# Identification of Heterogeneous Causal Effects

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## Identifying the Causal Effects

In this section we estimate the causal effects of additional funding on students performances. Namely, our outcome variables are *certificate* (which is a dummy variable that assumes value 1 if the student gets an "A" certificate: the highest possible grade in the Flanders) and *progress school* (which is a dummy recording whether or not the student got school retention).

## First Outcome: Certificate

We now foucus on the effects when we sample units in a bandwidth of 0.035 (which is the optimal bandwidth for the outcome *certificate*) around the cutoff (10%).

```
students_data_randomized_03_2011 <-
students_data_2011[which(students_data_2011$GOKpercentage >= .065
& students_data_2011$GOKpercentage <= .135),]</pre>
```

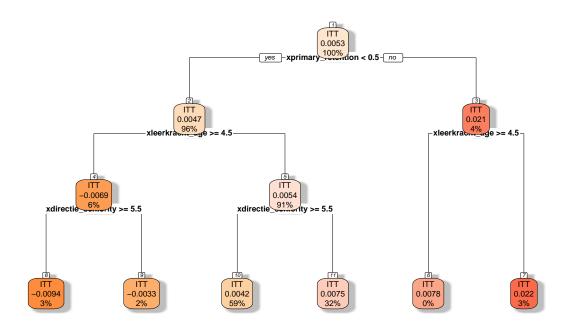
Moreover, from every school we sample a number students in order to increase the balance in the covariate and to guarantee an equal representation to all the schools, avoiding biases related to the over-representation of biggest schools' students. In the first case, we sample 50 students from each school.

```
schools <-
students_data_randomized_03_2011$school[which(
!duplicated(students_data_randomized_03_2011$school))]
sample_students <- as.data.frame(matrix(data = NA, nrow = 50*length(schools),</pre>
                                         ncol = ncol(students_data_randomized_03_2011)))
colnames(sample_students) <- colnames(students_data_randomized_03_2011)</pre>
for (j in (0:(length(schools)-1))){
  set.seed(j + 123)
  sample students [(1+(j*50)):(50+(j*50)),] < -
  students_data_randomized_03_2011[which(
  students_data_randomized_03_2011$school %in%
  schools[j+1]),][sample(1:nrow(students_data_randomized_03_2011[which(
  students_data_randomized_03_2011$school %in% schools[j+1]),]),
  50, replace = FALSE ),]
}
sample_student <- round(sample_students[, -(1:4)], 0)</pre>
sample_students <- cbind(sample_students[,1:4], sample_student)</pre>
```

Then we run our BCF-IV algorithm on this sample of units.

```
leerkracht_diploma,
           directie_age, directie_seniority
z <- as.matrix(eligible_dummy)</pre>
y <- as.matrix(certificate)</pre>
logit<-glm(eligible_dummy ~ GOKpercentage,</pre>
           data = sample_students, family = binomial(link = "logit"))
summary(logit)
pihat<-predict(logit, sample_students, type="response")</pre>
detach(sample_students)
# Running the BCF algorithm on the IV
set.seed(123)
bcf_fit <- bcf(y, z, x, x, pihat, nburn=2000, nsim=2000)</pre>
tau_post <- bcf_fit$tau</pre>
tauhat <- colMeans(tau_post)</pre>
exp <- as.data.frame(cbind(tauhat, y, x, z))</pre>
## n = 4300
##
## node), split, n, deviance, yval
         * denotes terminal node
##
##
##
    1) root 4300 1.248660e-01 0.005298605
      2) xprimary_retention< 0.5 4142 7.972906e-02 0.004688791
##
##
        4) xleerkracht_age>=4.5 241 2.307849e-03 -0.006942340
##
          8) xdirectie_seniority>=5.5 143 1.346278e-05 -0.009429468 *
          9) xdirectie_seniority< 5.5 98 1.190658e-04 -0.003313164 *
##
##
        5) xleerkracht_age< 4.5 3901 4.280376e-02 0.005407351
##
         10) xdirectie_seniority>=5.5 2523 1.473165e-02 0.004238946 *
##
         11) xdirectie_seniority< 5.5 1378 1.832152e-02 0.007546601 *
      3) xprimary_retention>=0.5 158 3.217465e-03 0.021284990
##
##
        6) xleerkracht_age>=4.5 9 2.739628e-05 0.007767681 *
##
        7) xleerkracht_age< 4.5 149 1.446280e-03 0.022101480 *
```

