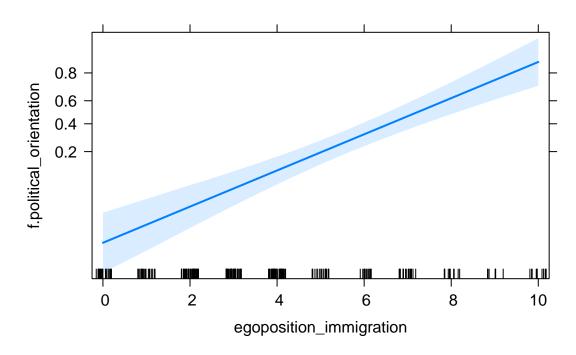


```
bh2m0$dev - bhm2_imm_con$dev
## [1] 84.36461
bh2m0$dev - bhm2_imm_con_sq$dev
## [1] 84.40058
bh2m0$dev - bhm2_imm_con_cb$dev
## [1] 95.40436
bh2m0$dev - bhm2_imm_con_qd$dev
## [1] 99.30075
anova(bhm2_imm_con, bhm2_imm_con_sq, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ egoposition_immigration
## Model 2: f.political orientation ~ poly(egoposition immigration, 2)
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           240
                   156.72
           239
## 2
                   156.68 1 0.035967
                                        0.8496
anova(bhm2_imm_con_sq, bhm2_imm_con_cb, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ poly(egoposition_immigration, 2)
## Model 2: f.political_orientation ~ poly(egoposition_immigration, 3)
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           239
                   156.68
```

```
## 2
          238
                  145.68 1
                              11.004 0.0009093 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(bhm2_imm_con_cb, bhm2_imm_con_qd, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political orientation ~ poly(egoposition immigration, 3)
## Model 2: f.political_orientation ~ poly(egoposition_immigration, 4)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
                  145.68
## 1
          238
## 2
          237
                  141.78 1
                              3.8964 0.04839 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm2 imm con, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political orientation
                          Df
                             Chisq Pr(>Chisq)
## egoposition_immigration 1 52.916 3.482e-13 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm2_imm_con_sq, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political orientation
                                   Df
                                      Chisq Pr(>Chisq)
## poly(egoposition_immigration, 2) 2 52.537 3.906e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm2 imm con cb, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political orientation
##
                                   Df
                                      Chisq Pr(>Chisq)
## poly(egoposition_immigration, 3) 3 61.847 2.369e-13 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Anova(bhm2_imm_con_qd, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
##
                                   Df Chisq Pr(>Chisq)
## poly(egoposition immigration, 4) 4 65.88 1.679e-13 ***
## ---
```

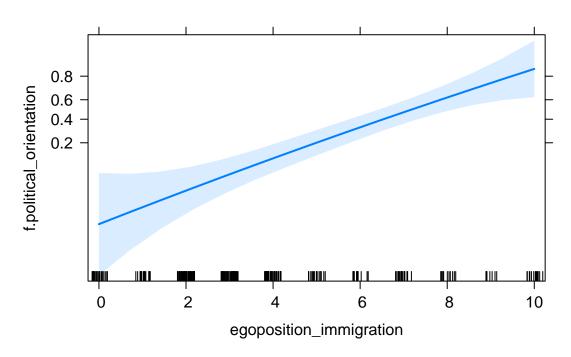
```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm2 imm cat, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
                               Chisq Pr(>Chisq)
                           Df
## f.egoposition_immigration 10 56.757
                                       1.48e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(bhm2 imm cat new, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
        Df Chisq Pr(>Chisq)
## f.Imm 4 70.592 1.702e-14 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(allEffects(bhm2_imm_con),ask=FALSE, main="Effects Imm Continuous")
```

#### **Effects Imm Continuous**



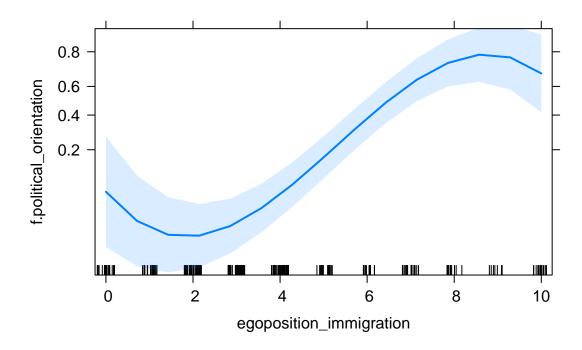
plot(allEffects(bhm2\_imm\_con\_sq),ask=FALSE,main="Effects Imm Continuous Squared")

