

The following table gives some hints on how to solve an equation for a variable  $x$ . The quantities  $X$ ,  $Y$ ,  $Z$ , and  $W$  match with any expression that involves  $x$  and the quantities  $a$  and  $b$  match with any number (or constant that doesn't depend on  $x$ ). Sometimes you'll need to do some algebra (divide both sides by a nonzero number, factor, or other such things) to make the match.

Rule	Replace	With	Condition(s)
1	$a = b$ and $a \neq b$	$\emptyset$	(none)
2	$0x = 1$	$\emptyset$	(none)
3	$0x = 0$	<b>R</b>	(none)
4	$ax = b$ and $a \neq 0$	$x = \frac{b}{a}$	(none)
5	$ax^2 + bx + c = 0$ and $a \neq 0$	$x = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$ or $x = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$	$b^2 - 4ac \geq 0$
6	$XY = 0$	$X = 0$ or $Y = 0$	(none)
7	$\frac{X}{Y} = 0$	$X = 0$	$Y \neq 0$
8	$\frac{W}{X} = \frac{Y}{Z}$	$WZ = XY$	$X \neq 0$ and $Z \neq 0$
9	$X^2 = Y$	$X = -\sqrt{Y}$ or $X = \sqrt{Y}$	$Y \geq 0$
10	$ X  = Y$	$X = Y$ or $X = -Y$	$Y \geq 0$
11	$\sqrt{X} = Y$	$X = Y^2$	$Y \geq 0$
12	$\exp(X) = a$	$X = \ln(a)$	$a > 0$
13	$a^X = b$ and $a > 0$ and $a \neq 1$ and $b > 0$	$X = \frac{\ln(b)}{\ln(a)}$	(none)
14	$\ln(X) = a$	$X = \exp(a)$	
15	$\cos(X) = a$	$X = 2\pi k + \cos^{-1}(a)$ or $X = 2\pi k - \cos^{-1}(a)$	$-1 \leq a \leq 1$ and $k \in \mathbf{Z}$
16	$\sin(X) = a$	$X = 2\pi k + \sin^{-1}(a)$ or $X = 2\pi k + \pi - \sin^{-1}(a)$	$-1 \leq a \leq 1$ and $k \in \mathbf{Z}$