### **BCF-IV First Stage**



```
ITT = mean(sample_students$certificate[which(sample_students$eligible_dummy==1)]) - mean(sample_student
ITT
## [1] 0.01185908
ITT = mean(students_data_randomized_03_2011$certificate[which(students_data_randomized_03_2011$eligible
ITT
## [1] 0.01134698
z <- as.matrix(sample_students$eligible_dummy)</pre>
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students),
        vcov = sandwich, diagnostics = TRUE)
##
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students)
##
## Residuals:
       Min
                  1Q
                      Median
                                    3Q
                                            Max
## -0.99019 0.06745 0.07285 0.09695 0.26186
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          0.823208
                                     0.057561 14.301 < 2e-16 ***
                         -0.144588
                                     0.033962 -4.257 2.11e-05 ***
## xprimary_retention
## xman
                         -0.025153
                                     0.008465 -2.972 0.00298 **
## xBULO
                          0.200284
                                     0.043835
                                               4.569 5.04e-06 ***
```

```
## xleerkracht_age
                         0.020336
                                    0.015522
                                              1.310 0.19023
## xleerkracht_seniority 0.007495
                                  0.013709
                                             0.547 0.58460
                                              0.961 0.33686
## xdirectie age
                         0.005404
                                   0.005626
## xdirectie_seniority
                      -0.006458
                                    0.006586 -0.981 0.32685
## GOKschool
                         0.051178
                                    0.037954
                                              1.348 0.17759
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 4291
                               591.935 <2e-16 ***
## Wu-Hausman
                      1 4290
                                 2.969
                                         0.085 .
## Sargan
                          NA
                                    NA
                                            NA
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2748 on 4291 degrees of freedom
## Multiple R-Squared: 0.00796, Adjusted R-squared: 0.006111
## Wald test: 7.633 on 8 and 4291 DF, p-value: 3.434e-10
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention < 0.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = primary_retention < 0.5)</pre>
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   30
                                           Max
## -0.99124 0.06601 0.07025 0.09782 0.11868
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         ## xman
                        -0.027719
                                   0.008414 -3.294 0.000995 ***
                                   0.015371
## xleerkracht_age
                         0.016378
                                             1.065 0.286714
                                    0.013693
                                             0.658 0.510528
## xleerkracht_seniority 0.009011
## xdirectie_age
                         0.004241
                                    0.005609
                                             0.756 0.449604
## xdirectie_seniority
                      -0.004387
                                    0.006560 -0.669 0.503710
## GOKschool
                         0.052863
                                    0.038095
                                             1.388 0.165314
##
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                      1 4135
                               561.461 <2e-16 ***
## Wu-Hausman
                      1 4134
                                 2.557
                                          0.11
## Sargan
                      0
                         NA
                                    NA
                                            NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2681 on 4135 degrees of freedom
## Multiple R-Squared: -0.0006994, Adjusted R-squared: -0.002151
## Wald test: 2.55 on 6 and 4135 DF, p-value: 0.01819
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention >= 0.5),
```

```
vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = primary_retention >= 0.5)
##
## Residuals:
##
                    Median
       Min
                 1Q
                                   3Q
                                           Max
## -0.90757 0.09386 0.20112 0.25236 0.31119
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         0.37432
                                   0.50003
                                             0.749
                                                       0.455
                                              0.652
## xman
                         0.04456
                                    0.06835
                                                       0.515
## xBULO
                         0.19732
                                    0.14389
                                             1.371
                                                       0.172
## xleerkracht_age
                         0.13617
                                    0.12988
                                             1.048
                                                       0.296
## xleerkracht_seniority -0.01808
                                    0.07523 - 0.240
                                                       0.810
## xdirectie_age
                                             0.808
                                                     0.421
                         0.03478
                                    0.04306
## xdirectie_seniority
                        -0.05529
                                    0.04468 -1.238
                                                       0.218
## GOKschool
                         0.06986
                                    0.24429
                                              0.286
                                                       0.775
##
## Diagnostic tests:
                   df1 df2 statistic p-value
                              29.593 2.12e-07 ***
## Weak instruments
                     1 150
## Wu-Hausman
                     1 149
                               0.649
                                        0.422
## Sargan
                     O NA
                                  NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4196 on 150 degrees of freedom
## Multiple R-Squared: 0.01037, Adjusted R-squared: -0.03581
## Wald test: 5.556 on 7 and 150 DF, p-value: 1.05e-05
\#summary(ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample\_students,
#
              subset = primary_retention < 0.5 & leerkracht_age >= 4.5),
        vcov = sandwich, diagnostics = TRUE)
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention < 0.5 & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = primary_retention < 0.5 & leerkracht_age < 4.5)</pre>
##
## Residuals:
       Min
                 1Q
                      Median
                                   30
                                           Max
## -1.00240 0.06944 0.07398 0.09948 0.12420
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.9450450 0.0852072 11.091 < 2e-16 ***
                        ## xman
```

```
## xleerkracht_age
                         -0.0228716 0.0257181 -0.889 0.373887
                                                0.992 0.321091
## xleerkracht_seniority 0.0152747 0.0153925
                                                 0.439 0.660821
## xdirectie age
                          0.0026272 0.0059871
## xdirectie_seniority
                                               -0.049 0.961012
                         -0.0003556 0.0072734
## GOKschool
                          0.0688538 0.0372556
                                                 1.848 0.064657 .
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
## Weak instruments
                       1 3894
                                598.095 <2e-16 ***
                                  4.721 0.0298 *
## Wu-Hausman
                       1 3893
## Sargan
                           NA
                                     NA
                                             NA
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2719 on 3894 degrees of freedom
## Multiple R-Squared: -0.003032, Adjusted R-squared: -0.004578
## Wald test: 3.164 on 6 and 3894 DF, p-value: 0.004256
\#summary(ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample\_students,
#
               subset = primary_retention >= 0.5 & leerkracht_age >= 4.5),
#
         vcov = sandwich, diagnostics = TRUE)
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = primary_retention >= 0.5 & leerkracht_age < 4.5),</pre>
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample students,
       subset = primary_retention >= 0.5 & leerkracht_age < 4.5)</pre>
##
## Residuals:
                1Q Median
                                3Q
## -0.8414 0.1018 0.2033 0.2595 0.2963
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          0.59828
                                     1.06333
                                              0.563
                                                        0.575
                                               0.330
## xman
                          0.02325
                                     0.07050
                                                        0.742
                                              1.474
## xBULO
                          0.22333
                                     0.15149
                                                        0.143
## xleerkracht_age
                          0.08586
                                     0.26333
                                              0.326
                                                        0.745
## xleerkracht_seniority -0.01287
                                     0.07928
                                             -0.162
                                                        0.871
## xdirectie_age
                         0.02981
                                     0.04192
                                              0.711
                                                        0.478
## xdirectie_seniority -0.05477
                                     0.04485
                                             -1.221
                                                        0.224
## GOKschool
                          0.01803
                                     0.24681
                                              0.073
                                                        0.942
##
## Diagnostic tests:
                    df1 df2 statistic p-value
                               27.175 6.48e-07 ***
## Weak instruments
                     1 141
## Wu-Hausman
                      1 140
                                0.371
                                         0.543
## Sargan
                      O NA
                                   NA
                                            NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4233 on 141 degrees of freedom
## Multiple R-Squared: 0.01659, Adjusted R-squared: -0.03224
```

```
## Wald test: 6.047 on 7 and 141 DF, p-value: 3.526e-06
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention < 0.5 & directie_seniority >= 5.5
             & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = primary retention < 0.5 & directie seniority >=
##
          5.5 & leerkracht_age < 4.5)
##
## Residuals:
       Min
                 1Q
                     Median
                                   3Q
## -0.98085 0.05397 0.07400 0.08370 0.10456
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         1.0654468 0.1141004
                                                9.338 < 2e-16 ***
## xman
                        ## xleerkracht_seniority 0.0001879 0.0243074
                                                0.008 0.99383
## xdirectie_age
                         0.0008311 0.0081300
                                                0.102 0.91858
## xdirectie_seniority
                        -0.0208591 0.0130134 -1.603 0.10908
## GOKschool
                         0.0331577 0.0502481
                                               0.660 0.50939
##
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                      1 2517
                               299.839 <2e-16 ***
## Wu-Hausman
                      1 2516
                                 1.718
                                          0.19
## Sargan
                          NA
                                    NA
                                            NA
                      0
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2647 on 2517 degrees of freedom
## Multiple R-Squared: 0.001372, Adjusted R-squared: -0.000612
## Wald test: 2.931 on 5 and 2517 DF, p-value: 0.01211
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention < 0.5 & directie_seniority < 5.5</pre>
             & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = primary_retention < 0.5 & directie_seniority < 5.5 &</pre>
##
##
          leerkracht_age < 4.5)</pre>
##
## Residuals:
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -1.07621 0.07297 0.09505 0.12082 0.15065
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
```

```
## (Intercept)
                         0.888908
                                   0.099599
                                             8.925
                                                      <2e-16 ***
                                   0.015717 -1.951
## xman
                                                      0.0512 .
                        -0.030666
## xleerkracht age
                        -0.007120
                                   0.033838 -0.210
                                                      0.8334
## xleerkracht_seniority 0.024932
                                   0.021701
                                              1.149
                                                      0.2508
## xdirectie_age
                         0.006144
                                   0.009978
                                             0.616
                                                      0.5381
## xdirectie seniority
                      -0.017187
                                   0.019436 -0.884
                                                     0.3767
## GOKschool
                                             2.370
                         0.165123
                                   0.069672
                                                      0.0179 *
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 1371
                              274.222 <2e-16 ***
                                5.235 0.0223 *
                      1 1370
## Wu-Hausman
## Sargan
                          NA
                                   NΑ
                                           NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2867 on 1371 degrees of freedom
## Multiple R-Squared: -0.02126,
                                  Adjusted R-squared: -0.02573
## Wald test: 2.101 on 6 and 1371 DF, p-value: 0.0504
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = leerkracht_age >= 3.5
             & leerkracht_age < 4.5
             & directie_seniority < 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = leerkracht_age >= 3.5 & leerkracht_age < 4.5 & directie_seniority <
##
          5.5)
##
## Residuals:
                     Median
                 1Q
                                  3Q
## -1.23418 0.06847 0.13412 0.14934 0.29161
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
                         ## (Intercept)
## xprimary_retention
                        -0.117080
                                   0.055796 -2.098 0.03607 *
## xman
                        -0.014662
                                   0.017508 -0.837 0.40249
## xBULO
                         0.004945
                                   0.107523
                                             0.046 0.96332
## xleerkracht_seniority 0.025195
                                   0.022549
                                              1.117 0.26406
## xdirectie_age
                         0.006786
                                   0.010044
                                             0.676 0.49941
## xdirectie seniority
                        -0.039889
                                   0.021546 - 1.851 \ 0.06435 .
## GOKschool
                         0.362066
                                   0.112579 3.216 0.00133 **
##
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                     1 1292
                              153.23 < 2e-16 ***
## Wu-Hausman
                      1 1291
                                10.02 0.00159 **
                                   NA
## Sargan
                      0
                          NA
                                           NΑ
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 0.3121 on 1292 degrees of freedom
## Multiple R-Squared: -0.1062, Adjusted R-squared: -0.1122
## Wald test: 2.802 on 7 and 1292 DF, p-value: 0.006738
# From the help file for AER, it says it does an F-test on the first stage regression; I believe the nu
# Let's see what happens when we rule out the dependency on "retention"
# Teacher Age
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
            subset = leerkracht_age <= 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = leerkracht_age <= 4.5)</pre>
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                         Max
## -0.99925  0.06848  0.07565  0.09980  0.26848
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        ## xprimary_retention
                       ## xman
## xBULO
                        0.202721
                                  0.045926
                                            4.414 1.04e-05 ***
## xleerkracht_age
                       -0.017217
                                  0.026015 -0.662 0.50814
## xleerkracht_seniority 0.012998
                                  0.015349
                                            0.847 0.39714
## xdirectie_age
                                  0.005986
                                            0.695 0.48725
                        0.004159
## xdirectie_seniority
                       -0.003157
                                  0.007265 -0.435 0.66395
## GOKschool
                        0.063573
                                  0.037077
                                             1.715 0.08649 .
##
## Diagnostic tests:
                   df1 df2 statistic p-value
## Weak instruments
                   1 4041 631.051 <2e-16 ***
## Wu-Hausman
                     1 4040
                                4.844 0.0278 *
                                          NA
## Sargan
                     0
                         NA
                                  NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2786 on 4041 degrees of freedom
## Multiple R-Squared: 0.00638, Adjusted R-squared: 0.004413
## Wald test: 7.119 on 8 and 4041 DF, p-value: 2.16e-09
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = leerkracht_age <= 4),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = leerkracht_age <= 4)</pre>
##
```

