# **Proper Hygiene**

The whole problem with the world is that fools and fanatics are always so certain of themselves, and wiser people so full of doubts.

Bertrand Russel

## Let's Play True or False

**True or False:** teddy bear, stinkbug, guacamole.

**Answer** This is not a statement—it's a list of things; it doesn't have a truth value. I'd say it's a trick question.

#### True or False Redact.

**True or False:** In my house this morning, you'll find either a teddy bear, a stinkbug, or guacamole.

**Answer** This is true. This morning I opened my fridge. On the middle shelf there was a container that passed the guacamole color, texture, and taste test; therefore it is true that in my house this morning, you'll find either a teddy bear, a stinkbug, or guacamole.

#### No with math

Question Is the following work correct?

$$\int_3^4 x \, \mathrm{d}x \quad \frac{1}{2}x^2 \quad \frac{7}{2}$$

**Answer** Just like the list "teddy bear, stink bug, guacomole," this is a list of mathematical expressions. As such it's not a statement and it doesn't have a truth value. It's a trick question.

### Math Redact

Question Is the following work correct?

$$\int_{3}^{4} x \, \mathrm{d}x = \left. \frac{1}{2} x^{2} \right|_{3}^{4} = \frac{7}{2}$$

**Answer** Yes, this work is correct. This time we're given something that has a truth value.

#### The Mad Gardener

Question Is this work correct? (Lewis Carroll, The Mad Gardener's Song)

He thought he saw an Argument That proved he was the Pope: He looked again, and found it was A Bar of Mottled Soap. "A fact so dread," he faintly said, "Extinguishes all hope!

**Answer** It's amusing nonsense poetry—it's meaningless and neither correct nor incorrect.

## With math

Question Is this work correct?

$$\int_{2}^{3} \sqrt{x+1} \, dx = \int \sqrt{z}$$

$$= \int \frac{3}{2} (1+z)^{3/2}$$

$$= \frac{3}{2} (4^{3/2} - 3^{3/2})$$

**Answer** Unlike the *The Mad Gardener's Song* this is **nonamusing** nonsense. It's meaningless and neither correct nor incorrect.

### Math Redact

Let z=x+1. Then  $\mathrm{d}z=\mathrm{d}x$ . Further x=2 implies z=3; and x=3 implies z=4. Now that we have gathered our four ingredients, we have

$$\int_{2}^{3} \sqrt{x+1} \, dx = \int_{3}^{4} \sqrt{z} \, dx$$
$$= \frac{3}{2} z^{3/2} \Big|_{3}^{4},$$
$$= \frac{3}{2} \left( 4^{3/2} - 3^{3/2} \right).$$