

Complex Analysis

MATH 365-01

Spring 2023

Instructor: Barton Willis, PhD, Professor of Mathematics

Office: Discovery Hall, Room 368

☎: 308-865-8868

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Zoom for classes: For Zoom class meetings, use the Meeting ID: 616 568 5706.

Office Hours: Monday, Wednesday, and Friday 10:00AM-11:00AM, Tuesday and Thursday 12:00 noon-2:00PM, and by appointment.

Class meeting time and place

This class meets Monday, Wednesday, and Friday in Discovery Hall, room 386 from 1:25PM to 2:15 PM.

Course Resources

Our textbook is *A First Course in Complex Analysis* edition 1.54, by Beck, Marchesi, Pixon, and Sabalka.

Important Dates

First Homework due	January 27
Exam 1	February 17
Exam 2	March 24
Exam 3	April 21
Final exam	May 17, 1:00 PM–3:00 PM

Grading

Your course grade will be based on weekly homework sets, class participation, three midterm exams, and a comprehensive final exam; specifically:

Weekly Homework 11 fifteen point assignments	165 (total)
Class participation	60 (total)
Mid-term exams 1,2, and 3 100 points each	300 (total)
Comprehensive Final exam	150 (total)

If it is necessary to adjust the number of homework assignments, your homework point total will be scaled to a total of 165. For example, if we have only ten homework sets, your homework score will be scaled by a factor of 165/150. The same holds for class participation.

The following table shows the *minimum* number of points (out of 675) that are required for each of the twelve letter grades D- through A+. For example, a point total of 581 points will earn you a grade of B+, and a point total of 608 points will earn you a grade of A-. A point total of 404 or less earns you a failing course grade.

D-	405	B-	540
D	425	B	560
D+	446	B+	581
C-	473	A-	608
C	493	A	628
C+	513	A+	662

Class participation

We will have various activities for earning class participation points. You might be assigned a problem to present to the class, or we might work do in-class pair work. Your class participation grade will be scaled to fifty points.

Prerequisite

The prerequisite for MATH 365 is an earned grade of D- or higher in MATH 260.

Catalog description

Complex Analysis (3 credit hours) Complex analysis is an introduction to the theory of complex variables and the calculus of analytic functions. Topics covered include the calculus of residues, the Cauchy Integration theorem, and the extension of exponential, logarithmic, and trigonometric functions to the complex plane.

Learning Outcomes

On completion of this course, students will

- (a) be able to represent complex numbers algebraically and geometrically.
- (b) be able to use the definition of the limit to prove that a function has a limit.
- (c) be able to find derivatives of complex valued functions from the limit definition.
- (d) understand the connection between the complex exponential and the trigonometric functions and be able to prove trigonometric identities using these connections.
- (e) be able to use the Cauchy-Riemann equations to determine if a function is analytic.
- (f) be able to represent functions using Laurent and power series and be able to find function residues, poles, and pole order.
- (g) be able to evaluate contour integrals using residues.
- (h) understand the Cauchy integral formula and its consequences, including the fundamental theorem of algebra.

Course Calendar

Generally, we'll adhere to the scheduled exam dates even if we are ahead or behind with course work. When we are ahead or behind, the topics on the exams will be appropriately adjusted.

Notices:

- (a) *Exams will be given on the **Friday** of the week they are assigned.*
- (b) Homework (**HW**) will be due at midnight on Saturday of the week they are assigned.

Week	Week Starting	Section(s)	Topic(s)	Assessment
1	January 23	\$1.1, \$1.2	Algebraic Properties; Geometric Properties	HW 1
2	January 30	\$1.3, \$1.4	Geometric Properties; Topology	HW 2
3	February 6	\$2.1, \$2.2	Limits & continuity; Derivatives	HW 3
4	February 13	\$2.3, \$2.4	Cauchy-Riemann; Constant functions	Exam 1
5	February 20	\$3.1, \$3.2	Möbius transformations; Cross ratio	HW 4
6	February 27	\$3.3, \$3.4, \$3.5	Exponential, trigonometric & logarithmic functions	HW 5
7	March 6	\$4.1, \$4.2	Integration; Antiderivatives	HW 6
8	March 20	\$4.3, \$4.4	Cauchy's Theorem & Cauchy's Integral Theorem	Exam 2
9	March 27	\$5.1, \$5.2, \$5.3	Applications of Cauchy's Theorem & Antiderivatives	HW 7
10	April 3	\$6.1, \$6.2	Harmonic Functions; Mean-Value Theorems	HW 8
11	April 10	\$7.1, \$7.2	Sequences & Series	HW 9
12	April 17	\$7.3, \$7.4	Sequences of functions; Regions of convergence	Exam 3
13	April 24	\$8.1, \$8.2	Power series	HW 10
14	May 1	\$8.3, \$10.1,	Classification of zeros; Infinite sums	HW 11
15	May 8	\$10.2, \$10.3	Binomial coefficients; Fibonacci numbers	
16	May 15			Final Exam