## Residuals:

```
Median
                 1Q
## -0.99925 0.06848 0.07565 0.09980 0.26848
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
                                     0.086855 10.802 < 2e-16 ***
## (Intercept)
                         0.938221
                                     0.035524 -4.181 2.97e-05 ***
## xprimary_retention
                         -0.148516
                                     0.008841 -3.186 0.00145 **
## xman
                         -0.028166
## xBULO
                         0.202721
                                     0.045926
                                                4.414 1.04e-05 ***
## xleerkracht_age
                         -0.017217
                                     0.026015 -0.662 0.50814
## xleerkracht_seniority 0.012998
                                     0.015349
                                               0.847
                                                      0.39714
## xdirectie_age
                          0.004159
                                     0.005986
                                                0.695
                                                      0.48725
                         -0.003157
                                     0.007265 -0.435
                                                      0.66395
## xdirectie_seniority
## GOKschool
                          0.063573
                                     0.037077
                                                1.715 0.08649 .
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
                       1 4041
                                631.051 <2e-16 ***
## Weak instruments
                       1 4040
                                  4.844 0.0278 *
## Wu-Hausman
## Sargan
                          NA
                                     NA
                                             NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2786 on 4041 degrees of freedom
## Multiple R-Squared: 0.00638, Adjusted R-squared: 0.004413
## Wald test: 7.119 on 8 and 4041 DF, p-value: 2.16e-09
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_age >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
  ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
       subset = directie_age >= 5.5)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
## -0.99370 0.06762 0.07612 0.09601 0.27917
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.737072 0.123501
                                              5.968 2.68e-09 ***
## xprimary_retention
                         -0.167318
                                     0.042085 -3.976 7.18e-05 ***
## xman
                         -0.020661
                                     0.010106 - 2.044
                                                         0.041 *
                                                1.167
## xleerkracht_age
                         0.026020
                                     0.022292
                                                         0.243
## xleerkracht_seniority 0.022032
                                     0.019796
                                                1.113
                                                         0.266
## xdirectie_age
                          0.006957
                                     0.008281
                                                0.840
                                                         0.401
## xdirectie_seniority
                         -0.007729
                                     0.009367
                                               -0.825
                                                         0.409
## GOKschool
                          0.055134
                                     0.048834
                                                1.129
                                                         0.259
##
## Diagnostic tests:
                     df1 df2 statistic p-value
## Weak instruments
                       1 2992
                                383.617 <2e-16 ***
## Wu-Hausman
                       1 2991
                                  2.393
                                          0.122
```

```
NA
## Sargan
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2747 on 2992 degrees of freedom
## Multiple R-Squared: 0.01108, Adjusted R-squared: 0.008768
## Wald test: 3.881 on 7 and 2992 DF, p-value: 0.0003244
summary(ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample students,
              subset = directie_age < 5.5),</pre>
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = directie_age < 5.5)</pre>
##
## Residuals:
                      Median
       Min
                  1Q
                                    3Q
## -0.95194 0.05550 0.08235 0.09171 0.21068
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    0.101831 8.444
                                                       <2e-16 ***
                          0.859819
## xprimary_retention
                         -0.088305
                                    0.055573 -1.589
                                                        0.1123
## xman
                                     0.015602 -2.321
                         -0.036206
                                                        0.0205 *
## xBULO
                          0.163037
                                    0.065053
                                               2.506
                                                        0.0123 *
## xleerkracht age
                          0.018053
                                     0.027384
                                               0.659
                                                        0.5098
## xleerkracht_seniority -0.016047
                                     0.024223 -0.662
                                                        0.5078
## xdirectie_age
                          0.011512
                                     0.012851
                                                0.896
                                                        0.3705
## xdirectie_seniority
                          0.003819
                                     0.012929
                                                0.295
                                                        0.7678
## GOKschool
                          0.002912
                                     0.071257
                                                0.041
                                                        0.9674
##
## Diagnostic tests:
                     df1 df2 statistic p-value
## Weak instruments
                       1 1291
                                205.222 <2e-16 ***
                                  0.094
                                          0.759
## Wu-Hausman
                       1 1290
## Sargan
                           NA
                                     NA
                                             NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2744 on 1291 degrees of freedom
## Multiple R-Squared: 0.01015, Adjusted R-squared: 0.004018
## Wald test: 4.175 on 8 and 1291 DF, p-value: 6.026e-05
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_seniority < 5.5</pre>
              & leerkracht_age < 4.5),</pre>
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
       subset = directie_seniority < 5.5 & leerkracht_age < 4.5)</pre>
##
```

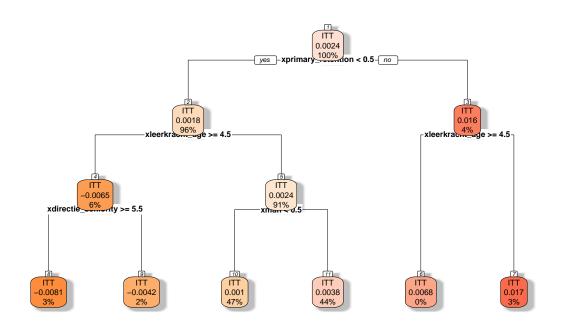
```
## Residuals:
##
        Min
                  10
                      Median
                                     30
                                             Max
## -1.08163 0.07402 0.10436 0.12339 0.26817
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
##
                          0.870039 0.102014 8.529
## (Intercept)
                                                         <2e-16 ***
                                      0.052334 -2.363
## xprimary_retention
                         -0.123683
                                                         0.0182 *
                                      0.015688 -1.345
## xman
                         -0.021102
                                                         0.1788
## xBULO
                          0.125496
                                     0.070429 1.782
                                                         0.0750 .
## xleerkracht_age
                          0.006340
                                     0.034368
                                                0.184
                                                         0.8537
                                                         0.3754
## xleerkracht_seniority 0.019023
                                      0.021456
                                                 0.887
## xdirectie_age
                          0.009095
                                     0.009952
                                                0.914
                                                        0.3609
                                      0.019209 -1.263
## xdirectie_seniority -0.024266
                                                        0.2067
## GOKschool
                          0.176895
                                                2.570
                                                        0.0103 *
                                      0.068838
##
## Diagnostic tests:
                     df1 df2 statistic p-value
                       1 1441
                                294.564 <2e-16 ***
## Weak instruments
## Wu-Hausman
                       1 1440
                                  7.319 0.0069 **
## Sargan
                       0
                           NA
                                     NA
                                              NΔ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2949 on 1441 degrees of freedom
## Multiple R-Squared: -0.02383,
                                     Adjusted R-squared: -0.02951
## Wald test: 2.827 on 8 and 1441 DF, p-value: 0.004093
In the second case we sample 62 students from every school (where 62 units is the size of the smallest school).
# Attaching the Sample and the Covariates
attach(sample_students)
x <- cbind(primary_retention, man, BULO,
           leerkracht_age , leerkracht_seniority,
           directie_age, directie_seniority
)
z <- as.matrix(eligible_dummy)</pre>
y <- as.matrix(certificate)</pre>
logit<-glm(eligible_dummy ~ GOKpercentage,</pre>
           data = sample students, family = binomial(link = "logit"))
summary(logit)
pihat<-predict(logit, sample_students, type="response")</pre>
detach(sample_students)
# Running the BCF algorithm on the IV
set.seed(123)
bcf_fit <- bcf(y, z, x, x, pihat, nburn=2000, nsim=2000)</pre>
tau_post <- bcf_fit$tau</pre>
tauhat <- colMeans(tau_post)</pre>
exp <- as.data.frame(cbind(tauhat, y, x, z))</pre>
```

As we can see from the plot the most important variables detected are the same: teacher age and primary retention.

```
## n= 5332
```

```
##
## node), split, n, deviance, yval
##
         * denotes terminal node
##
##
   1) root 5332 1.030680e-01 0.002373500
##
      2) xprimary_retention< 0.5 5134 6.159266e-02 0.001842070
##
        4) xleerkracht_age>=4.5 298 1.428775e-03 -0.006471185
          8) xdirectie_seniority>=5.5 176 2.269976e-04 -0.008054058 *
##
##
          9) xdirectie_seniority< 5.5 122 1.246648e-04 -0.004187697 *
##
        5) xleerkracht_age< 4.5 4836 3.829997e-02 0.002354343
##
         10) xman< 0.5 2506 1.786845e-02 0.001039199 *
         11) xman>=0.5 2330 1.143535e-02 0.003768827 *
##
##
      3) xprimary_retention>=0.5 198 2.429774e-03 0.016153090
##
        6) xleerkracht_age>=4.5 12 1.138136e-05 0.006847326 *
##
        7) xleerkracht_age< 4.5 186 1.312183e-03 0.016753460 *
```