# **Effects Imm Continuous Squared**



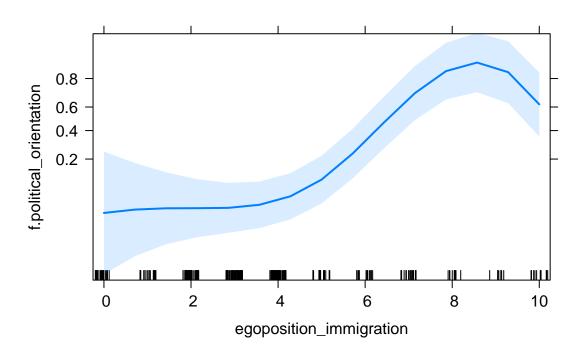
plot(allEffects(bhm2\_imm\_con\_cb),ask=FALSE, main="Effects Imm Continuous Cubed")

### **Effects Imm Continuous Cubed**



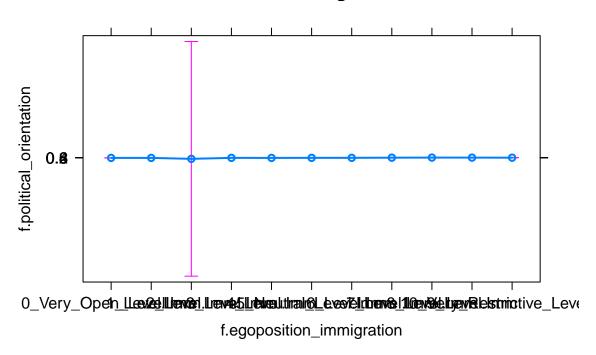
plot(allEffects(bhm2\_imm\_con\_qd),ask=FALSE, main="Effects Imm Continuous Quadratic")

## **Effects Imm Continuous Quadratic**



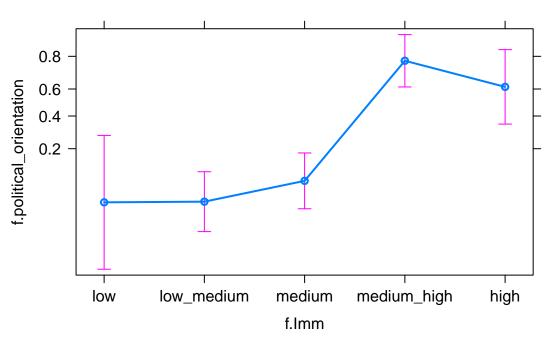
plot(allEffects(bhm2\_imm\_cat),ask=FALSE, main="Effects Imm Categorical")

# **Effects Imm Categorical**



plot(allEffects(bhm2\_imm\_cat\_new),ask=FALSE, main="Effects Imm Categorical")

