

**Week 12 FLO** (Friday Learning Opportunity)

1. Find each of the following limits:

(a)  $\lim_{x \rightarrow \infty} \frac{e^x}{x^2}$

(b)  $\lim_{x \rightarrow 0^{(+)}} x \ln(x)$

(c)  $\lim_{x \rightarrow -\infty} x e^x$

(d)  $\lim_{x \rightarrow \infty} x^{1/x}$

(e)  $\lim_{x \rightarrow 0^{(+)}} x^x$

(f)  $\lim_{x \rightarrow 0} \frac{\sin(x) - x}{x^3}$

(g)  $\lim_{x \rightarrow 0} \frac{\cos(x) - 1}{x^2}$

(h)  $\lim_{x \rightarrow \infty} \frac{x + \cos(x)}{x}$

2. I need to design a soup can with height  $h$  and radius  $r$ . The volume  $V$  of the can is  $V = \pi r^2 h$  and its surface area  $A$  is  $A = 2\pi r^2 + 2\pi r h$ . Let's say the surface area is  $2\pi$ . Thus  $2\pi = 2\pi r^2 + 2\pi r h$ . And that makes  $1 = r^2 + 2r h$ . For the constraint  $1 = r^2 + 2r h$ , find  $r$  and  $h$  that maximize the volume  $V = \pi r^2 h$ .