## **BCF-IV First Stage**



```
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students)
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                            Max
## -0.96645 0.06714 0.07105 0.09195 0.22746
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          0.828619
                                     0.051265 16.163 < 2e-16 ***
## xprimary_retention
                                     0.028576 -4.016 5.99e-05 ***
                         -0.114774
## xman
                         -0.022850
                                     0.007512 -3.042 0.00236 **
## xBULO
                          0.183079
                                     0.036621
                                                4.999 5.94e-07 ***
                          0.025882
                                     0.013603
## xleerkracht_age
                                                1.903 0.05714 .
## xleerkracht_seniority 0.002620
                                     0.011818
                                                0.222
                                                       0.82456
## xdirectie_age
                          0.003857
                                     0.004980
                                                0.774 0.43871
## xdirectie seniority
                         -0.005811
                                     0.005915
                                               -0.982 0.32594
## GOKschool
                          0.020797
                                     0.033705
                                               0.617 0.53724
##
## Diagnostic tests:
                     df1 df2 statistic p-value
## Weak instruments
                       1 5323
                                734.671 <2e-16 ***
## Wu-Hausman
                       1 5322
                                  1.599
                                          0.206
## Sargan
                       0
                           NA
                                     NA
                                             NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2715 on 5323 degrees of freedom
## Multiple R-Squared: 0.007356,
                                  Adjusted R-squared: 0.005864
## Wald test: 12.86 on 8 and 5323 DF, p-value: < 2.2e-16
summary(ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample_students,
              subset = primary_retention < 0.5),</pre>
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
  ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = primary_retention < 0.5)</pre>
##
## Residuals:
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -0.96325 0.06616 0.06892 0.09288 0.11570
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                     0.051373 16.112 < 2e-16 ***
                          0.827704
## xman
                         -0.025061
                                     0.007495 -3.344 0.000833 ***
## xleerkracht_age
                          0.024466
                                     0.013575
                                               1.802 0.071567 .
## xleerkracht_seniority 0.003296
                                     0.011820
                                                0.279 0.780362
                                                0.551 0.581543
## xdirectie_age
                          0.002754
                                     0.004997
## xdirectie_seniority
                         -0.003850
                                     0.005930 -0.649 0.516180
## GOKschool
                          0.023290
                                     0.033956
                                                0.686 0.492813
##
```

```
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                                695.57 <2e-16 ***
                    1 5127
## Wu-Hausman
                      1 5126
                                  1.54
                                         0.215
## Sargan
                          NA
                                    NA
                                            NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2659 on 5127 degrees of freedom
## Multiple R-Squared: 0.001329,
                                   Adjusted R-squared: 0.0001601
## Wald test: 2.705 on 6 and 5127 DF, p-value: 0.01268
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention >= 0.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
      subset = primary_retention >= 0.5)
##
## Residuals:
      Min
               10 Median
                               30
## -0.8681 0.1221 0.1698 0.2158 0.2844
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.692131
                                   0.365136 1.896 0.0595 .
## xman
                                   0.056925 0.592
                         0.033686
                                                      0.5547
## xBULO
                         0.206488
                                    0.125182
                                               1.649
                                                       0.1007
## xleerkracht_age
                                    0.094829
                                              0.680
                                                      0.4973
                         0.064494
## xleerkracht_seniority -0.008888
                                    0.066866 -0.133
                                                       0.8944
## xdirectie_age
                         0.028118
                                    0.033105
                                              0.849
                                                       0.3967
## xdirectie_seniority -0.051551
                                    0.037849 -1.362
                                                       0.1748
## GOKschool
                        -0.006835
                                   0.204307 -0.033
                                                      0.9733
##
## Diagnostic tests:
                   df1 df2 statistic p-value
                              39.474 2.22e-09 ***
## Weak instruments 1 190
## Wu-Hausman
                               0.085
                                        0.772
                     1 189
## Sargan
                     O NA
                                  NΑ
                                           NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3944 on 190 degrees of freedom
## Multiple R-Squared: 0.01787, Adjusted R-squared: -0.01831
## Wald test: 5.68 on 7 and 190 DF, p-value: 5.665e-06
\#summary(ivreq(formula = y \sim x + GOKschool \mid x + z, data = sample students,
              subset = primary_retention < 0.5 & leerkracht_age >= 4.5),
#
        vcov = sandwich, diagnostics = TRUE)
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention < 0.5 & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
```

```
##
## Call:
## ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample students,
       subset = primary_retention < 0.5 & leerkracht_age < 4.5)</pre>
##
## Residuals:
       Min
                 10
                      Median
                                   30
## -0.96889 0.06811 0.07000 0.09551 0.10764
##
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          ## xman
                        -0.0268919 0.0078548 -3.424 0.000623 ***
## xleerkracht_age
                        -0.0088074 0.0240459 -0.366 0.714176
## xleerkracht_seniority 0.0084156 0.0132701
                                                0.634 0.525997
## xdirectie_age
                         0.0013794
                                    0.0053372
                                                0.258 0.796068
## xdirectie_seniority
                        -0.0004329 0.0065595
                                              -0.066 0.947384
## GOKschool
                         0.0351890 0.0331987
                                                1.060 0.289220
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
                               740.839 <2e-16 ***
## Weak instruments
                      1 4829
                                 2.959 0.0855 .
## Wu-Hausman
                       1 4828
## Sargan
                          NA
                                    NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.27 on 4829 degrees of freedom
## Multiple R-Squared: -0.0004453, Adjusted R-squared: -0.001688
## Wald test: 2.4 on 6 and 4829 DF, p-value: 0.02565
\#summary(ivreq(formula = y \sim x + GOKschool \mid x + z, data = sample\_students,
              subset = primary_retention >= 0.5 & leerkracht_age >= 4.5),
#
        vcov = sandwich, diagnostics = TRUE)
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = primary_retention >= 0.5 & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = primary_retention >= 0.5 & leerkracht_age < 4.5)</pre>
##
## Residuals:
##
       Min
                  10
                      Median
                                   30
                                            Max
## -0.85537 0.09838 0.17555 0.21965 0.33809
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    0.602798
                                              2.026
                                                       0.0443 *
                         1.221208
                                    0.058484
                                               0.325
                                                       0.7453
## xman
                         0.019026
## xBULO
                                                       0.0550 .
                         0.257316
                                    0.133201
                                               1.932
## xleerkracht_age
                        -0.071732
                                    0.155486 -0.461
                                                       0.6451
## xleerkracht_seniority -0.004872
                                    0.071670 -0.068
                                                       0.9459
## xdirectie_age
                         0.026299
                                    0.032628
                                              0.806
                                                       0.4213
```

```
## xdirectie_seniority
                        -0.048223
                                     0.038244 -1.261
                                                        0.2090
## GOKschool
                        -0.073117
                                    0.203074 -0.360
                                                        0.7192
##
## Diagnostic tests:
                   df1 df2 statistic p-value
                                37.56 5.56e-09 ***
## Weak instruments
                     1 178
                                 0.00
                                        0.989
## Wu-Hausman
                     1 177
## Sargan
                     O NA
                                   NΑ
                                            NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3995 on 178 degrees of freedom
## Multiple R-Squared: 0.02161, Adjusted R-squared: -0.01686
## Wald test: 4.191 on 7 and 178 DF, p-value: 0.0002676
summary(ivreg(formula = y \sim x + GOKschool \mid x + z, data = sample_students,
              subset = primary_retention < 0.5 & directie_seniority >= 5.5
              & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = primary_retention < 0.5 & directie_seniority >=
##
          5.5 & leerkracht_age < 4.5)
##
## Residuals:
       Min
                  1Q
                     Median
                                    30
## -0.95684 0.04901 0.07499 0.07700 0.10301
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
                                    0.097886 11.465 < 2e-16 ***
## (Intercept)
                         1.122217
                         -0.026015
                                    0.009409 -2.765 0.00573 **
## xleerkracht_seniority -0.003842
                                    0.020659 -0.186 0.85247
## xdirectie_age
                         0.002008
                                     0.007208
                                              0.279 0.78054
## xdirectie_seniority
                         -0.027985
                                     0.011710 -2.390 0.01691 *
## GOKschool
                          0.001635
                                     0.045044
                                                0.036 0.97104
##
## Diagnostic tests:
                     df1 df2 statistic p-value
## Weak instruments
                      1 3121
                               371.102 <2e-16 ***
                                  0.889
                                          0.346
## Wu-Hausman
                       1 3120
## Sargan
                          NΑ
                                    NΑ
                                             NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2627 on 3121 degrees of freedom
## Multiple R-Squared: 0.004747,
                                   Adjusted R-squared: 0.003152
## Wald test: 3.624 on 5 and 3121 DF, p-value: 0.002851
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = primary_retention < 0.5 & directie_seniority < 5.5</pre>
              & leerkracht_age < 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
```

```
##
## Call:
  ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = primary_retention < 0.5 & directie_seniority < 5.5 &</pre>
##
##
          leerkracht_age < 4.5)</pre>
##
## Residuals:
##
       Min
                  1Q
                     Median
                                    3Q
## -1.02105 0.07010 0.08569 0.11516 0.13216
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                          8.981e-01 9.265e-02
                                               9.694
                                                         <2e-16 ***
                         -2.964e-02 1.405e-02 -2.110
## xman
                                                         0.0350 *
## xleerkracht_age
                         -3.155e-03 3.034e-02 -0.104
                                                         0.9172
## xleerkracht_seniority 1.691e-02
                                    1.885e-02
                                                0.897
                                                         0.3697
## xdirectie_age
                         8.797e-05 8.732e-03
                                                0.010
                                                         0.9920
## xdirectie seniority
                        -7.839e-03 1.684e-02
                                               -0.465
                                                         0.6417
## GOKschool
                         1.066e-01 5.989e-02
                                               1.779
                                                         0.0754 .
##
## Diagnostic tests:
                     df1 df2 statistic p-value
## Weak instruments
                      1 1702
                                340.975 <2e-16 ***
                       1 1701
                                  3.494 0.0618 .
## Wu-Hausman
## Sargan
                       0
                          NA
                                     NA
                                             NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2832 on 1702 degrees of freedom
## Multiple R-Squared: -0.009766, Adjusted R-squared: -0.01333
## Wald test: 1.553 on 6 and 1702 DF, p-value: 0.1571
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = leerkracht_age >= 3.5
              & leerkracht_age < 4.5
              & directie_seniority < 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
       subset = leerkracht_age >= 3.5 & leerkracht_age < 4.5 & directie_seniority <</pre>
##
          5.5)
##
## Residuals:
##
       Min
                  1Q
                     Median
                                    30
## -1.14981 0.06761 0.11809 0.13344 0.24428
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          0.9347140 0.0965239
                                                 9.684 < 2e-16 ***
## xprimary_retention
                                               -1.953 0.05097 .
                         -0.0923678 0.0472908
## xman
                         -0.0150113 0.0150609
                                                -0.997 0.31906
## xBULO
                          0.0258112 0.0868474
                                                0.297 0.76635
## xleerkracht_seniority 0.0184740 0.0192897
                                                0.958 0.33835
```

```
## xdirectie_age
                         0.0006785 0.0086824
                                                0.078 0.93772
## xdirectie_seniority
                       -0.0260867 0.0184389 -1.415 0.15733
## GOKschool
                                               2.816 0.00492 **
                         0.2675673 0.0950020
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 1604
                               191.333 <2e-16 ***
## Wu-Hausman
                      1 1603
                                 7.864 0.0051 **
## Sargan
                          NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3002 on 1604 degrees of freedom
## Multiple R-Squared: -0.06259,
                                   Adjusted R-squared: -0.06723
## Wald test: 2.482 on 7 and 1604 DF, p-value: 0.01551
# From the help file for AER, it says it does an F-test on the first stage regression; I believe the nu
# Let's see what happens when we rule out the dependency on "retention"
# Teacher Age
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = leerkracht_age <= 4.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = leerkracht_age <= 4.5)</pre>
##
## Residuals:
       Min
                 1Q
                     Median
                                   3Q
## -0.96474 0.06721 0.06991 0.09485 0.22421
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.938086 0.082169 11.417 < 2e-16 ***
## xprimary_retention
                        -0.119101 0.029964 -3.975 7.14e-05 ***
                                   0.007866 -3.178 0.00149 **
## xman
                        -0.024996
## xBULO
                         0.187940
                                   0.038238
                                              4.915 9.16e-07 ***
## xleerkracht age
                        -0.009581
                                   0.023937 -0.400 0.68899
## xleerkracht_seniority 0.007690
                                   0.013229
                                              0.581 0.56109
## xdirectie age
                         0.002699
                                    0.005302
                                               0.509 0.61071
## xdirectie_seniority -0.002761
                                    0.006514 -0.424 0.67172
## GOKschool
                         0.029197
                                    0.032916
                                              0.887 0.37511
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 5013
                               783.329 <2e-16 ***
## Wu-Hausman
                      1 5012
                                 2.683
                                         0.102
## Sargan
                          NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2756 on 5013 degrees of freedom
## Multiple R-Squared: 0.0063, Adjusted R-squared: 0.004714
```

```
## Wald test: 10.81 on 8 and 5013 DF, p-value: 3.333e-15
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = leerkracht_age <= 4),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = leerkracht_age <= 4)</pre>
##
## Residuals:
                 1Q
                     Median
## -0.96474 0.06721 0.06991 0.09485 0.22421
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.938086
                                   0.082169 11.417 < 2e-16 ***
                                   0.029964 -3.975 7.14e-05 ***
## xprimary_retention
                        -0.119101
                        -0.024996
                                   0.007866 -3.178 0.00149 **
## xman
## xBULO
                         0.187940
                                    0.038238
                                              4.915 9.16e-07 ***
## xleerkracht_age
                        -0.009581
                                    0.023937 -0.400 0.68899
## xleerkracht_seniority 0.007690
                                    0.013229
                                              0.581 0.56109
## xdirectie_age
                         0.002699
                                   0.005302
                                              0.509 0.61071
## xdirectie_seniority -0.002761
                                    0.006514 -0.424 0.67172
## GOKschool
                         0.029197
                                    0.032916
                                              0.887 0.37511
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
                      1 5013
                               783.329 <2e-16 ***
## Weak instruments
                                 2.683
## Wu-Hausman
                      1 5012
                                         0.102
## Sargan
                         NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2756 on 5013 degrees of freedom
## Multiple R-Squared: 0.0063, Adjusted R-squared: 0.004714
## Wald test: 10.81 on 8 and 5013 DF, p-value: 3.333e-15
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = directie_age >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = directie_age >= 5.5)
##
##
## Residuals:
                 1Q
                     Median
                                   30
## -0.97653 0.06418 0.07431 0.09057 0.24444
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
                                   0.107288 7.158 9.79e-13 ***
## (Intercept)
                         0.768011
```

```
## xprimary_retention
                         -0.136099
                                     0.035769 -3.805 0.000144 ***
                                     0.008952 -2.281 0.022629 *
## xman
                         -0.020416
## xleerkracht age
                          0.027094
                                     0.019104
                                                1.418 0.156194
## xleerkracht_seniority 0.019594
                                                1.142 0.253533
                                     0.017158
## xdirectie_age
                          0.005979
                                     0.007303
                                                0.819 0.413046
## xdirectie seniority
                                     0.008430 -1.202 0.229498
                         -0.010131
## GOKschool
                          0.025445
                                     0.043524
                                               0.585 0.558836
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
## Weak instruments
                       1 3712
                                475.927 <2e-16 ***
                       1 3711
                                          0.231
## Wu-Hausman
                                  1.438
## Sargan
                           NA
                                     NA
                                             NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2716 on 3712 degrees of freedom
## Multiple R-Squared: 0.01009, Adjusted R-squared: 0.008223
## Wald test: 4.094 on 7 and 3712 DF, p-value: 0.0001736
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_age < 5.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = directie age < 5.5)
##
## Residuals:
       Min
##
                  1Q
                      Median
                                    3Q
                                            Max
## -0.95287 0.05569 0.07647 0.08984
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          0.885386
                                     0.091301
                                                9.697 < 2e-16 ***
                                     0.045790 -1.412 0.15805
## xprimary_retention
                         -0.064670
## xman
                         -0.029342
                                     0.013898 -2.111
                                                       0.03491 *
## xBULO
                          0.155266
                                     0.053931
                                                2.879
                                                       0.00404 **
## xleerkracht_age
                          0.021514
                                     0.024547
                                                0.876
                                                      0.38092
## xleerkracht_seniority -0.023495
                                     0.021320 -1.102
                                                       0.27063
## xdirectie_age
                          0.004806
                                     0.011175
                                                0.430
                                                       0.66724
## xdirectie_seniority
                          0.008563
                                     0.011398
                                                0.751
                                                      0.45259
## GOKschool
                         -0.039610
                                     0.062931 -0.629 0.52916
##
## Diagnostic tests:
                     df1 df2 statistic p-value
                                254.196 <2e-16 ***
## Weak instruments
                       1 1603
## Wu-Hausman
                       1 1602
                                  0.027
                                          0.868
## Sargan
                           NA
                                     NA
                                             NA
                       0
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.271 on 1603 degrees of freedom
## Multiple R-Squared: 0.007881,
                                    Adjusted R-squared: 0.00293
```

```
## Wald test: 8.925 on 8 and 1603 DF, p-value: 4.945e-12
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_seniority < 5.5</pre>
              & leerkracht_age < 4.5),
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
       subset = directie_seniority < 5.5 & leerkracht_age < 4.5)</pre>
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -1.02903 0.07117 0.09355 0.11331
                                         0.22131
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           0.891500
                                      0.093312
                                                 9.554
                                                          <2e-16 ***
                                                          0.0337 *
## xprimary_retention
                         -0.092144
                                      0.043345
                                                -2.126
## xman
                         -0.022144
                                      0.013968
                                                -1.585
                                                          0.1131
## xBULO
                           0.116313
                                      0.057046
                                                 2.039
                                                          0.0416 *
## xleerkracht_age
                          0.004257
                                      0.030390
                                                 0.140
                                                         0.8886
## xleerkracht_seniority 0.013470
                                      0.018561
                                                 0.726
                                                          0.4681
                          0.002389
                                      0.008667
                                                 0.276
                                                          0.7829
## xdirectie_age
## xdirectie_seniority
                         -0.013580
                                      0.016592
                                                -0.818
                                                          0.4132
## GOKschool
                          0.120197
                                      0.059146
                                                 2.032
                                                         0.0423 *
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
## Weak instruments
                       1 1789
                                 365.500 <2e-16 ***
## Wu-Hausman
                       1 1788
                                   5.347
                                          0.0209 *
## Sargan
                       0
                           NA
                                      NA
                                              NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2896 on 1789 degrees of freedom
## Multiple R-Squared: -0.01235,
                                     Adjusted R-squared: -0.01688
## Wald test: 3.051 on 8 and 1789 DF, p-value: 0.002055
```