### **Effects Imm Categorical**



```
# bhm2_imm_con_qd is better concerning AIC
bh2m0$dev - bhm2_polint_con$dev
## [1] 0.001939783
bh2m0$dev - bhm2_polint_con_sq$dev
## [1] 1.531539
bh2m0$dev - bhm2_polint_con_cb$dev
## [1] 2.700847
bh2m0$dev - bhm2_polint_con_qd$dev
## [1] 3.520738
anova(bhm2_polint_con, bhm2_polint_con_sq, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ political_interest
## Model 2: f.political_orientation ~ poly(political_interest, 2)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
           240
                   241.08
## 1
## 2
           239
                   239.55 1
                               1.5296
                                        0.2162
anova(bhm2_polint_con_sq, bhm2_polint_con_cb, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ poly(political_interest, 2)
## Model 2: f.political_orientation ~ poly(political_interest, 3)
```

```
Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
           239
                   239.55
## 2
           238
                   238.38 1
                               1.1693
                                        0.2795
anova(bhm2_polint_con_cb, bhm2_polint_con_qd, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ poly(political_interest, 3)
## Model 2: f.political_orientation ~ poly(political_interest, 4)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
                   238.38
## 1
           238
## 2
           237
                   237.56 1 0.81989
                                        0.3652
Anova(bhm2_polint_con, test="Wald")
## Analysis of Deviance Table (Type II tests)
## Response: f.political_orientation
##
                      Df Chisq Pr(>Chisq)
## political interest 1 0.0019
                                    0.9649
Anova(bhm2_polint_con_sq, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
##
                               Df
                                  Chisq Pr(>Chisq)
## poly(political_interest, 2)
                                2 1.5906
                                             0.4514
Anova(bhm2 polint con cb, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political orientation
                               Df
                                  Chisq Pr(>Chisq)
## poly(political interest, 3) 3 2.1387
                                             0.5441
Anova(bhm2_polint_con_qd, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political orientation
##
                               Df Chisq Pr(>Chisq)
## poly(political_interest, 4) 4 0.2708
                                             0.9916
Anova(bhm2_polint_cat, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
##
                           Chisq Pr(>Chisq)
                        Df
## f.political interest 4 0.2708
                                      0.9916
```

```
Anova(bhm2_polint_cat_new, test="Wald")

## Analysis of Deviance Table (Type II tests)

##

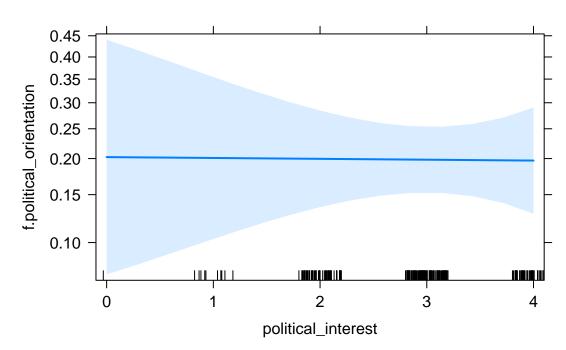
## Response: f.political_orientation

## Df Chisq Pr(>Chisq)

## f.PolInt 2 0.2351  0.8891

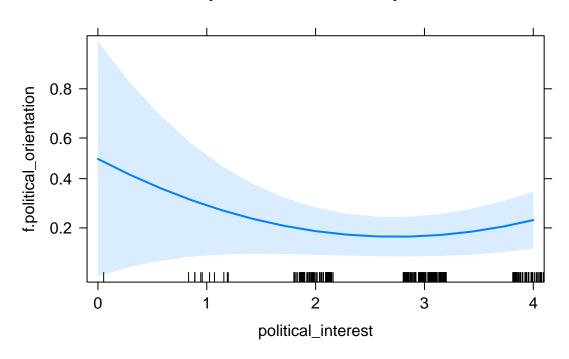
plot(allEffects(bhm2_polint_con),ask=FALSE, main="Effects polint Continuous")
```

### **Effects polint Continuous**



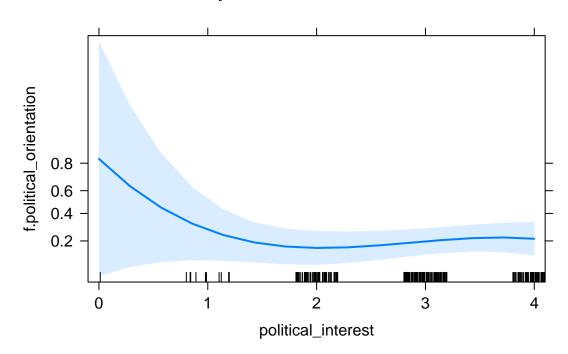
plot(allEffects(bhm2\_polint\_con\_sq),ask=FALSE,main="Effects polint Continuous Squared")

# **Effects polint Continuous Squared**



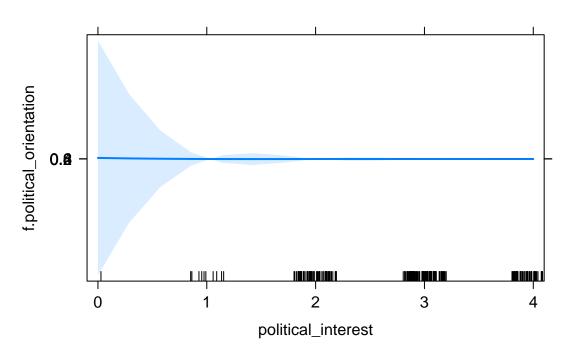
plot(allEffects(bhm2\_polint\_con\_cb),ask=FALSE, main="Effects polint Continuous Cubed")

