Greek Characters

Name	Symbol	Typical use(s)
alpha	α	angle, constant
beta	β	angle, constant
gamma	γ	angle, constant
epsilon	ϵ or ε	angle, constant
theta	θ or ϑ	angle, constant
pi	π or π	circular constant
phi	ϕ or φ	angle,constant

Named Sets

empty set	$\varnothing$
real numbers	$\mathbf{R}$
ordered pairs of reals	$\mathbf{R}^2$
integers	$\mathbf{Z}$
positive integers	$\mathbf{Z}_{>0}$
positive real numbers	$\mathbf{R}_{>0}$

Set Symbols

Meaning	Symbol
is a member	$\in$
subset	$\subset$
intersection	$\cap$
union	$\cup$
set minus	$\setminus$

Intervals

For numbers a and b, we define the intervals:

$$(a,b) = \{x \in \mathbf{R} \mid a < x < b\}$$
$$[a,b) = \{x \in \mathbf{R} \mid a \le x < b\}$$
$$(a,b] = \{x \in \mathbf{R} \mid a < x \le b\}$$
$$[a,b] = \{x \in \mathbf{R} \mid a \le x \le b\}$$
$$(-\infty,a) = \{x \mid x < a\}$$
$$(-\infty,a] = \{x \mid x \le a\}$$
$$(a,\infty) = \{x \mid a < x\}$$
$$[a,\infty) = \{x \mid a \le x\}$$

Logic Symbols

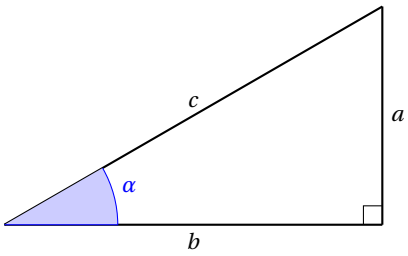
Meaning	Symbol
negation	$\neg$
and	$\wedge$
or	$\vee$
implies	$\Longrightarrow$
equivalent	$\equiv$
for all	$\forall$
there exists	$\exists$

Exponents

For $a, b > 0$ and m, n real:

$$a^0 = 1$$
$$0^a = 0$$
$$1^a = 1$$
$$a^n a^m = a^{n+m}$$
$$a^n / a^m = a^{n-m}$$
$$(a^n)^m = a^{n \cdot m}$$
$$a^{-m} = 1/a^m$$
$$(a/b)^m = a^m / b^m$$

Right triangle trigonometry



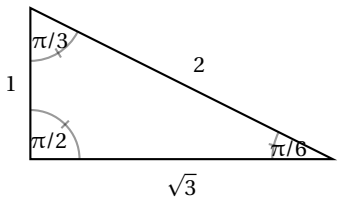
$$\sin\alpha = a/c \qquad \cos\alpha = b/c$$
$$\tan\alpha = a/b \qquad \cot\alpha = b/a$$

Trigonometric identities

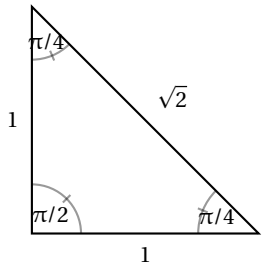
$$\sin(x)^2 + \cos(x)^2 = 1$$
$$2\cos(x)^2 = 1 + \cos(2x)$$
$$2\sin(x)^2 = 1 - \cos(2x)$$
$$\sin(x+y) = \sin(x)\cos(y) + \cos(x)\sin(y)$$
$$\cos(x+y) = \cos(x)\cos(y) - \sin(x)\sin(y)$$

Famous Triangles

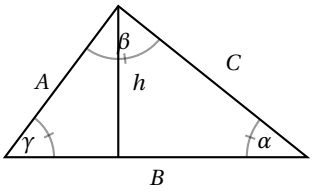
The 30-60-90 triangle



The 45-45-90 triangle



Laws of Cosine & Sine



Law of cosine

$$C^2 = A^2 + B^2 - 2AB\cos(\gamma)$$

Law of sines

$$\frac{\sin\alpha}{A} = \frac{\sin\beta}{B} = \frac{\sin\gamma}{C}$$

Area

$$\text{Area} = \frac{1}{2}hB = \frac{1}{2}AB\sin(\gamma)$$

Solution of equations

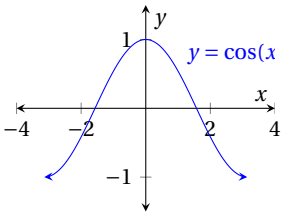
Algebraic

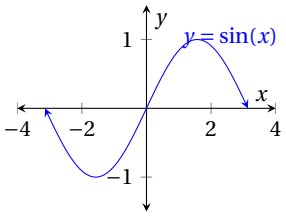
$$[ab = 0] \equiv [a = 0 \textbf{ or } b = 0]$$
$$[a^2 = b^2] \equiv [a = b \textbf{ or } a = -b]$$
$$\left[\frac{a}{b} = 0\right] \equiv [a = 0 \textbf{ and } b \neq 0]$$
$$\left[\frac{a}{b} = \frac{c}{d}\right] \equiv [ad = bc \textbf{ and } b \neq 0 \textbf{ and } d \neq 0]$$
$$[|a| = |b|] \equiv [a = b \textbf{ or } a = -b]$$
$$[\sqrt{a} = b] \equiv [a = b^2 \textbf{ and } b \geq 0]$$