# Second Outcome: School Progress

We now foucus on the effects when we sample units in a bandwidth of 0.035 (which is the optimal bandwidth for the outcome  $progress\_school$ ) around the cutoff (10%).

```
students_data_randomized_03_2011 <-
students_data_2011[which(students_data_2011$GOKpercentage >= .063
& students_data_2011$GOKpercentage <= .137),]</pre>
```

Moreover, from every school we sample a number students in order to increase the balance in the covariate and to guarantee an equal representation to all the schools, avoiding biases related to the over-representation of biggest schools' students. In the first case, we sample 50 students from each school.

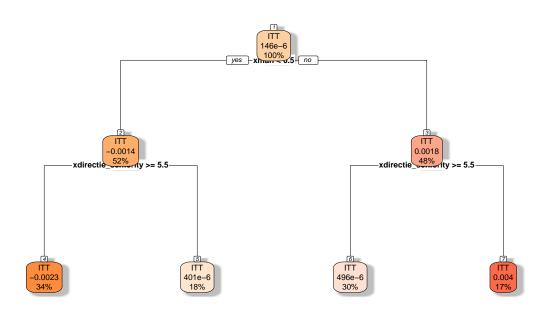
```
schools <-
students_data_randomized_03_2011$school[which(
!duplicated(students data randomized 03 2011$school))]
sample_students <- as.data.frame(matrix(data = NA, nrow = 50*length(schools),</pre>
                                           ncol = ncol(students_data_randomized_03_2011)))
colnames(sample_students) <- colnames(students_data_randomized_03_2011)</pre>
for (j in (0:(length(schools)-1))){
  set.seed(j + 123)
  sample_students[(1+(j*50)):(50+(j*50)),] <-
  students_data_randomized_03_2011[which(
  students_data_randomized_03_2011$school %in%
  schools[j+1]),][sample(1:nrow(students_data_randomized_03_2011[which(
  students_data_randomized_03_2011\$school \(\frac{\text{in\frac{\text{vin\frac{\text{vin\frac{\text{sthools}[j+1]}{\text{j}}}}}\),
  50, replace = FALSE ),]
}
sample_student <- round(sample_students[, -(1:4)], 0)</pre>
sample_students <- cbind(sample_students[,1:4], sample_student)</pre>
Then we run our BCF-IV algorithm on this sample of units.
# Attaching the Sample and the Covariates
attach(sample students)
x <- cbind(primary_retention , man , BULO,
           leerkracht_age , leerkracht_seniority,
           directie_age, directie_seniority
)
z <- as.matrix(eligible_dummy)</pre>
y <- as.matrix(progress_school)</pre>
logit<-glm(eligible_dummy ~ GOKpercentage,</pre>
           data = sample_students, family = binomial(link = "logit"))
summary(logit)
pihat<-predict(logit, sample_students, type="response")</pre>
detach(sample_students)
# Running the BCF algorithm on the IV
set.seed(123)
bcf_fit <- bcf(y, z, x, x, pihat, nburn=2000, nsim=2000)</pre>
tau_post <- bcf_fit$tau</pre>
tauhat <- colMeans(tau_post)</pre>
exp <- as.data.frame(cbind(tauhat, y, x, z))</pre>
## n= 4450
##
## node), split, n, deviance, yval
         * denotes terminal node
##
##
## 1) root 4450 0.0258251000 0.0001457822
     2) xman< 0.5 2317 0.0063970160 -0.0013556030
##
       4) xdirectie_seniority>=5.5 1495 0.0006833538 -0.0023216590 *
       5) xdirectie_seniority< 5.5 822 0.0017808740 0.0004013981 *
##
```