# **Effects polint Continuous Cubed**



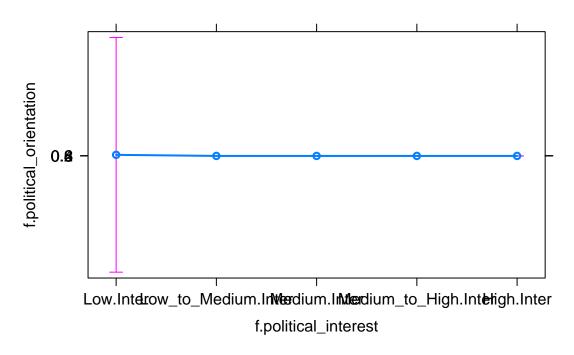
plot(allEffects(bhm2\_polint\_con\_qd), ask=FALSE, main="Effects polint Continuous Quadratic

# **Effects polint Continuous Quadratic**



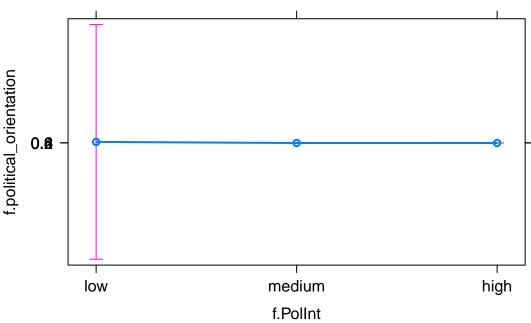
plot(allEffects(bhm2\_polint\_cat),ask=FALSE, main="Effects polint Categorical")

## **Effects polint Categorical**



plot(allEffects(bhm2\_polint\_cat\_new),ask=FALSE, main="Effects polint Categorical")

### **Effects polint Categorical**



```
bh2m0$dev - bhm2_inc_con$dev
## [1] 0.003212806
bh2m0$dev - bhm2_inc_con_sq$dev
## [1] 0.2958203
bh2m0$dev - bhm2_inc_con_cb$dev
## [1] 5.451673
bh2m0$dev - bhm2_inc_con_qd$dev
## [1] 5.749227
anova(bhm2_inc_con, bhm2_inc_con_sq, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ income
## Model 2: f.political orientation ~ poly(income, 2)
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           240
                   241.08
           239
## 2
                   240.79 1 0.29261
anova(bhm2_inc_con_sq, bhm2_inc_con_cb, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political_orientation ~ poly(income, 2)
## Model 2: f.political_orientation ~ poly(income, 3)
##
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           239
                   240.79
```

```
## 2
           238
                   235.63 1 5.1559 0.02317 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(bhm2_inc_con_cb, bhm2_inc_con_qd, test="Chisq")
## Analysis of Deviance Table
##
## Model 1: f.political orientation ~ poly(income, 3)
## Model 2: f.political_orientation ~ poly(income, 4)
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           238
                   235.63
## 2
           237
                   235.33 1 0.29755 0.5854
Anova(bhm2 inc con, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
##
         Df Chisq Pr(>Chisq)
## income 1 0.0032
                        0.9548
Anova(bhm2_inc_con_sq, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
##
                   Df Chisq Pr(>Chisq)
## poly(income, 2) 2 0.31
                                0.8564
Anova(bhm2 inc con cb, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
                   Df
                     Chisq Pr(>Chisq)
## poly(income, 3) 3 5.0218
                                 0.1702
Anova(bhm2_inc_con_qd, test="Wald")
## Analysis of Deviance Table (Type II tests)
##
## Response: f.political_orientation
##
                   Df Chisq Pr(>Chisq)
## poly(income, 4) 4 4.4184
                                 0.3523
Anova(bhm2 inc cat, test="Wald")
## Analysis of Deviance Table (Type II tests)
## Response: f.political_orientation
            Df Chisq Pr(>Chisq)
## f.income 4 4.4184
                        0.3523
```

```
Anova(bhm2_inc_cat_new, test="Wald")

## Analysis of Deviance Table (Type II tests)

##

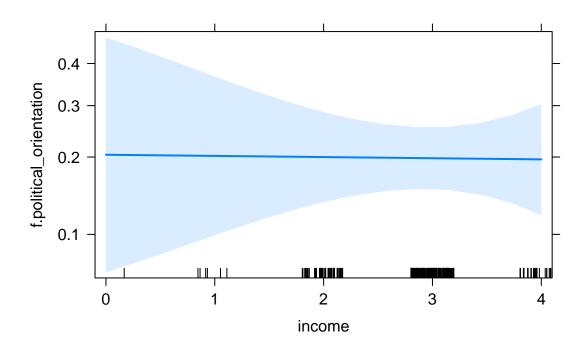
## Response: f.political_orientation

## Df Chisq Pr(>Chisq)

## f.IncSat 3 2.0817  0.5556

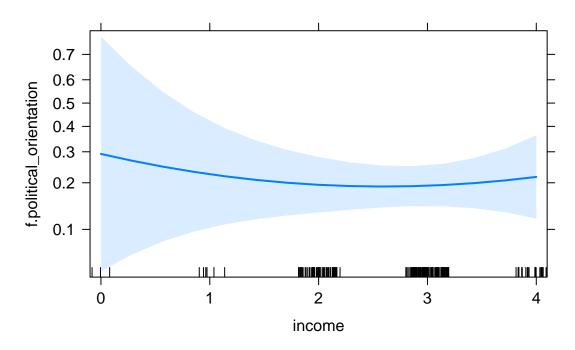
plot(allEffects(bhm2_inc_con),ask=FALSE, main="Effects inc Continuous")
```

