

# Midterm Review

Machine Learning 10-601

Tom M. Mitchell  
Machine Learning Department  
Carnegie Mellon University

October 25, 2011

See practice exams on our website

**Midterm is in class October 27**

**Midterm is open book, open notes, NO computers, NO internet**

**Covers all material presented up through today's class.**

## Some Topics We've Covered

### Decision trees

entropy, mutual info., overfitting

### Sources of Error

unavoidable error, bias, variance

### Probability basics

Bayes rule, MLE, MAP,  
conditional indep.

### Overfitting, and Avoiding it

priors over H  
cross validation  
PAC theory: probabilistic bound on overfitting

### Naïve Bayes

conditional independence,  
# of parameters to estimate,  
decision surface

### Bayesian Networks

factored *representation* of joint  
distribution, conditional independence  
assumptions, D-separation  
*inference* in Bayes nets  
*learning* from fully/partly observed data

### Logistic regression

form of  $P(Y|X)$   
generative vs. discriminative

### PAC Learning

sample complexity  
probabilistic bounds on  $\text{error}_{\text{train}} - \text{error}_{\text{true}}$   
VC dimension

### Linear Regression

minimizing sum sq. error (why?)  
regularization  $\sim$  MAP

## Understanding/Comparing Learning Methods

Form of learned model

- Inputs:
- Outputs:

Optimization Objective:

Algorithm:

Assumptions:

Guarantees?:

Decision boundary:

Generative/Discriminative?

### Naïve Bayes

### Logistic Regression

Form of learned model

- Inputs:
- Outputs:

Optimization Objective:

Algorithm:

Assumptions:

Guarantees?:

Decision boundary:

Generative/Discriminative?

## Four Fundamentals for ML

### 1. Learning is an optimization problem

- many algorithms are best understood as optimization algs
- what objective do they optimize, and how? Local minima?
- gradient descent/ascent as general fallback approach

## Four Fundamentals for ML

### 1. Learning is an optimization problem

- many algorithms are best understood as optimization algs
- what objective do they optimize, and how?

### 2. Learning is a parameter estimation problem

- the more training data, the more accurate the estimates
- MLE, MAP, M(Conditional)LE, ...
- to measure accuracy of learned model, we must use test (not train) data

## Four Fundamentals for ML

1. Learning is an optimization problem
  - many algorithms are best understood as optimization algs
  - what objective do they optimize, and how?
2. Learning is a parameter estimation problem
  - the more training data, the more accurate the estimates
  - MLE, MAP, M(Conditional)LE, ...
  - to measure accuracy of learned model, we must use test (not train) data
3. Error arises from three sources
  - unavoidable error, bias, variance
  - PAC learning theory: probabilistic bound on overfitting:  $\text{error}_{\text{true}} - \text{error}_{\text{train}}$

## Bias and Variance of Estimators

given some estimator  $Y$  for some parameter  $\theta$ , we note  $Y$  is a random variable (why?)

the bias of estimator  $Y$  :  $E[Y] - \theta$

the variance of estimator  $Y$  :  $E[(Y - E[Y])^2]$

consider when

- $\theta$  is the probability of “heads” for my coin
- $Y$  = proportion of heads observed from 3 flips

consider when

- $\theta$  is the vector of correct parameters for learner
- $Y$  = parameters output by learning algorithm

## Four Fundamentals for ML

1. Learning is an optimization problem
  - many algorithms are best understood as optimization algs
  - what objective do they optimize, and how?
2. Learning is a parameter estimation problem
  - the more training data, the more accurate the estimates
  - MLE, MAP, M(Conditional)LE, ...
  - to measure accuracy of learned model, we must use test (not train) data
3. Error arises from three sources
  - unavoidable error, bias, variance
  - PAC learning theory: probabilistic bound on overfitting:  $\text{error}_{\text{true}} - \text{error}_{\text{train}}$
4. Practical learning requires making assumptions
  - Why?
  - form of the  $f: X \rightarrow Y$ , or  $P(Y|X)$  to be learned
  - priors on parameters: MAP, regularization
  - Conditional independence: Naive Bayes, Bayes nets, HMM's