3) xman>=0.5 2133 0.0085317830 0.0017766820

##

- ## 6) xdirectie\_seniority>=5.5 1355 0.0007275679 0.0004959880 \*
- ## 7) xdirectie\_seniority< 5.5 778 0.0017110760 0.0040071960 \*

#### **Causal Tree**



```
ITT = mean(sample_students$progress_school[which(sample_students$eligible_dummy==1)]) - mean(sample_students$progress_school[which(sample_students$eligible_dummy==1)]) - mean(sample_students$progress_school[which(sample_students$eligible_dummy==1)])
## [1] 0.001494949
ITT = mean(students_data_randomized_03_2011$progress_school[which(students_data_randomized_03_2011$elig
ITT
## [1] -0.001654283
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students),
         vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students)
##
## Residuals:
##
          Min
                       1Q
                              Median
                                               ЗQ
                                                          Max
## -0.996598 0.008796 0.013402 0.017221 0.029630
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             0.961428
                                          0.026799 35.875
                                                                <2e-16 ***
## xprimary_retention
                             0.006956
                                          0.006454 1.078
                                                                  0.2811
## xman
                             -0.008257
                                          0.003514 -2.350 0.0188 *
```

```
## xBULO
                         0.009780
                                    0.009426
                                               1.037
                                                       0.2996
## xleerkracht_age
                         0.002255
                                               0.290
                                   0.007775
                                                       0.7718
## xleerkracht seniority 0.005440
                                                       0.3774
                                    0.006161
                                               0.883
                                                       0.1256
## xdirectie_age
                        -0.003652
                                    0.002384 -1.532
## xdirectie_seniority
                         0.003485
                                    0.003227
                                               1.080
                                                       0.2803
## GOKschool
                         0.001910
                                    0.012471
                                               0.153
                                                       0.8783
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 4441
                               847.466 <2e-16 ***
## Wu-Hausman
                      1 4440
                                 0.234
                                         0.629
## Sargan
                      0
                          NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1153 on 4441 degrees of freedom
## Multiple R-Squared: 0.002509,
                                   Adjusted R-squared: 0.000712
## Wald test: 2.836 on 8 and 4441 DF, p-value: 0.00385
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man < 0.5),
       vcov = sandwich, diagnostics = TRUE)
##
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
      subset = man < 0.5)
##
## Residuals:
##
                   1Q
                         Median
                                       3Q
## -0.998958 0.004870 0.009273 0.012751 0.029864
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         1.005368
                                   0.021699 46.332 < 2e-16 ***
                                   0.002547
                                               4.095 4.37e-05 ***
## xprimary_retention
                         0.010430
## xBULO
                                    0.011252
                                               1.441
                                                       0.1497
                         0.016214
## xleerkracht_age
                        -0.015006
                                    0.009583 -1.566
                                                       0.1175
## xleerkracht_seniority 0.017113
                                    0.009413
                                              1.818
                                                      0.0692 .
## xdirectie_age
                        -0.002202
                                    0.002805 - 0.785
                                                       0.4326
## xdirectie_seniority
                       -0.001276
                                    0.003781 -0.338
                                                      0.7358
## GOKschool
                        -0.007540
                                    0.013197 -0.571
                                                       0.5678
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                               502.071 <2e-16 ***
                      1 2309
## Wu-Hausman
                      1 2308
                                 0.009
                                         0.923
## Sargan
                          NA
                                    NA
                                            NΑ
                      0
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.09691 on 2309 degrees of freedom
## Multiple R-Squared: 0.004915,
                                   Adjusted R-squared: 0.001899
## Wald test: 3.094 on 7 and 2309 DF, p-value: 0.002998
```

```
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man > 0.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man > 0.5)
##
## Residuals:
##
       Min
                 1Q
                    Median
                                  30
## -1.00779 0.01375 0.01661 0.02194 0.05103
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.885626
                                  0.055958 15.826
                                                    <2e-16 ***
## xprimary_retention
                         0.002929
                                   0.013562
                                             0.216
                                                      0.8291
## xBULO
                         0.002617
                                   0.016627
                                              0.157
                                                      0.8750
## xleerkracht_age
                         0.025304
                                   0.013802
                                             1.833
                                                     0.0669 .
## xleerkracht_seniority -0.006980
                                   0.008485 -0.823
                                                     0.4108
## xdirectie_age
                        -0.005992
                                   0.004080 -1.469
                                                      0.1421
## xdirectie_seniority
                         0.009582
                                   0.005534
                                              1.732
                                                      0.0835 .
## GOKschool
                         0.017941
                                   0.023201
                                                      0.4394
                                              0.773
##
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                      1 2125
                              348.383 <2e-16 ***
                                        0.451
## Wu-Hausman
                      1 2124
                                 0.569
## Sargan
                         NA
                                   NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1324 on 2125 degrees of freedom
## Multiple R-Squared: 0.002227,
                                  Adjusted R-squared: -0.00106
## Wald test: 1.073 on 7 and 2125 DF, p-value: 0.3784
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man < 0.5 & directie_seniority >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
      subset = man < 0.5 & directie_seniority >= 5.5)
##
## Residuals:
                   1Q
                        Median
                                      3Q
## -0.990166 -0.002412 0.012797 0.012797 0.044397
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         ## xprimary_retention
                         0.014315
                                   0.004404
                                              3.250 0.00118 **
## xBULO
                         0.023261
                                   0.014364
                                              1.619 0.10556
```

```
## xleerkracht_age
                       -0.028950
                                    0.021747 -1.331 0.18333
## xleerkracht_seniority 0.020325
                                               1.339 0.18080
                                    0.015180
                                    0.003967
## xdirectie age
                         0.002963
                                               0.747 0.45520
## xdirectie_seniority
                                    0.007268 -2.501 0.01251 *
                        -0.018172
## GOKschool
                        -0.028636
                                    0.017907 -1.599 0.11001
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 1487
                               296.852 <2e-16 ***
                                 0.293
                                         0.589
## Wu-Hausman
                      1 1486
## Sargan
                          NA
                                    NA
                                            NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.09947 on 1487 degrees of freedom
## Multiple R-Squared: 0.009251,
                                 Adjusted R-squared: 0.004587
## Wald test: 2.187 on 7 and 1487 DF, p-value: 0.03286
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man < 0.5 & directie_seniority < 5.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man < 0.5 & directie_seniority < 5.5)</pre>
##
## Residuals:
        Min
                   1Q
                         Median
                                       3Q
                                                Max
## -0.996387 0.001192 0.003613 0.014034 0.037943
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         0.985647
                                    0.017240 57.171
                                                     <2e-16 ***
## xprimary_retention
                         0.009305
                                    0.003811
                                               2.441
                                                       0.0148 *
## xBULO
                                              0.258
                                                      0.7968
                         0.001104
                                    0.004288
                                    0.008646 -1.765
## xleerkracht_age
                        -0.015264
                                                      0.0779 .
                                              1.501
## xleerkracht_seniority 0.019462
                                    0.012969
                                                       0.1338
                                    0.004094 -1.816
                                                      0.0698 .
## xdirectie_age
                        -0.007434
## xdirectie seniority
                         0.006224
                                   0.009018
                                             0.690
                                                      0.4903
## GOKschool
                         0.005231
                                    0.014698 0.356
                                                     0.7220
##
## Diagnostic tests:
                   df1 df2 statistic p-value
## Weak instruments
                     1 814
                               163.3 <2e-16 ***
                                 0.3
                                       0.584
## Wu-Hausman
                     1 813
## Sargan
                     O NA
                                  NA
                                          NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09164 on 814 degrees of freedom
## Multiple R-Squared: 0.015, Adjusted R-squared: 0.006526
## Wald test: 1.026 on 7 and 814 DF, p-value: 0.4109
```

```
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man > 0.5 & directie_seniority >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man > 0.5 & directie_seniority >= 5.5)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   30
## -0.99228 0.01280 0.01542 0.01738 0.04547
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.958873
                                   0.081266 11.799 < 2e-16 ***
## xprimary_retention
                         0.017278
                                   0.004179
                                              4.135 3.78e-05 ***
## xBULO
                                              3.286 0.00104 **
                         0.017376
                                   0.005288
## xleerkracht_age
                         0.027486
                                   0.010792
                                              2.547 0.01098 *
## xleerkracht_seniority -0.018130
                                   0.005573 -3.253 0.00117 **
## xdirectie_age
                        -0.007699
                                    0.005575 -1.381
                                                     0.16752
## xdirectie_seniority
                         0.005746
                                    0.008949
                                              0.642 0.52096
## GOKschool
                        -0.014653
                                    0.032154 -0.456 0.64866
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                      1 1347
                                167.34 <2e-16 ***
## Wu-Hausman
                                  0.12
                                         0.729
                      1 1346
## Sargan
                          NA
                                    NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1265 on 1347 degrees of freedom
## Multiple R-Squared: 0.003894,
                                   Adjusted R-squared: -0.001282
## Wald test: 3.209 on 7 and 1347 DF, p-value: 0.002239
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man > 0.5 & directie_seniority < 5.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
      subset = man > 0.5 & directie_seniority < 5.5)</pre>
##
## Residuals:
                     Median
                 1Q
                                   3Q
## -1.00474 0.01010 0.01930 0.02806 0.06176
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   0.091351 9.184 <2e-16 ***
                         0.838956
## xprimary_retention
                        -0.015026
                                    0.033489 -0.449
                                                        0.654
## xBULO
                         0.012681
                                    0.057039 0.222
                                                        0.824
```