#### **Effects inc Continuous**



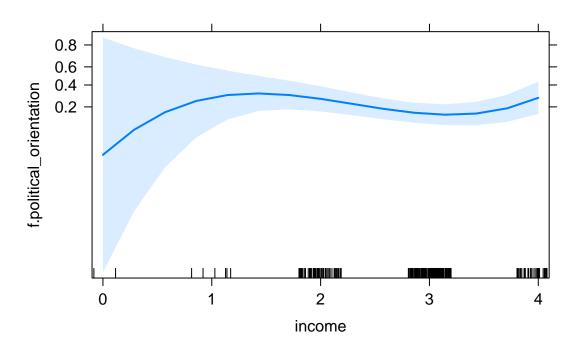
plot(allEffects(bhm2\_inc\_con\_sq),ask=FALSE,main="Effects inc Continuous Squared")

# **Effects inc Continuous Squared**



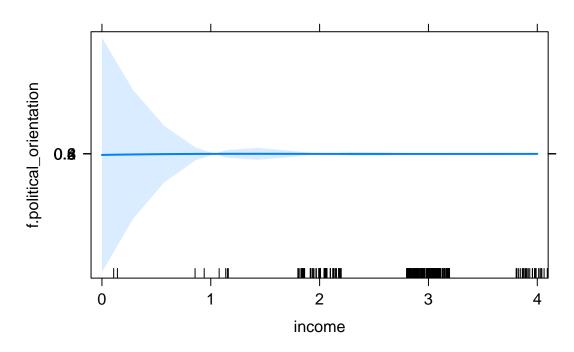
plot(allEffects(bhm2\_inc\_con\_cb),ask=FALSE, main="Effects inc Continuous Cubed")

## **Effects inc Continuous Cubed**



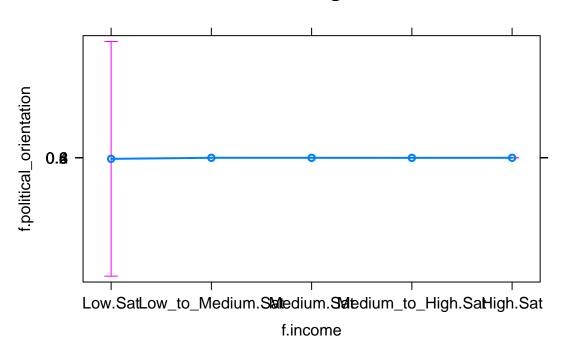
plot(allEffects(bhm2\_inc\_con\_qd),ask=FALSE, main="Effects inc Continuous Quadratic")

## **Effects inc Continuous Quadratic**



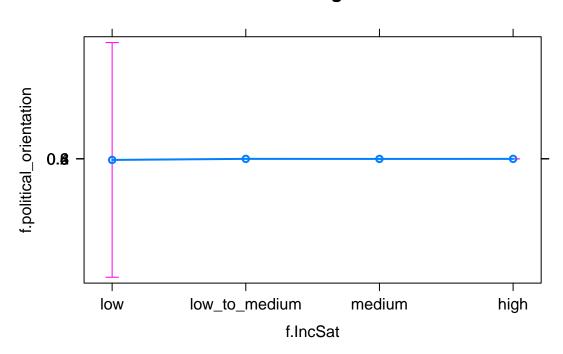
plot(allEffects(bhm2\_inc\_cat),ask=FALSE, main="Effects inc Categorical")

