

## Greek Characters

Name	Symbol	Typical use(s)
alpha	$\alpha$	angle, constant
beta	$\beta$	angle, constant
gamma	$\gamma$	angle, constant
epsilon	$\epsilon$ or $\varepsilon$	angle, constant
theta	$\theta$ or $\vartheta$	angle, constant
pi	$\pi$ or $\pi$	circular constant
phi	$\phi$ or $\varphi$	angle, constant

## Named Sets

empty set	$\emptyset$
real numbers	$\mathbf{R}$
ordered pairs of reals	$\mathbf{R}^2$
integers	$\mathbf{Z}$
positive integers	$\mathbf{Z}_{>0}$
positive real numbers	$\mathbf{R}_{>0}$

## Set Symbols

Meaning	Symbol
is a member	$\in$
subset	$\subset$
intersection	$\cap$
union	$\cup$
set minus	$\setminus$

## Intervals

For numbers  $a$  and  $b$ , we define the intervals:

$$(a, b) = \{x \in \mathbf{R} \mid a < x < b\}$$

$$[a, b) = \{x \in \mathbf{R} \mid a \leq x < b\}$$

$$(a, b] = \{x \in \mathbf{R} \mid a < x \leq b\}$$

$$[a, b] = \{x \in \mathbf{R} \mid a \leq x \leq b\}$$

$$(-\infty, a) = \{x \mid x < a\}$$

$$(-\infty, a] = \{x \mid x \leq a\}$$

$$(a, \infty) = \{x \mid a < x\}$$

$$[a, \infty) = \{x \mid a \leq x\}$$

## Logic Symbols

Meaning	Symbol
negation	$\neg$
and	$\wedge$
or	$\vee$
implies	$\Rightarrow$
equivalent	$\equiv$
for all	$\forall$
there exists	$\exists$

## Exponents

For  $a, b > 0$  and  $m, n$  real:

$$a^0 = 1$$

$$0^a = 0$$

$$1^a = 1$$

$$a^n a^m = a^{n+m}$$

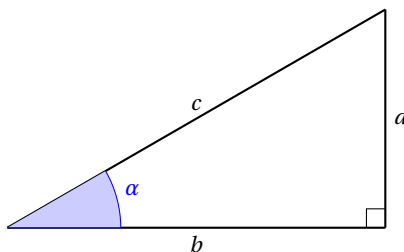
$$a^n / a^m = a^{n-m}$$

$$(a^n)^m = a^{n \cdot m}$$

$$a^{-m} = 1/a^m$$

$$(a/b)^m = a^m / b^m$$

## Right triangle Trigonometry



$$\sin(\alpha) = a/c \quad \cos(\alpha) = b/c \quad \tan(\alpha) = a/b$$

$$\csc(\alpha) = c/a \quad \sec(\alpha) = c/b \quad \cot(\alpha) = b/a$$

## Trigonometric Identities

$$\sin^2(x) + \cos^2(x) = 1$$

$$2\cos^2(x) = 1 + \cos(2x)$$

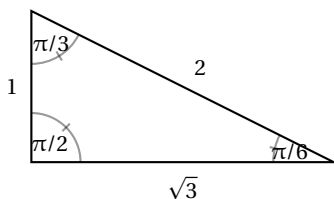
$$2\sin^2(x) = 1 - \cos(2x)$$

$$\sin(x+y) = \sin(x)\cos(y) + \cos(x)\sin(y)$$

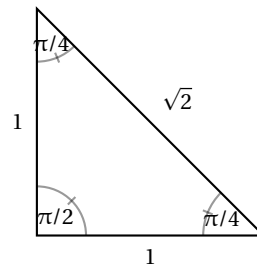
$$\cos(x+y) = \cos(x)\cos(y) - \sin(x)\sin(y)$$

## Famous Triangles

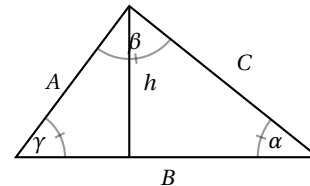
### The 30-60-90 triangle



### The 45-45-90 triangle



## Laws of Cosine & Sine



### Law of cosines

$$c^2 = a^2 + b^2 - 2ab \cos(\gamma)$$

### Law of sines

$$\frac{\sin \alpha}{A} = \frac{\sin \beta}{B} = \frac{\sin \gamma}{C}$$

### Area

$$\text{Area} = hB/2 = AB \sin(\gamma)/2$$

## Solution of equations

### Algebraic

$$[ab = 0] \equiv [a = 0 \text{ or } b = 0]$$

$$[a^2 = b^2] \equiv [a = b \text{ or } a = -b]$$

$$\left[\frac{a}{b} = 0\right] \equiv [a = 0 \text{ and } b \neq 0]$$

$$\left[\frac{a}{b} = \frac{c}{d}\right] \equiv [ad = bc \text{ and } b \neq 0 \text{ and } d \neq 0]$$

$$[|a| = |b|] \equiv [a = b \text{ or } a = -b]$$

$$[\sqrt{a} = b] \equiv [a = b^2 \text{ and } b \geq 0]$$

For  $a \neq 0$ ,

$$[ax^2 + bx + c = 0] \equiv \left[x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}\right]$$

### Trig

$$[\cos(a) = 0] \equiv [a = (k - 1/2)\pi, k \in \mathbf{Z}]$$

$$[\sin(a) = 0] \equiv [a = k\pi, k \in \mathbf{Z}]$$

$$[\tan(a) = 0] \equiv [a = k\pi, k \in \mathbf{Z}]$$

# Graphs

## Cosine, sine, and tangent

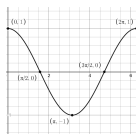


Figure 1: Graph of  $y = \cos(x)$  on  $[0, 2\pi]$ .