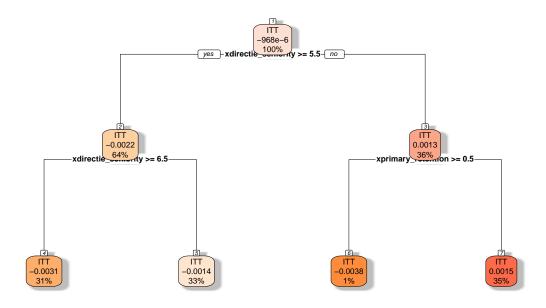
```
## xleerkracht_age
                         0.005631
                                    0.027005
                                               0.209
                                                        0.835
## xleerkracht_seniority 0.009208
                                    0.013236
                                               0.696
                                                        0.487
## xdirectie_age
                                    0.006439 -1.002
                        -0.006455
                                                        0.316
## xdirectie_seniority
                         0.024773
                                    0.015617
                                               1.586
                                                        0.113
## GOKschool
                         0.015196
                                    0.038595
                                               0.394
                                                        0.694
##
## Diagnostic tests:
##
                   df1 df2 statistic p-value
                     1 770
                             152.159 <2e-16 ***
## Weak instruments
## Wu-Hausman
                     1 769
                               0.154
                                       0.695
## Sargan
                     O NA
                                  NA
                                          NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1419 on 770 degrees of freedom
## Multiple R-Squared: 0.01035, Adjusted R-squared: 0.001356
## Wald test: 2.36 on 7 and 770 DF, p-value: 0.02171
# From the help file for AER, it says it does an F-test on the first stage regression; I believe the nu
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_seniority >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = directie_seniority >= 5.5)
##
## Residuals:
       Min
                  1Q
                      Median
                                   3Q
                                           Max
## -0.99599 0.00835 0.01117 0.01857 0.03952
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         1.0510029 0.0534439 19.666 < 2e-16 ***
## xprimary_retention
                         0.0152511 0.0029613
                                               5.150 2.78e-07 ***
## xman
                        -0.0073966 0.0043595
                                              -1.697 0.08987
## xBULO
                         0.0229080 0.0077260
                                                2.965 0.00305 **
## xleerkracht age
                        -0.0012778 0.0124648
                                              -0.103 0.91836
## xleerkracht_seniority 0.0004941 0.0077217
                                                0.064 0.94898
## xdirectie_age
                        -0.0017816 0.0033494
                                               -0.532 0.59482
## xdirectie_seniority -0.0066522 0.0057704
                                              -1.153 0.24908
## GOKschool
                        -0.0227343 0.0167930 -1.354 0.17591
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
## Weak instruments
                      1 2841
                               462.554 <2e-16 ***
## Wu-Hausman
                       1 2840
                                 0.394
                                          0.53
## Sargan
                       0
                          NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1132 on 2841 degrees of freedom
## Multiple R-Squared: 0.002901,
                                   Adjusted R-squared: 9.342e-05
```

```
## Wald test: 4.031 on 8 and 2841 DF, p-value: 8.924e-05
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_seniority < 5.5),</pre>
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = directie_seniority < 5.5)</pre>
##
## Residuals:
                          Median
                    1Q
                                         3Q
                                                  Max
## -0.999437 0.002451 0.013426 0.022301 0.042140
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          0.929891
                                      0.036735 25.313
                                                         <2e-16 ***
                                      0.016106 -0.142
                                                         0.8871
## xprimary_retention
                         -0.002286
                         -0.012073
                                      0.006130 -1.969
                                                         0.0491 *
## xman
## xBULO
                          0.008164
                                      0.024696
                                                0.331
                                                         0.7410
## xleerkracht_age
                         -0.007395
                                      0.010517 -0.703
                                                         0.4821
## xleerkracht_seniority 0.014382
                                      0.008540
                                                1.684
                                                         0.0924 .
## xdirectie_age
                         -0.006432
                                      0.003538 -1.818
                                                         0.0692 .
## xdirectie_seniority
                          0.014752
                                      0.008808
                                                1.675
                                                         0.0942 .
## GOKschool
                          0.008671
                                      0.018133
                                                 0.478
                                                         0.6326
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
                       1 1591
                                 331.187 <2e-16 ***
## Weak instruments
## Wu-Hausman
                       1 1590
                                   0.016
                                             0.9
## Sargan
                           NA
                                      NA
                                              NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1188 on 1591 degrees of freedom
## Multiple R-Squared: 0.009721,
                                     Adjusted R-squared: 0.004742
## Wald test: 1.608 on 8 and 1591 DF, p-value: 0.1175
In the second case we sample 62 students from every school (where 62 units is the size of the smallest school).
# Attaching the Sample and the Covariates
attach(sample students)
x <- cbind(primary_retention , man , BULO,
           leerkracht_age , leerkracht_seniority,
           directie_age, directie_seniority
)
z <- as.matrix(eligible dummy)</pre>
y <- as.matrix(progress_school)
logit<-glm(eligible_dummy ~ GOKpercentage,</pre>
           data = sample_students, family = binomial(link = "logit"))
summary(logit)
pihat<-predict(logit, sample_students, type="response")</pre>
detach(sample_students)
# Running the BCF algorithm on the IV
```

```
set.seed(123)
bcf_fit <- bcf(y, z, x, x, pihat, nburn=2000, nsim=2000)
tau_post <- bcf_fit$tau
tauhat <- colMeans(tau_post)

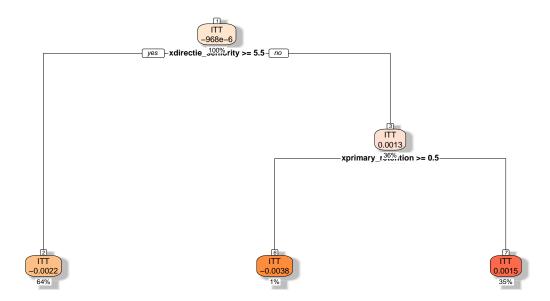
exp <- as.data.frame(cbind(tauhat, y, x, z))</pre>
```

## **Causal Tree**



We can further trim the tree.