## **Effects inc Categorical**



plot(allEffects(bhm2\_inc\_cat\_new),ask=FALSE, main="Effects inc Categorical")

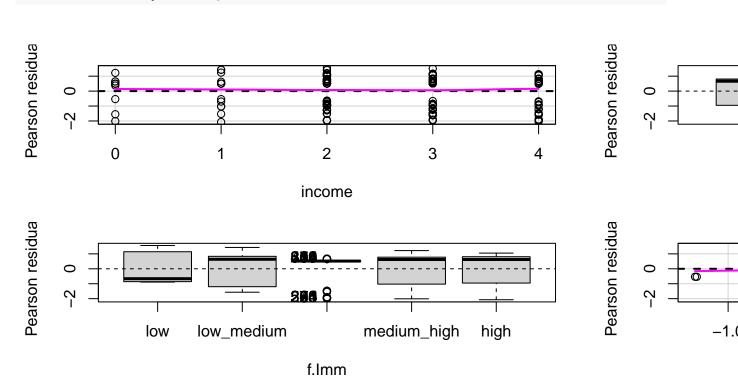
# **Effects inc Categorical**



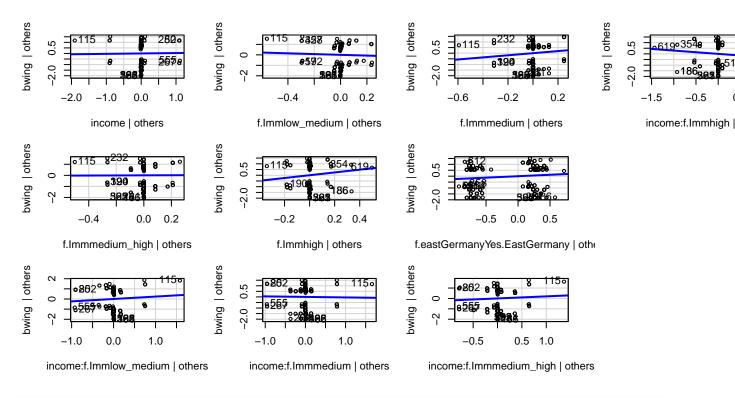
#### 4.3.4 Influential Data

#### LAYER 1

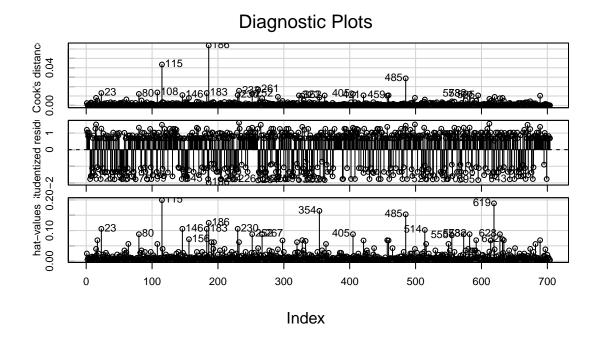
residualPlots(layer1, layout=c(2, 1))



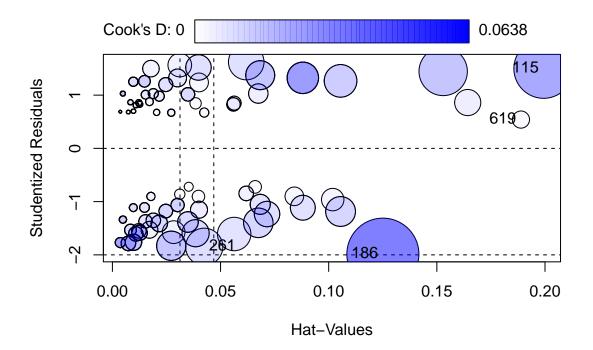
#### avPlots(layer1,id=list(n=5))



influenceIndexPlot(layer1,id=list(n=20),vars=c("Cook", "Student","hat"))