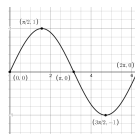


Figure 2: Graph of  $y = \sin(x)$  on  $[0, 2\pi]$ .

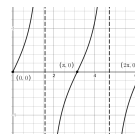


Figure 3: Graph of  $y = \tan(x)$  on  $[0, 2\pi]$ .

## Arccosine, arcsine, and arctangent

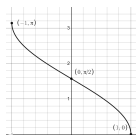


Figure 4: Graph of  $y = \arccos(x)$  on  $[-1, 1]$ .

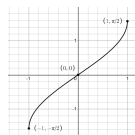


Figure 5: Graph of  $y = \arcsin(x)$  on  $[-1, 1]$ .

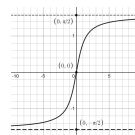
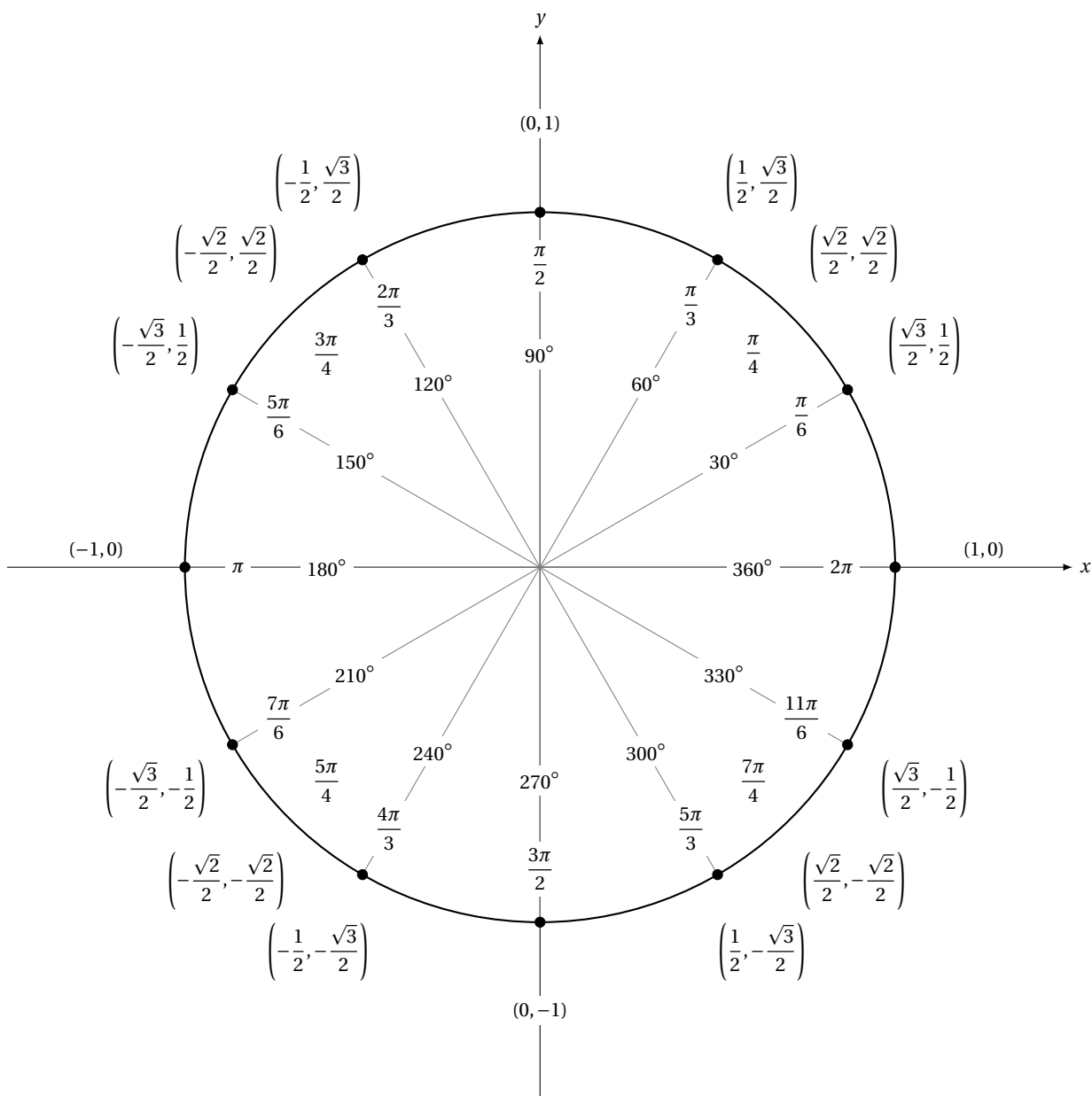


Figure 6: Graph of  $y = \arctan(x)$  on  $[-10, 10]$ .

# Unit Circle



For a comprehensive list of trigonometric function facts, see <https://dlmf.nist.gov/4.14>.

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