Policies

Unless an assessment is *explicitly* stated to be a group project, *all work you turn in for a grade must be your own*. If you need assistance in completing a homework assignment, you may ask me for help. Googling for answers, seeking help from the Learning Commons or other faculty members, or using solution keys from previous terms (either from UNK or other universities) is also prohibited. Violation of these rules will result in earning a grade of zero on the assessment. Each homework assignment you turn in for a grade must include the statement:

I have neither given nor received unauthorized assistance on this assignment.

If two assignments are so similar that only collaboration could explain their similarities, both assignments will receive a grade of zero. Using unauthorized materials or communication devices (cell phone, for example) while taking a test will earn you a grade of zero on that assessment. For the university academic integrity policy, please read <https://catalog.unk.edu/undergraduate/academics/academic-regulations/academic-integrity-policy/>

Specially, our course policies are:

1. Regular in person class attendance is required. If you are ill or need to miss class due to athletics, please let me know ahead of time and I will make an effort to put the class on Zoom. Our classroom technology often doesn't work, so do not rely on watching recorded classes.
2. There is no explicit grade penalty for not attending class. But if you choose to not attend class for reasons other than illness or athletics, I reserve the right to not be all that helpful in giving you assistance on homework or helping you learn missed material.
3. All examinations, including the final exam, must be taken in person.
4. For examinations and in class assignments, show your work. *No credit will be given for multistep problems without the necessary work. Your solution must contain enough detail so that I am convinced that you could correctly work any similar problem.* Also erase or clearly mark any work you want me to ignore; otherwise, I'll grade it.
5. The work you turn in is expected to be *accurate, complete, concise, neat, and well-organized. You will not earn full credit on work that falls short of these expectations.*
6. Class cancellations due to weather, illness, or other unplanned circumstances may require that we make adjustments to the course calendar, exam dates, due dates, or specifics for course assessments.

7. Extra credit is not allowed.
8. For examinations, you may use a teacher provided quick reference sheet, but no other reference materials. You may also use a pencil, eraser, and a scientific calculator. For examinations, your phone and all such devices must be turned off and *out of sight*.
9. Generally, if you are ill or absent for any reason (including athletics), you must turn in your in class work on time. Permission to turn in work late must be made before the due date, otherwise late in class work will count zero points.
10. During class time, please refrain from using electronic devices. If your device usage distracts your classmates, I will ask you to put it away. If it's my impression that you are often not paying attention in class, I reserve the right to decline to help you during office hours.
11. The final examination will be *comprehensive* and it will be given during the time scheduled by the University. Except for *extraordinary circumstances* you must take the exam at this time.
12. If you have questions about how your work has been graded, make an appointment with me immediately.
13. Please regularly check Canvas to verify that your scores have been recorded correctly. If I made a mistake in recording one of your grades, I'll correct it provided you saved your paper.
14. The course calendar might be modified. It is your responsibility to attend class and to keep up to date on modifications to the course calendar.

Reporting Student Sexual Harassment, Sexual Violence or Sexual Assault

Reporting allegations of rape, domestic violence, dating violence, sexual assault, sexual harassment, and stalking enables the University to promptly provide support to the impacted student(s), and to take appropriate action to prevent a recurrence of such sexual misconduct and protect the campus community. Confidentiality will be respected to the greatest degree possible. Any student who believes they may be the victim of sexual misconduct is encouraged to report to one or more of the following resources:

Local Domestic Violence, Sexual Assault Advocacy Agency 308-237-2599

Campus Police (or Security) 308-865-8911

Title IX Coordinator 308-865-8655

Retaliation against the student making the report, whether by students or University employees, will not be tolerated.