influencePlot(layer1,id=list(method="noteworthy"))



```
## StudRes Hat CookD

## 115 1.4984544 0.19935318 0.043472427

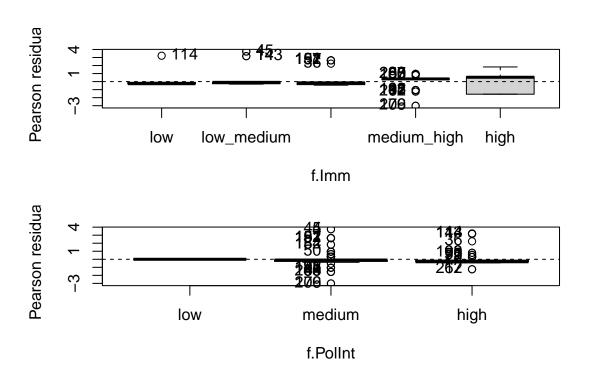
## 186 -1.9868059 0.12504695 0.063779519

## 261 -1.8485185 0.04245303 0.017034566

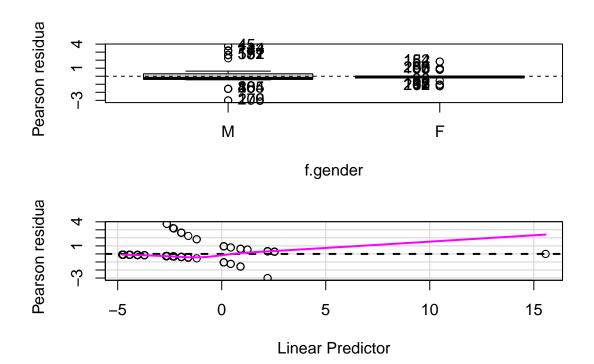
## 619 0.5409559 0.18888395 0.003627381
```

LAYER 2

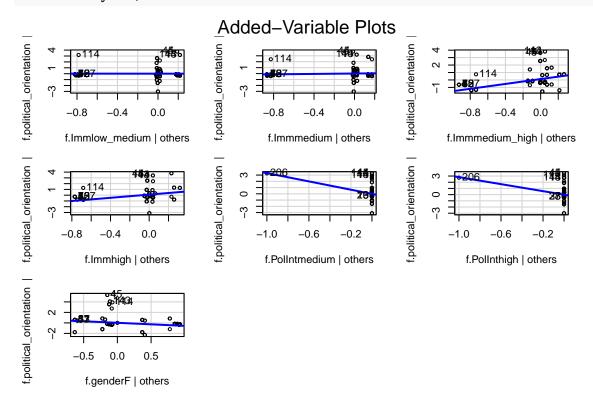
residualPlots(layer2, layout=c(2, 1))



## Warning in residualPlots.default(model, ...): No possible lack-of-fit tests

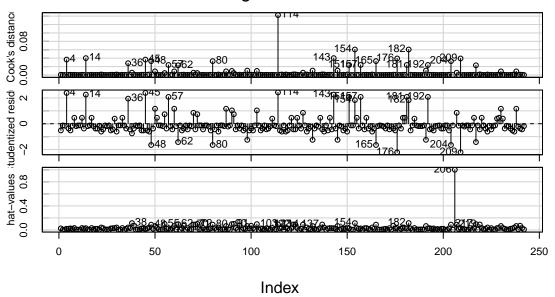


#### avPlots(layer2,id=list(n=5))

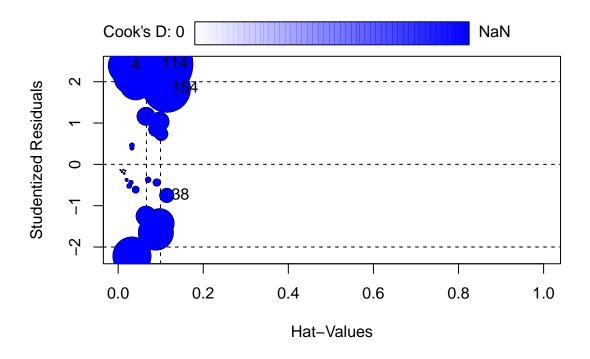


influenceIndexPlot(layer2,id=list(n=20),vars=c("Cook", "Student","hat"))

## Diagnostic Plots



influencePlot(layer2,id=list(method="noteworthy"))



```
## StudRes Hat CookD

## 4 2.3879624 0.02010491 0.036625502

## 38 -0.7514112 0.11430610 0.005477099

## 114 2.4288202 0.09081611 0.142481145

## 154 1.8325554 0.11430610 0.060572236

## 206 NaN 1.00000000 NaN
```