#### **Causal Tree**



Let's now see if the heterogeneous effects are robust:

```
ITT = mean(sample_students$progress_school[which(sample_students$eligible_dummy==1)]) - mean(sample_stu
ITT
## [1] -0.001735093
ITT = mean(students_data_randomized_03_2011$progress_school[which(students_data_randomized_03_2011$elig
ITT
## [1] -0.001654283
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students),
       vcov = sandwich, diagnostics = TRUE)
##
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students)
##
## Residuals:
##
         Min
                    1Q
                         Median
                                       3Q
                                                Max
## -0.996760 0.007166 0.013351 0.015120 0.038743
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.975971
                                    0.021953 44.456 <2e-16 ***
                                    0.010452 -0.826
## xprimary_retention
                        -0.008629
                                                       0.4090
## xman
                        -0.007143
                                    0.003059 -2.335
                                                       0.0196 *
## xBULO
                         0.022654
                                   0.010624 2.132 0.0330 *
```

```
## xleerkracht_age
                        0.002345
                                   0.006300
                                            0.372
                                                     0.7098
## xleerkracht_seniority 0.002291
                                            0.454
                                  0.005051
                                                     0.6502
                       -0.003925
                                   0.002172 -1.807
## xdirectie_age
                                                     0.0708 .
## xdirectie_seniority
                                             1.268
                                                     0.2049
                        0.003686
                                   0.002907
## GOKschool
                       -0.008194
                                   0.010850 -0.755
                                                     0.4501
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                     1 5509 1050.848 <2e-16 ***
                                0.001
                                        0.974
## Wu-Hausman
                     1 5508
## Sargan
                         NA
                                   NA
                                          NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1118 on 5509 degrees of freedom
## Multiple R-Squared: 0.002906, Adjusted R-squared: 0.001458
## Wald test: 3.169 on 8 and 5509 DF, p-value: 0.001377
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man < 0.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man < 0.5)
##
## Residuals:
        Min
                  1Q
                        Median
                                      3Q
                                              Max
## -0.997309 0.005092 0.007049 0.013809 0.046212
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                        ## xprimary_retention
                       -0.019211
                                  0.016335 -1.176
                                                    0.2397
## xBULO
                                            2.047
                        0.031943
                                  0.015606
                                                     0.0408 *
## xleerkracht_age
                                   0.007760 -1.364
                                                     0.1727
                       -0.010584
                                            1.319
## xleerkracht_seniority 0.010064
                                   0.007632
                                                     0.1874
                                   0.002670 -1.633
## xdirectie_age
                       -0.004359
                                                    0.1026
## xdirectie seniority
                        0.002401
                                   0.003501
                                            0.686
                                                     0.4929
## GOKschool
                       -0.013192
                                   0.011905 -1.108
                                                     0.2679
##
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                     1 2876
                              607.219 <2e-16 ***
                                0.226
                     1 2875
                                        0.634
## Wu-Hausman
## Sargan
                        NA
                                          NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0962 on 2876 degrees of freedom
## Multiple R-Squared: 0.004858, Adjusted R-squared: 0.002435
## Wald test: 1.288 on 7 and 2876 DF, p-value: 0.2518
```

```
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man > 0.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man > 0.5)
##
## Residuals:
##
       Min
                 1Q
                    Median
                                  30
## -0.99448 0.01431 0.01623 0.01816 0.03633
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        9.227e-01 4.502e-02 20.496 <2e-16 ***
## xprimary_retention
                        3.963e-03 1.170e-02
                                              0.339
                                                      0.7348
## xBULO
                                              0.493
                        7.864e-03 1.594e-02
                                                      0.6218
## xleerkracht_age
                        1.853e-02 1.104e-02
                                              1.678
                                                      0.0934
## xleerkracht_seniority -5.910e-03 6.931e-03 -0.853
                                                      0.3939
## xdirectie_age
                        -3.830e-03 3.580e-03 -1.070
                                                      0.2848
## xdirectie seniority
                        5.570e-03 4.869e-03
                                              1.144
                                                      0.2527
## GOKschool
                       -2.679e-05 1.949e-02 -0.001
                                                      0.9989
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                     1 2626
                              447.171 <2e-16 ***
                                0.144
                                        0.704
## Wu-Hausman
                      1 2625
## Sargan
                         NA
                                   NΑ
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1268 on 2626 degrees of freedom
## Multiple R-Squared: 0.002136,
                                  Adjusted R-squared: -0.0005241
## Wald test: 2.977 on 7 and 2626 DF, p-value: 0.004119
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man < 0.5 & directie_seniority >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
      subset = man < 0.5 & directie_seniority >= 5.5)
##
## Residuals:
                        Median
                   1Q
                                      3Q
## -1.003234 -0.001514 0.009861 0.009861 0.038757
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         ## xprimary_retention
                        0.011932
                                   0.003576 3.336 0.000866 ***
## xBULO
                                   0.012749 1.878 0.060540 .
                         0.023942
```

```
## xleerkracht_age
                        -0.021638
                                    0.016850 -1.284 0.199240
## xleerkracht_seniority 0.015038
                                                1.259 0.208055
                                    0.011941
## xdirectie age
                         0.001720
                                     0.003335
                                              0.516 0.606090
## xdirectie_seniority
                        -0.013096
                                    0.005997 -2.184 0.029116 *
## GOKschool
                         -0.027176
                                    0.015151 -1.794 0.073033 .
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
## Weak instruments
                      1 1846
                               354.586 <2e-16 ***
## Wu-Hausman
                       1 1845
                                  0.783
                                          0.376
## Sargan
                          NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09248 on 1846 degrees of freedom
## Multiple R-Squared: 0.00468, Adjusted R-squared: 0.0009062
## Wald test: 2.318 on 7 and 1846 DF, p-value: 0.02352
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = man < 0.5 & directie_seniority < 5.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man < 0.5 & directie_seniority < 5.5)</pre>
##
## Residuals:
##
        Min
                    1Q
                         Median
                                        3Q
                                                 Max
## -0.994308 0.001066 0.005692 0.015361 0.089013
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                    0.020566 49.161
                                                       <2e-16 ***
                         1.011031
                                    0.039596 -1.616
## xprimary_retention
                        -0.063982
                                                       0.1064
## xBULO
                         0.065969
                                    0.043338
                                               1.522
                                                       0.1283
## xleerkracht_age
                                     0.008226 -0.728
                                                       0.4666
                        -0.005991
## xleerkracht_seniority 0.007560
                                     0.011086
                                               0.682
                                                       0.4954
                                     0.004205 -2.300
## xdirectie_age
                         -0.009669
                                                       0.0217 *
## xdirectie seniority
                         0.005069
                                    0.008677
                                               0.584
                                                       0.5592
## GOKschool
                          0.001596
                                    0.022538
                                              0.071
                                                        0.9436
##
## Diagnostic tests:
                     df1 df2 statistic p-value
## Weak instruments
                       1 1022
                               206.543 <2e-16 ***
                       1 1021
                                  0.004
                                          0.949
## Wu-Hausman
## Sargan
                          NA
                                    NA
                                             NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1019 on 1022 degrees of freedom
## Multiple R-Squared: 0.02577, Adjusted R-squared: 0.01909
## Wald test: 1.641 on 7 and 1022 DF, p-value: 0.1201
```

```
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man > 0.5 & directie_seniority >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = man > 0.5 & directie_seniority >= 5.5)
##
## Residuals:
##
       Min
                 1Q
                    Median
                                  30
## -0.99200 0.01068 0.01346 0.01615 0.05109
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         ## xprimary_retention
                         0.016954
                                  0.003907
                                             4.340 1.51e-05 ***
## xBULO
                                  0.004500
                                             3.589 0.000341 ***
                         0.016150
## xleerkracht_age
                                  0.009352
                                             1.987 0.047046 *
                         0.018586
## xleerkracht_seniority -0.012317
                                  0.004823 -2.554 0.010748 *
## xdirectie_age
                        -0.002686
                                   0.004923 -0.546 0.585339
## xdirectie_seniority
                       -0.002779
                                    0.008476 -0.328 0.743027
## GOKschool
                        -0.035038
                                   0.028229 -1.241 0.214717
##
## Diagnostic tests:
                    df1 df2 statistic p-value
## Weak instruments
                      1 1672
                               222.360 <2e-16 ***
                                 0.732
                                        0.392
## Wu-Hausman
                      1 1671
## Sargan
                         NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1237 on 1672 degrees of freedom
## Multiple R-Squared: 0.001123,
                                 Adjusted R-squared: -0.003059
## Wald test: 3.779 on 7 and 1672 DF, p-value: 0.0004481
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = man > 0.5 & directie_seniority < 5.5),</pre>
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
##
      subset = man > 0.5 & directie_seniority < 5.5)</pre>
##
## Residuals:
                   1Q
                        Median
                                      3Q
## -1.001279 0.007727 0.015487 0.027381 0.051308
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.884159
                                  0.070077 12.617
                                                    <2e-16 ***
## xprimary_retention
                        -0.014745
                                   0.029454 -0.501
                                                      0.6168
## xBULO
                         0.018426
                                   0.047036 0.392 0.6953
```

```
## xleerkracht_age
                         0.002625
                                    0.020652
                                               0.127
                                                       0.8989
## xleerkracht_seniority 0.006382
                                              0.595
                                    0.010725
                                                       0.5520
                        -0.006658
## xdirectie_age
                                    0.005366 - 1.241
                                                       0.2150
## xdirectie_seniority
                                                       0.0957 .
                         0.021076
                                    0.012638
                                               1.668
## GOKschool
                         0.003770
                                    0.031750
                                               0.119
                                                       0.9055
##
## Diagnostic tests:
##
                   df1 df2 statistic p-value
                     1 946
                             191.414 <2e-16 ***
## Weak instruments
## Wu-Hausman
                     1 945
                               0.096
                                       0.756
## Sargan
                     O NA
                                  NA
                                          NA
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1323 on 946 degrees of freedom
## Multiple R-Squared: 0.007944,
                                  Adjusted R-squared: 0.000603
## Wald test: 2.493 on 7 and 946 DF, p-value: 0.01533
# From the help file for AER, it says it does an F-test on the first stage regression; I believe the nu
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
              subset = directie_seniority >= 5.5),
       vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
       subset = directie_seniority >= 5.5)
##
## Residuals:
        Min
                   1Q
                         Median
                                        3Q
                                                Max
## -0.999463 0.008285 0.008855 0.016950 0.047566
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         1.056704   0.044806   23.584   < 2e-16 ***
## xprimary_retention
                         0.014335
                                   0.002681
                                              5.347 9.5e-08 ***
                                    0.003765 -2.150 0.03162 *
## xman
                         -0.008095
## xBULO
                         0.024139
                                   0.008062
                                              2.994 0.00277 **
## xleerkracht age
                        -0.002774
                                   0.010114 -0.274 0.78390
## xleerkracht_seniority 0.001245
                                   0.006272
                                              0.199 0.84266
## xdirectie_age
                        -0.000174
                                    0.002913 -0.060 0.95239
## xdirectie_seniority -0.008318
                                   0.005195 -1.601 0.10944
## GOKschool
                        -0.030790
                                    0.014710 -2.093 0.03640 *
##
## Diagnostic tests:
##
                     df1 df2 statistic p-value
## Weak instruments
                      1 3525
                               575.698 <2e-16 ***
## Wu-Hausman
                      1 3524
                                 1.599
                                         0.206
## Sargan
                       0
                          NA
                                    NA
                                            NA
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1084 on 3525 degrees of freedom
## Multiple R-Squared: 0.001862,
                                   Adjusted R-squared: -0.0004037
```

```
## Wald test: 4.032 on 8 and 3525 DF, p-value: 8.807e-05
summary(ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
             subset = directie_seniority < 5.5),</pre>
        vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = y ~ x + GOKschool | x + z, data = sample_students,
      subset = directie_seniority < 5.5)</pre>
##
## Residuals:
                   1Q
                         Median
                                       3Q
## -0.996927 0.003073 0.010150 0.019376 0.070756
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         0.957861
                                    0.030754 31.146
                                                       <2e-16 ***
                        -0.042220
                                    0.026075 -1.619
                                                       0.1056
## xprimary_retention
## xman
                        -0.007077
                                    0.005373 -1.317
                                                       0.1879
## xBULO
                         0.046501
                                    0.031534
                                              1.475
                                                       0.1405
## xleerkracht_age
                        -0.002538
                                    0.009059 -0.280
                                                       0.7794
## xleerkracht_seniority 0.006579
                                    0.007251
                                              0.907
                                                       0.3643
## xdirectie_age
                        -0.008152
                                    0.003263 -2.498
                                                       0.0126 *
## xdirectie_seniority
                         0.012732
                                    0.007548 1.687
                                                       0.0918 .
## GOKschool
                         0.001938
                                    0.018302
                                              0.106
                                                      0.9157
##
## Diagnostic tests:
##
                    df1 df2 statistic p-value
## Weak instruments
                      1 1975
                               409.687 <2e-16 ***
                                 0.063
                                         0.802
## Wu-Hausman
                      1 1974
## Sargan
                         NA
                                    NA
                                            NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1176 on 1975 degrees of freedom
## Multiple R-Squared: 0.01064, Adjusted R-squared: 0.006632
## Wald test: 2.608 on 8 and 1975 DF, p-value: 0.007743
```