Students with Disabilities

It is the policy of the University of Nebraska at Kearney to provide flexible and individualized reasonable accommodation to students with documented disabilities. To receive accommodation services for a disability, students must be registered with the UNK Disabilities Services for Students (DSS) office, 175 Memorial Student Affairs Building, 308-865-8214 or by email unkdso@unk.edu

Students Who are Pregnant

It is the policy of the University of Nebraska at Kearney to provide flexible and individualized reasonable accommodation to students who are pregnant. To receive accommodation services due to pregnancy, students must contact the Student Health office at 308-865-8218. The following links provide information for students and faculty regarding pregnancy rights:

1. <https://thepregnantscholar.org/title-ix-basics/>
2. <https://nwlc.org/resource/faq-pregnant-and-parenting-college-graduate-students-rights/UNKStatementInclusion>

UNK Statement of Diversity & Inclusion

UNK stands in solidarity and unity with our students of color, our Latinx and international students, our LGBTQIA+ students and students from other marginalized groups in opposition to racism and prejudice in any form, wherever it may exist. It is the job of institutions of higher education, indeed their duty, to provide a haven for the safe and meaningful exchange of ideas and to support peaceful disagreement and discussion. In our classes, we strive to maintain a positive learning environment based upon open communication and mutual respect. UNK does not discriminate on the basis of race, color, national origin, age, religion, sex, gender, sexual orientation, disability or political affiliation. Respect for the diversity of our backgrounds and varied life experiences is essential to learning from our similarities as well as our differences. The following link provides resources and other information regarding D&I: <https://www.unk.edu/about/equity-access-diversity.php>

Barton Willis, PhD

Professor of Mathematics and Statistics

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Blocks marked "Appointments" (light yellow highlight) means usually available to make appointments.

	Monday	Tuesday	Wednesday	Thursday	Friday
9:00	MATH 102 9:05-9:55 DSCH 116	Unavailable 8:00-12:00	MATH 102 9:05-9:55 DSCH 116	Unavailable 8:00-12:00	MATH 102 9:05-9:55 DSCH 116
10:00	Office Hours 10:00-11:00 DSCH 368		Office Hours 10:00-11:00 DSCH 368		Office Hours 10:00-11:00 DSCH 368
11:00	Lunch 11:00-12:00 Off campus	Lunch 11:00-12:00 Off campus	Lunch 11:00-12:00 Off campus	Lunch 11:00-12:00 Off campus	Lunch 11:00-12:00 Off campus
12:00	Appointments 12:00-13:20 DSCH 368	Office Hours 12:00-14:00 DSCH 368	Appointments 12:00-13:20 DSCH 368	Office Hours 12:00-14:00 DSCH 368	Appointments 12:00-13:20 DSCH 368
13:00					
13:30	MATH 365-01 13:25-14:15 DSCH 386		MATH 365-01 13:25-14:15 DSCH 386		MATH 365-01 13:25-14:15 DSCH 386
14:00		Meeting 14:00-15:00		Meetings 14:00-15:00	
14:15					
14:30	MATH 250-01 14:30-15:20 DSCH 386		MATH 250-01 14:30-15:20 DSCH 386		MATH 250-01 14:30-15:20 DSCH 386
14:45					
15:00	Unavailable 15:30-16:30	Appointments 15:00-16:30 DSCH 368	Unavailable 15:30-16:30	Appointments 15:00-16:30 DSCH 368	Unavailable 15:30-16:30
15:15					
15:30					
15:45					
16:00					

Greek characters

Name	Symbol	Typical use(s)
alpha	α	angle, constant
beta	β	angle, constant
gamma	γ	angle, constant
delta	δ	limit definition
epsilon	ϵ or ε	limit definition
theta	θ or ϑ	angle
pi	π or π	circular constant
phi	ϕ or φ	angle, constant

Named sets

empty set	\emptyset	integers	\mathbf{Z}
real numbers	\mathbf{R}	positive integers	$\mathbf{Z}_{>0}$
ordered pairs	\mathbf{R}^2	positive reals	$\mathbf{R}_{>0}$

Set symbols

Meaning	Symbol	Meaning	Symbol
is a member	\in	union	\cup
subset	\subset	complement	superscript ^C
intersection	\cap	set minus	\setminus

Logic symbols

Meaning	Symbol	Meaning	Symbol
negation	\neg	equivalent	\equiv
and	\wedge	iff	\iff
or	\vee	for all	\forall
implies	\implies	there exists	\exists

Function notation

$\text{dom}(F)$	domain of function F
$\text{range}(F)$	range of function F
C_A	set of continuous functions on set A
C_A^1	set of differentiable functions on set A
$A \rightarrow B$	set of functions from A to B

Triangle inequalities

For all $x, y \in \mathbf{C}$, we have

$$|x + y| \leq |x| + |y|$$
$$||x| - |y|| \leq |x - y|$$