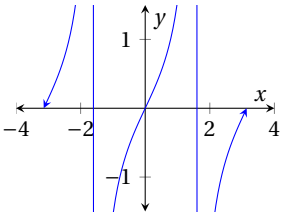
Trig

$$[\cos(a) = 0] \equiv [a = (k - 1/2)\pi, k \in \mathbf{Z}]$$
$$[\sin(a) = 0] \equiv [a = k\pi, k \in \mathbf{Z}]$$
$$[\tan(a) = 0] \equiv [a = k\pi, k \in \mathbf{Z}]$$

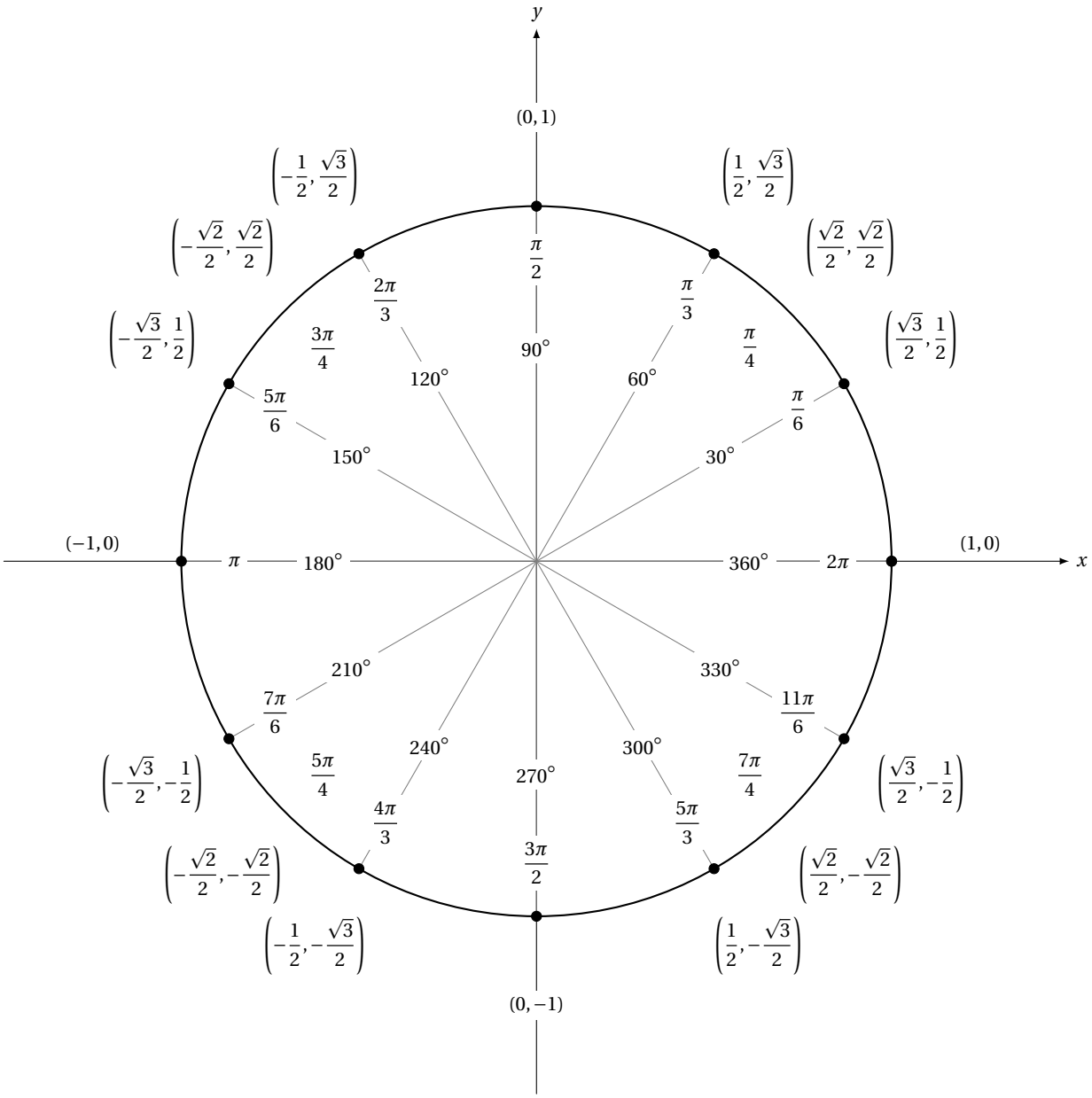
Graphs







Unit Circle



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