Here are some thoughts from Nathan Graybeal's YouTube post 9 Steps to Mastering Any Jazz Standard.

Learn the Melody

Serves as the melodic basis of your solo.
   Embellish the melody.

- Change the rhythm

- Add repeated notes and accents

- Add extra notes and pitches

- Improvise over long notes or rests

Learn arpeggios of every chord