Let  $n \in \mathbf{R}$  and let  $a \in \mathbf{R}$ . Let x be the independent variable and let u and v be dependent variables. Where every both u and v are differentiable, we have

**Rule #0 (constant rule)**  $\frac{d}{dx}[a] = 0$ 

**Rule #1 (power rule)**  $\frac{d}{dx}[x^n] = nx^{n-1}$ . When n = 1, the rule is  $\frac{d}{dx}[x] = 1$ .

**Rule #2 (outative rule)**  $\frac{d}{dx}[au] = a\frac{du}{dx}$ .

**Rule #3 (additive rule)**  $\frac{d}{dx}[u+v] = \frac{du}{dx} + \frac{dv}{dx}$ .

**Rule #4 (product rule)**  $\frac{d}{dx}[uv] = \frac{du}{dx}v + u\frac{dv}{dx}$ 

Rule #5 (quotient rule)  $\frac{d}{dx} \left[ \frac{u}{v} \right] = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$ 

**Rule #6 (exponential rule)**  $\frac{d}{dx}[e^x] = e^x$ 

**Rule #7 (absolute value rule)**  $\frac{d}{dx}[|x|] = \begin{cases} -1 & x < 0 \\ 1 & x > 0 \end{cases}$ . The absolute value function is *not* differentiable at zero.

Notice: The product and quotient rules require that both factors are differentiable. When either fails to be differentiable, anything can happen.