

Greek characters

Name	Symbol	Typical use(s)
alpha	α	angle, constant
beta	β	angle, constant
gamma	γ	angle, constant
delta	δ	limit definition
epsilon	ϵ or ε	limit definition
theta	θ or ϑ	angle
pi	π or ϖ	circular constant
phi	ϕ or φ	angle, constant

Named sets

empty set	\emptyset	integers	\mathbf{Z}
real numbers	\mathbf{R}	positive integers	$\mathbf{Z}_{>0}$
ordered pairs	\mathbf{R}^2	positive reals	$\mathbf{R}_{>0}$

Set symbols

Meaning	Symbol	Meaning	Symbol
is a member	\in	union	\cup
subset	\subset	complement	superscript ^C
intersection	\cap	set minus	\setminus

Logic symbols

Meaning	Symbol	Meaning	Symbol
negation	\neg	equivalent	\equiv
and	\wedge	iff	\iff
or	\vee	for all	\forall
implies	\implies	there exists	\exists

Arithmetic properties

$(\forall a, b \in \mathbf{R})(a + b = b + a)$	commutivity
$(\forall a, b, c \in \mathbf{R})(a + (b + c) = (a + b) + c)$	commutivity
$(\forall a, b \in \mathbf{R})(ab = ba)$	commutivity
$(\forall a, b, c \in \mathbf{R})(a(bc) = (ab)c)$	commutivity
$(\forall a, b, c \in \mathbf{R})(a(b + c) = ab + ac)$	distributive

Distance & Midpoint

The distance between the points (x_1, y_1) and (x_2, y_2) is

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}.$$

The midpoint is the point

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right).$$

Exponents

For $a, b > 0$ and m, n real:

$$\begin{aligned} a^0 &= 1, & 0^a &= 0 \\ 1^a &= 1, & a^n a^m &= a^{n+m} \\ a^n / a^m &= a^{n-m}, & (a^n)^m &= a^{n \cdot m} \\ a^{-m} &= 1/a^m, & (a/b)^m &= a^m / b^m \end{aligned}$$

Solution of Equations

Algebraic

$$\begin{aligned} [ab = 0] &\equiv [a = 0 \text{ or } b = 0] \\ [a^2 = b^2] &\equiv [a = b \text{ or } a = -b] \\ \left[\frac{a}{b} = 0\right] &\equiv [a = 0 \text{ and } b \neq 0] \\ \left[\frac{a}{b} = \frac{c}{d}\right] &\equiv [ad = bc \text{ and } b \neq 0 \text{ and } d \neq 0] \\ [|a| = |b|] &\equiv [a = b \text{ or } a = -b] \\ [\sqrt{a} = b] &\equiv [a = b^2 \text{ and } b \geq 0] \end{aligned}$$

For $a \neq 0$,

$$[ax^2 + bx + c = 0] \equiv \left[x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}\right]$$

Exponential

$$\begin{aligned} [\ln(a) = 0] &\equiv [a = 1] \\ [\text{euler}^a = 1] &\equiv [a = 0] \\ [\ln(a) = b] &\equiv [a = \text{euler}^b] \\ [\ln(a) = b] &\equiv [a = \text{euler}^b] \end{aligned}$$

Parabolas & Lines

The vertex of the parabola $ax^2 + bx + c = y$ is

$$\left(x = -\frac{b}{2a}, y = c - \frac{b^2}{4a}\right).$$

An equation of the line that contains the points $(x = x_1, y = y_1), (x = x_2, y = y_2)$ is

$$y - y_1 = \left(\frac{y_2 - y_1}{x_2 - x_1}\right)(x - x_1).$$

The number $\frac{y_2 - y_1}{x_2 - x_1}$ is the slope.

Radicals

$$\begin{aligned} \sqrt[n]{a} &= a^{1/n} \\ \sqrt[n]{ab} &= \sqrt[n]{a} \sqrt[n]{b} \quad (\text{provided } a, b \geq 0) \\ \sqrt[m]{\sqrt[n]{a}} &= \sqrt[mn]{a} \\ \sqrt[n]{\frac{a}{b}} &= \frac{\sqrt[n]{a}}{\sqrt[n]{b}} \\ \sqrt[n]{a^n} &= \begin{cases} a & n \text{ odd} \\ |a| & n \text{ even} \end{cases} \end{aligned}$$

Identities

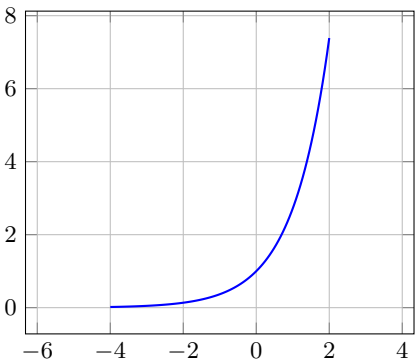
$$\begin{aligned} a(b + c) &= ab + ac \\ ((a + b))(c + d) &= ac + ad + bc + bd \\ \frac{ab + ac}{a} &= b + c \quad (\text{provided } a \neq 0) \\ \frac{\frac{a}{b}}{\frac{c}{d}} &= \frac{ad}{bc} \quad (\text{provided } b, d \neq 0) \\ \sqrt{ab} &= \sqrt{a}\sqrt{b} \quad (\text{provided } a \geq 0, b \geq 0) \\ \ln(ab) &= \ln(a) + \ln(b) \quad (\text{provided } a \geq 0, b \geq 0) \end{aligned}$$

Function notation

$\text{dom}(F)$	domain of function F
$\text{range}(F)$	range of function F

Domains, Ranges, and Zeros

Function	Domain	Range	Zeros
ln, log	$(0, \infty)$	$(-\infty, \infty)$	1
exp	$(-\infty, \infty)$	$(0, \infty)$	\emptyset
abs	$(-\infty, \infty)$	$(0, \infty)$	0
$\sqrt{}$	$(0, \infty)$	$(0, \infty)$	0
$\sqrt[3]{}$	$(-\infty, \infty)$	$(-\infty, \infty)$	0
floor	$(-\infty, \infty)$	\mathbf{Z}	$[0, 1)$
ceiling	$(-\infty, \infty)$	\mathbf{Z}	$(-1, 0]$

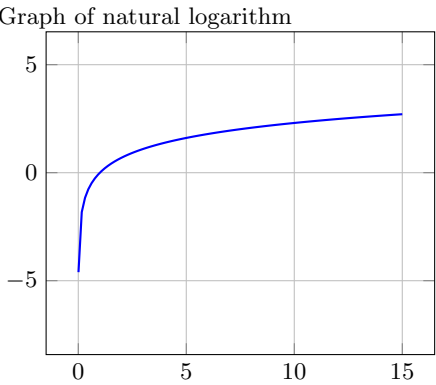


Graph Translations

For the graph of $F(x, y) = 0$

- The graph of $F(x - h, y) = 0$ is the graph of $F(x, y) = 0$ translated h units to the right.
- The graph of $F(x, y - k) = 0$ is the graph of $F(x, y) = 0$ translated k units up.
- The graph of $F(x/c, y) = 0$ is the graph of $F(x, y) = 0$ stretched a factor of c horizontally.
- The graph of $F(x, y/c) = 0$ is the graph of $F(x, y) = 0$ stretched a factor of c vertically.

Graphs



Graph of natural exponential